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"Phase Equilibria in Materials"

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• How is the reaction in three phase region among liquid, α and β ?



Fig. 149. Criteria for distinguishing eutectic and peritectic reactions in ternary three-phase equilibrium.

The tangent to the liquid curve at a particular temperature is extrapolated to meet the tie line connecting the α and β phases.

- 1) If the extrapolated line intersected the $\alpha\beta$ tie line, the equilibrium was considered to be eutectic
- 2) If it met the $\alpha\beta$ tie line only when the latter was extrapolated, the equilibrium was considered to be peritectic.

Similarly, a eutectoid reaction could be distinguished from a peritectoid and a monotectic from a syntectic.

• How is the reaction in three phase region?

<Hillert's criterion>

Basically, the reaction we can expect is eutectic reaction

 $(/ \rightarrow \alpha + \beta)$. But, in reality, we can have eutectic and peritectic reaction <u>depending on the relative amount of three phase</u>.

The <u>average composition of the alloy</u> then determines <u>for a particular temperature whether</u> <u>the reaction will be eutectic or peritectic.</u>



A small change in temperature, d7, causes a small change in the composition and amounts of each phase, but not of the alloy itself,



Fig. 150. Illustration of Hillert's criterion for distinguishing eutectic and peritectic reaction in ternary threephase equilibrium; ———, equilibrium at T; -----, equilibrium at T-dT.

To simplify the calculation,

Assumption, $X_{A}^{\beta} = X_{A}^{\prime} > X_{A}^{\alpha}$ (New coordinate system) $\Delta m_{\beta} + \Delta m_{l} = -\Delta m_{\alpha}$ $\Delta X_{A} = m_{\alpha} \cdot \Delta X_{A}^{\alpha} + m_{\beta} \cdot \Delta X_{A}^{\beta} + m_{l} \cdot \Delta X_{A}^{l} + X_{A}^{\alpha} \cdot \Delta m_{\alpha} + X_{A}^{\beta} \cdot \Delta m_{\beta} + X_{A}^{l} \cdot \Delta m_{l} = 0$ $\underline{-X_{A}^{\alpha} \Delta m_{\alpha} - X_{A}^{\beta} \Delta m_{\beta} - X_{A}^{l} \Delta m_{l}} = m_{\alpha} \Delta X_{A}^{\alpha} + m_{\beta} \Delta X_{A}^{\beta} + m_{l} \Delta X_{A}^{l}$

 $\Delta m_{\alpha}(X_{A}^{\beta}-X_{A}^{\alpha}) = m_{\alpha}\Delta X_{A}^{\alpha} + m_{\beta}\Delta X_{A}^{\beta} + m_{l}\Delta X_{A}^{l}$

Sign	Assumption	Sign		
$\Delta m_{\alpha}(X_{\rm A}{}^{\beta} - X_{\rm A}{}^{\alpha})$	$X_{\rm A}{}^{\beta} = X_{\rm A}{}^{l} > X_{\rm A}{}^{\alpha}$	$m_{\alpha}\Delta X_{\rm A}{}^{\alpha} + m_{\beta}\Delta X_{\rm A}{}^{\beta} + m_{l}\Delta X_{\rm A}{}^{l}$		
$\Delta m_{\beta}(X_{\rm A}{}^{\alpha} - X_{\rm A}{}^{\beta})$	$X_{\rm A}^{\alpha} = X_{\rm A}^{\ l} > X_{\rm A}^{\ \beta}$	$m_{\alpha}\Delta X_{\rm A}{}^{\alpha} + m_{\beta}\Delta X_{\rm A}{}^{\beta} + m_{l}\Delta X_{\rm A}{}^{l}$		
$\Delta m_l (X_{\rm A}^{\alpha} - X_{\rm A}^{l})$	$X_{\rm A}^{\alpha} = X_{\rm A}^{\beta} > X_{\rm A}^{l}$	$m_{\alpha}\Delta X_{\rm A}{}^{\alpha} + m_{\beta}\Delta X_{\rm A}{}^{\beta} + m_{l}\Delta X_{\rm A}{}^{l}$		

here, Δm_{α} : change of α phase fraction with ΔT

Δm_{α}	Δm_{eta}	Δm_l		
+	+	-	$l \rightarrow \alpha + \beta$	eutectic
+	-	-	$l + \beta \rightarrow \alpha$	peritectic
-	+	-	$l + \alpha \rightarrow \beta$	peritectic

<u>Hillert's criterion indicates that the relative amounts of the α , β and liquid phases (the average alloy composition) are of importance in determining the type of reaction.</u>

• three phase regions $a_1e_1b_1$, $a_2e_2b_2$, ..., $a_7e_7(b_7)$ projected on the concentration triangle.



To determine whether the reaction is always a monovariant eutectic type, irrespective of alloy composition within the three-phase region, we apply Hillert's criterion to each pair of isotherms.

- 9.3. THREE-PHASE EQUILIBRIUM INVOLVING EUTECTIC REACTIONS
 - Relative position of vertex in tie triangle with ΔT



Consider tie triangle $a_4e_4b_4$, and $a_5e_5b_5$



• How to decide the boundary btw eutectic & peritectic?

Reactions in the tie triangle $a_4e_4b_4$, along boundary, β plays no role $\rightarrow l = \alpha$



$$X_{A}^{\alpha} = X_{A}^{l} > X_{A}^{\beta}$$

$$\Delta m_{\beta}(X_{A}^{\alpha} - X_{A}^{\beta}) = m_{\alpha}\Delta X_{A}^{\alpha} + m_{\beta}\Delta X_{A}^{\beta} + m_{l}\Delta X_{A}^{l}$$

$$(\Delta X_{A}^{\alpha} = -1, \Delta X_{A}^{\beta} = 3.5, \Delta X_{A}^{l} = 3) \quad (\text{next page})$$

$$-m_{\alpha} + 3.5m_{\beta} + 3m_{l} = 0 \quad (m_{\alpha} + m_{\beta} + m_{l} = 100)$$

$$-100 + 4.5m_{\beta} + 4m_{l} = 0$$

if $m_{\beta} = 0, m_{l} = 25$
if $m_{l} = 0, m_{\beta} = 22.2$

Initially, peritectic region confined the α corner.

Consideration of three-phase triangles at lower temperatures will indicate that the peritectic region sweeps round from the α corner towards the β and liquid corners.





The boundary line can be determined by measuring ΔX_A^{α} , ΔX_A^{β} , and ΔX_A^{l} .

In Fig. 151, $\Delta X_A^{\alpha} = -1$, $\Delta X_A^{\beta} = -3.5$ and $\Delta X_A^{l} = 3$ units.

	<i>X</i> _B ,	X _C		<i>X</i> _B ,	X _C		Х _В ,	$X_{\mathbf{C}}$
· e.	33,	16	a_1	17,	6	b_1	78,	3
e_{2}	29,	27	a_2	14,	20	b_2	69,	15
e.	26,	37	a_3	15,	31	b_3	62,	22
e1	25.3.	41	a_{Λ}	19,	37	b_4	56,	27
e _z	25,	44	a_5	25,	39	b_5	52,	30
e _e	25,	47	a_6	34,	39	b_6	45,	34
e7	25,	50	$a_{7}(b_{7})$	40,	37			

Figure 151

Table 2

Monovariant β curve coincides with the $|\alpha|$ tie line between isotherms $a_5e_5b_5$ and $a_6e_6b_6$ Second peritectic reaction area appears at the β corner of the three-phase triangle



To summarise, the three-phase reaction is initially eutectic for all alloys untill the temperature of the three phase triangle $a_4e_4b_{4,}$ is reached. From that temperature until the end of the three-phase reaction at the tie line $e_7a_7(b_7)$, the reaction type is dependent on the alloy composition within the sequence of the three-phase triangles. 11















9.2. THREE-PHASE EQUILIBRIUM

① Coalescence of miscibility gap and two phase region

• How we can have 3 phase equil.?



Fig. 136. Production of a ternary three-phase equilibrium by the coalescence of two two-phase regions

9.2. THREE-PHASE EQUILIBRIUM

② Coalescence of two two-phase region



Fig. 138. Alternative method to Fig. 136 for the production of a ternary three-phase equilibrium by the coalescence of two two-phase regions



• Vertical section



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Vertical section



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• Vertical section



• Vertical section



Vertical section



Vertical section







Projection of the solidification sequence for alloy Y on the concentration triangle

• A maximum critical point

Basically, the reaction we can expect is eutectic reaction $(l \rightarrow \alpha + \beta)$. But, in reality, we can have eutectic and peritectic reaction <u>depending on the</u> <u>relative amount of three phase</u>.

Application of I' Hillert's criterion

 $I \leftrightarrow \alpha + \beta$





Vertical section

l $l + \alpha(\beta)$ $l + \alpha + \beta$ β $\alpha + \beta$ I

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• A limiting case: solubility gap just reaches one of the binary systems.

• A limiting case

Fig. 165. The phase regions in Fig. 164a.

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• A peritectic solubility gap in one binary system

PP₁: monovariant curve for liquid

Points P_1 and c lie at the same temperature and the line P_1c is a degenerate tie triangle.

isothermal section

• A peritectic solubility gap in one binary system

• A peritectic solubility gap in two binary system

 $T_B > P > T_A > T_c > e$

• A transition from a binary eutectic to a binary peritectic reaction

- curve *pe* always lies above curve *aa*₁
- Tie lines are drawn on the I β and I α surfaces only.
- By Hillert to show that <u>the transition form a peritectic to</u> <u>a eutectic reaction does not occur at a unique temperature.</u>

• Binary Monotectic, syntectic and metatectic reactions in combination with each other as well as with binary eutectic and peritectic reactions.

