### 새로운 나노 광전자공학 - 플라즈모닉스

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### Contents

□ Introduction

**Photonic crystals** 

□ Vectorial diffractive optics

**Plasmonics - Surface plasmon polaritons** 

**Concluding remarks** 





#### Nano



# "There is Plenty of Room at the Bottom"

Prof. Richard P. Feynman December, 1959 California Institute of Technology <u>http://www.zyvex.com/nanotech/feynman.html</u>





### **Photonic crystals**



[Y. A. Vlasov et al., Nature 414, 289 (2001).]



Figure 6 The green colour of Parides sesostris is created by a photonic crystal. a, b,



**Figure 3** Iridescence in the butterfly *Morpho rhetenor*. **a**, Real colour image of the blue iridescence from a *M. rhetenor* ving. **b**, Transmission electron micrograph (TEM) images showing wing-scale cross-sections of *M. rhetenor*. **c**, TEM images of a wing-scale cross-section of the related species *M. didius* reveal its discretely configured multilayers. The high occupancy and high layer number of *M. rhetenor* in **b** creates an intense reflectivity that contrasts with the more diffusely coloured appearance of *M. didius*, in which an overlying second layer of scales effects strong diffraction<sup>4</sup>. Bars, **a**, 1 cm; **b**, 1.8  $\mu$ m; **c**, 1.3  $\mu$ m.





### **Photonic crystals**



Light cavities

Light waveguides ('wires')

### Periodic electromagnetic media Photonic bandgap: optical insulator





### **Photonic bandgap waveguides**



- a: guide
- b : sharp bend c : add/drop

- d: Y-coupler e: filter f: dispersive element



#### **Photonic crystals**

### **Holey fibers**





### Mitsubishi Cable

클래딩 지름	80µm	
유효 코어 모드 지름	11.5 µm	
전송 손실 (1550nm)	0.35dB/km	
허용 곡률 반경	7.5mm	
벤딩 손실 (1550nm) φ 15mm × 10 turn	<0.1dB	



### Fujikura

FutureGuide<sup>®</sup>-SR15 →허용 곡률 반경 15 mm

FutureGuide<sup>®</sup>–SR7.5 → 허용 곡률 반경 7.5 mm





#### **Optical analysis**

### **Two categories of diffractive optics**







#### Vectorial diffractive optics

### Finite-difference time-domain (FDTD) method

□ FDTD is a rigorous analysis method with widely applications from nano- to all length-scales using the Maxwell's equations and curl equations





#### Vectorial diffractive optics

### Solid immersion lens simulation (FDTD)







Ex-component

Ey-component

Extension to three-dimensional solid immersion lens nano-focusing for high density optical memory



### **Frequency domain method for the Maxwell equations**

Homogeneous Maxwell equations in the spatial domain

$$\nabla \times \underline{E} = jw\mu_0\mu(x, y, z)(\hat{x}H_x + \hat{y}H_y + \hat{z}H_z)$$
  
$$\nabla \times \underline{H} = -jw\varepsilon_0\varepsilon(x, y, z)(\hat{x}E_x + \hat{y}E_y + \hat{z}E_z)$$

transform

Fourier

Homogeneous Maxwell equations in the (spatial) frequency domain

$$k_{0}\begin{bmatrix}\underline{\underline{\mathcal{E}}}_{(x)} & 0 & 0 & 0 & 0 & 0\\ 0 & \underline{\mathcal{E}}_{(y)} & 0 & 0 & 0 & 0\\ 0 & 0 & \underline{\mathcal{E}}_{(z)} & 0 & 0 & 0\\ 0 & 0 & 0 & \underline{\mathcal{H}}_{(x)} & 0 & 0\\ 0 & 0 & 0 & 0 & \underline{\mathcal{H}}_{(x)} & 0 & 0\\ 0 & 0 & 0 & 0 & \underline{\mathcal{H}}_{(y)} & 0\\ 0 & 0 & 0 & 0 & \underline{\mathcal{H}}_{(y)} & 0\\ 0 & 0 & 0 & 0 & 0 & \underline{\mathcal{H}}_{(z)}\end{bmatrix}\begin{bmatrix}\underline{E}_{x}\\ \underline{E}_{y}\\ \underline{E}_{z}\\ \underline{H}_{x}\\ \underline{H}_{y}\\ \underline{H}_{z}\end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & 0 & j\underline{K}_{z} & -j\underline{K}_{y}\\ 0 & 0 & 0 & j\underline{K}_{z} & -j\underline{K}_{x} & 0\\ 0 & j\underline{K}_{z} & -j\underline{K}_{y} & 0 & 0 & 0\\ -j\underline{K}_{z} & 0 & j\underline{K}_{x} & 0 & 0 & 0\\ -j\underline{K}_{z} & 0 & j\underline{K}_{x} & 0 & 0 & 0\\ j\underline{K}_{y} & -j\underline{K}_{x} & 0 & 0 & 0\\ \end{bmatrix}\begin{bmatrix} \underline{E}_{x}\\ \underline{E}_{y}\\ \underline{E}_{z}\\ \underline{H}_{x}\\ \underline{H}_{y}\\ \underline{H}_{z}\end{bmatrix}$$

The Maxwell equations in the spatial domain have partial differential operators. But Maxwell equations in the frequency domain are described by several algebraic equations.





#### Vectorial diffractive optics

### **Rigorous coupled wave analysis (RCWA)**



Fourier representation of the permittivity of the i<sup>th</sup> layer

$$\varepsilon^{(i)}(x, y) = \sum_{g,h} \varepsilon^{(i)}_{gh} \exp\left[j(G_{x,g}x + G_{x,h}y)\right]$$

#### Fourier representation of the EM fields in the i<sup>th</sup> layer

$$\underline{E}^{(i)} = \sum_{m=-M}^{M} \sum_{n=-N}^{N} \left[ \underline{x} S_{x,mn}^{(i)}(z) + \underline{y} S_{y,mn}^{(i)}(z) + \underline{z} S_{z,mn}^{(i)}(z) \right] \exp\left[ j \left( k_{x,m} x + k_{y,n} y \right) \right]$$
$$\underline{H}^{(i)} = j \sqrt{\frac{\varepsilon_0}{\mu_0}} \sum_{m=-M}^{M} \sum_{n=-N}^{N} \left[ \underline{x} U_{x,mn}^{(i)}(z) + \underline{y} U_{y,mn}^{(i)}(z) + \underline{z} U_{z,mn}^{(i)}(z) \right] \exp\left[ j \left( k_{x,m} x + k_{y,n} y \right) \right]$$

The boundary conditions between adjacent layers are satisfied by

the S-matrix method. Seoul National University



2D-binary dielectric grating showing polarization-dependent diffraction







- Modal analysis of dielectric waveguide
  - The eigenmode extraction from total-field by observing the eigenvalue.









#### 3D micro-pyramid structure (15 level staircase approximation)





x-y crosssection

 $E_y$ 

x-y crosssection







3D micro-metal-sphere structure (15 level staircase approximation)





#### Vectorial diffractive optics

### **Pseudo-Fourier modal analysis (PFMA)**

#### Structure modeling (3D Fourier series)



$$\varepsilon(x, y, z) = \sum_{s=-2M}^{2M} \sum_{t=-2N}^{2N} \sum_{p=-2H}^{2H} \tilde{\varepsilon}_{stp} \exp\left(j\left(k_{x,stp} x + k_{y,stp} y + k_{z,stp} z\right)\right)$$

#### **Pseudo-Fourier representation of the E-M field**

$$\tilde{\mathbf{E}}_{\mathbf{k}} = \mathrm{e}^{j\left(k_{x,0}x + k_{y,0}y + k_{z,0}z\right)} \sum_{m,n,q} \left(E_{x,m,n,q}\underline{x} + E_{y,m,n,q}\underline{y} + E_{z,m,n,q}\underline{z}\right) \exp\left(j\left(k_{x,mnq}x + k_{y,mnq}y + k_{z,mnq}z\right)\right)$$

#### Maxwell equation in the PFMA

$$\begin{bmatrix} -j\underline{G}_{z} & 0 & \underline{K}_{y}\underline{\varepsilon}_{(z)}^{-1}\underline{K}_{z} & \underline{\mu}_{(z)} - \underline{K}_{y}\underline{\varepsilon}_{(z)}^{-1}\underline{K}_{y} \\ 0 & -j\underline{G}_{z} & -\underline{\mu}_{(y)} + \underline{K}_{z}\underline{\varepsilon}_{(z)}^{-1}\underline{K}_{z} & -\underline{K}_{z}\underline{\varepsilon}_{(z)}^{-1}\underline{K}_{y} \\ \underline{K}_{z}y\underline{\mu}_{(z)}^{-1}\underline{K}_{z} & \underline{\varepsilon}_{(x)} - \underline{K}_{y}y\underline{\mu}_{(z)}^{-1}\underline{K}_{y} & -j\underline{G}_{z} & 0 \\ -\underline{\varepsilon}_{(y)} + \underline{K}_{z}\underline{\mu}_{(z)}^{-1}\underline{K}_{z} & -\underline{K}_{z}\underline{\mu}_{(z)}^{-1}\underline{K}_{y} & 0 & -j\underline{G}_{z} \\ \end{bmatrix} = \begin{bmatrix} jk_{z,0} \\ \underline{K}_{y} \\ \underline{H}_{y} \\ \underline{H}_{z} \\ \underline{H}_{z} \\ \underline{H}_{z} \end{bmatrix}$$
  
Eigenmode profile



Eigenvalue



### **PFMA example**

#### Longitudinally periodic and finite 2D photonic crystals

 $\mathbf{E} = \sum_{g} C_{g} \tilde{\mathbf{E}}_{\mathbf{k}}$  Total field distribution is a superposition of pseudo-Fourier eigenmodes with appropriate coupling coefficients.





Wavelength( $\lambda$ )=532nm Period=1.2 $\lambda$ , radius=0.4  $\lambda$ Normal incidence







### Comparison

	FDTD	RCWA	PFMA
Domain	Space	Frequency	Frequency
Field representation	Finite-difference method	Piles of truncated 2D- pseudo-Fourier series	Truncated 3D-pseudo- Fourier series
Structure modeling	Mesh-structure	Staircase approximation & piles of 2D-Fourier series	<b>3D-Fourier series</b> (no staircase approximation)
Aperiodic structure Analysis	Yes	No (If using PML, yes)	No (If using PML, yes)
Evanescent field analysis	No (Cannot separate)	Yes	Yes
Modal analysis	No	No	Yes
Computation cost	Very huge	Large	Huge





### **Parallel computing**

#### **Parallel computing system**







#### What is a plasmon?

- "Plasma-oscillation": density fluctuation of free electrons



Bulk plasmon

Surface plasmon



Confined plasmon in nanoparticle



#### The Lycurgus Cup (glass) British Museum 4th century A.D.

Green when illuminated from outside and red when illuminated from within the cup due to very small amounts of gold powder about 40 parts per million)



#### "Labors of the Months" Norwich, England ca. 1480

The ruby color is attributed to gold nanoparticles.





### Surface plasmon

#### Surface plasmon (SP)

- EM surface-bound wave between a metal and dielectric surface (ppolarized, TM wave)
- The metal behaves like a plasma, having equal amounts of positive and negative charges, of which the electrons are mobile.
- The bound wave has an evanescent field which decays exponentially perpendicular to the surface.
- SPs can be produced by photons in the attenuated total reflection device.
- SPs have played a significant role in a variety of areas of fundamental and applied research, from surface sensitive technique to surface plasmon resonance microscopy and a wide range of photonic applications.

- Dispersion of SP

$$k_{SP} = k_0 \sqrt{\frac{\varepsilon_d \varepsilon_m}{\varepsilon_d + \varepsilon_m}} = \frac{\omega}{c} \sqrt{\frac{\varepsilon_d \varepsilon_m}{\varepsilon_d + \varepsilon_m}}$$

ex) for silver-air interface,  $k_{sp} = 1.03k_o$ 

- Propagation length,  $\delta_{SP}$ 

$$\delta_{SP} = \frac{1}{2k_{SP}''} = \frac{c}{\omega} \left(\frac{\varepsilon_m' + \varepsilon_d}{\varepsilon_m' \varepsilon_d}\right)^{3/2} \frac{(\varepsilon_m')^2}{\varepsilon_m''}$$

ex) for silver-air interface,  $\delta_{SP} = 20 \ \mu m$ 



Surface charges, evanescent fields, and dispersion curve for SP mode Seoul National University

### **Surface plasmon excitation**

#### Excitation methods

- Kretschmann geometry, Otto geometry, SNOM probe
- Diffraction grating, bumped metal surfaces



SPP excitation configurations





### **Surface plasmon**







### **Surface plasmons in nanoparticles**

#### **Confined SPs in Nanoparticles**





Frequency (10<sup>14</sup> Hz)

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- Uniform sphere, spheroid, rod shaped metal nano-particles
- Interaction between particles, plasmonic chains
- Focusing and guidance of light at nanometer length scales

### Surface plasmon polariton



$$\vec{E}_d(x,z,t) = \vec{E}_{d,0}e^{i(k_x x + k_z z - \omega t)}$$
$$\vec{E}_m(x,z,t) = \vec{E}_{m,0}e^{i(k_x x - k_z z - \omega t)}$$

EM wave is coupled to the plasma oscillations of the surface charges



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#### **Plasmonics:** A bridge between electronics and photonics



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### **Surface plasmon dispersion relation**





### **Surface plasmon dispersion relation**

#### Semi-infinite metal structure





### **Surface plasmon dispersion relation**

#### Finite metal slab structure







#### Surface plasmon polaritons

### **Metal surface relief gratings**



S. Kitson, PRL, 77, 2670, (1996)



ω+

ω

b

00

S. Bozhevolnyi, PRL, 86, 3008, (2001)





# Surface plasmon excitation by Gaussian beams and pulses in TIR geometry

#### Finite metal slab structure



Surface plasmon excited by Gaussian beam



At metal surface



Surface plasmon excited by Gaussian pulse beam Seoul National University



At metal surface OEOELab

### Surface plasmon excitation by NSOM tips





### Surface plasmon excited by a normal incident focused Gaussian beam by a dielectric grating coupler



#### **Plasmonics applications**

### **Beaming light from a subwavelength aperture**





Light usually diffracts in all directions when it emerges from a subwavelength aperture, which puts a lower limit on the size of features that can be used in photonics. This limitation can be overcome by creating a periodic texture on the exit side of a single aperture in a metal film. The transmitted light emerges from the aperture as a beam with a small angular divergence

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#### Plasmonics applications

### Surface plasmon subwavelength optics

W. L. Barnes, A. Degiron, and T. W. Ebbesen, Nature, vol. 424, pp. 824-830, 2003.

#### Bull's eye structure- beaming light by subwavelength structures





Metal-gap waveguide analysis

#### Metal-gap waveguide with bottom surface grating







Metal-gap waveguide analysis

Metal-gap waveguide with upper surface grating







**Flat surface** 

### **Off-axis directional beaming** (Applied Physics Letters)



S. Kim, H. Kim, Y. Lim, and B. Lee, "Off-axis directional beaming of optical field diffracted by a single subwavelength metal slit with asymmetric dielectric surface gratings," **Applied Physics Letters**, vol. 90, no. 5, 051113, 2007.





### Vector field microscopic imaging of light (Nature Photonics)



K. G. Lee, H. W. Kihm, J. E. Kihm, W. J. Choi, H. Kim, C. Ropers, D. J. Park, Y. C. Yoon, S. B. Choi, D. H. Woo, J. Kim, B. Lee, Q. H. Park, C. Lienau, and D. S. Kim, "Vector field microscopic imaging of light," **Nature Photonics**, vol. 1, no. 1, pp. 53-56, 2007.







### **SPR biosensors**







### Surface plasmon resonance on a flat boundary



### **Multiple SPR on multilayer structures**







AZ 1512 (3000 rpm for 30sec)



Seoul National University

AZ 1512 (2000 rpm for 30sec)



AZ 1512 (1000 rpm for 30sec)







### **SPR** analysis

K. Choi, H. Kim, Y. Lim, S. Kim, and B. Lee, *Optics Express*, vol. 13, no. 22, pp. 8866-8874, 2005.

Visualization of SPR using R-TMM and Gaussian angular spectrum decomposition



### **Surface plasmon applications**

#### SPP Applications

- Surface sensitive techniques, SPR microscopy
- SPR technologies and a wide range of photonic ICs.



Waveguides of surface plasmons Surface plasmon Bragg reflectors Bio- and flow-sensors using SPR <sup>a</sup> Light transmission enhancement Laser beam shaping

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Optical

detection

40 nm thick, 2.5 µm wide gold stripe lying on a glass substrate

J. C. Weeber et al., *Phys. Rev. B* 64, 045411(2001).





Ag Film with hole arrays (Period = 300, 450, 550nm Hole diameter=155,180,225nm)

A. Degiron et al. Appl. Phys. Lett. 81, 4327 (2002).



### **Plasmonic nanolithography**

W. Srituravanich, N. Fang, C. Sun, Q. Luo, and X. Zhang, *Nano Letters*, vol. 4, no. 6, pp. 1085-1088, 2004.



Metal mask : 90nm holes, 170nm period

#### **Surface plasmons**

- 1. Much shorter wavelength compared to the excitation light wavelength
- 2. E-field intensity of surface plasmons can be boosted by several orders of magnitude compared to the excitation light





#### Plasmonics applications

### Nano metal rod memory







### **Resonant surface plasmon couplings (SuperLens)**

#### **Superlens-based nanopatterning**

- A flat plane of NRM behaves as superlens and amplifies evanescent waves in near-field through a series of plasmon resonances.
- This allows super-resolutions below diffraction limit.
- Experimentally achieved improvements in UV range: 5-10x beyond the operating wavelength
- Applicable for direct imaging of evanescent modes, thus for immediate recognition of analytes
- Also applicable for nanopatterning through subwavelength contact lithography







Thin silver film





### **Resonant surface plasmon couplings (LED)**

#### Ultrahigh efficiency LED via plasmon light extraction

46x PL enhancement for wafers with periodicities of 480nm and 650nm.







### Nanodot focusing array



- (A) SEM image of a nanodot focusing array coupled to a 250-nm-wide Ag strip guide.
- (B) NSOM image of the SP intensity showing subwavelength focusing.

W. Nomura, M. Ohtsu, and T. Yatsui, Appl. Phys. Lett. 86, 181108 (2005).





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### **Plasmonic toolbox:** ω, **e**(ω), **d** - engineer λ(ω)

#### Plasmonic modulator & IC **Plasmonic multiplexer & Concentrator** Signal SPI AMF . WDM Pump -Signa **Plasmonic resonator & laser Plasmonic Bragg mirror & waveguide** (a) 50000 40000 5 µm E+> 国 30000 (C) flow cell with 20000 circulating dye solution (gain medium) 10000 BK7 prism with thin silver film 20000 40000 probe beam pump beam @ 633 nm 6 580 nm (d) 2 µm field overlap

http://www.plasmonanodevices.org/



#### Active plasmonics: Electrical/optical active switching/amplification of SPP



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### Left-handed material

#### • V.G. Veselago, Soviet Physics Uspekhi 10, 509 (1968)



 $k\sin \varphi = k_1\sin \varphi_1.$ 

Однако последнее равенство удовлетворяется как при угле  $\phi_1$ , так и при угле  $\pi - \phi_1$ .

Требуя по-прежнему, чтобы энергия во второй среде оттекала от границы раздела, мы приходим тогда к тому, что фаза должна набегать на эту границу и, следовательно, направление распространения преломленной волны будет составлять с нормалью угол



п — ф1. Как ни непривычно такое построение, но, конечно, ничего удивительного в нем нет, ибо фазовая скорость еще ничего не говорит о направлении потока энергии.

> четвертая лекция (5. V 1944 г.)



### Metamaterial

# A lens less ordinary

In the 1960s, a Russian physicist considered the properties of a material that didn't yet exist. Now researchers appear to have fulfilled his predictions — but is everything as it seems? Liesbeth Venema investigates.

here are some truths in physics on which we have come to depend. Light rays, for example, bend when they cross the boundary between two materials. That's why an oar dipped into water appears to bend towards the surface, and why the pool itself looks shallower than it really is.

But this familiar phenomenon, called refraction, is beginning to look less straightforward. In the lab of David Smith, a physicist at the University of California, San Diego, a strange array of metal wires and loops has been pieced together. In April 2001, Smith and his team showed that this construction, which they refer to as a 'metamaterial', has a peculiar property: it bends electromagnetic waves in the opposite direction to normal materials<sup>1</sup>.

If a pool of water had this property, known as negative refraction, oars would bend away from the surface, and the pool







### Light propagation in negative index material







### Split ring resonators

 J.B. Pendry et al., IEEE transactions on microwave theory and techniques 47, 2075 (1999).



Effective magnetic permeability









### Coordinate transform

• G.R. Newkome et al., Science 312, 1782 (2006).



When the coordinate is transformed, the Maxwell equations have exactly the same form but the  $\varepsilon$  and  $\mu$  are scaled by a common factor. Seoul National University

### Basic concept of cloaking



Any radiation attempting to penetrate the secure volume is smoothly guided around by the cloak to emerge traveling in the same direction as if it had passed through the empty volume of space.

$$region r < R_2 \longrightarrow region R_1 < r < R_2$$

$$r' = R_1 + r(R_2 - R_1) / R_2$$
$$\theta' = \theta$$
$$\phi' = \phi$$

$$\varepsilon'_{r'} = \mu'_{r'} = \frac{R_2}{R_2 - R_1} \frac{(r' - R_1)^2}{r'}$$
$$\varepsilon'_{\theta'} = \mu'_{\theta'} = \frac{R_2}{R_2 - R_1}$$
$$\varepsilon'_{\phi'} = \mu'_{\phi'} = \frac{R_2}{R_2 - R_1}$$





### Simulation of cloaking structures



A : Ideal parameter & lossless C : 8-layers approximation Seoul National University

- **B** : Ideal parameter & lossy
- D : Reduced approximation

### Microwave cloaking structure

### D. Schurig et al., Science, in press (2006).









#### Remark

### 레이저가 늦게 발명된 이유



#### Charles H. Townes (1915-)

"대부분의 물리학자들은 전자공학과 증폭기에 대해서 몰랐었고, 전기공학자들은 대개 양자역학을 배우지 않았다. 하지만 제 2차 세계대전으로 인해 레이다 (radar) 개발을 위해 공학자들과 자연과학자들이 함께 일하게 되었고, 물리학자들이 전자공학에 접근할 수 있게 되었다."

(*IEEE J. Selected Topics in Quantum Electronics*, Nov./Dec. issue, 2000)







"...If it were possible to introduce at every part of the aperture of the grating an arbitrary retardation, all the light might be concentrated in any desired spectrum. By supposing the retardation to vary uniformly and continuously we fall upon the case of an ordinary prism; but there is then no diffraction spectrum in the usual sense. To obtain such it would be necessary that the retardation should gradually alter by a wave-length in passing over any element of the grating, and then fall back to its previous value, thus springing suddenly over a wave-length. It is not likely that such a result will ever be fully attained in practice; but the case is worth stating, in order to show that there is no theoretical limit to the concentration of light of assigned wave-length in one spectrum..."

Encylopaedia Britannica, 9<sup>th</sup> ed., Vol. 24, "Wave Theory of Light" (New York, Charles Schribner's Sons, 1888), p. 437



