2019 Spring

"Phase Equilibria *in* Materials"

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Chapter 10. Ternary phase Diagrams

Four-Phase Equilibrium

a. THE TERNARY EUTECTIC EQUILIBRIUM ($l = \alpha + \beta + \gamma$)

b. THE QUASI-PERITECTIC EQUILIBRIUM ($l + \alpha = \beta + \gamma$)

c. THE TERNARY PERIECTIC EQUILIBRIUM ($l + \alpha + \beta = \gamma$)

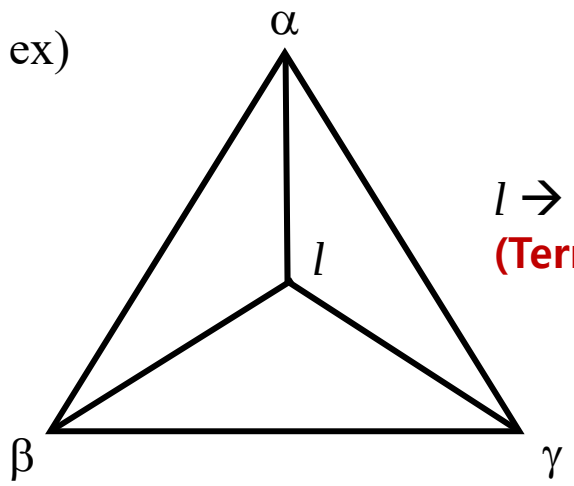
10.1. THE EUTECTIC EQUILIBRIUM ($l = \alpha + \beta + \gamma$)

Three phase equil. (*f* = 1) - eutectic, peritectic

Now we consider of four-phase equilibrium

- **max *N* of phase**
- ***f* = 0** : composition of four phases at temp.→ fixed
- **isothermal four phase regions**

ex)



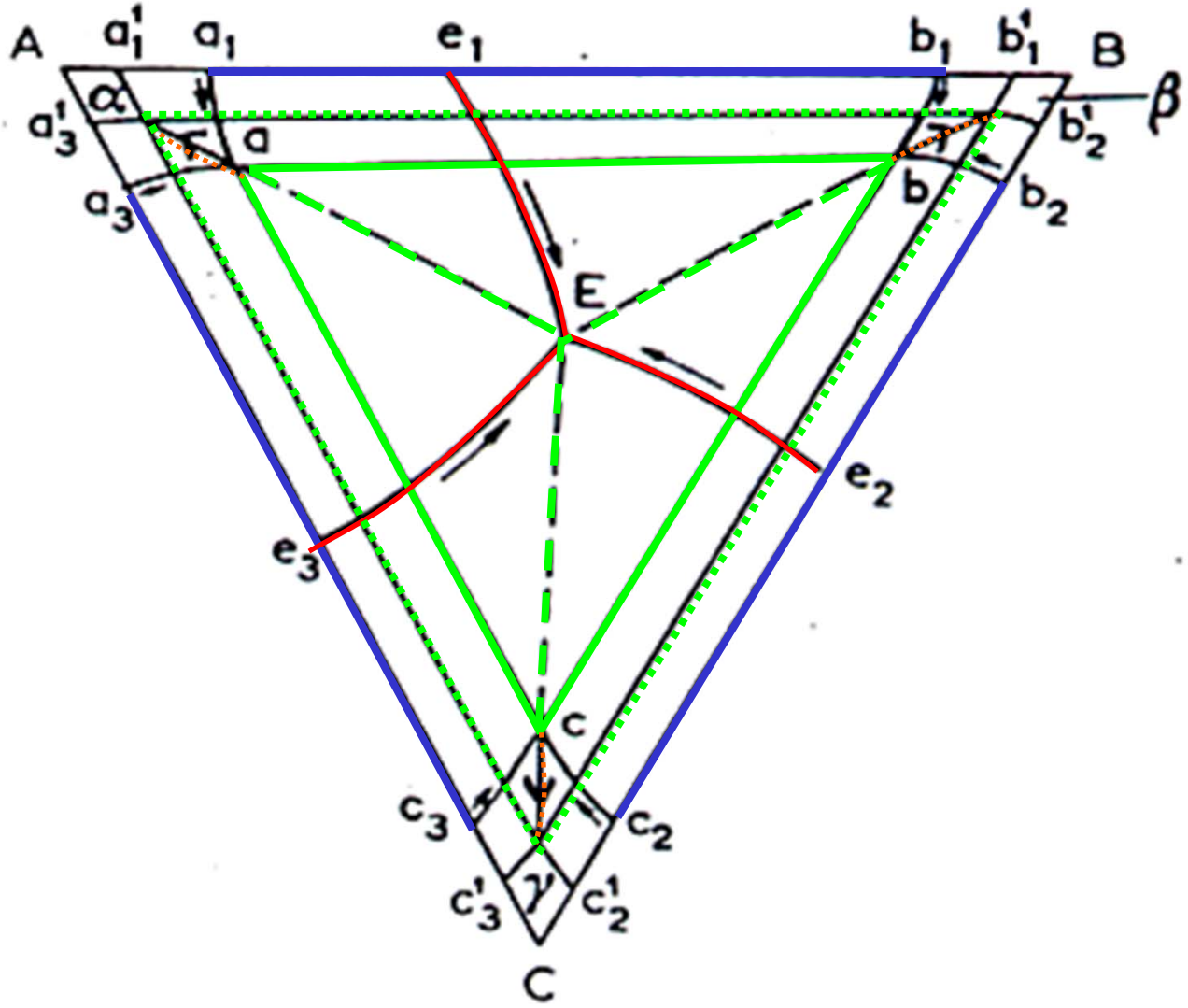
$l \rightarrow \alpha + \beta + \gamma$
(Ternary eutectic)

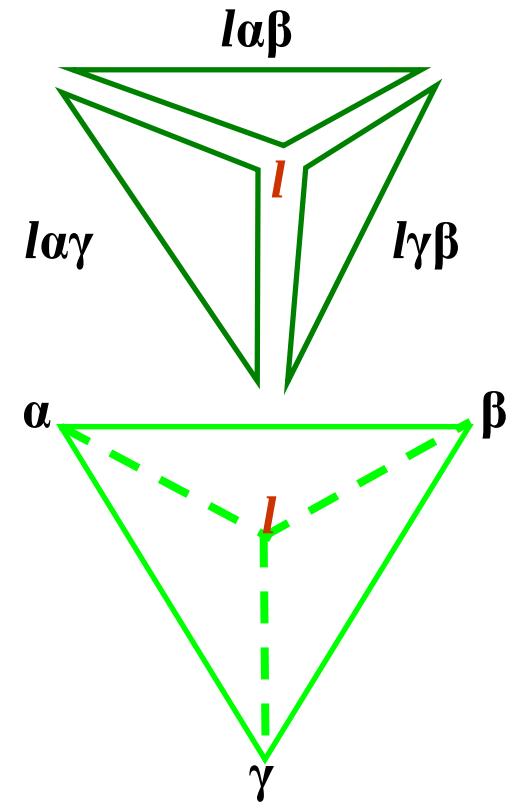
cf) $l + \alpha \rightarrow \beta + \gamma$: **ternary quasi-peritectic**

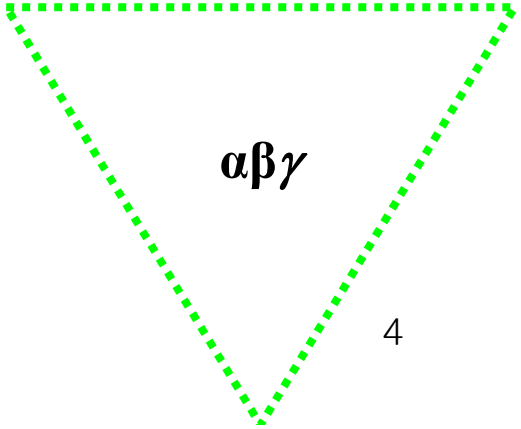
$l + \alpha + \beta \rightarrow \gamma$: **ternary peritectic**

THE TERNARY EUTECTIC EQUILIBRIUM ($l = \alpha + \beta + \gamma$)

- **Projection** : solid solubility limit surface
  : monovariant liquidus curve

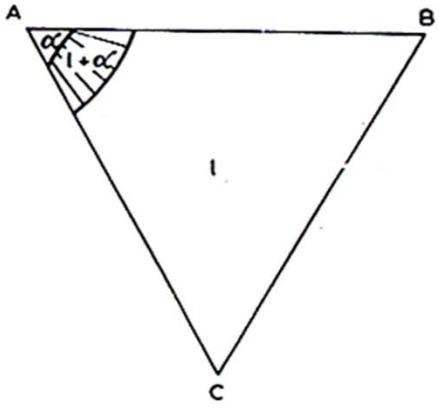




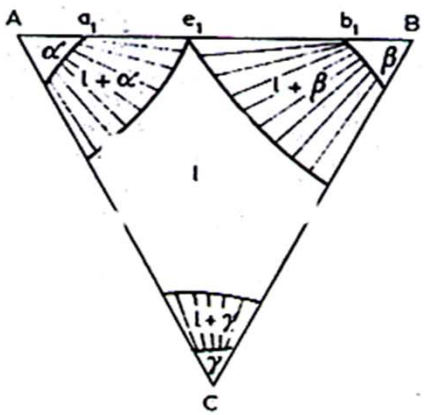


10.1. THE EUTECTIC EQUILIBRIUM (l = α + β + γ)

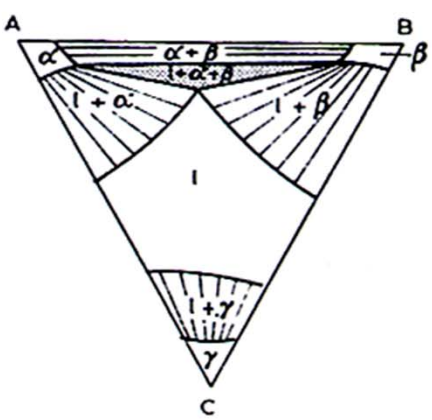
- **Isothermal section** ($T_A > T > T_B$)



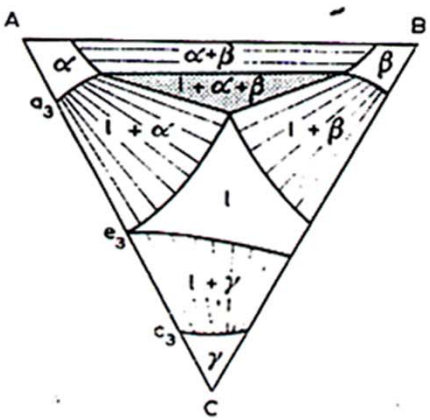
(a) $T_A > T > T_B$



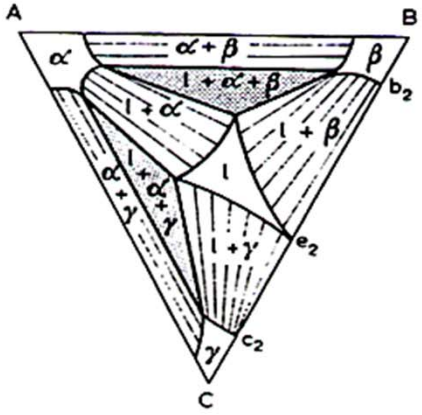
(b) $T = e_1$



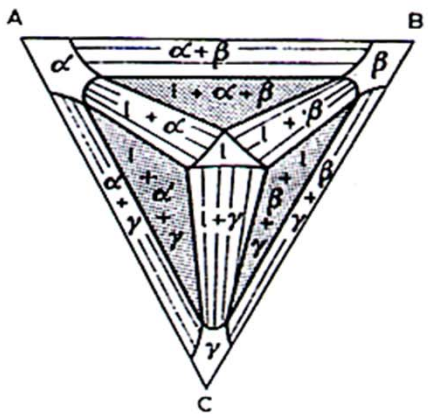
(c) $e_1 > T > e_3$



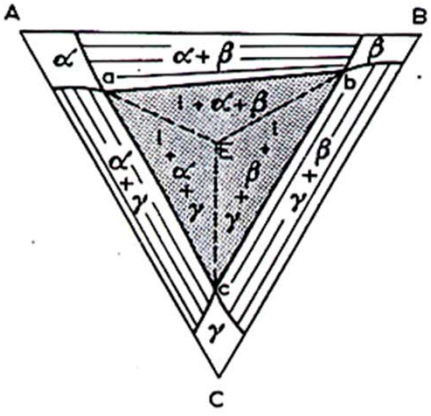
(d) $T = e_3$



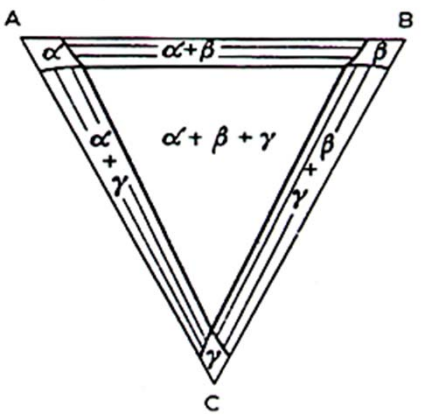
(e) $T = e_2$



(f) $e_2 > T > E$



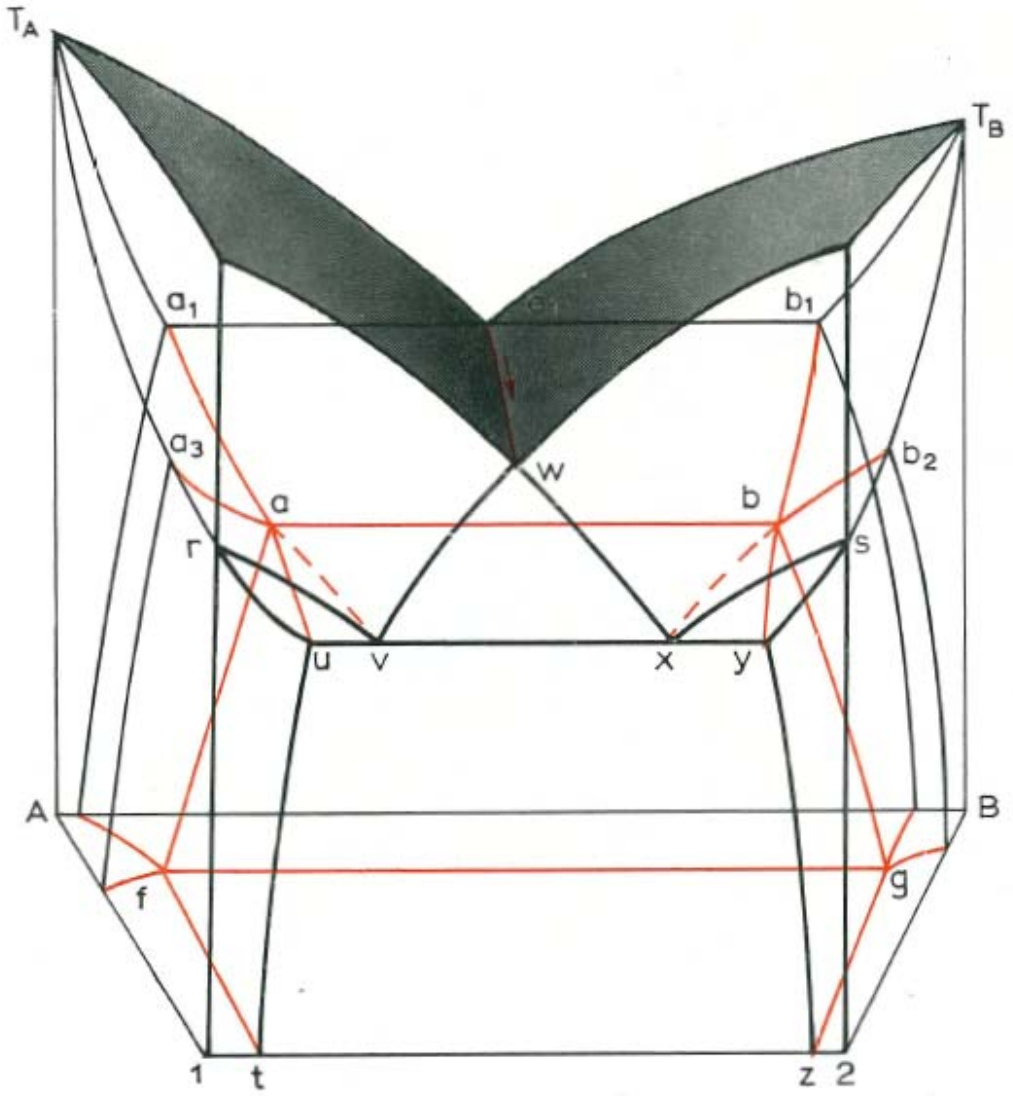
(g) $T_A = E$



(h) E = T

10.1. THE EUTECTIC EQUILIBRIUM ($l = \alpha + \beta + \gamma$)

Vertical section **Location of vertical section**



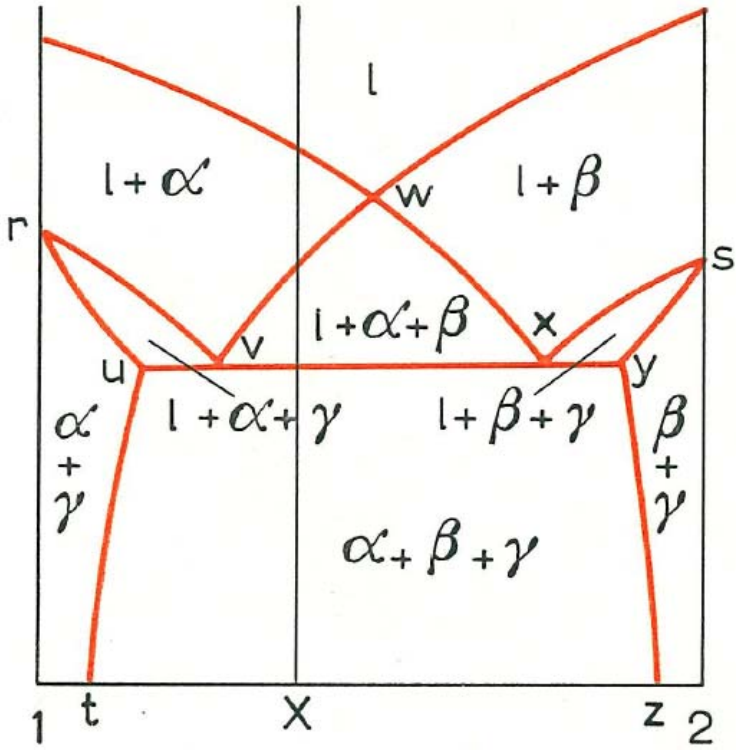
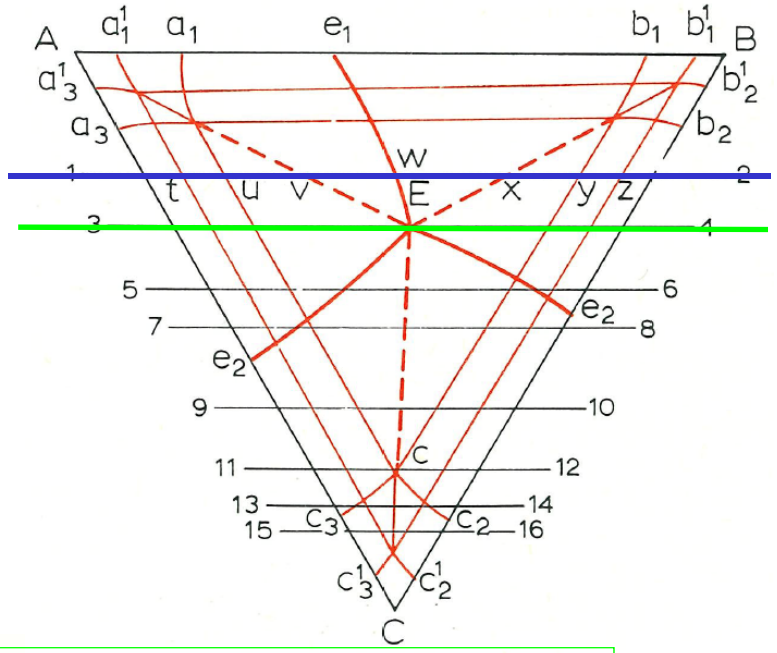


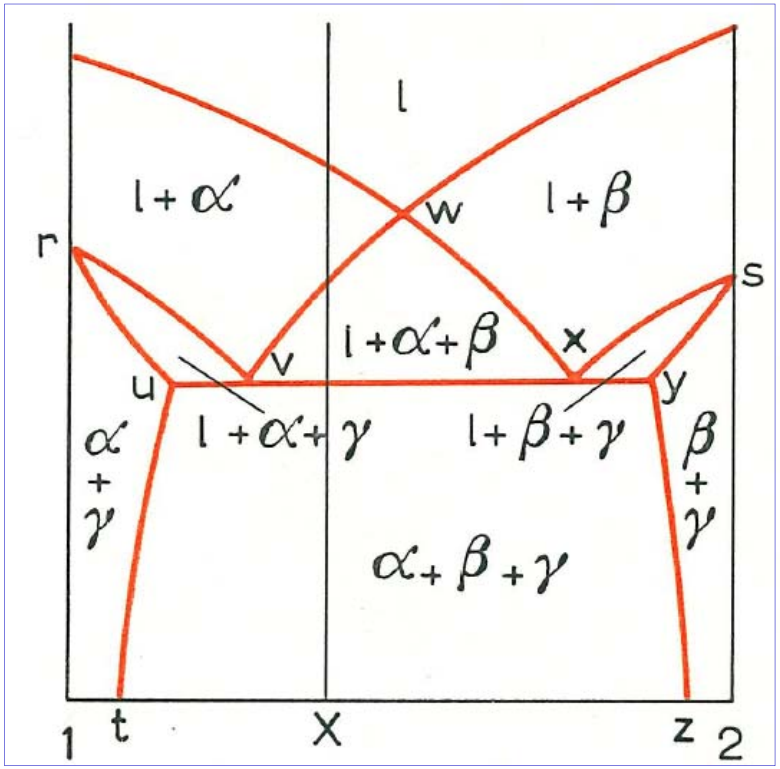
Fig. 179. Construction of vertical section 1–2.

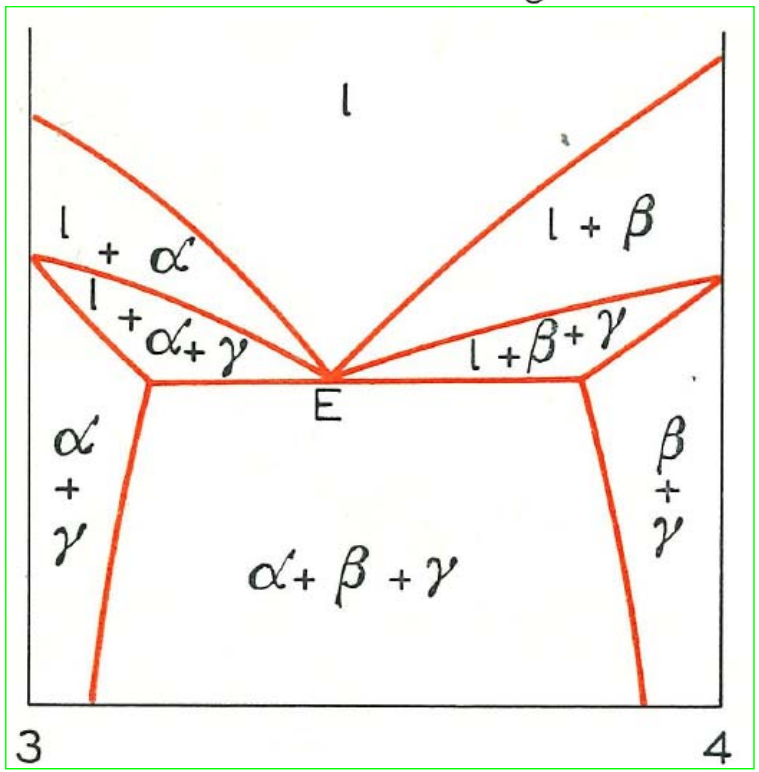
10.1. THE EUTECTIC EQUILIBRIUM

$(l = \alpha + \beta + \gamma)$

Vertical section **Location of vertical section**

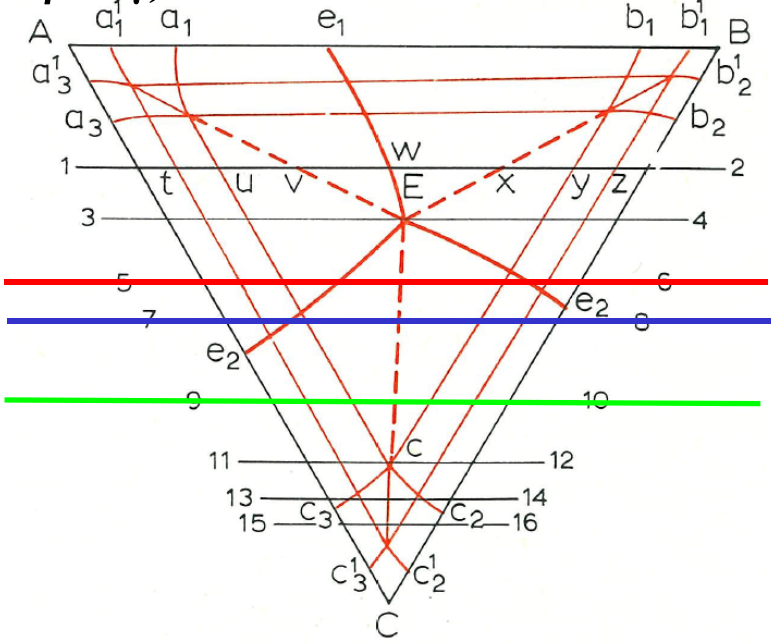


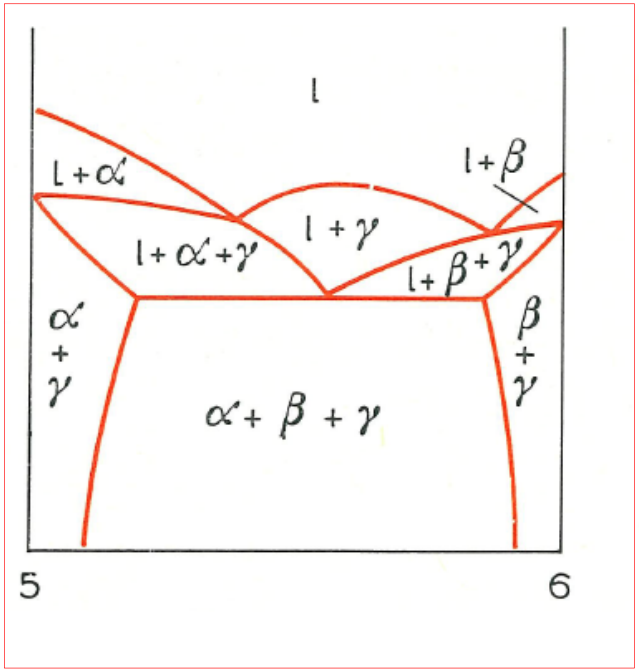


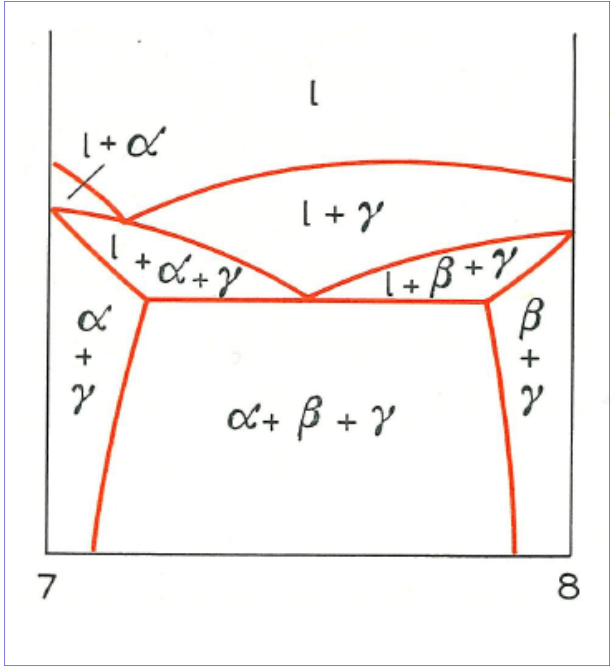


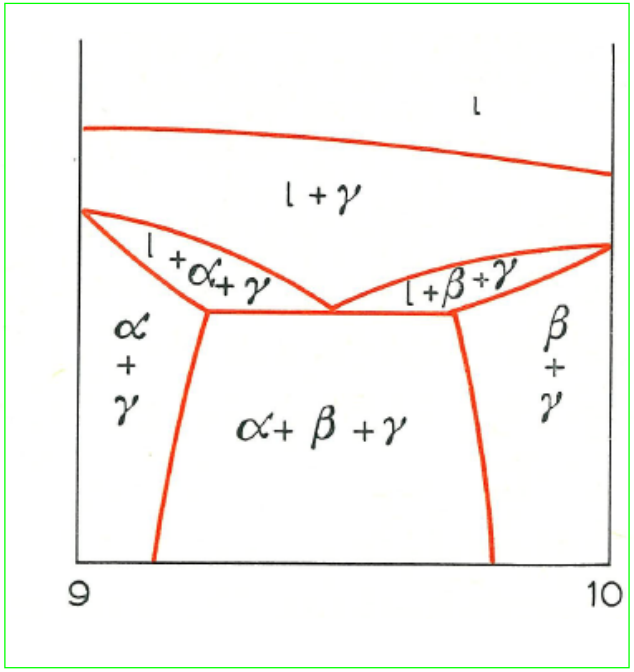
10.1. THE EUTECTIC EQUILIBRIUM ($l = \alpha + \beta + \gamma$)

Vertical section **Location of vertical section**



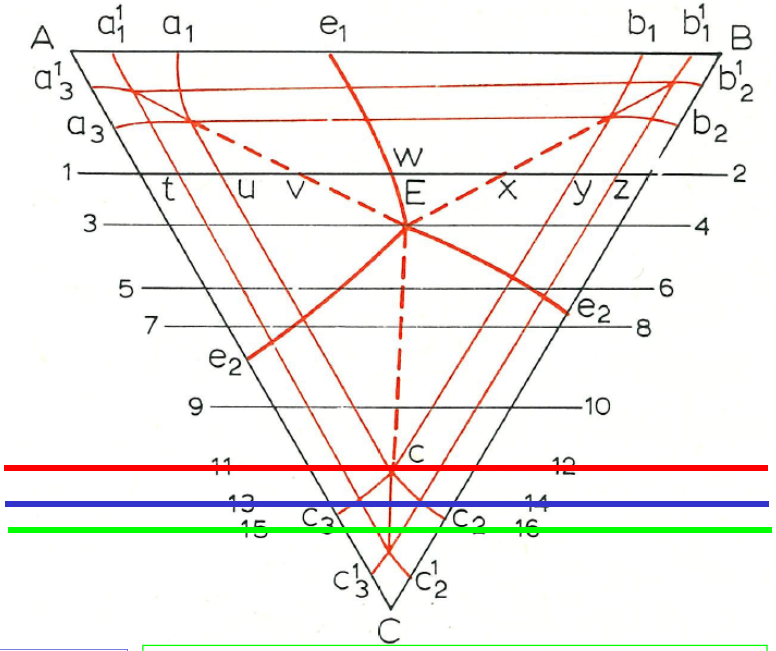


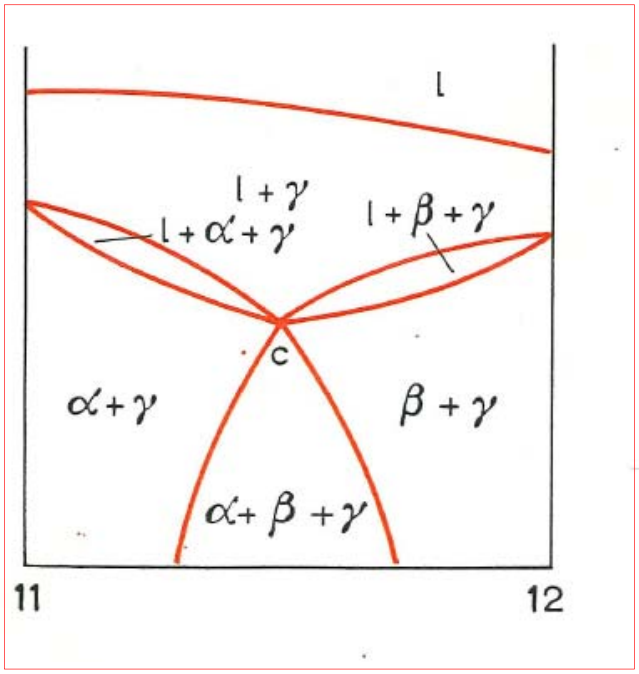


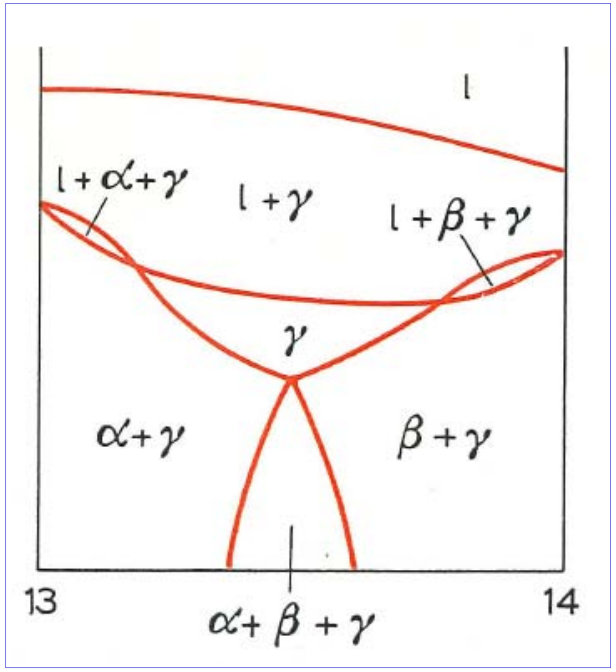


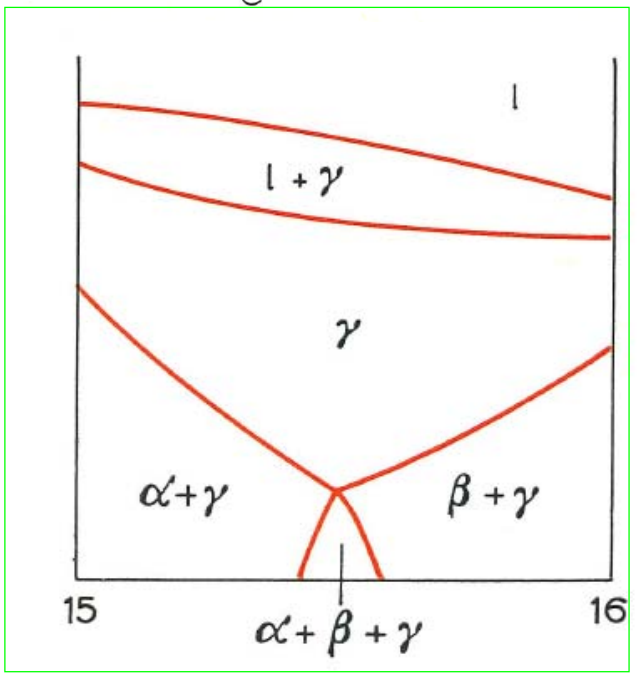
10.1. THE EUTECTIC EQUILIBRIUM ($l = \alpha + \beta + \gamma$)

Vertical section **Location of vertical section**

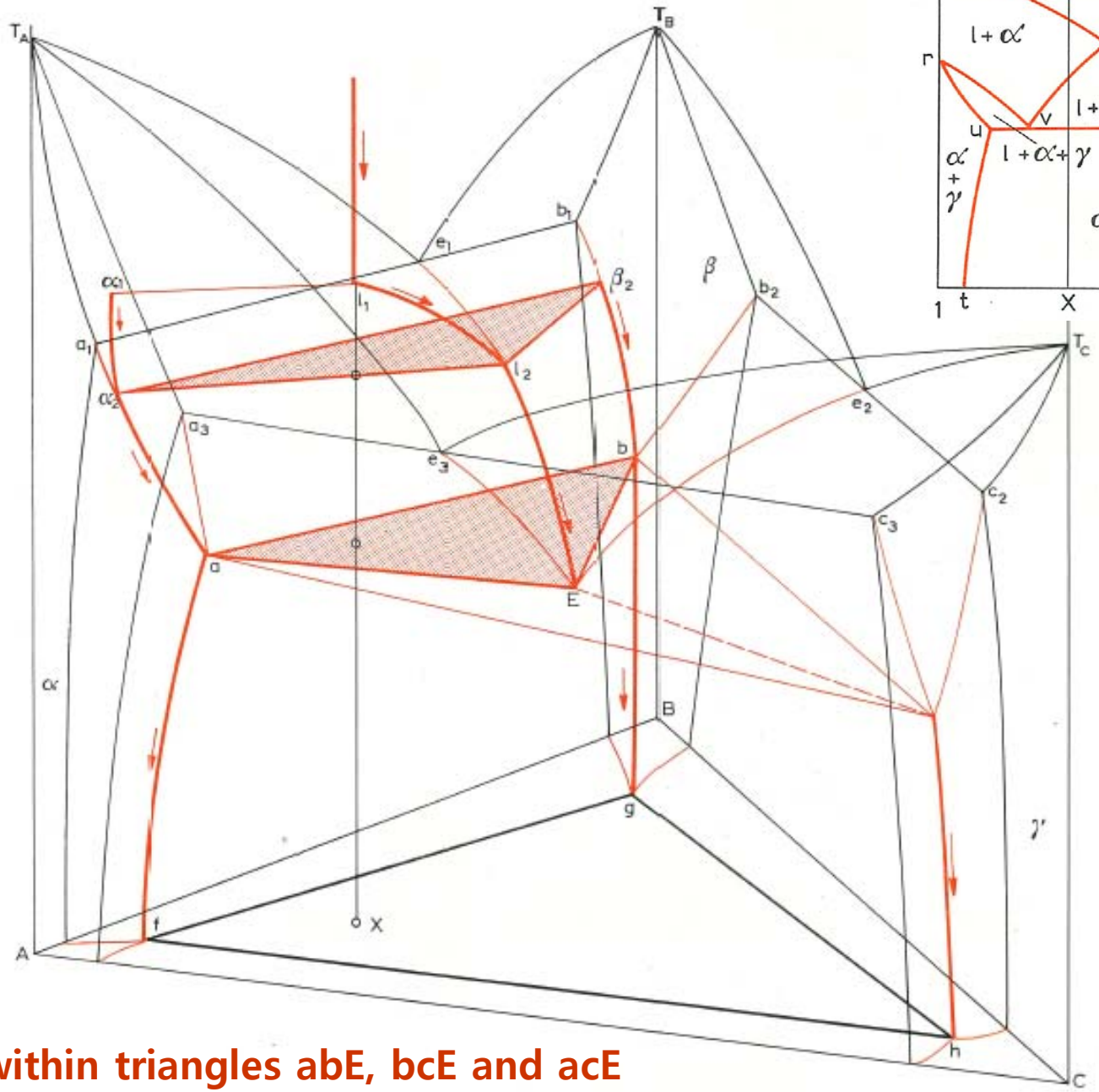


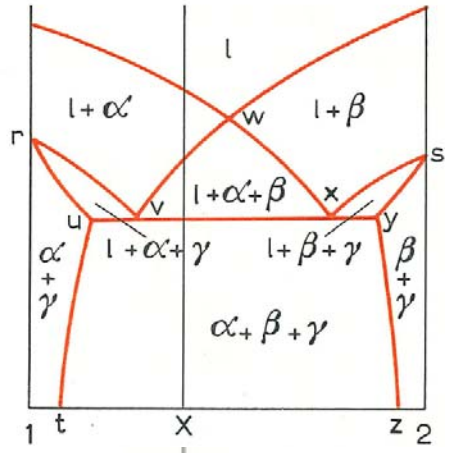






Transformation during cooling



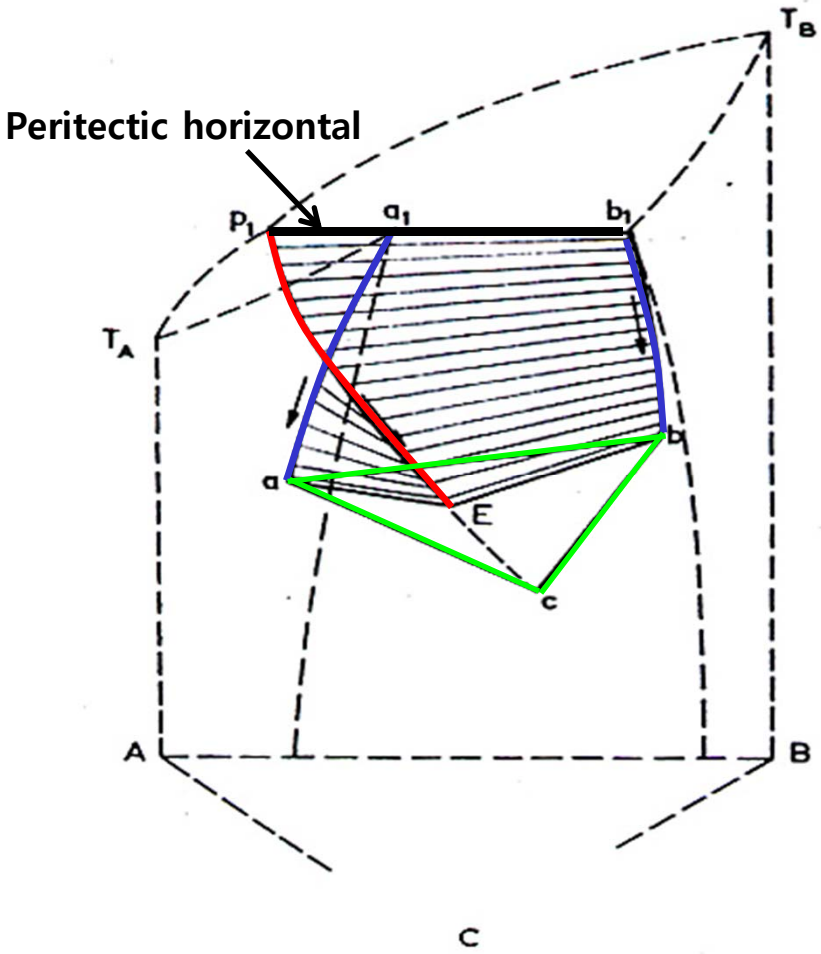


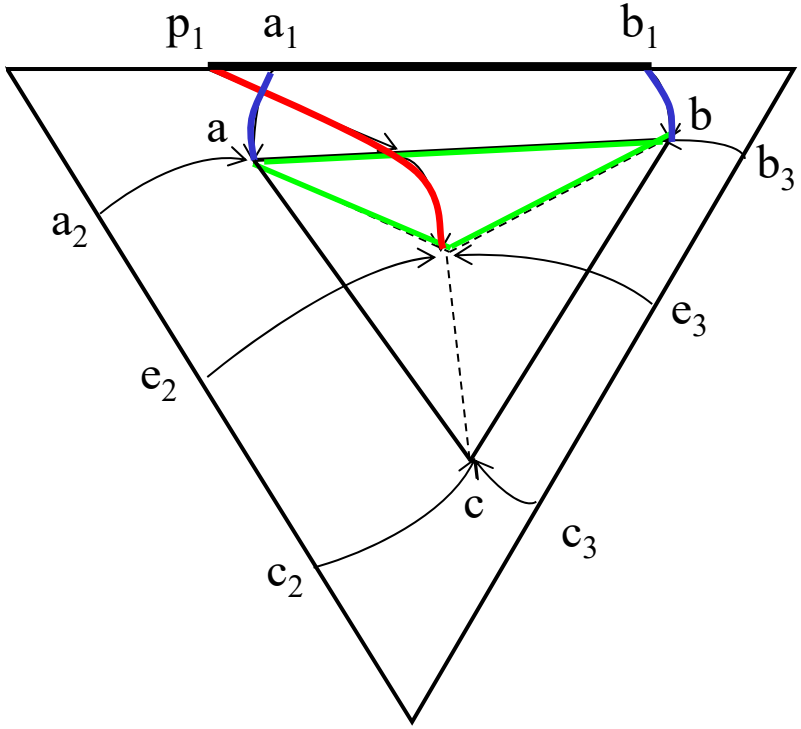
④ **Alloys within triangles abE, bcE and acE**

ex) abE: $l + \alpha$ (or β) → $l + \alpha + \beta$ → (l → $\alpha + \beta + \gamma$ at T_E)

10.2. VARIANTS OF THE TERNARY EUTECTIC DIAGRAM

(a) Variant of the ternary eutectic system in which one binary is a peritectic



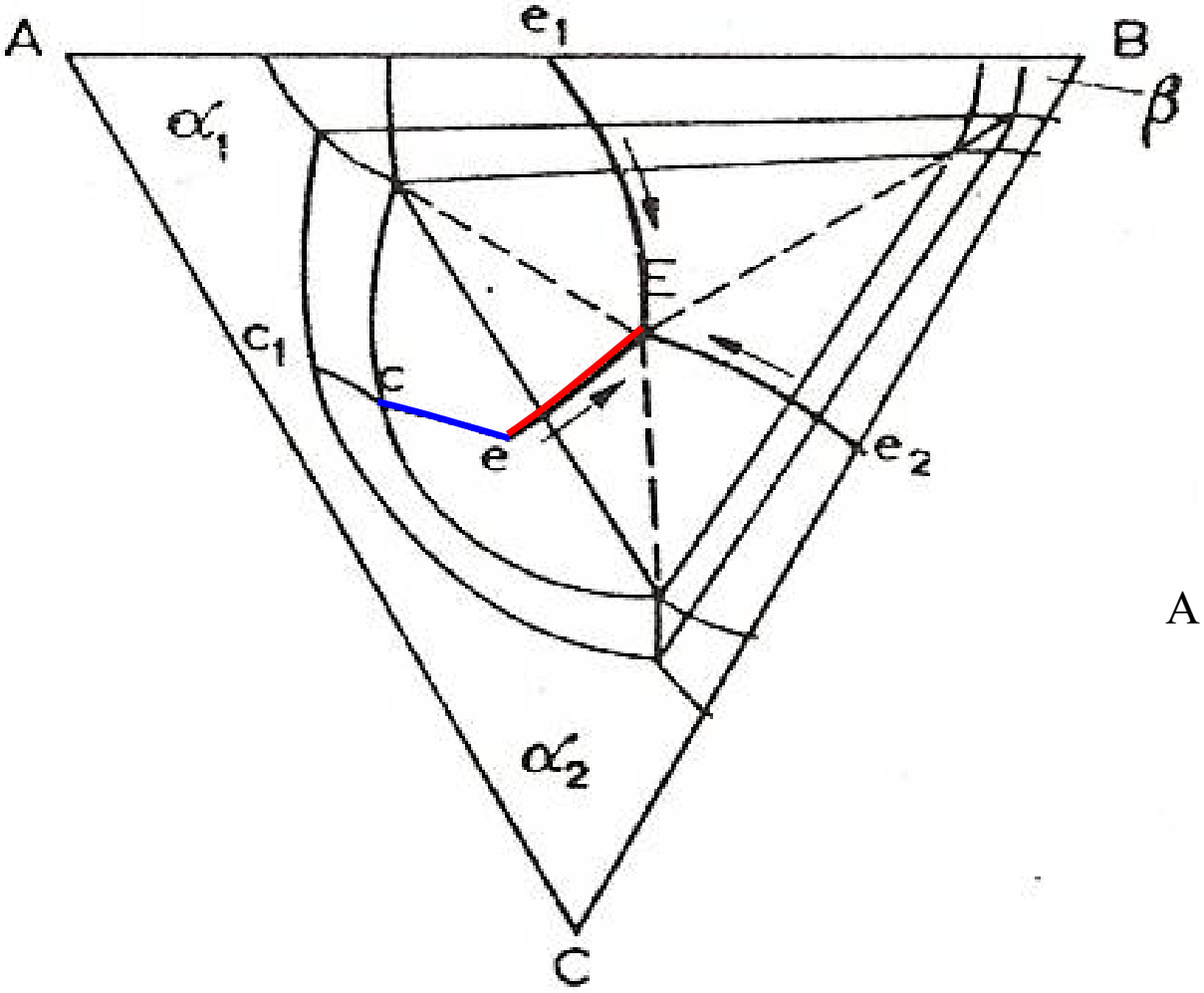


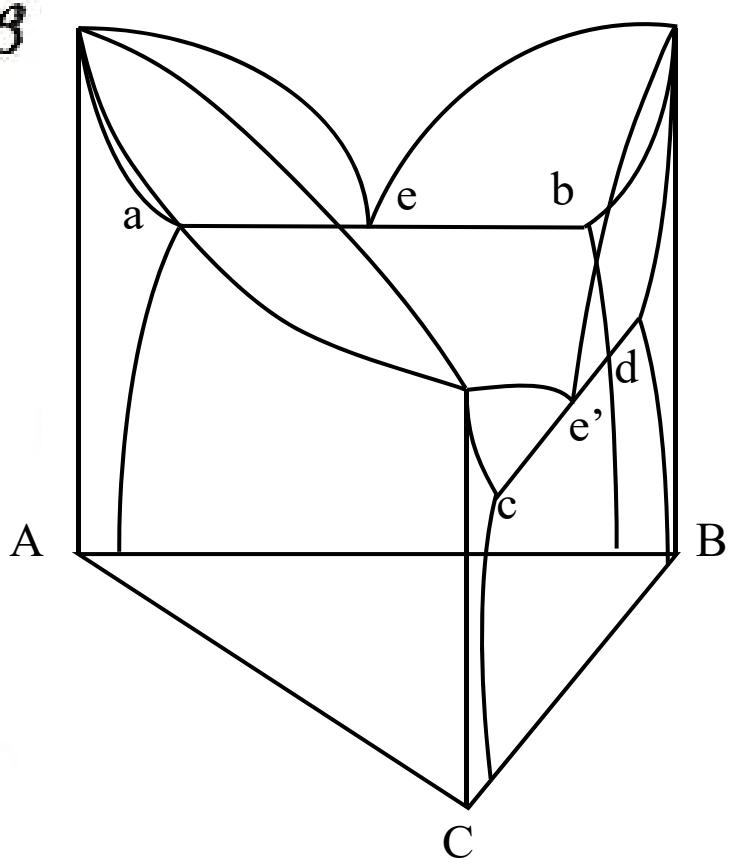
Monovariant liquidus line (P_1E) lies above monovariant solidus line (a_1a).

→ **A ternary eutectic can be produced with one, two or three binary peritectic systems.**

10.2. VARIANTS OF THE TERNARY EUTECTIC DIAGRAM

(b) Ternary eutectic system
in which two of the binary eutectics and one of ternary miscibility gap exist.



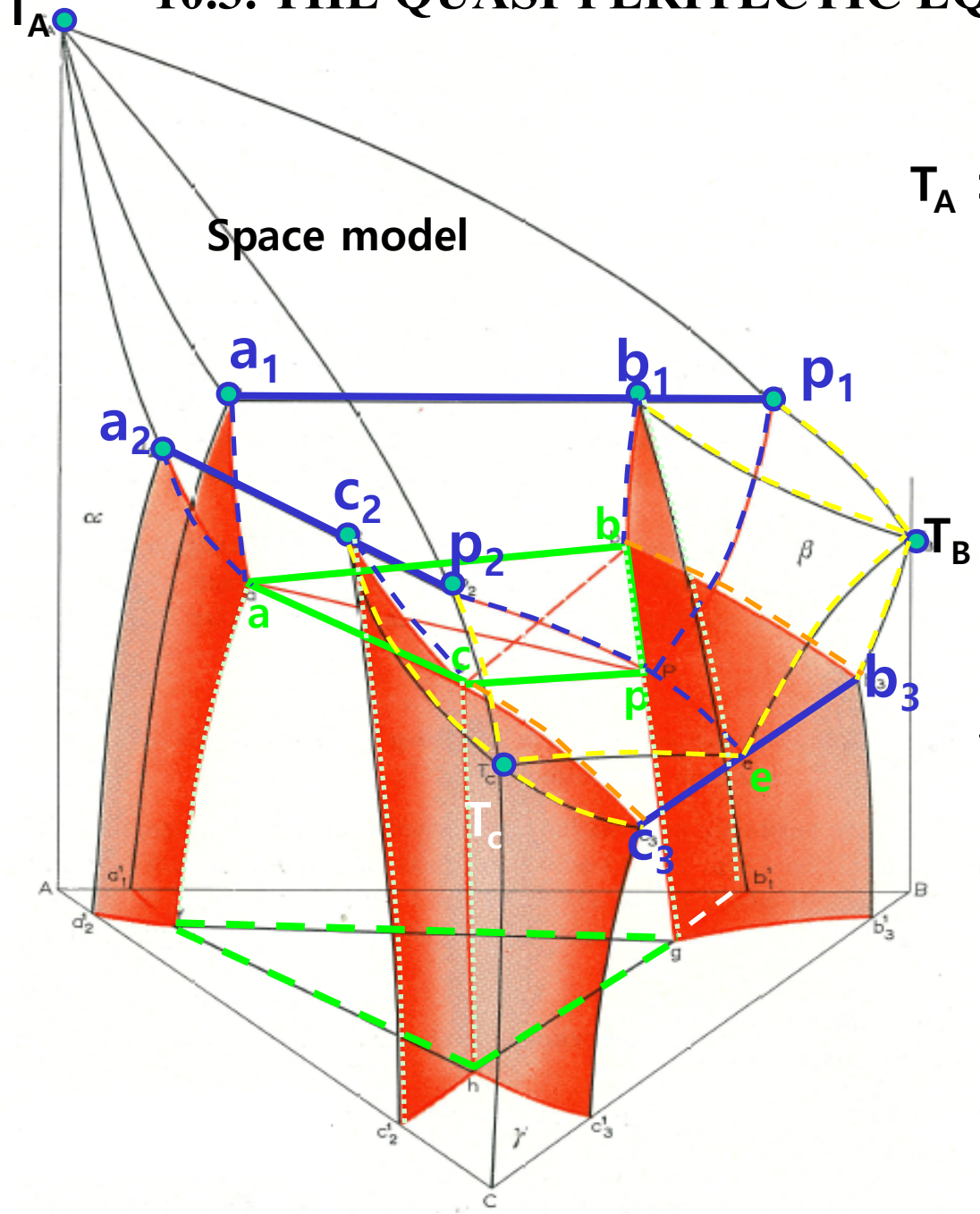


<one complete solid solution + two binary eutectic>

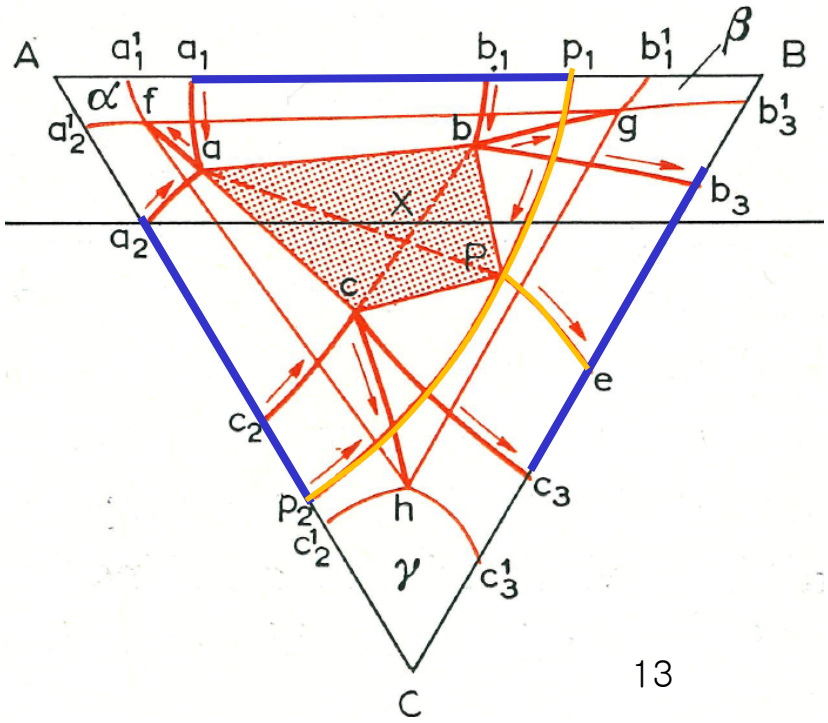
10.3. THE QUASI-PERITECTIC EQUILIBRIUM ($l + \alpha = \beta + \gamma$)

$T_A > P_1 > P_2 > T_B > P > T_C > e$

Space model

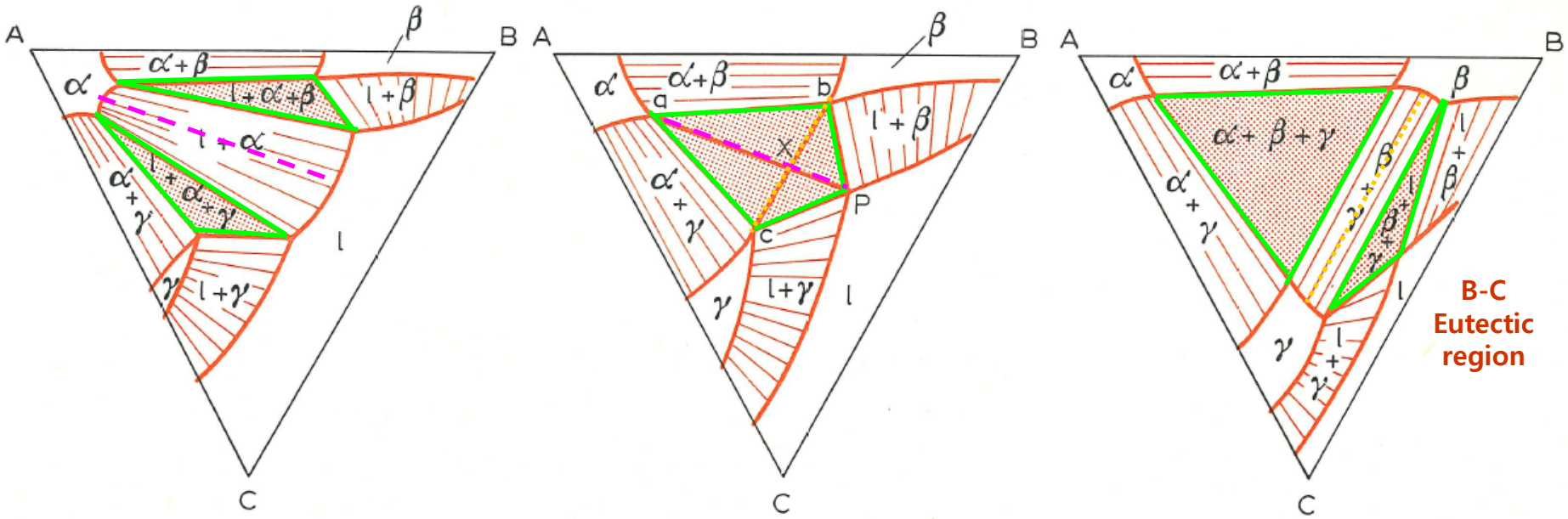


Projection



10.3. THE QUASI-PERITECTIC EQUILIBRIUM ($l + \alpha = \beta + \gamma$)

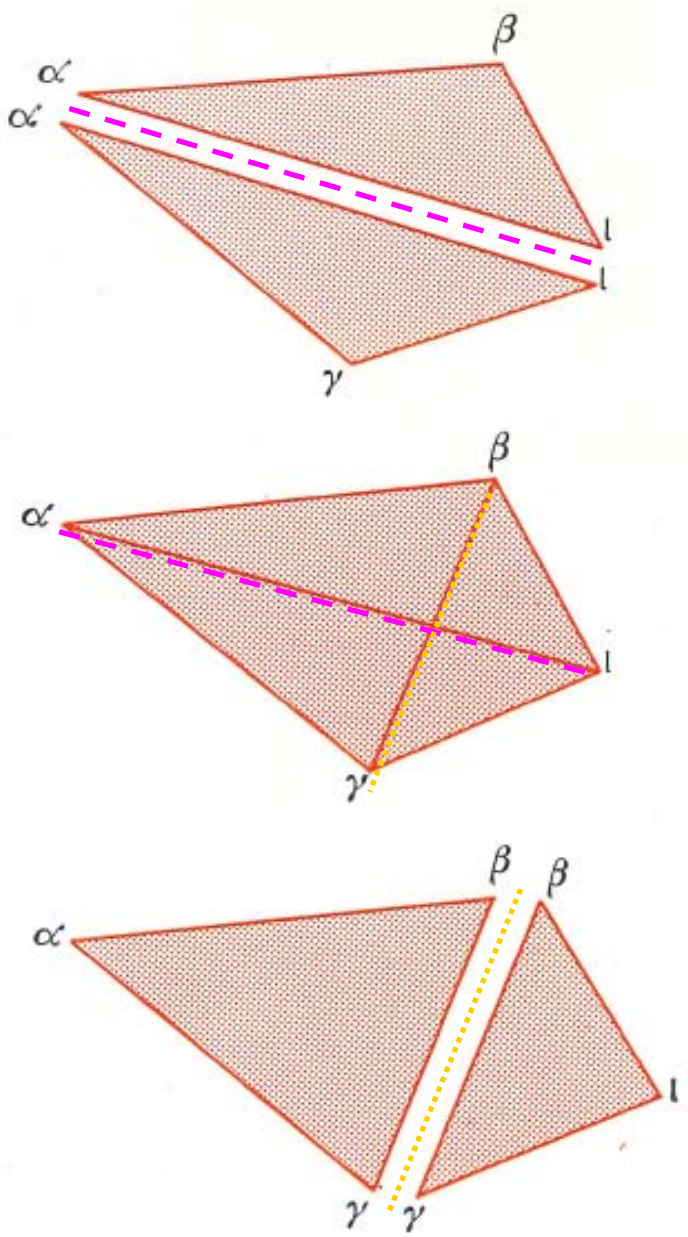
Isothermal section



$T_B > T > P$ $\qquad$ $T = P$ $\qquad$ $P > T > T_C$

abP	peritectic	$l\alpha\beta$ equilibrium	descending to the four-phase plane;
acP	peritectic	$l\alpha\gamma$ equilibrium	
bcP	eutectic	$l\beta\gamma$ equilibrium	descending from the four-phase plane.
abc		$\alpha\beta\gamma$ equilibrium	

10.3. THE QUASI-PERITECTIC EQUILIBRIUM ($l + \alpha = \beta + \gamma$)



Both three phase monovariant equilibria preceding the quasi-peritectic reaction are peritectic

abP peritectic lαβ equilibrium

acP peritectic lαγ equilibrium

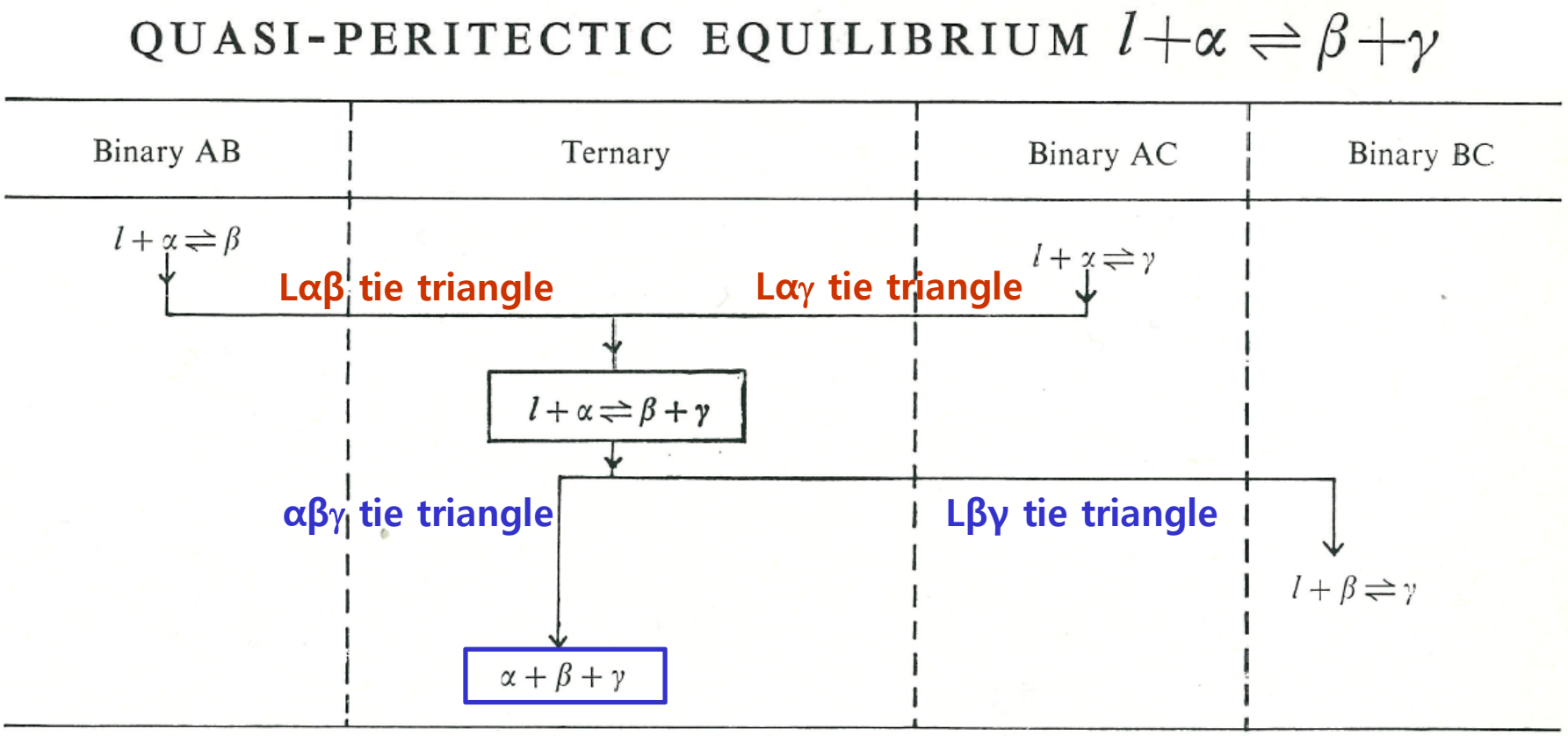
decreasing temperature

bcP eutectic lβγ equilibrium

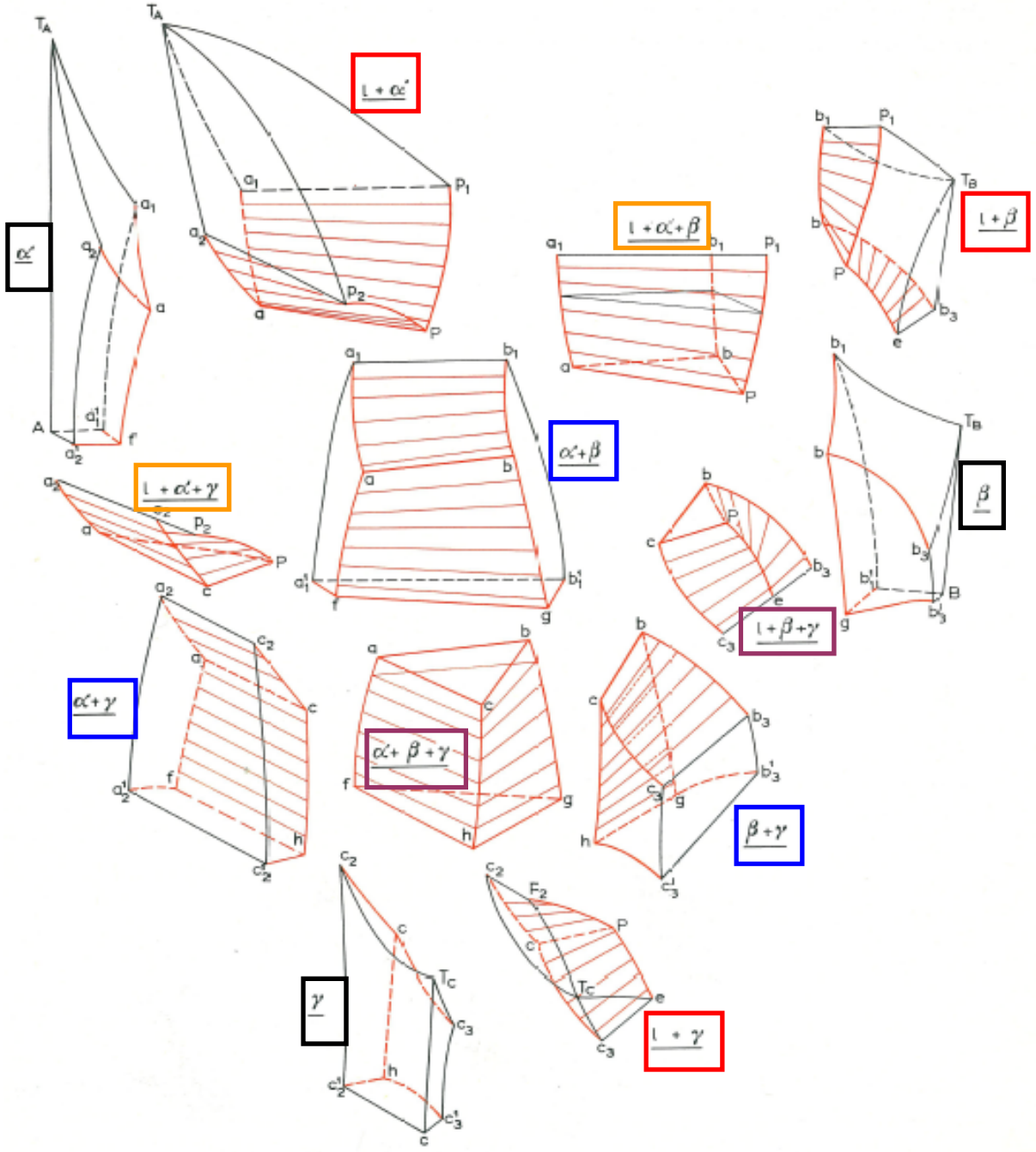
abc peritectic αβγ equilibrium

Tabular representation of ternary equilibria:

interlinks the binary and ternary reactions in tabular form

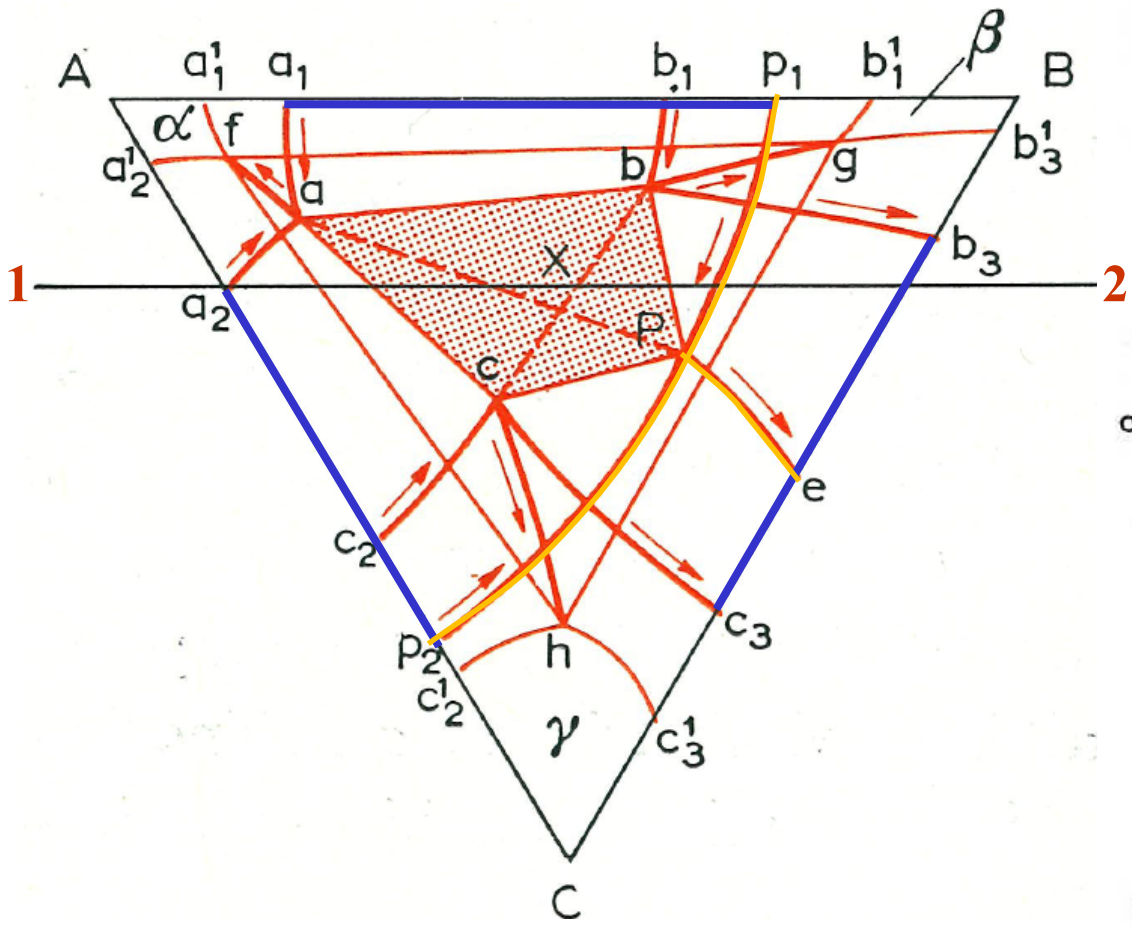


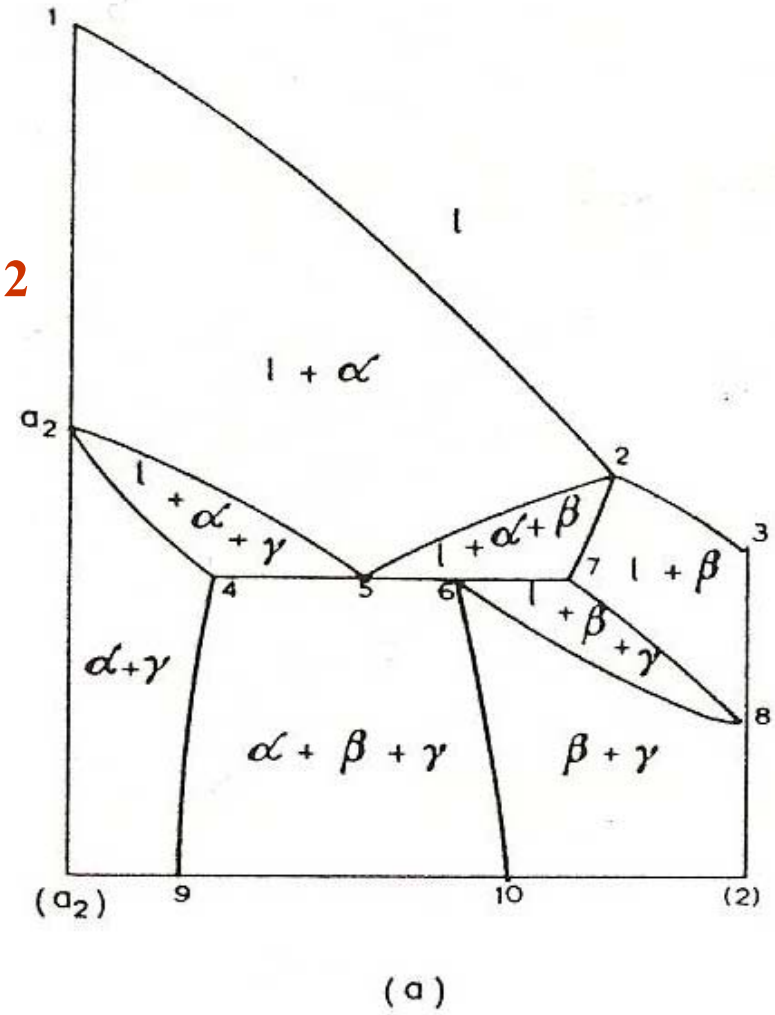
10.3. THE QUASI-PERITECTIC EQUILIBRIUM ($l + \alpha = \beta + \gamma$)



10.3. THE QUASI-PERITECTIC EQUILIBRIUM ($l + \alpha = \beta + \gamma$)

Vertical section

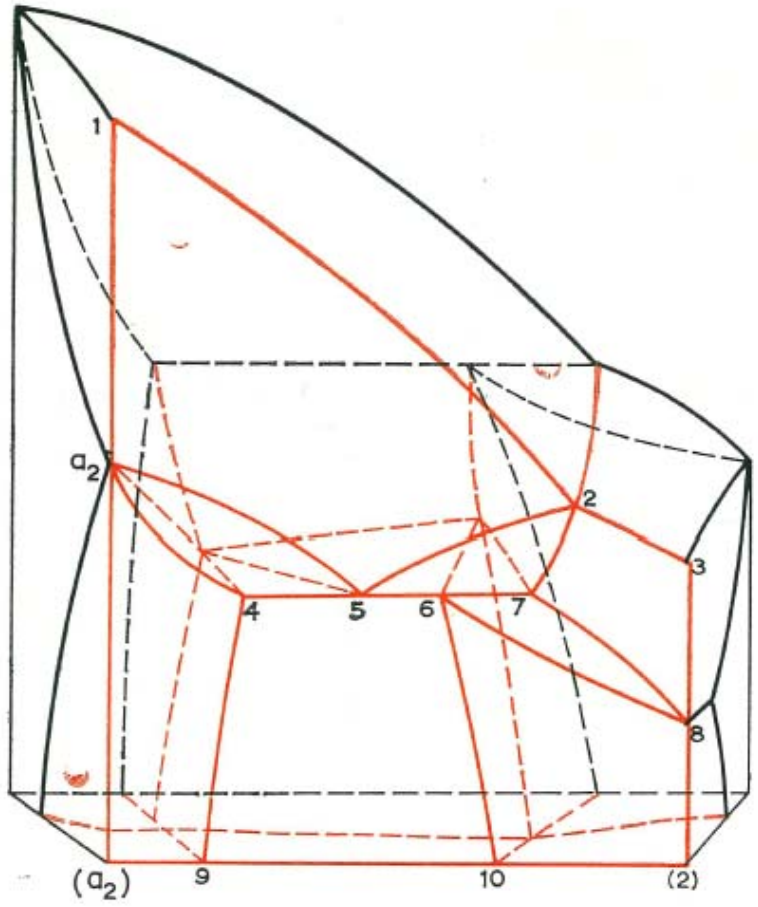




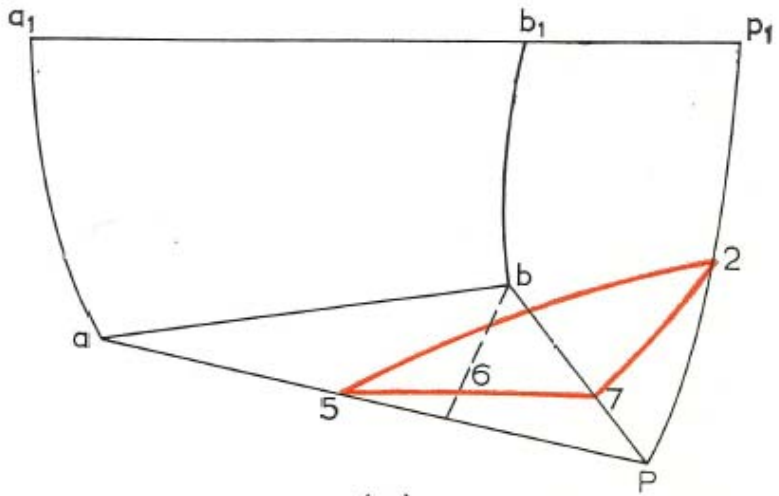
(a)

10.3. THE QUASI-PERITECTIC EQUILIBRIUM ($l + \alpha = \beta + \gamma$)

Vertical section



(b)



(c)

Fig. 188. A vertical section through the space model of Fig. 185a. (a) The vertical section a_2–2; (b) construction of the vertical section; (c) intersection of the vertical section with the $l+\alpha+\beta$ phase region.

10.3.2. one of the three phase monovariant equilibria preceding the quasi-peritectic reaction is eutectic and one peritectic.

*** Ternary system involving an incogruently-melting binary intermediate phase:**

Quasi-peritectic diagram and ternary eutectic diagram

e.g.* Au-Ge-Sb ternary *in which the δ phase is intermediate phase $AuSb_2$.

$P_1d_1b_1 \rightarrow dbp\ (\delta\beta L)$ / $b_3e_3c_3 \rightarrow bpc\ (\beta L\gamma)$

⇩

$d^1\varepsilon c(\delta + \gamma + L)$ / **gfn(β + δ + γ)**

$d^1\varepsilon c^1(\delta\gamma L)$ / $a_1e_1d_2 \rightarrow a^1\varepsilon d^1(\alpha\delta L)$ / $a_2e_2c_2 \rightarrow a^1\varepsilon c^1(\alpha L\gamma)$

⇩

Jkm (α + γ + δ)

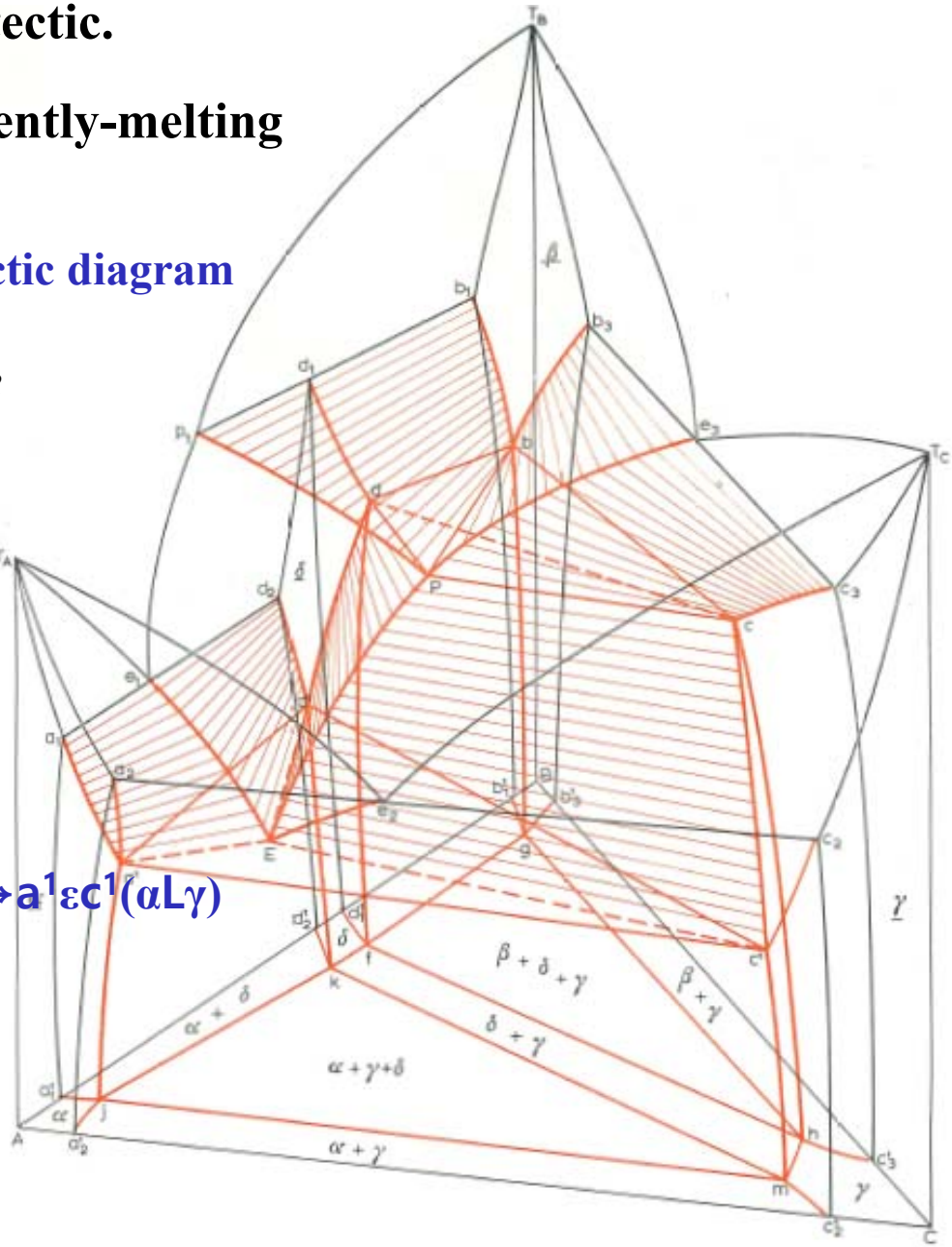
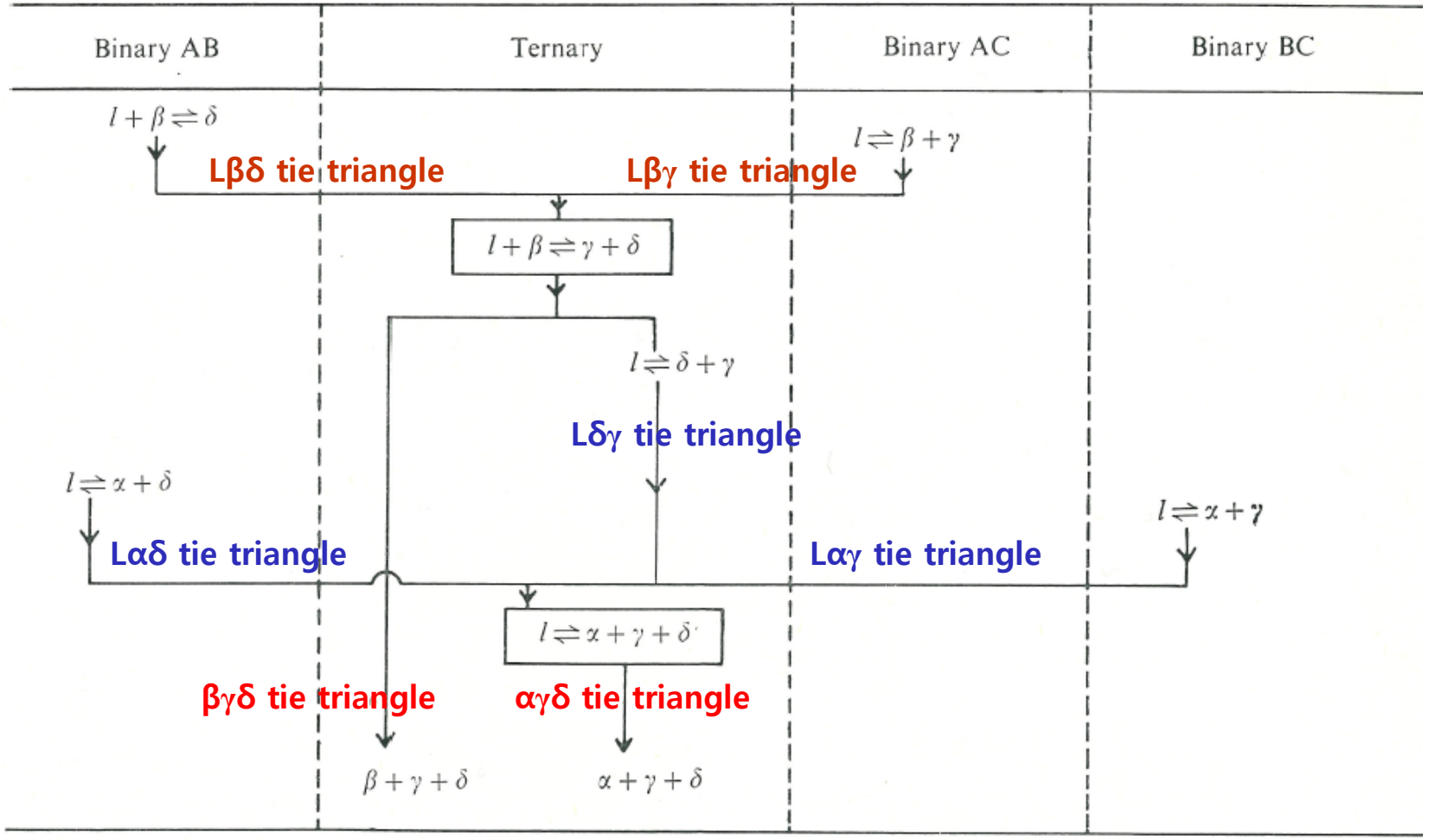


Fig. 189. Ternary system involving an incongruently-melting binary intermediate phase.

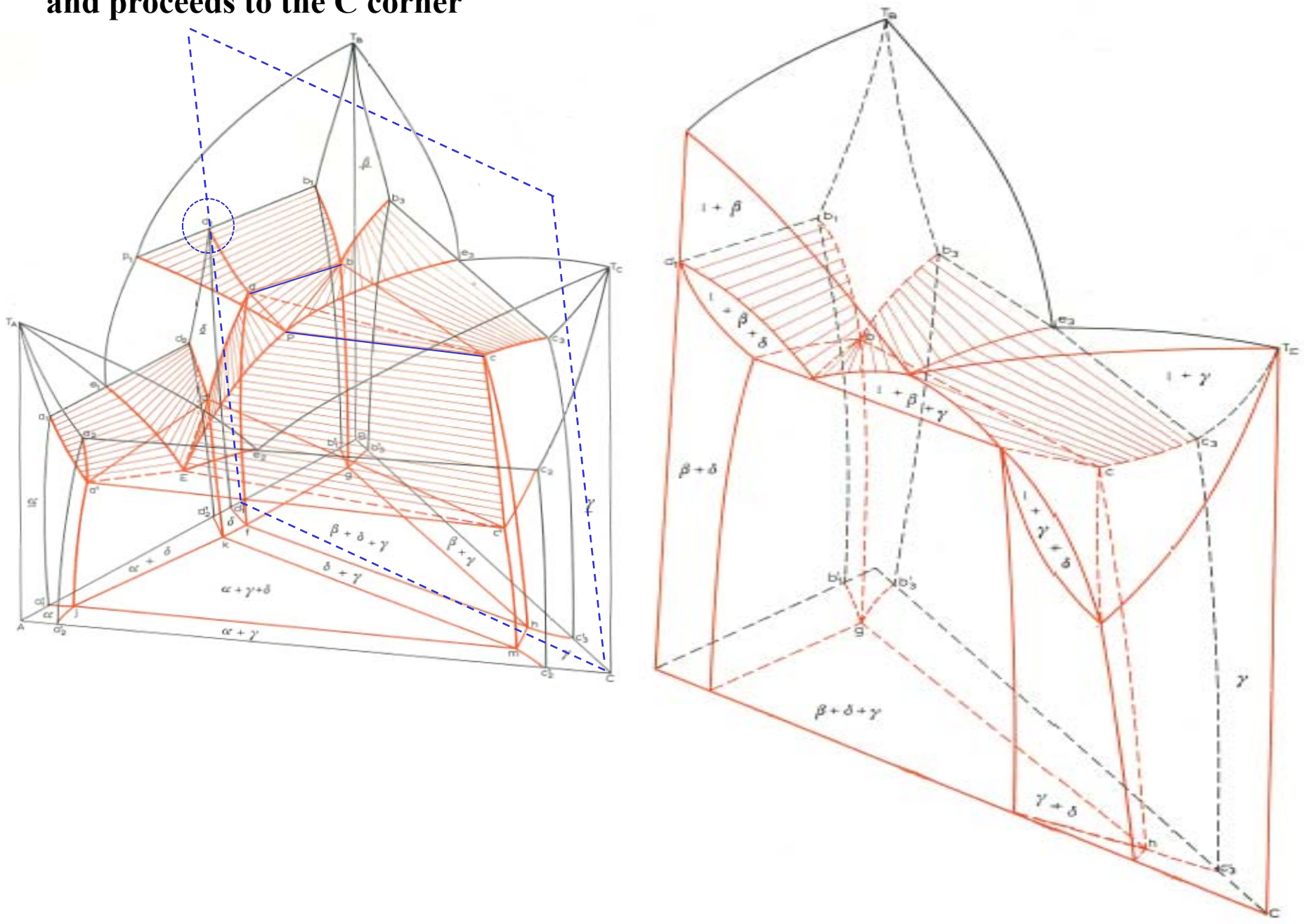
Tabular representation of ternary equilibria:

interlinks the binary and ternary reactions in tabular form

Quasi-peritectic diagram and ternary eutectic diagram

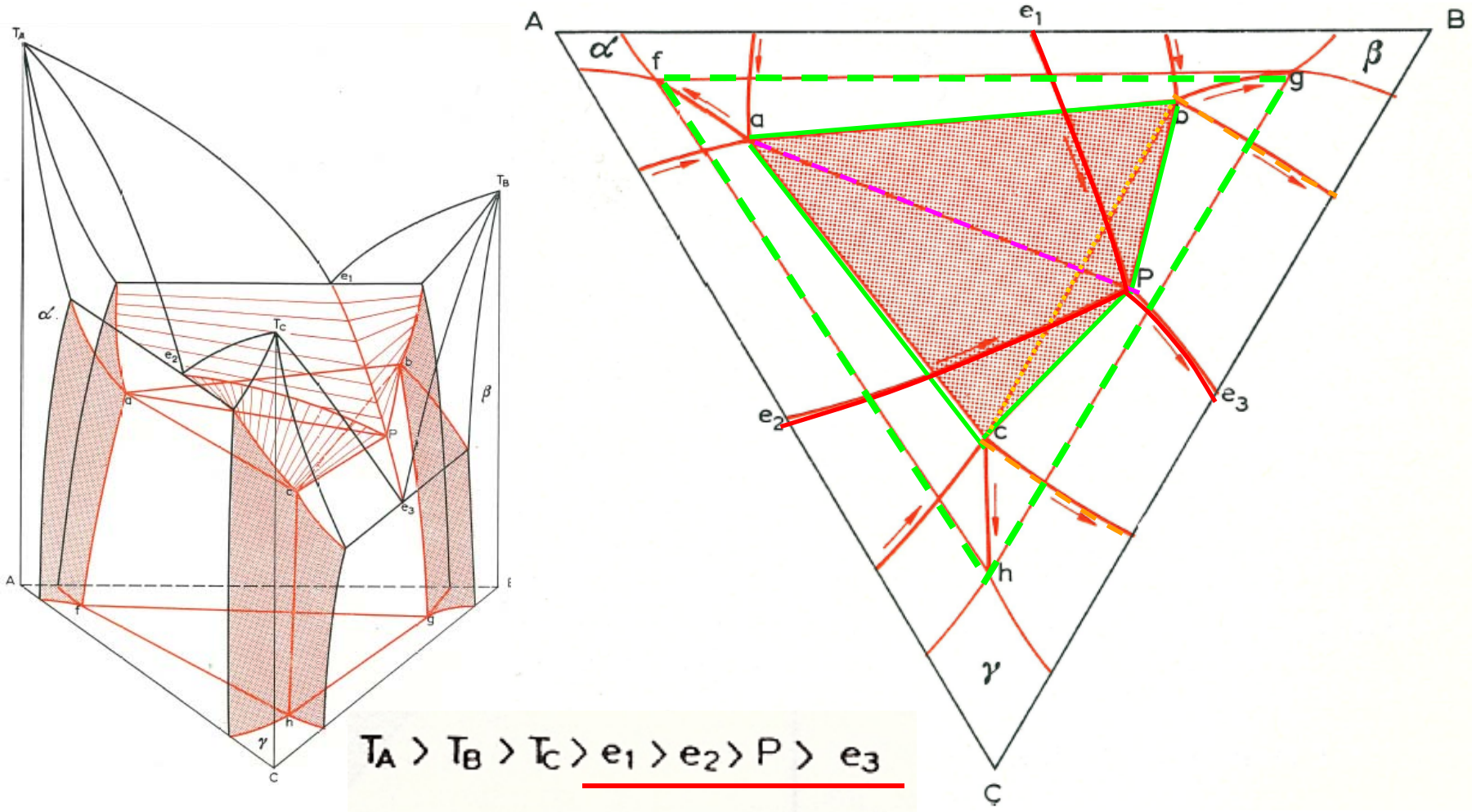


Vertical section **which intersects point d1 on the AB binary, the tie lines db and Pc, and proceeds to the C corner**

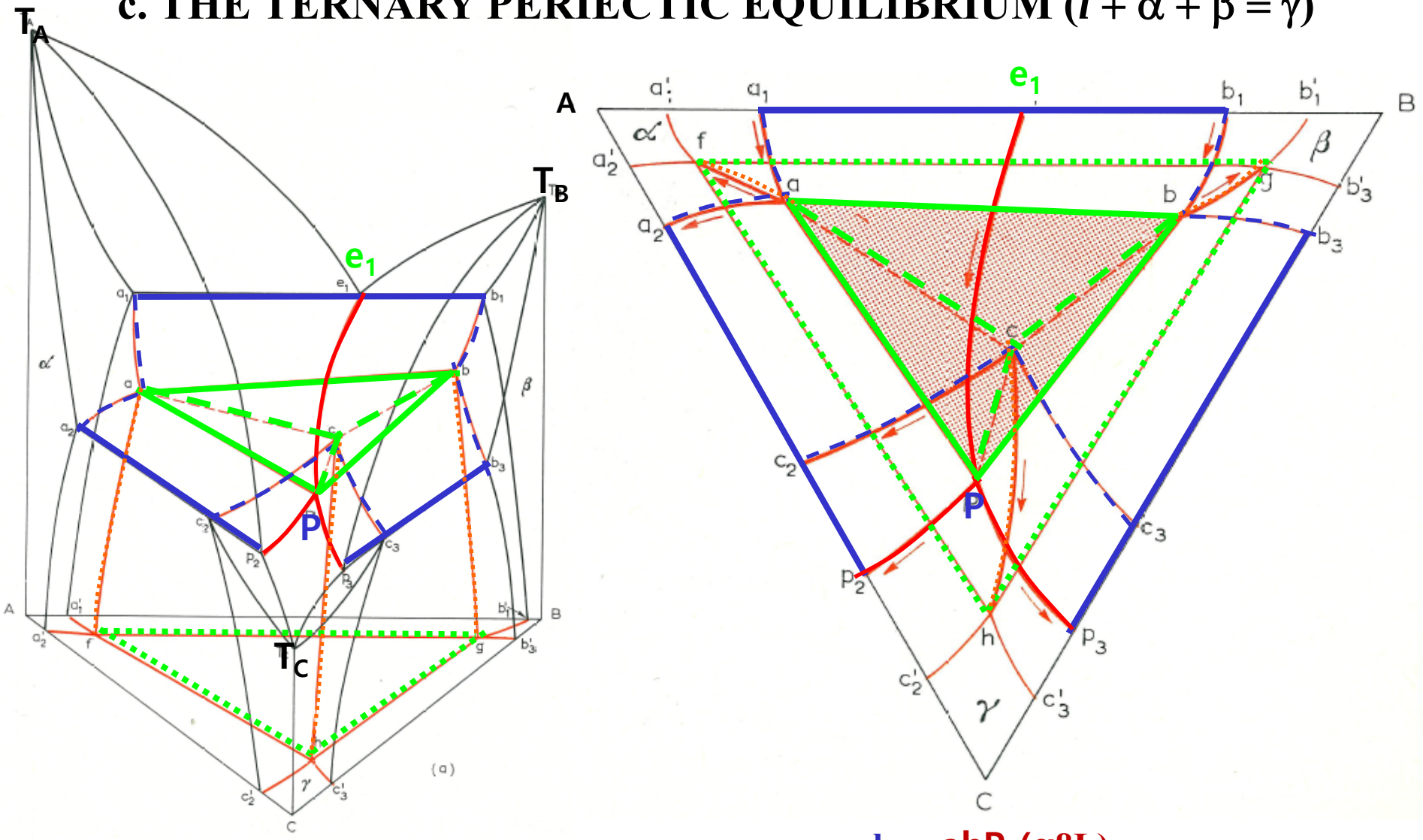


10.3. THE QUASI-PERITECTIC EQUILIBRIUM ($l + \alpha = \beta + \gamma$)

Fig. 191. The ternary quasi-peritectic system formed when all three binaries are eutectics. (a) Space model; (b) projection on the concentration triangle.



c. THE TERNARY PERIECTIC EQUILIBRIUM ($l + \alpha + \beta = \gamma$)

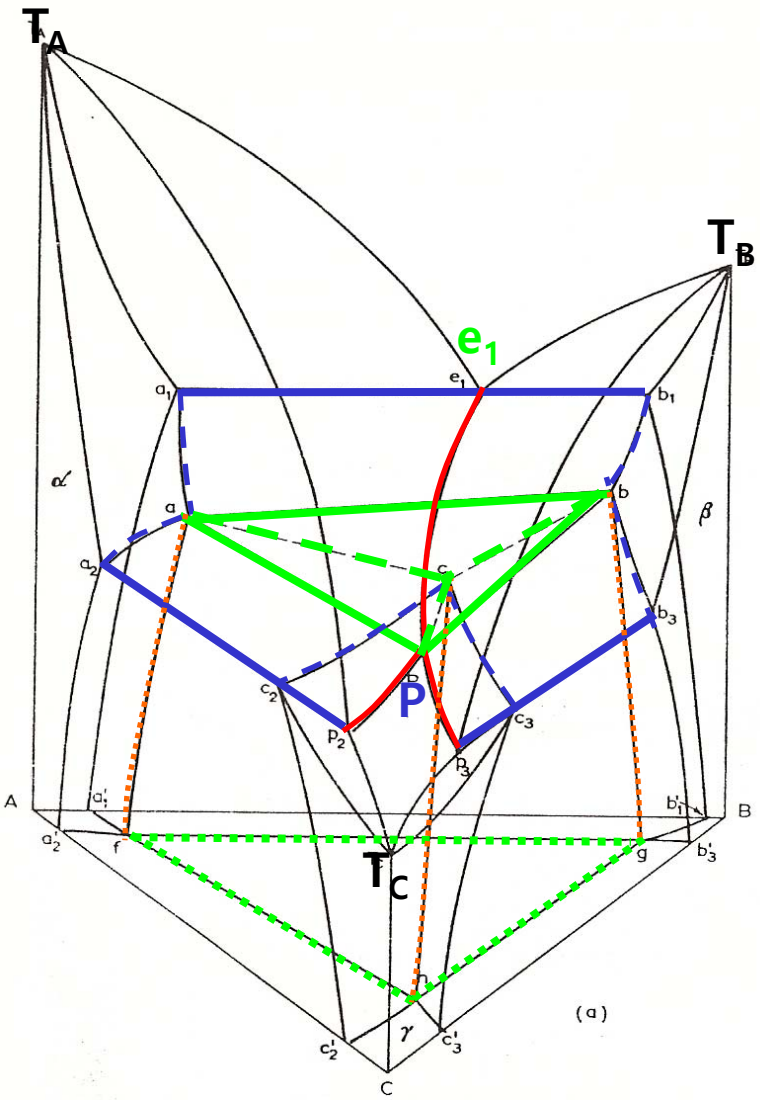


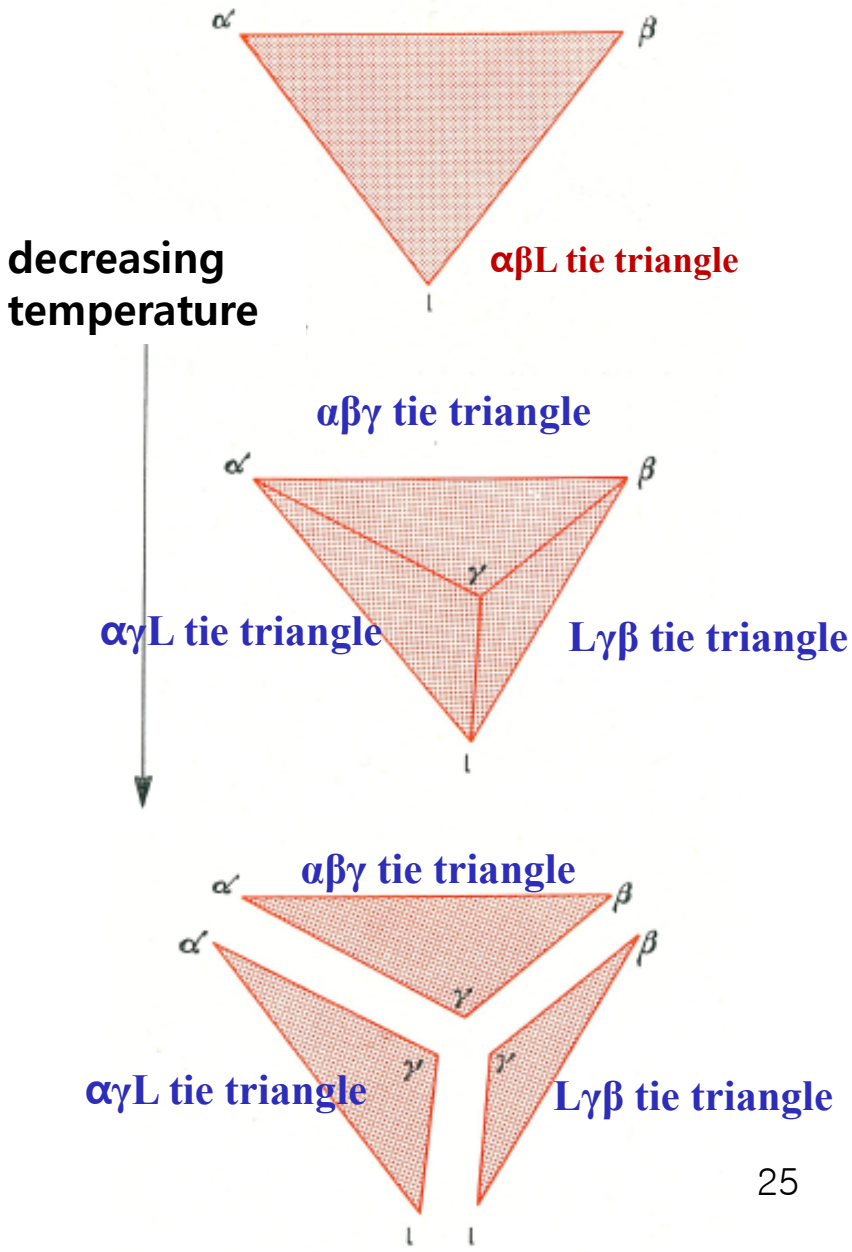
$T_A > T_B > \underline{e_1 > P > P_2 > P_3} > T_C$

$\underline{a_1 e_1 b_1} \rightarrow abP\ (\alpha\beta L)$

$aPc(\alpha\gamma L) \rightarrow \underline{a_2 c_2 P_2}\ /\ Pcb(L\gamma\beta) \rightarrow \underline{P_3 c_3 b_3}\ /\ abc(\alpha\beta\gamma) \rightarrow fgh\ (\alpha\beta\gamma)$

10.4. THE TERNARY PERIECTIC EQUILIBRIUM ($l + \alpha + \beta = \gamma$)

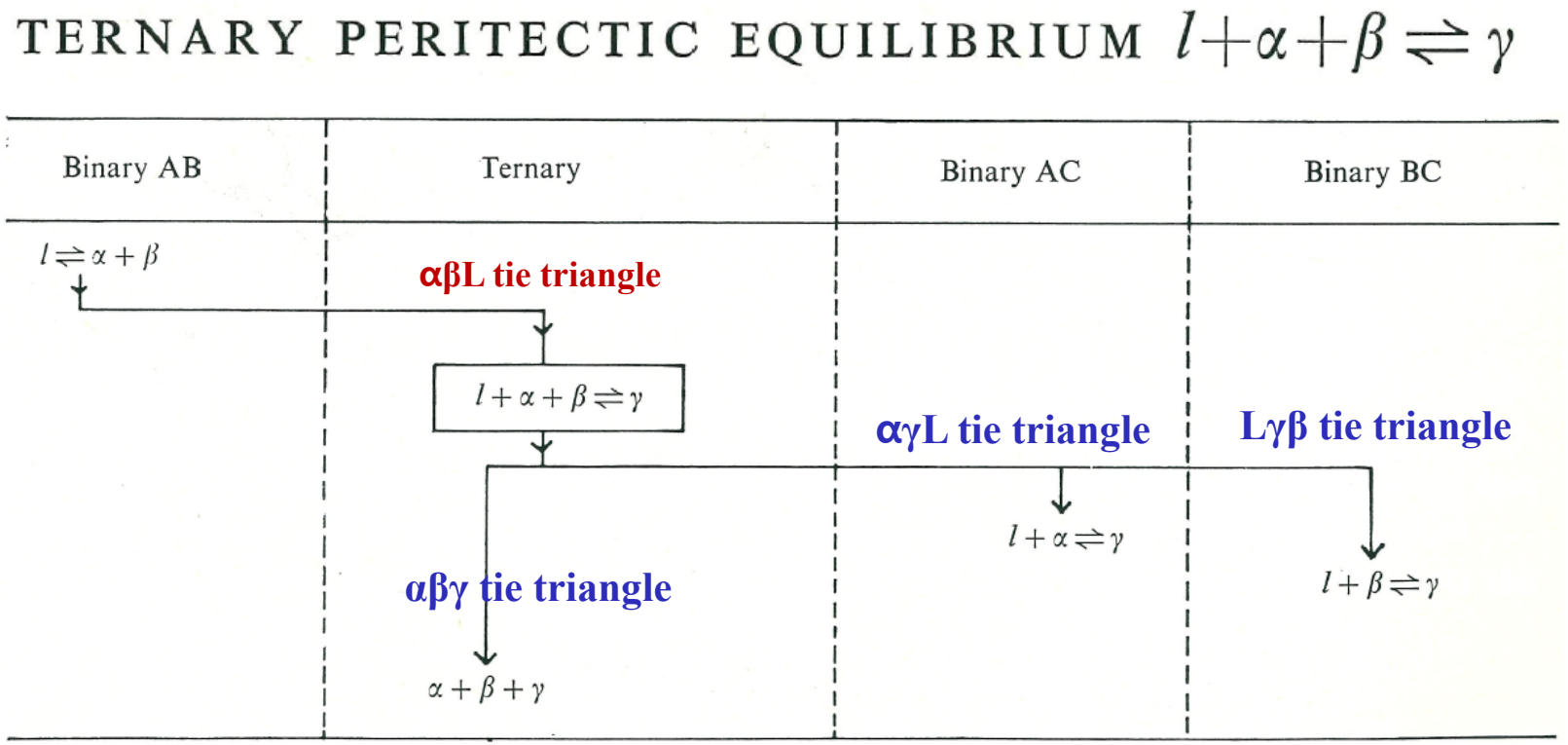




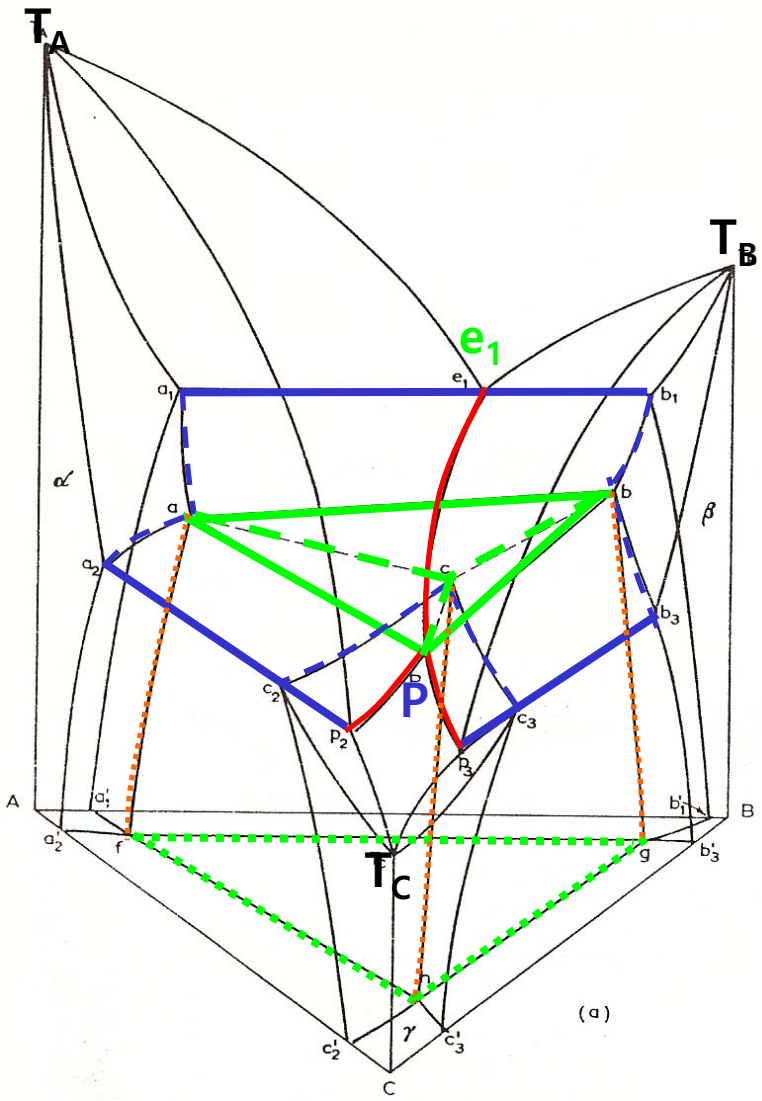
$T_A > T_B > e_1 > P > P_2 > P_3 > T_C$

Tabular representation of ternary equilibria:

interlinks the binary and ternary reactions in tabular form

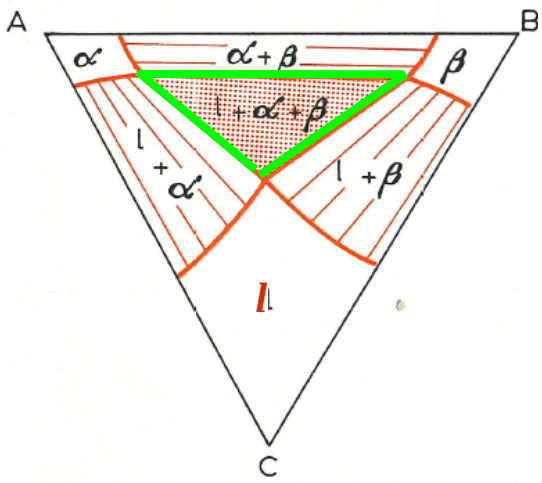


10.4. THE TERNARY PERIECTIC EQUILIBRIUM ($l + \alpha + \beta = \gamma$)

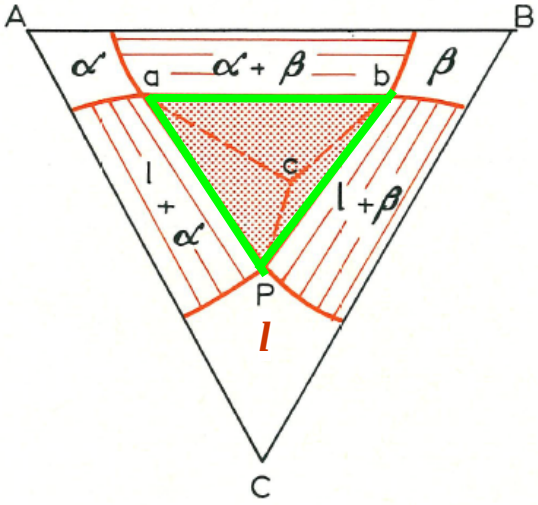


$T_A > T_B > e_1 > P > P_2 > P_3 > T_C$

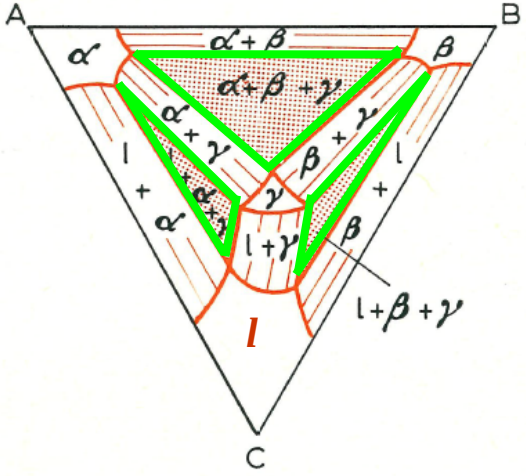
Isothermal section



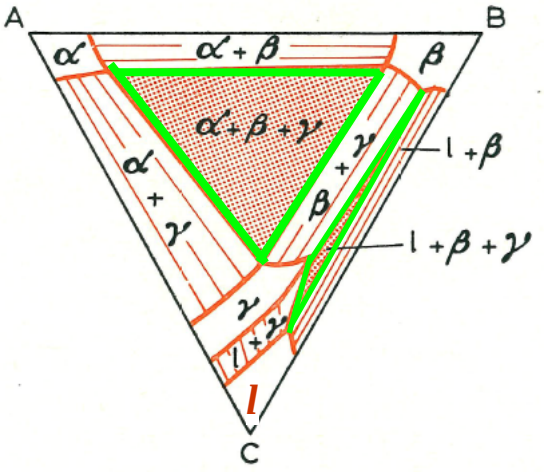
$e_1 > T > P$



$T = P$

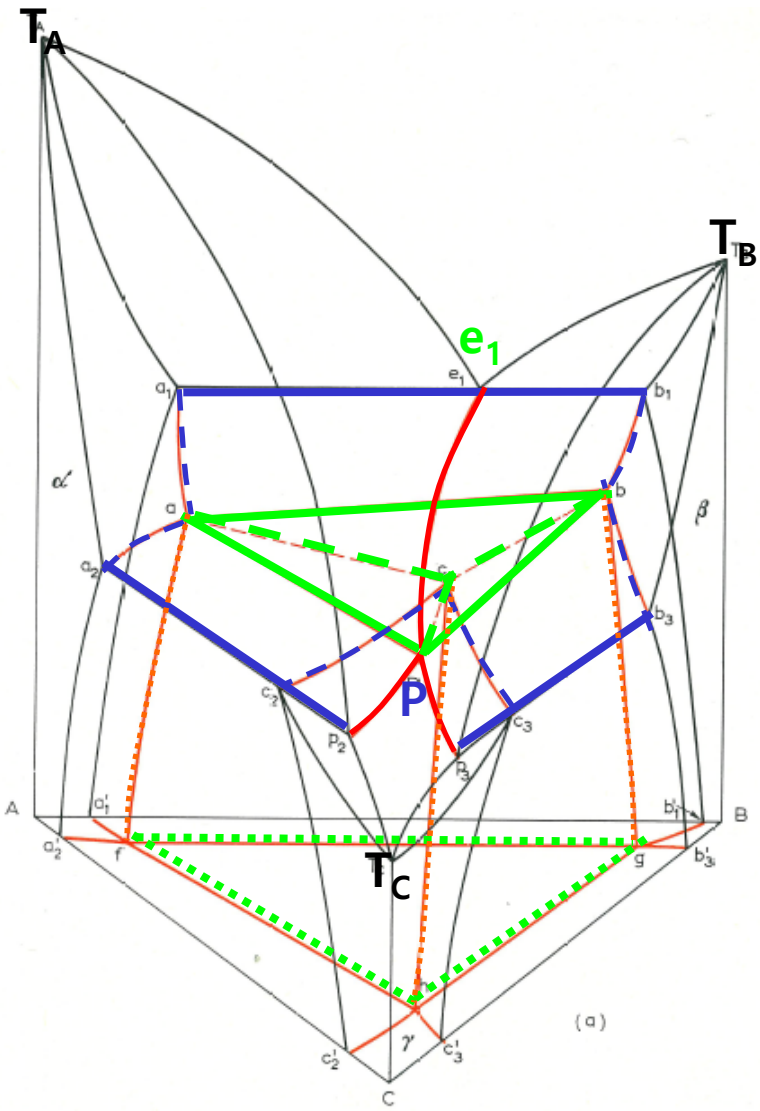


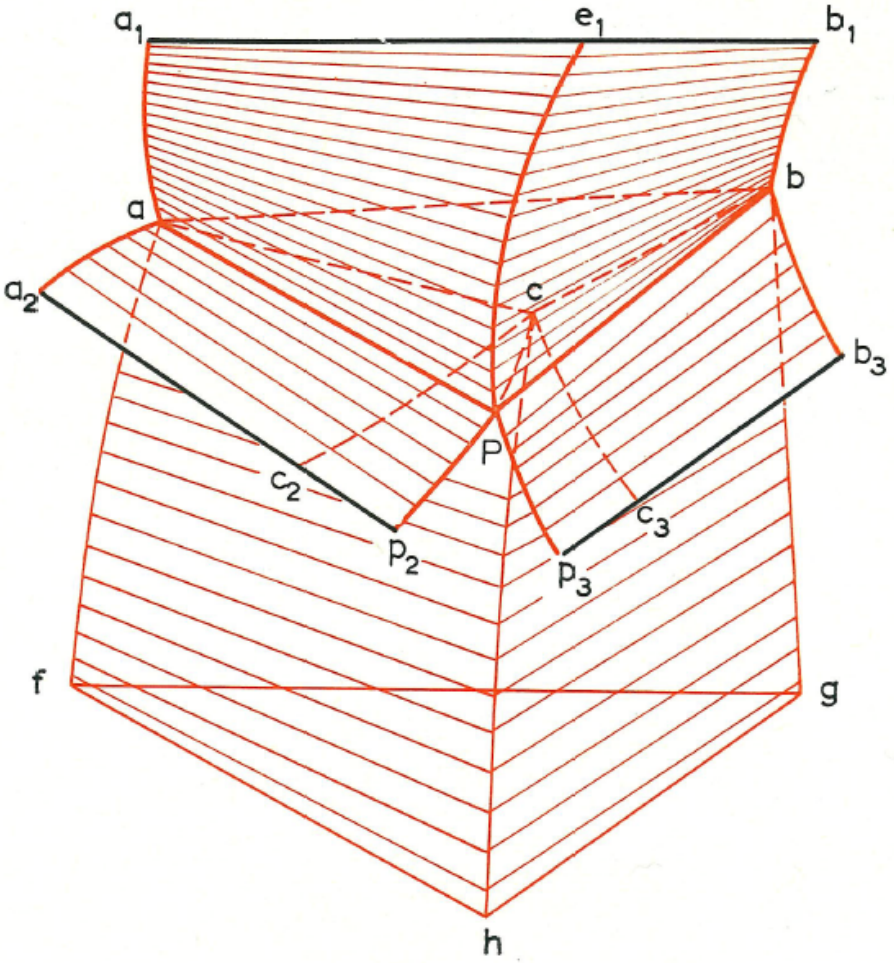
$P > T > P_2$



$P_2 > T > P_3$

10.4. THE TERNARY PERIECTIC EQUILIBRIUM ($l + \alpha + \beta = \gamma$)





$T_A > T_B > e_1 > P > P_2 > P_3 > T_C$

The ternary peritectic four-phase plane as the junction of four tie triangles

10.4. THE TERNARY PERIECTIC EQUILIBRIUM ($l + \alpha + \beta = \gamma$)