Physical Chemistry for Energy Engineering (5^{rh}: 2018/09/17)

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*The class follows the text book: D.A. McQuarrie, J.D. Simon, "Physical Chemistry: A Molecular Approach", University Science Books (1997).

Course schedule (tentative)

Lecture #	Date	Contents		
1	3-Sep	Introduction		
2	5-Sep	1. Thermodynamics: Basic concepts of thermodynamics		
3	10-Sep	1. Thermodynamics: The first law of thermodynamics		
4	12-Sep	1. Thermodynamics: Thermodynamic process and cycle		
5	17-Sep	1. Thermodynamics: The second and third laws of thermodynamics-1		
6	19-Sep	1. Thermodynamics: The second and third laws of thermodynamics-2		
	24-Sep	No lecture (holiday)		
	26-Sep	No lecture (holiday)		
7	1-Oct	1. Equation of state of gas		
	3-Oct	No lecture (holiday)		
8	8-Oct	Answer of homework-1		
9	10-Oct	Exam-01 (2 hour)		
10	15-Oct	2. Introduction to equilibrium theory		
11	17-Oct	2. Free energy-1		
12	22-Oct	2. Free energy-2		
13	24-Oct	2. Calculation of thermodynamic quantities		
	29-Oct	No lecture		
	31-Oct			

Contents of today

<Last class on 9/12>

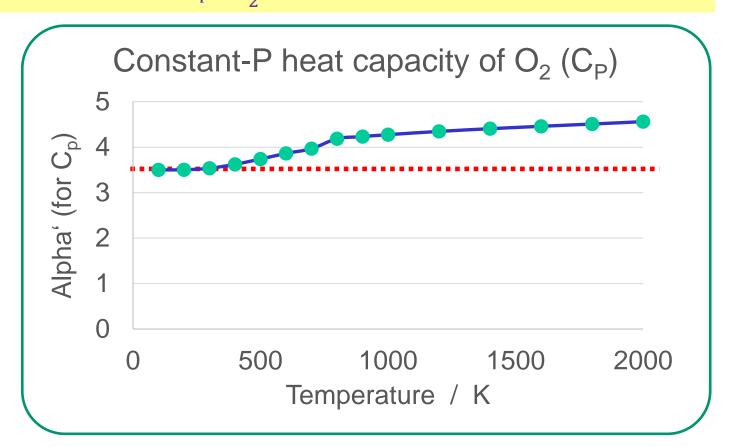
1.2.1. Thermodynamic process

<Today's class on 9/17>

- **1.2.2. Thermodynamic cycle**
- 1.3.1. The second law of thermodynamics

(in the last class) 1.2.1. Thermodynamic process - Heat capacity of real gas-

For ideal gas, " $C_V = \alpha nR$ [J K⁻¹], where $\alpha = \frac{3}{2}$ for He (monoatomic gas), $\alpha = \frac{5}{2}$ for O₂ (diatomic gas). $C_P - C_V = nR$ thus $C_p = \frac{7}{2}nR$ for O₂ in ideal gas approximation

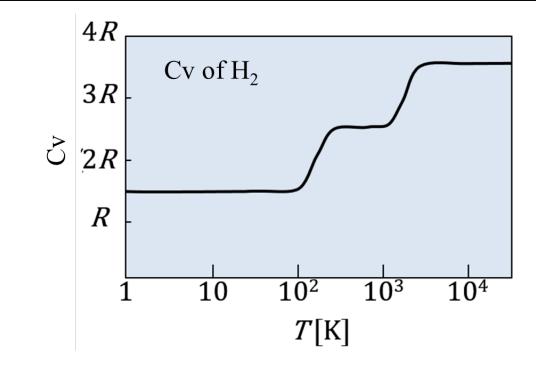


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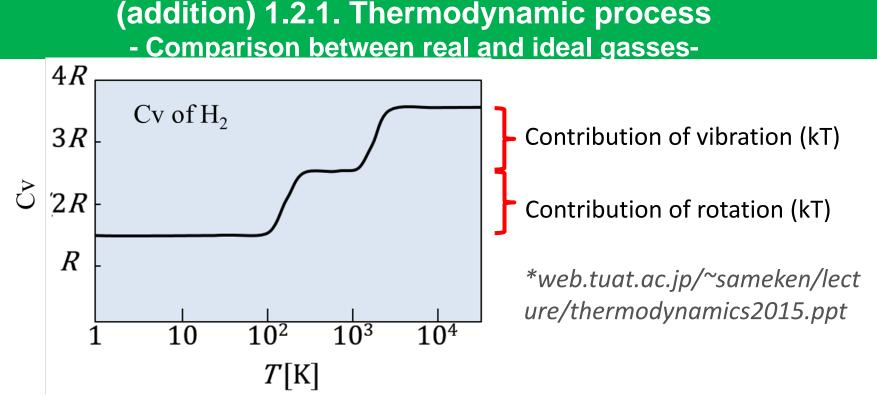
(in the last class) 1.2.1. Thermodynamic process - Heat capacity of real gas-

For each vibrational mode, there are two degrees of freedom: (i) kinetic energy and (ii) potential energy.

$$E_{vib} = \left\langle \frac{1}{2} m v_x^2 + \frac{1}{2} k x^2 \right\rangle = \left\langle \frac{1}{2} m v_x^2 \right\rangle + \left\langle \frac{1}{2} k x^2 \right\rangle = \frac{1}{2} k T + \frac{1}{2} k T = k T$$

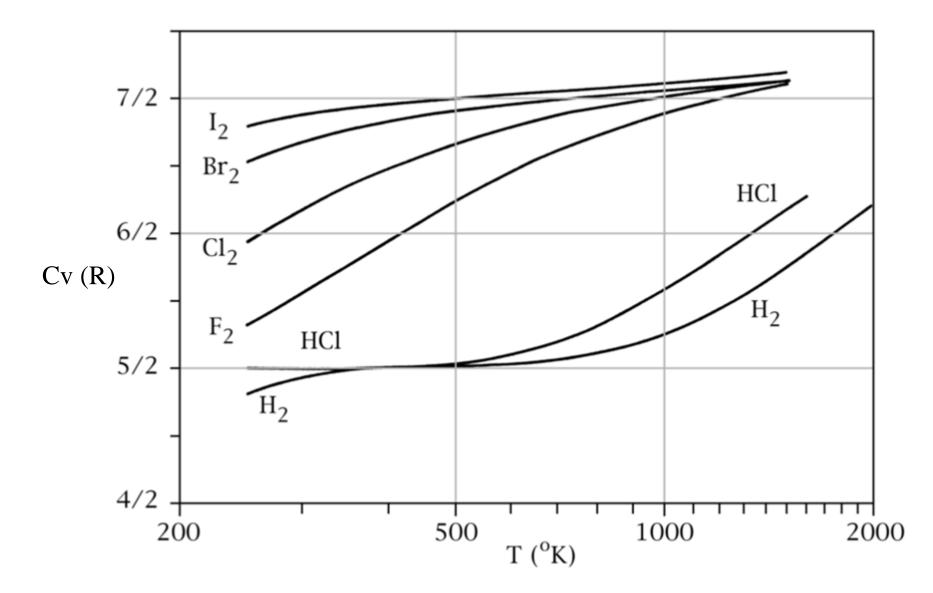


*web.tuat.ac.jp/~sameken/lect ure/thermodynamics2015.ppt



- ✓ For both real H2 gas and diatomic ideal gas, the translational degrees of freedom (of the center of mass) always contribute to the heat capacity (3/2 kT)
- ✓ In real H₂ gas, the rotational and vibrational degrees of freedom do not contribute to the heat capacity below ~100 K and ~1000 K respectively, due to the quantum effects. This makes the heat capacity of real H₂ gas as in the figure above.
- ✓ In ideal diatomic gas, the rotational contribution happens from 0 K, while no vibrational contribution. Because ideal gas is classical (not quantum), and there is no interaction between atoms/molecules. (we imagine a fixed H-H structure, where H-H distance never changes. Even in this case, the rotation can occur. As a result, Cv becomes (5/2)kT for diatomic molecule independent of the temperature.

(addition) 1.2.1. Thermodynamic process - Comparison between real and ideal gasses-

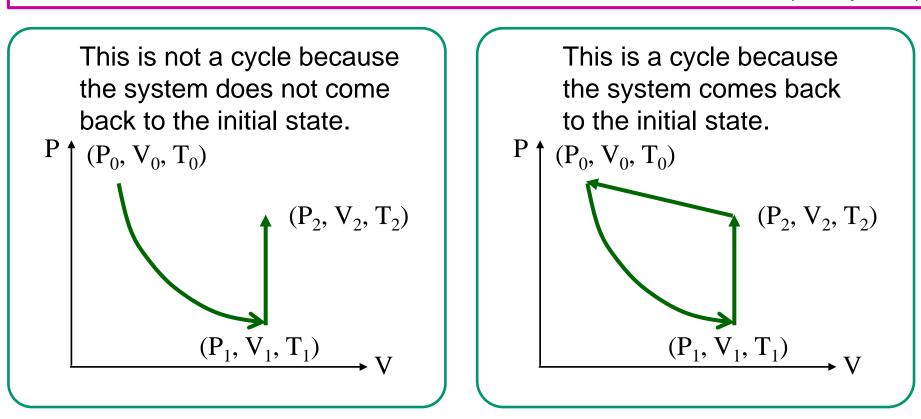


*https://en.wikipedia.org/wiki/Heat_capacity#/media/File:DiatomicSpecHeat2.png

1.2.2. Thermodynamic cycle - definition -

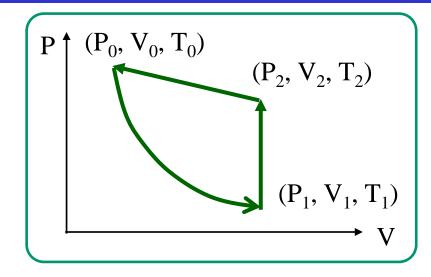
"A thermodynamic cycle consists of a linked sequence of thermodynamic processes that involve the transference of heat and work into and out of the system, while varying pressure, temperature, and other state variables within the system, and that eventually returns the system to its initial state."

(*wikipedia)



1.2.2. Thermodynamic cycle - what do we do with a cycle? -

We usually calculate (1) energy transfer (heat & work), (2) variation of state functions along processes involved in the cycle.



In a cycle, because the initial and the final states are identical, there are several constraints in state functions, for examples:

$$P_{ini} = P_{fin}$$
 $\Delta U_{cycle} = \oint dU = U_{fin} - U_{ini} = 0$

Be careful about the difference between state functions and path functions.

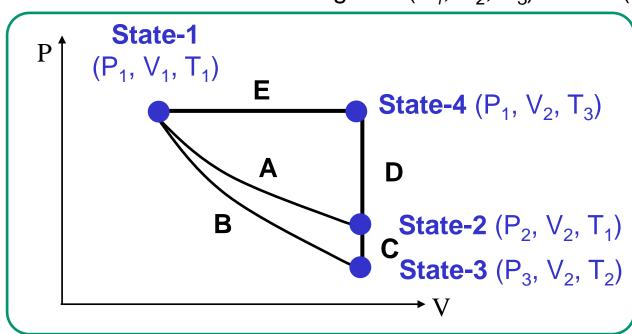
$$q_{cycle} = \oint \delta q \neq 0 \qquad w_{cycle} = \oint \delta w \neq 0$$
$$q_{cycle} + w_{cycle} = \oint \delta q + \oint \delta w = \Delta U_{cycle} = 0$$

*Of course, q_{cycle} and w_{cycle} may be 0 accidentally, but not necessarily.

1.2.2. Thermodynamic cycle (\$19.4) - a case of thermodynamic cycle: exercise -

Assuming *n* mole of idea gas (PV = nRT, U = U(T), $dU = C_V dT$ and $C_V = \alpha nR = const.$), please evaluate (1) ΔU , (2) *q*, (3) w, for each process.

✓ [Path-A] Reversible isothermal expansion: s-1 (P_1 , V_1 , T_1)→ s-2 (P_2 , V_2 , T_1) ✓ [Path-B] Reversible adiabatic expansion: s-1 (P_1 , V_1 , T_1) → s-3 (P_3 , V_2 , T_2) ✓ [Path-C] Reversible constant-V heating: s-3 (P_3 , V_2 , T_2) → s-2(P_2 , V_2 , T_1) ✓ [Path-D] Reversible constant-V heating: s-2 (P_2 , V_2 , T_1) → s-4 (P_1 , V_2 , T_3) ✓ [Path-E] Reversible constant-P cooling: s-4 (P_1 , V_2 , T_3) → s-1 (P_1 , V_1 , T_1)

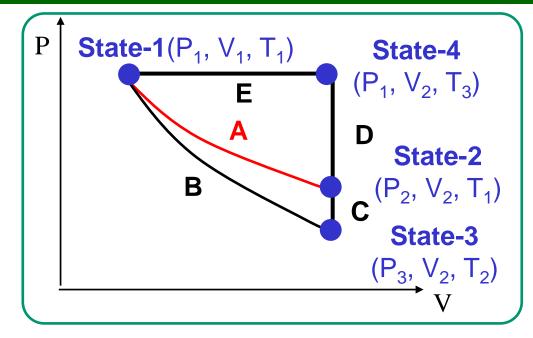


1st law: [derivative form] $dU = \delta q + \delta w$; [integral form] $\Delta U = q + w$

1.2.2. Thermodynamic cycle (\$19.4) - a case of thermodynamic cycle: exercise (path-A)-

Assuming *n* mole of idea gas $(PV = nRT, U = U(T), dU = C_V dT$ and $C_V = \alpha nR = const.$), please evaluate (1) ΔU , (2) *q*, (3) w, for each process.

> [Path-A] Reversible isothermal expansion: s-1 $(P_1, V_1, T_1) \rightarrow$ s-2 (P_2, V_2, T_1)

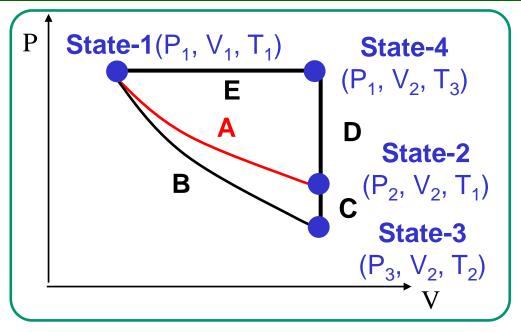


$\Delta U_A =$	
$q_A =$	
$w_A =$	



Assuming *n* mole of idea gas $(PV = nRT, U = U(T), dU = C_V dT$ and $C_V = \alpha nR = const.$), please evaluate (1) ΔU , (2) *q*, (3) w, for each process.

> [Path-A] Reversible isothermal expansion: s-1 $(P_1, V_1, T_1) \rightarrow$ s-2 (P_2, V_2, T_1)



As the energy of ideal gas only depends on temperature and dT = 0, $\Delta U_A = U(T_1) - U(T_1) = 0$

The first law can be re-written: $w_A = -q_A$ As a reversible process (as $P = P_{ext}$) $V_A^2 = V_A^2 dV$

$$w_{A} = -\int_{V_{1}}^{V_{2}} P \, dV = -nRT_{1} \int_{V_{1}}^{V_{2}} \frac{dV}{V} = -nRT_{1} \times \ln \frac{V_{2}}{V_{1}}$$

$$\Delta U_A = 0$$

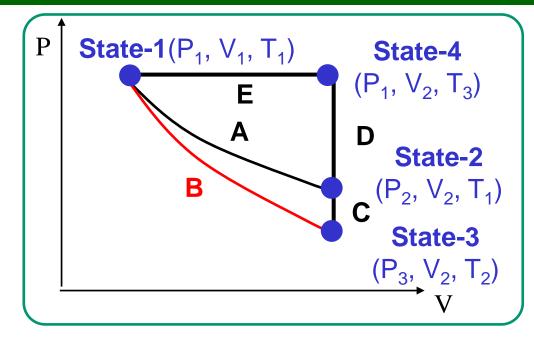
$$q_A = nRT_1 \times \ln \frac{V_2}{V_1}$$

$$w_A = -nRT_1 \times \ln \frac{V_2}{V_1}$$

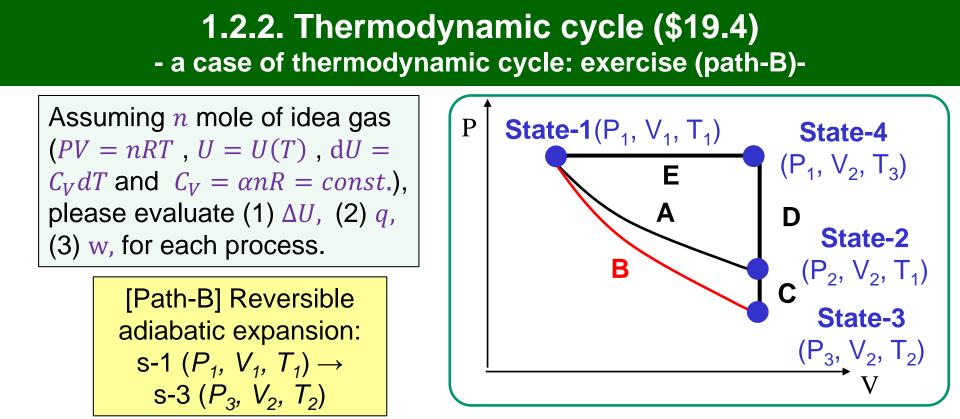
1.2.2. Thermodynamic cycle (\$19.4) - a case of thermodynamic cycle: exercise (path-B)-

Assuming *n* mole of idea gas $(PV = nRT, U = U(T), dU = C_V dT$ and $C_V = \alpha nR = const.$), please evaluate (1) ΔU , (2) *q*, (3) w, for each process.

> [Path-B] Reversible adiabatic expansion: s-1 (P_1 , V_1 , T_1) \rightarrow s-3 (P_3 , V_2 , T_2)



$\Delta U_B =$	
$q_B =$	
$w_B =$	



As adiabatic process ($\delta q = 0$ and then q = 0), the first law is: $dU_B = \delta w_B$

As we assume the system is of an ideal gas:

$$\Delta U_B = \int_{T_1}^{T_2} C_V dT = C_V (T_2 - T_1)$$

$$\Delta U_B = C_V (T_2 - T_1)$$

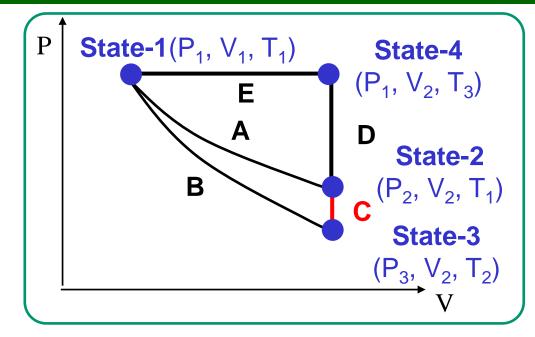
$$q_B = 0$$

$$w_B = C_V (T_2 - T_1)$$

1.2.2. Thermodynamic cycle (\$19.4) - a case of thermodynamic cycle: exercise (path-C)-

Assuming *n* mole of idea gas $(PV = nRT, U = U(T), dU = C_V dT$ and $C_V = \alpha nR = const.$), please evaluate (1) ΔU , (2) *q*, (3) w, for each process.

> [Path-C] Reversible constant-V heating: s-3 (P_3 , V_2 , T_2) \rightarrow s-2(P_2 , V_2 , T_1)

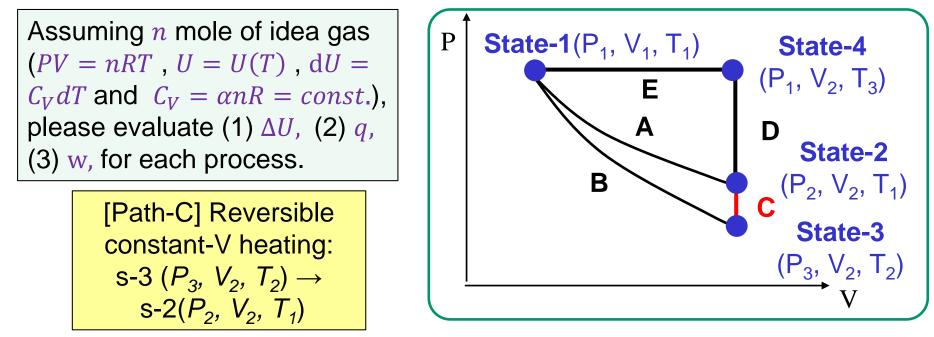


$$\Delta U_C =$$

$$q_c =$$

$$w_c =$$





As constant-V process (dV = 0), $\delta w_C = -P_{ext}dV = 0$. Then, the first law is: $dU_C = \delta q_C$

As we assume the system is of an ideal gas:

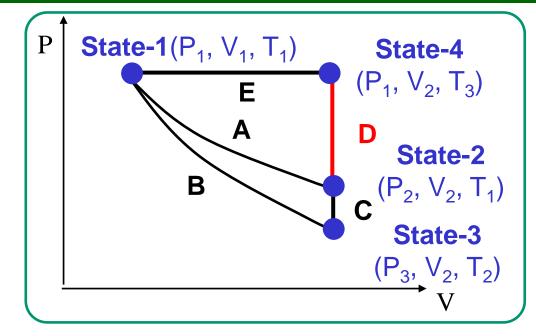
$$\Delta U_{C} = \int_{T_{2}}^{T_{1}} C_{V} dT = C_{V} (T_{1} - T_{2})$$

$$\Delta U_C = C_V (T_1 - T_2)$$
$$q_c = C_V (T_1 - T_2)$$
$$w_c = 0$$

1.2.2. Thermodynamic cycle (\$19.4) - a case of thermodynamic cycle: exercise (path-D)-

Assuming *n* mole of idea gas $(PV = nRT, U = U(T), dU = C_V dT$ and $C_V = \alpha nR = const.$), please evaluate (1) ΔU , (2) *q*, (3) w, for each process.

> [Path-D] Reversible constant-V heating: s-2 $(P_2, V_2, T_1) \rightarrow$ s-4 (P_1, V_2, T_3)

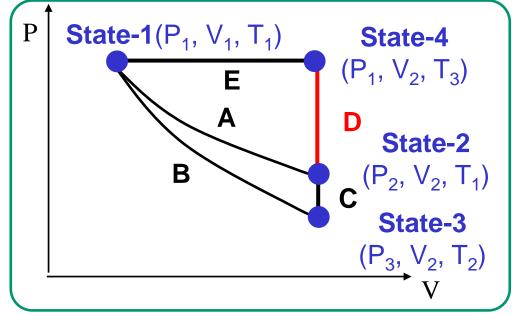


$\Delta U_D =$	
$q_D =$	
$w_D =$	



Assuming *n* mole of idea gas $(PV = nRT, U = U(T), dU = C_V dT$ and $C_V = \alpha nR = const.$), please evaluate (1) ΔU , (2) *q*, (3) w, for each process.

> [Path-D] Reversible constant-V heating: s-2 $(P_2, V_2, T_1) \rightarrow$ s-4 (P_1, V_2, T_3)



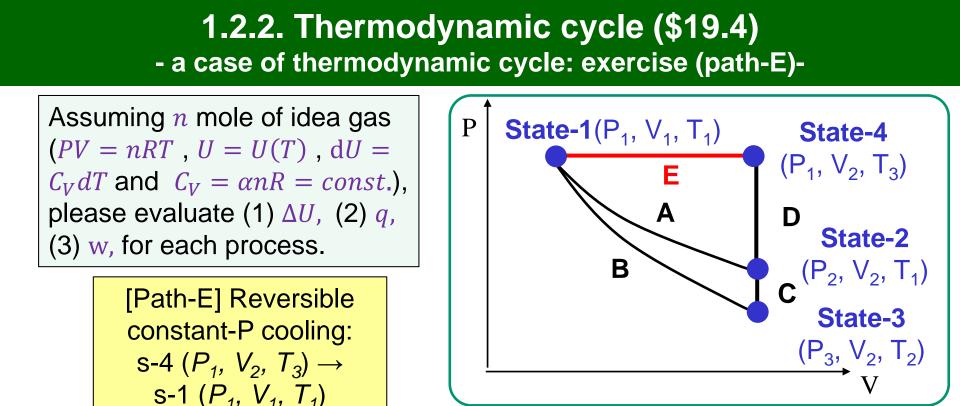
As constant-V process (dV = 0), $\delta w_D = -P_{ext}dV = 0$.

Then, the first law is: $dU_D = \delta q_D$

As we assume the system is of an ideal gas:

$$\Delta U_D = \int_{T_1}^{T_3} C_V dT = C_V (T_3 - T_1)$$

$$\Delta U_D = C_V (T_3 - T_1)$$
$$q_D = C_V (T_3 - T_1)$$
$$w_D = 0$$



As reversible constant-P process ($P = P_{ext}$ and dP = 0),

$$w_E = -\int P dV = -P_1 \int dV = -P_1 (V_1 - V_2).$$

As we assume the system is of an ideal gas: $\Delta U_E = \int_{T_3}^{T_1} C_V dT = C_V (T_1 - T_3)$

Then, using the first law:

 $q_E = \Delta U_E - w_E = C_V (T_1 - T_3) + P_1 (V_1 - V_2)$

$$\Delta U_E = C_V (T_1 - T_3)$$

$$q_E = C_V (T_1 - T_3) + P_1 (V_1 - V_2)$$

$$w_E = -P_1 (V_1 - V_2)$$

1.2.2. Thermodynamic cycle (\$19.4) - a case of thermodynamic cycle: exercise (summary)-

Path	$\Delta \boldsymbol{U}$	q	W	P s-1 F
Α	0	$nRT_1 \times \ln \frac{V_2}{V_1}$	$-nRT_1 \times \ln \frac{V_2}{V_1}$	$e^{s-1} = E$
В	$C_V(T_2 - T_1)$	0	$C_V(T_2 - T_1)$	A D
С	$C_V(T_1 - T_2)$	$C_V(T_1 - T_2)$	0	B s-2
D	$C_V(T_3 - T_1)$	$C_V(T_3 - T_1)$	0	C s-3
E	$C_V(T_1 - T_3)$	$ \begin{array}{c} C_V(T_1 - T_3) \\ + P_1(V_1 - V_2) \end{array} $	$-P_1(V_1-V_2)$	

(1) [Path-A] v.s. [Path-B+C]

 $\Delta U_{B+C} = C_V (T_2 - T_1) + C_V (T_1 - T_2) = 0 = \Delta U_A$ $q_{B+C} = 0 + C_V (T_1 - T_2) = C_V (T_1 - T_2) \neq q_A$ $w_{B+C} = C_V (T_2 - T_1) + 0 = C_V (T_2 - T_1) \neq w_A$

- ✓ As the initial and final states are identical in two paths, the change in state functions (e.g. U) is identical.
- \checkmark However, path functions (e.g. q and w) depend on the path.

1.2.2. Thermodynamic cycle (\$19.4) - a case of thermodynamic cycle: exercise (summary)-

Path	ΔU	q	W	P
A	0	$nRT_1 \times \ln \frac{V_2}{V_1}$	$-nRT_1 \times \ln \frac{V_2}{V_1}$	s-1 E
В	$C_V(T_2 - T_1)$	0	$C_V(T_2 - T_1)$	A D
С	$C_V(T_1 - T_2)$	$C_V(T_1 - T_2)$	0	B s-2
D	$C_V(T_3 - T_1)$	$C_V(T_3 - T_1)$	0	
E	$C_V(T_1 - T_3)$	$C_V(T_1 - T_3) + P_1(V_1 - V_2)$	$-P_1(V_1-V_2)$	

(2) [Cycle-a: $1 \rightarrow 2 \rightarrow 4 \rightarrow 1$] v.s. [Cycle-b: $1 \rightarrow 3 (\rightarrow 2) \rightarrow 4 \rightarrow 1$]

$$\Delta U_a = \Delta U_A + \Delta U_D + \Delta U_E = 0$$

$$q_a = q_A + q_D + q_E$$

$$= nRT_1 \times \ln \frac{V_2}{V_1} + P_1(V_1 - V_2)$$

$$w_a = w_A + w_D + w_E$$

$$= -nRT_1 \times \ln \frac{V_2}{V_1} - P_1(V_1 - V_2)$$

 $\Delta U_b = \Delta U_B + \Delta U_C + \Delta U_D + \Delta U_E = 0$

$$q_b = q_B + q_C + q_D + q_E = C_V (T_1 - T_2) + P_1 (V_1 - V_2)$$

$$w_b = w_B + w_C + w_D + w_E$$

= $C_V (T_2 - T_1) - P_1 (V_1 - V_2)$

1.2.2. Thermodynamic cycle (\$19.4) - a case of thermodynamic cycle: exercise (summary) -

(2) [Cycle-a: $1 \rightarrow 2 \rightarrow 4 \rightarrow 1$] v.s. [Cycle-b: $1 \rightarrow 3 (\rightarrow 2) \rightarrow 4 \rightarrow 1$]

$$\Delta U_{a} = \Delta U_{A} + \Delta U_{D} + \Delta U_{E} = 0$$

$$q_{a} = q_{A} + q_{D} + q_{E}$$

$$= nRT_{1} \times \ln \frac{V_{2}}{V_{1}} + P_{1}(V_{1} - V_{2})$$

$$w_{a} = w_{A} + w_{D} + w_{E}$$

$$= -nRT_{1} \times \ln \frac{V_{2}}{V_{1}} - P_{1}(V_{1} - V_{2})$$

$$\Delta U_b = \Delta U_B + \Delta U_C + \Delta U_D + \Delta U_E = 0$$

$$q_b = q_B + q_C + q_D + q_E$$

$$= C_V (T_1 - T_2) + P_1 (V_1 - V_2)$$

$$w_b = w_B + w_C + w_D + w_E$$

$$= C_V (T_2 - T_1) - P_1 (V_1 - V_2)$$

✓ As cycle is closed, "[initial state] = [final state]" is required. Then: $\Delta U_{cycle} = \oint dU = U_{fin} - U_{ini} = 0$

This is also applicable for other (extensive) state functions like enthalpy

 \checkmark On the other hands, path functions do not have such result as:

 $w_{cycle} = \oint \delta w \neq 0$ $q_{cycle} = \oint \delta q \neq 0$

1.2.2. Thermodynamic cycle (\$19.4) - a case of thermodynamic cycle: exercise (summary) -

(2) [Cycle-a: $1 \rightarrow 2 \rightarrow 4 \rightarrow 1$] v.s. [Cycle-b: $1 \rightarrow 3 (\rightarrow 2) \rightarrow 4 \rightarrow 1$]

$$\Delta U_a = \Delta U_A + \Delta U_D + \Delta U_E = \oint dU = 0$$
$$\Delta U_b = \Delta U_B + \Delta U_C + \Delta U_D + \Delta U_E = \oint dU = 0$$

- ✓ Using this character of state function in a cycle (i.e. $\oint dU = 0$, for example), we can sometimes easily determine the change of a state function in a certain path.
 - ✓ For example, here assuming the cycle is composed by 4 processes.

 $\Delta U_{cycle} = \Delta U_{path-1} + \Delta U_{path-2} + \Delta U_{path-3} + \Delta U_{path-4} = 0$

✓ If ΔU_{path-4} is difficult to be directly calculated but we know the contour integral is 0, we can determine it as:

 $\Delta U_{path-4} = -\Delta U_{path-1} - \Delta U_{path-2} - \Delta U_{path-3}$

Contents of today

<Last class>

1.2.1. Thermodynamic process

<Today's class>

- 1.2.2. Thermodynamic cycle
- **1.3.1.** The second law of thermodynamics

1.3.1. The 2nd law of thermodynamics - description-

- "The entropy of an isolated system never decreases, because isolated systems always evolve toward thermodynamic equilibrium—the state with the maximum possible entropy." (wikipedia)
- ✓ "Heat cannot spontaneously flow from cold regions to hot regions without external work being performed on the system." (a version of Clausius statement)
- "It is impossible, by means of inanimate material agency, to derive mechanical effect from any portion of matter by cooling it below the temperature of the coldest of the surrounding objects." (a version of Kelvin statement)
- "The efficiency of a quasi-static or reversible Carnot cycle depends only on the temperatures of the two heat reservoirs, and is independent of the working substance. A Carnot engine operated in this way is the most efficient possible heat engine using those two temperatures." (Carnot's principle)

1.3.1. The 2nd law of thermodynamics - perpetual motion (machines) -

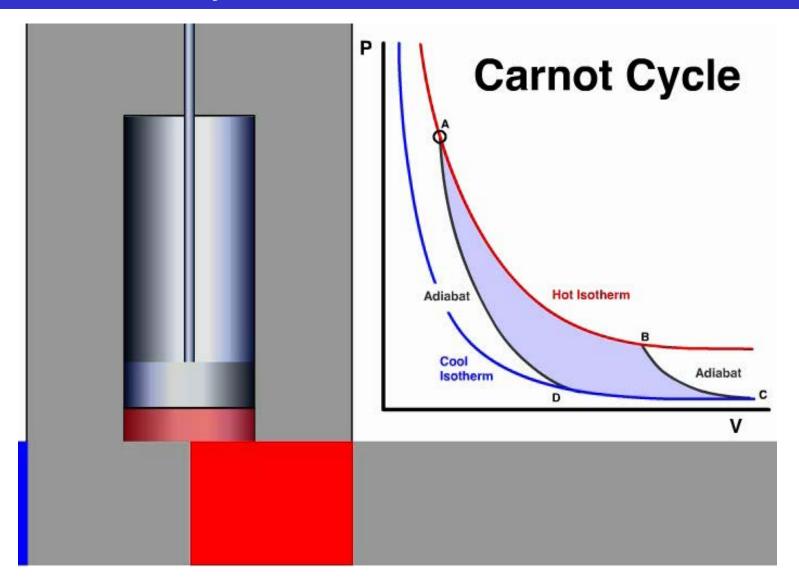
(1) Perpetual motion machine of the 1st kind:

- "a machine that can do work to the surroundings without obtaining any inputs from the surroundings."
- \checkmark This motion violates the 1st law of thermodynamics, thus unfeasible.

(2) Perpetual motion machine of the 2nd kind:

- "a machine/cycle that receives a heat from a thermostat (surroundings) and do equivalent amount of work to the surroundings."
- \checkmark This motion violates the 2nd law of thermodynamics, thus unfeasible.

1.3.1. The 2nd law of thermodynamics - a cycle combined with 2 thermostats -



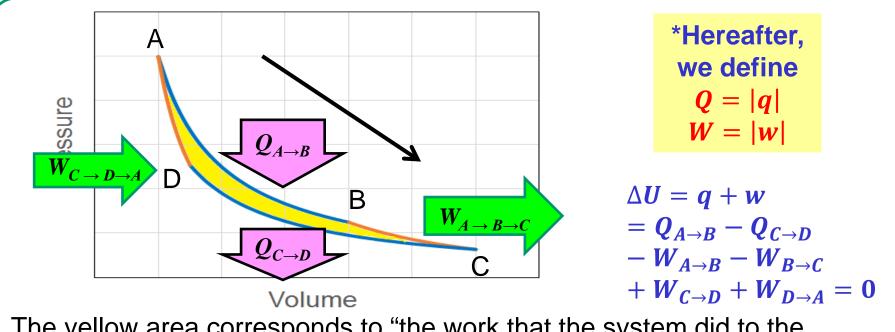
http://science.sbcc.edu/~physics/flash/heatengines/Carnot%20cycle.html

1.3.1. The 2nd law of thermodynamics - a cycle combined with 2 thermostats (cont'd)-

We consider a cycle combined with 2 thermostats:

- (1) $[A \rightarrow B]$ isothermal expansion (T_H)
- (2) $[B \rightarrow C]$ adiabatic expansion
- (3) [C \rightarrow D] isothermal compression (T_L)
- (4) $[D \rightarrow A]$ adiabatic compression

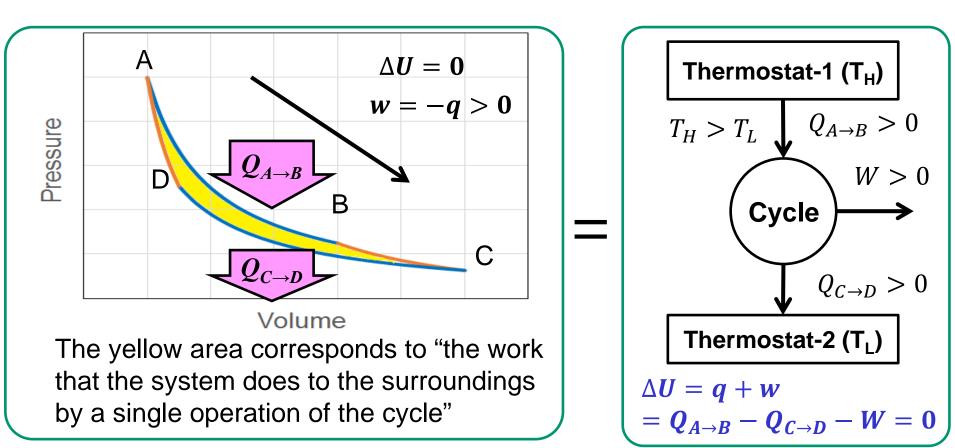
where $T_H > T_L$ and assuming all processes are reversible.



The yellow area corresponds to "the work that the system did to the surroundings by a single operation of the cycle"

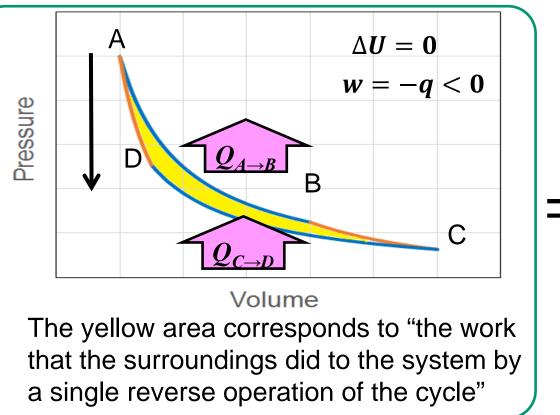
1.3.1. The 2nd law of thermodynamics - a cycle combined with 2 thermostats: forward operation -

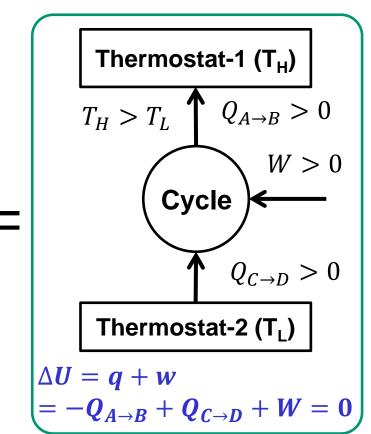
- ✓ A single operation of this cycle ("A → B → C → D → A") is conceptually redrawn as in the right figure, which indicates that the cycle "outputs work *W* by absorbing heat $Q_{A\to B}$ from the higher-temperature thermostat and discarding heat $Q_{C\to D}$ to the lower-temperature thermostat."
- \checkmark This kind of devices include engines and turbines.



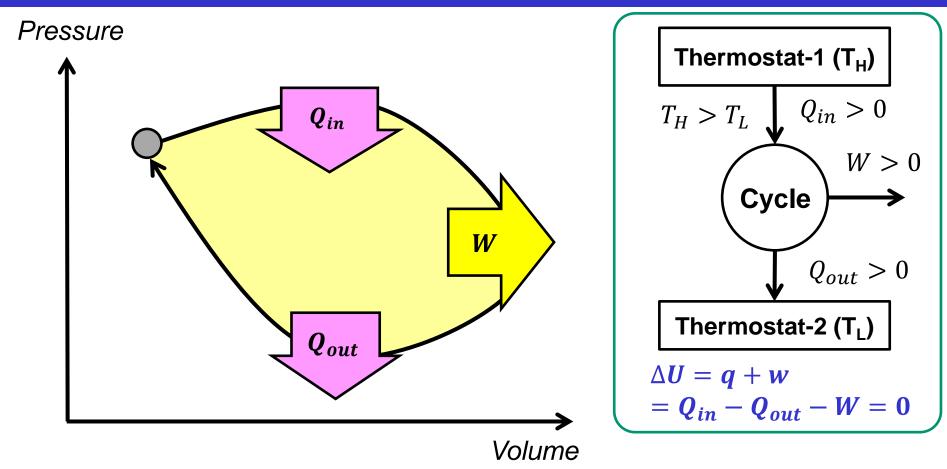
1.3.1. The 2nd law of thermodynamics - a cycle combined with 2 thermostats: backward operation -

- ✓ If all processes are reversible, we can reversely operate the cycle as "A → D → C → B → A".
- ✓ This reverse operation makes a device that "absorbs heat $Q_{C \to D}$ from the lower-temperature thermostat and discards heat $Q_{A \to B}$ to the higher-temperature thermostat by receiving work *W* from the surroundings".
- $\checkmark\,$ A cooler uses this kind of cycle, for example.



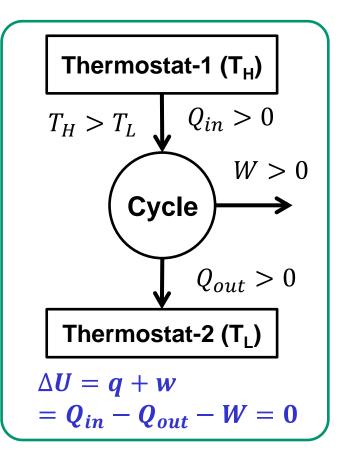


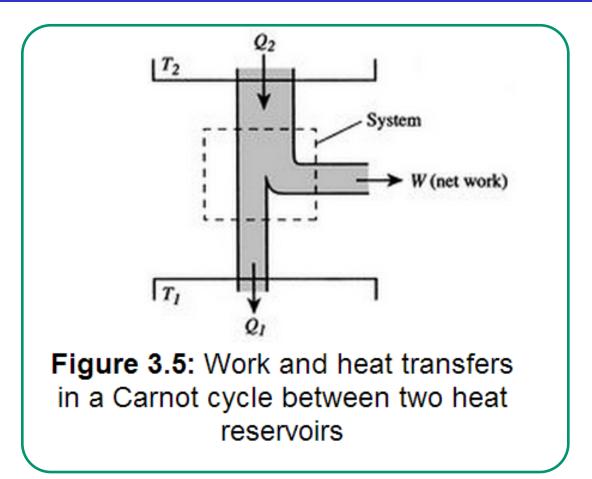
1.3.1. The 2nd law of thermodynamics - a cycle combined with 2 thermostats, more generalized-



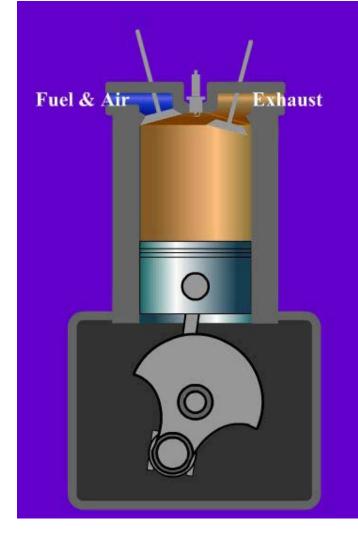
- The area surrounded by the cycle (P-V diagram) corresponds to the amount of work which the system makes to the surrounding by a single operation of the cycle.
- \checkmark If the operation is reverse, the surroundings makes the work to the system.

1.3.1. The 2nd law of thermodynamics - a cycle combined with 2 thermostats, another drawing -





http://web.mit.edu/16.unified/www/FALL/ thermodynamics/notes/node24.html 1.3.1. The 2nd law of thermodynamics - application of cycle: an internal combustion engine (2/2) -



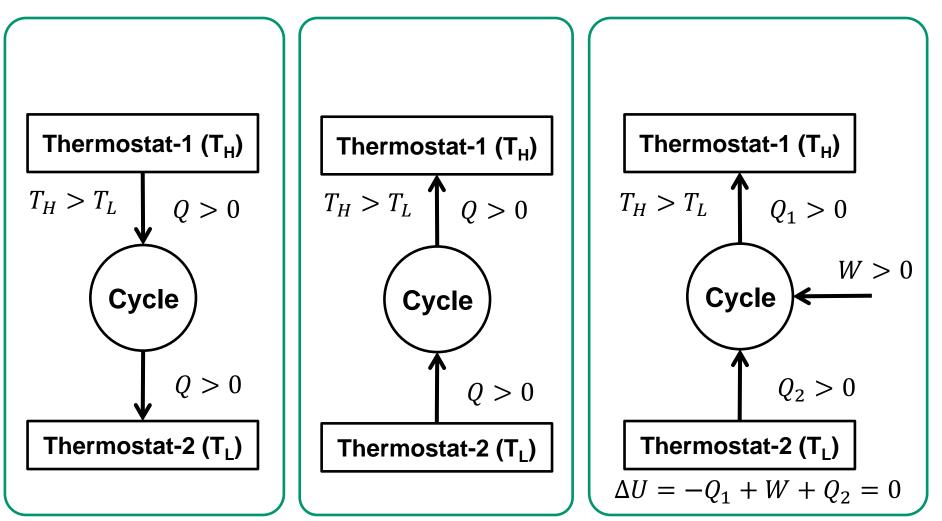
The Four-Stroke Internal Combustion Engine

Exhaust Stroke

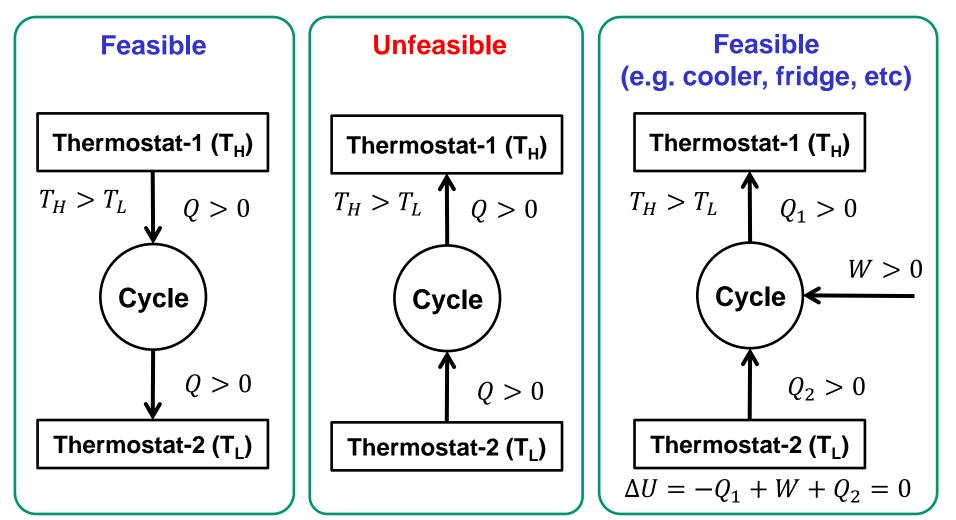
http://www.phy.ntnu.edu.tw/ntnujava/index.php?topic=23

*This is a kind of Otto cycle.

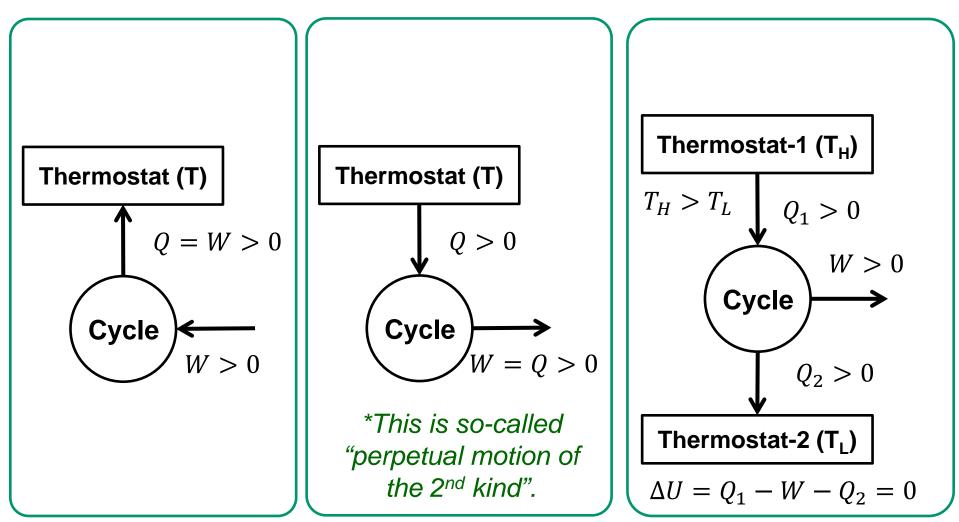
"There is no thermodynamic cycle that can absorb energy (>0) from lowertemperature thermostat and release energy (>0) to higher-temperature thermostat, without making any change other than these energy transfers."



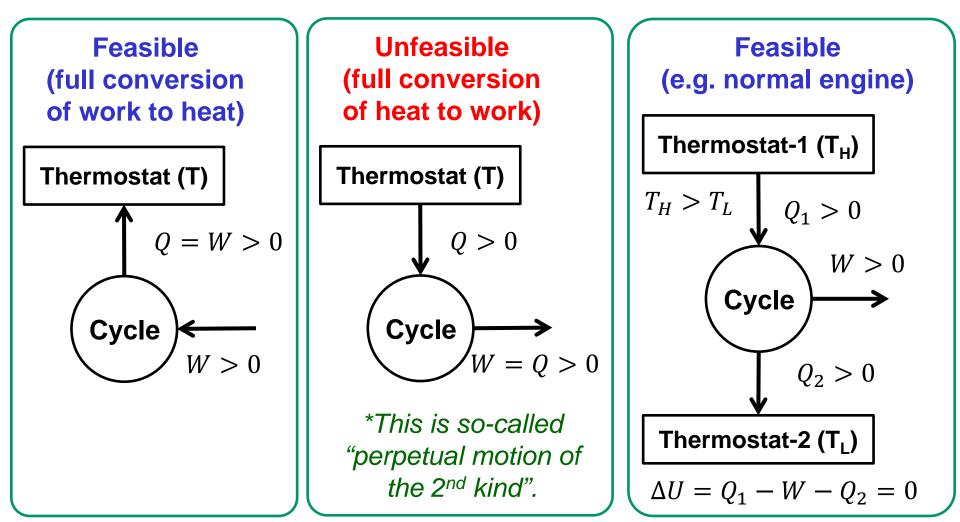
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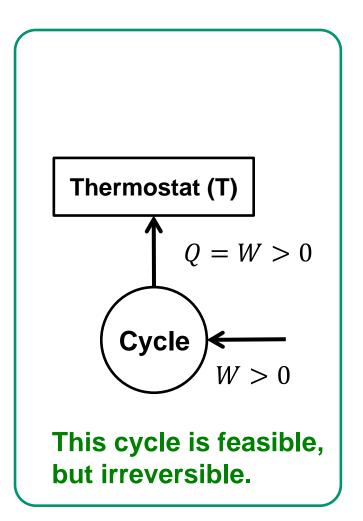
"There is no thermodynamic cycle that can absorb energy (>0) from a sole thermostat and then convert all the absorbed energy to a work to the surroundings."



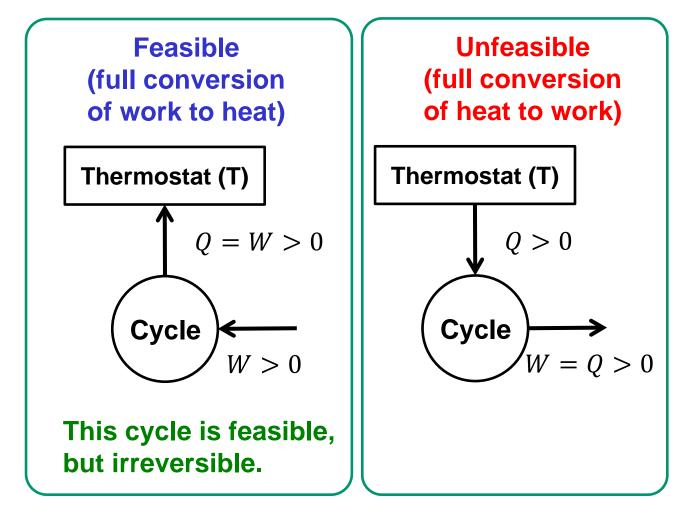
"There is no thermodynamic cycle that can absorb energy (>0) from a sole thermostat and then convert all the absorbed energy to a work to the surroundings."



Thomson's statement also indicate that "a cycle that convert all work to heat (as left figure) is irreversible". Why?



Thomson's statement also indicate that "a cycle that convert all work to heat (as left figure) is irreversible", because to make it reversible, we need to make a backward operation of it, which is forbidden (right figure).



Review of the last class -quasi-static/reversible/irreversible process>

- < Definition of quasi-static process (in this course, we use definition (1)!) >
 - 1) Very (infinitesimally) slow process so that we consider the system is always at some equilibrium state.
 - Very (infinitesimally) slow process and the process takes place with adhering the system to some equilibrium state and keeping concerned thermodynamic quantities of the system and the surroundings equal.
 > for this definition, "quasi-static" is equivalent with "reversible"
 > In this course, this is the definition of reversible process.

✓ "A reversible process is a process that, after it has taken place, can be reversed and causes no change in either the system or its surroundings." (*wikipedia)
 ✓ If some change remains, the process is an irreversible process.

- ✓ Even if the left engine is impossible, if Q_2 in the right engine can be extremely minimized, we may approximately consider $W \sim Q_1$, which means all absorbed heat is almost converted to a work.
 - ✓ However, it is impossible to "extremely minimize Q_2 ". There is a principle to restrict it. (to be given latter)

