
powder diffraction file PDF

1 CHANPARK, MSE, SNU Spring-2019 Crystal Structure Analyses

ICDD & PDF

ICDD - International Centre for Diffraction Data

- A non-profit scientific organization dedicated to collecting, editing, publishing, and distributing powder diffraction data for the identification of crystalline materials
- Joint Committee for Chemical Analysis by Powder Diffraction Methods ; founded in 1941
- Joint Committee on Powder Diffraction Standards (JCPDS) ; established in 1969
- Renamed to ICDD in 1978

PDF - powder diffraction file

- a collection of single-phase XRPD patterns in the form of tables of characteristic interplanar spacings (d's) and corresponding relative intensities (I's) along with other pertinent physical and crystallographic properties
- dif file
- ###.dif

XRPD: X-ray Powder Diffraction

www.icdd.com

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PDF card

Quality mark

* Highest quality
 i reasonable quality
 o low quality
 blank quality lower than o
 c calculated data
 r d's from Rietveld refinement

Set number
 Add 1950 → year

Chemical formula
 Chemical name
 Mineral name

Experimental info
 Types of X-ray
 Wavelength
 Monochromator/filter
 Method of d measurement
 Max measurable d-spacing
 Method of I measurement
 I/I(corundum)
 Literature source

Physical data
 Xtal system
 International tables space group symbol
 Axial lengths
 Axial ratios
 Interaxial angles
 Number of chemical formulas in unit cell
 Melting point
 Literature source
 X-ray density
 Measured density
 Figure of Merit

5- 628

NaCl	d Å	Int	h k l	d Å	Int	h k l
Sodium Chloride	3.26	13	111			
	2.821	100	200			
	1.994	55	220			
Halite, syn	1.701	2	311			
Rad. CuKα, λ 1.5405 Filter Ni d-sp	1.628	15	222			
Cutoff Int. Diffractometer I/I_{cor}: 4.40	1.410	6	400			
Ref. Swanson, Fuyai, Natl. Bur. Stand. (U.S.), Circ. 539, II 41 (1953)	1.294	1	331			
	1.261	11	420			
	1.1515	7	422			
	1.0855	1	511			
	0.9969	2	440			
	0.9533	1	531			
	0.9401	3	600			
	0.8917	4	620			
	0.8601	1	533			
	0.8503	32	622			
	0.8141	2	444			

General comments

D's, I's and Miller indices

PDF card

PDF # 050628,

CAS; chemical abstracts service registry number

05-0628 Quality: *

CAS Number: 7647-14-5

PDF # 050628, Wave

05-0628 Quality: *
 CAS Number: 7647-14-5
 Molecular Weight: 58.44
 Volume[CD]: 179.43
 Dx: 2.163 Dm: 2.168
 Sys: Cubic
 Lattice: Face-centered
 S.G.: Fm $\bar{3}$ m (225)
 Cell Parameters:
 a 5.640 b c
 α β γ
 SS/FOM: F17=93(.0108, 17)
 I/I_{cor}: 4.40
 Rad: CuKα1
 Lambda: 1.5405
 Filter: Ni
 d-sp:
 Mineral Name:
 Halite syn

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I/I_{cor}: 4.40
 Rad: CuKα1
 Lambda: 1.5405
 Filter: Ni
 d-sp:

Mineral Name:
 Halite syn

k	l	d(A)	Int-f	h	k	l
3	1	.94010	3	6	0	0
2	0	.89170	4	6	2	0
2	2	.86010	1	5	3	3
1	1	.85030	3	6	2	2
4	0	.81410	2	4	4	4
3	1					

PDF

- PDF-2
- PDF-4+: most advanced database, designed for both phase ID and quantitative analysis.

Data Entry Source	PDF-2 2016	PDF-4+ 2016 WebPDF-4+ 2016	PDF-4/ Minerals 2016	PDF-4/ Organics 2017
00- ICDD	115,066	115,066	12,031	39,395
01- FIZ	165,264	67,498	12,294	12,185
02- CCDC	0	0	0	431,359
03- NIST	10,067	2,960	216	281
04- MPDS	0	198,367	19,748	0
05- ICDD Crystal Data	722	722	52	32,785
Total No. of Data Sets	291,119	384,613	44,341	516,054
Subfile Distribution:				
Inorganic	258,130	351,612	44,285	33,943
Organic	41,386	42,229	701	505,530
New Entries	12,616	18,736	1,489	14,090
Rietveld—No. with atomic coordinates	0	271,449	33,574	96,825
Reference Intensity Ratio (RIR)—I/I ₀	193,567	286,885	33,362	484,021
Experimental Digital Patterns	0	11,287	127	6,062
Pattern Fitting—Calculated Digital Patterns	0	384,613	44,341	516,054

All ICDD databases combine the power of both powder diffraction and crystal structure reference data. We are the only crystallographic database in the world with quality marks and quality review processes that are ISO certified. Each PDF database includes our integrated data mining software.

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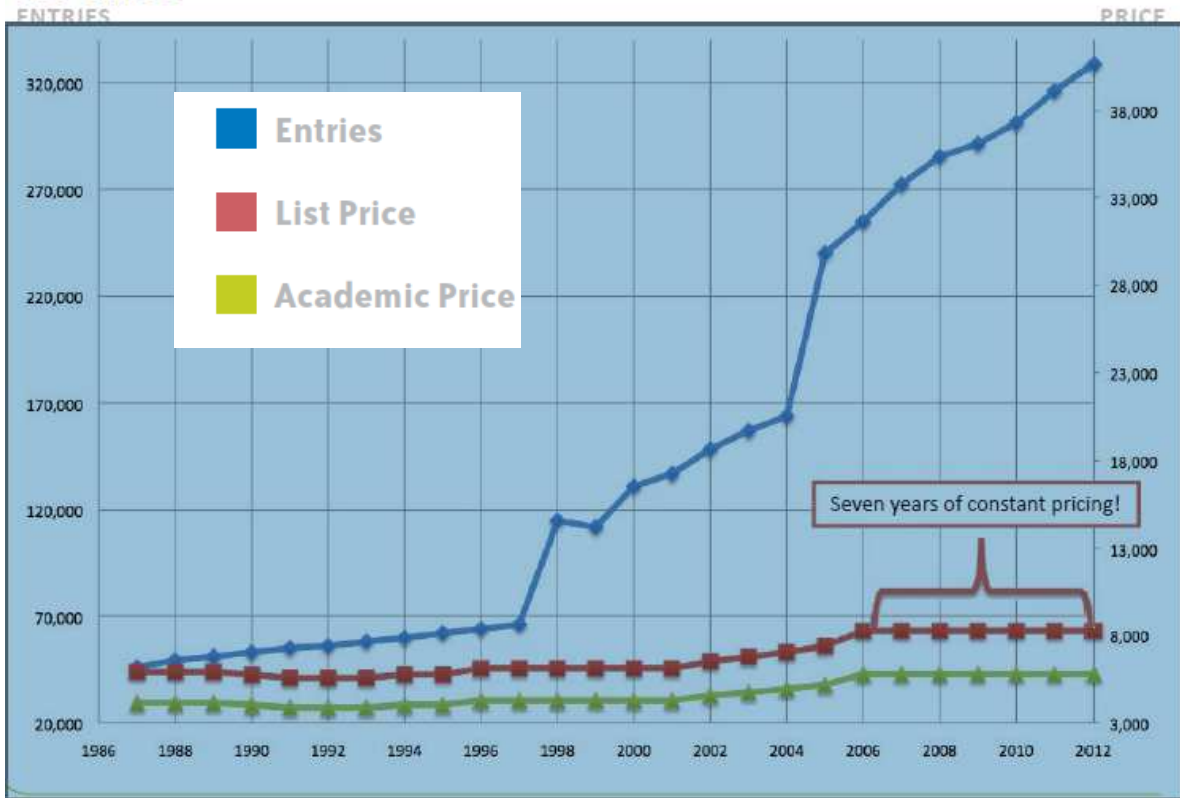
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PDF VALUE



PDF - Quality Mark & Figure of Merit

Quality Mark

- * highest quality - average $\Delta 2\theta < 0.03$ degree, all lines were indexed, I measured quantitatively
- i reasonable quality - average $\Delta 2\theta < 0.06$ degree, indexed with no more than two lines being unaccounted for, I measured quantitatively
- o low quality - low precision, poorly characterized, no unit cell data
- blank quality lower than o
- c calculated data
- r d's from Rietveld refinement
- h (hypothetical)

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"Evaluating Data Quality" from ICDD

PDF # 050628,	
05-0628	Quality: *
CAS Number: 7647-14-5	
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γ	
SS/FOM: F17=93(0108, 17)	
I/lor:	4.40
Rad:	CuK α 1
Lambda:	1.5405
Filter:	Ni
d-sp:	
Mineral Name:	
Halite syn	

Figure of Merit

- To quantify better the quality of a given set of d-spacings
- To judge the credibility and worth of the results
- To evaluate the quality of d measurements
- The higher, the better < 20 → poor quality

SS/FOM (Smith & Snyder FOM)

$$F_N = \frac{1}{|\Delta 2\theta|} \frac{N_{obs}}{N_{poss}}$$

F_N = Figure of merit

$\Delta 2\theta$ = The average error in 2θ

N_{obs} = The number of lines observed

N_{poss} = Number of lines possible

Space Group, International Table

International Tables for Crystallography, Brief teaching edition of Volume A: Space-group symmetry
Edited by Theo Hahn

International Tables for Crystallography, Volume A: Space-group symmetry
Edited by Theo Hahn

International Tables for Crystallography, Volume H: Powder Diffraction
Edited by C.J. Gilmore, J.A. Kaduk and H. Schenk

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International Tables

NEW for 2014

Volume H: Powder diffraction

Editors: Christopher J. Gilmore, James A. Kaduk and Henk Schenk

ISBN 978-1-118-41628-0
IUCr/Wiley

Powder diffraction is the most widely used crystallographic method with applications spanning all aspects of structural science. This new volume of *International Tables* will cover all aspects of the technique with over 50 chapters written by experts in the field.

The volume will be about 800 pages long and will be available both in print and online. It will be split into seven sections (see provisional contents overleaf):

- Part 1. Introduction
- Part 2. Instrumentation and sample preparation
- Part 3. Methodology


P:
P:
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International Tables for Crystallography, Volume H, Powder Diffraction

Christopher Gilmore, H. U. Schenk

ISBN: 978-1-118-41628-0
600 pages
September 2017

Hardcover \$310.00 **ADD TO CART**



2019

Part 1. Introduction
Part 2. Instrumentation and sample preparation
Part 3. Methodology
Part 4. Structure determination
Part 5. Defects, texture, microstructure and fibres
Part 6. Software
Part 7. Applications

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Contents (provisional)

Part 1. Introduction

Overview and principles of powder diffraction (R. E. Dinnebier and S. J. L. Billinge)

Part 2. Instrumentation and sample preparation

Instrumentation – laboratory X-rays (A. Kern)
 Synchrotron radiation and powder diffraction (A. Fitch)
 Neutrons (J. Rodriguez-Carvajal)
 Electrons (J. M. Zuo, J. L. Libán, J. Zhang, T. E. Gorelik and U. Kolb)
 Two-dimensional powder diffraction (B. B. He)
 Temperature (C. Reiss)
 Sample environment – high-pressure devices (A. Katrusiak)
 Magnetic and electric fields in powder diffraction (H. Ehrenberg and H. Fuess)
 Cells for in situ powder diffraction investigation of chemical reactions (W. van Beek and P. Pattison)
 Sample preparation (P. Whittfield and A. Huq)

Part 3. Methodology

The optics, alignment and calibration of the Bragg-Brentano laboratory X-ray diffractometer (J. Cline)
 Diffraction from powders (P. Stephens)
 Data processing – powder diffraction peak profiles (R. B. Von Dreele)
 Indexing (A. Allomare, C. Cuocci, A. Moltneri and R. Rizzi)
 Data reduction to I_{hkl} (A. Le Bail)
 Whole powder pattern modelling: microstructure determination from powder diffraction data (M. Leoni)
 Crystallographic databases and powder diffraction (J. A. Kaduk)
 The clustering and visualization of powder diffraction data (C. Gilmore)
 Quantitative phase analysis (J. Madsen, N. Scarlett, R. Kleeberg and K. Knorr)

Part 4. Structure determination

An overview of currently used structure determination methods for powder diffraction data (K. Shankland)
 Solving crystal structures using reciprocal-space methods (A. Altomare, C. Cuocci, A. Moltneri and R. Rizzi)
 Real-space methods for structure solution from powder diffraction data: application to molecular structures (W. The use of supplementary information to solve crystal structures from powder diffraction (A. J. Florence)
 Solving and refining inorganic structures (R. Gerni)
 Solving and refining zeolite structures (L. B. McCusker and C. Baerlocher)
 Magnetic structure determination and refinement using neutron powder diffraction (J. Rodriguez-Carvajal)
 Rietveld refinement (B. H. Toby)
 Application of the maximum entropy method to powder diffraction data (O. V. Magdysyuk, S. van Smaalen and Structure validation (J. A. Kaduk)
 Powder CIF (B. H. Toby)

Part 5. Defects, texture, microstructure and fibres

Domain size and domain size distributions (M. Leoni)
 Stress and strain (N. C. Popa)
 Quantitative texture analysis and combined analysis (D. Chateigner, L. Lutterotti and M. Morales)
 Thin films and multilayers (M. Birkholz)
 Multigrain crystallography and three-dimensional grain mapping (H. F. Poulsen and G. B. M. Vaughan)
 X-ray diffraction from non-crystalline materials: the Debye model (S. Bates)
 Nanometre-scale structure from powder diffraction: total scattering and atomic pair distribution function
 Scattering methods for disordered heterogeneous materials (A. J. Allen)
 Fibres (P. Langan)

Part 6. Software

Software for powder diffraction (C. J. Gilmore, J. A. Kaduk and H. Schenk)

Part 7. Applications

Macromolecular powder diffraction (I. Margiolaki)
 Mining and mineral processing (N. V. Y. Scarlett and D. L. Bish)
 Ceramic materials and powder diffraction (W. Wong-Ng)
 Applications in glass ceramics (S. T. Misture)
 Powder diffraction characterization of cements (M. A. G. Aranda, A. G. De La Torre and L. Leon-Reina)
 Fibre diffraction and whole powder pattern fitting in polymers (R. Somestekar)
 Powder diffraction and pharmaceuticals (J. Bernstein, S. M. Reutzel-Edens and J.-O. Henck)
 Forensic applications of X-ray powder diffraction (D. F. Rendle)
 Materials for energy storage and conversion (M. A. Rodriguez)
 X-ray diffraction in the petroleum industry (R. W. Morton and D. E. Simon)
 Superconductivity (Q. Huang)
 Organic pigments (M. Schmidt)
 Selected applications of Rietveld XRD analysis in the aluminium industry (F. R. Fere)
 Powder diffraction in art and archaeology (C. Artioli)

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Software for powder diffraction (C. J. Gilmore, J. A. Kaduk and H. Schenk)

Part 7. Applications

Symmetry operation

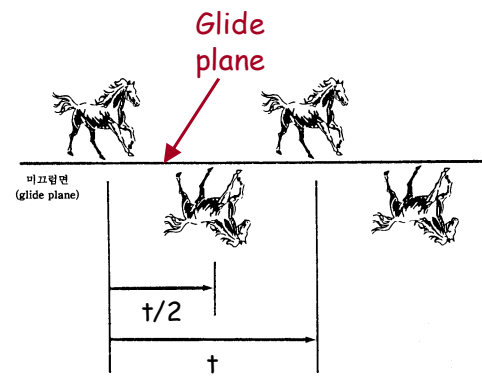
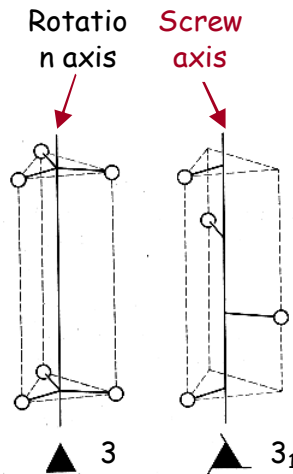
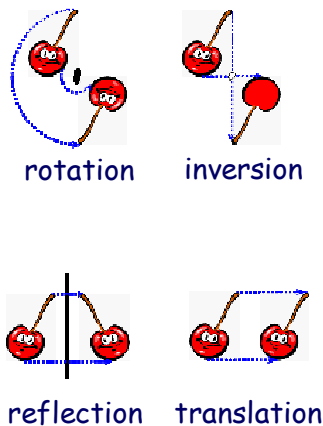
(1) Rotation; 1 2 3 4 6 (2) Reflection; m ($= \bar{2}$)

(3) Inversion (center of symmetry) ($= \bar{1}$)

(4) Rotation-inversion; $\bar{1}$ (=center of symmetry), $\bar{2}$ (= mirror), $\bar{3}$, $\bar{4}$, $\bar{6}$

(5) Screw axis; rotation + translation $2_1, 3_1, 3_2, 4_1, 4_2, 4_3, 6_1, \dots, 6_5$

(6) Glide plane; reflection + translation, a, b, c, n, d



Crystal symmetry, 14 Bravais lattice

Crystal System	Bravais Lattices	Symmetry	Symmetry	Axis System
Cubic	P, I, F	m3m	m3m	$a=b=c, \alpha=\beta=\gamma=90$
Tetragonal	P, I	4/mmm	4/mmm	$a=b \neq c, \alpha=\beta=\gamma=90$
Orthorhombic	P, C, I, F	mmm	mmm	$a \neq b \neq c, \alpha=\beta=\gamma=90$
Hexagonal	P	6/mmm	6/mmm	$a=b \neq c, \alpha=\beta=90, \gamma=120$
Rhombohedral	R	3m	3m	$a=b=c, \alpha=\beta=\gamma \neq 90$
Monoclinic	P, C	2/m	2/m	$a \neq b \neq c, \alpha=\gamma=90, \beta \neq 90$
Triclinic	P	1	1	$a \neq b \neq c, \alpha \neq \beta \neq \gamma \neq 90$

Quartz

Crystal System: trigonal

Bravais Lattice: primitive

Space Group: **P3₂21**

Lattice Parameters: 4.9134 x 4.9134 x 5.4052 Å

Atom Positions:

	x	y	z
Si	0.470	0	0.667
O	0.414	0.268	0.786

P3₂21

P 3₂ 2 1

6/mmm

6/m m m

Symmetry directions, Space group

Xtal systems	Symmetry directions		
Triclinic			
Monoclinic		b	
Orthorhombic	a	b	c
Tetragonal	c	<a>	<110>
Trigonal	c	<a>	
Hexagonal	c	<a>	<210>
Cubic	<a>	<111>	<110>

Fmmm

Face centered lattice

m ⊥ to a axis

m ⊥ to b axis

m ⊥ to c axis

P3₂21

Primitive lattice

3₂ along the c axis

2 fold rot axis along the a axis

1 fold rot axis along the <210>

Fd3m

Face centered lattice

d ⊥ to a axis

3 fold axis along the <111>

m ⊥ to c axis

Short Hermann-Mauguin symbol

Point group

Schoenflies symbol

Crystal system symbol

Space group number

Full Hermann-Mauguin symbol

from International Tables for X-ray Crystallography

Choice of origin
Asymmetric unit
Symmetry operations

$P2_1/c$ No. 14
UNIQUE AXIS b , CELL CHOICE 1

C_{2h}^5 $P12_1/c1$

$2/m$ Patterson symmetry $P12/m1$

Monoclinic

Projection of symmetry elements

Projection of a general position

Origin at $\bar{1}$
Asymmetric unit $0 \leq x \leq 1; 0 \leq y \leq \frac{1}{2}; 0 \leq z \leq 1$
Symmetry operations:
(1) 1 (2) $2(0, \frac{1}{2}, 0) 0, y, \frac{1}{2}$ (3) $\bar{1} 0, 0, 0$ (4) $c x, \frac{1}{2}, z$

International Tables for X-ray Crystallography

General & special positions

CONTINUED		No. 14	$P2_1/c$
Generators selected (1); $\tau(1,0,0)$; $\tau(0,1,0)$; $\tau(0,0,1)$; (2); (3)			
Positions	Coordinates	Reflection conditions	
Multiplicity, Wyckoff letter, Site symmetry		General:	
4 e 1	(1) x, y, z (2) $\bar{x}, y + \frac{1}{2}, \bar{z} + \frac{1}{2}$ (3) \bar{x}, y, \bar{z} (4) $x, y + \frac{1}{2}, z + \frac{1}{2}$	$h0l : l = 2n$ $0k0 : k = 2n$ $00l : l = 2n$ Special: as above, plus $hkl : k + l = 2n$ $hkl : k + l = 2n$ $hkl : k + l = 2n$ $hkl : k + l = 2n$	
2 d $\bar{1}$	$\frac{1}{2}, 0, \frac{1}{2}$ $\frac{1}{2}, \frac{1}{2}, 0$	General position Special position	
2 c $\bar{1}$	$0, 0, \frac{1}{2}$ $0, \frac{1}{2}, 0$		
2 b $\bar{1}$	$\frac{1}{2}, 0, 0$ $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$		
2 a $\bar{1}$	$0, 0, 0$ $0, \frac{1}{2}, \frac{1}{2}$		
Symmetry of special projections			
Along [001] $p2gm$ $a' = a$ $b' = b$ Origin at $0, 0, z$	Along [100] $p2gg$ $a' = b$ $b' = c$ Origin at $x, 0, 0$	Along [010] $p2$ $a' = \frac{1}{2}c$ $b' = a$ Origin at $0, y, 0$	
Maximal non-isomorphic subgroups			
I	[2] $P1c1 (Pc, 7)$ 1; 4 [2] $P12_11 (P2_1, 4)$ 1; 2 [2] $P\bar{1} (2)$ 1; 3		
IIa	none		
IIb	none		
Maximal isomorphic subgroups of lowest index			
IIc	[2] $P12_1/c1 (a' = 2a \text{ or } a' = 2a, c' = 2a + c) (P2_1/c, 14)$; [3] $P12_1/c1 (b' = 3b) (P2_1/c, 14)$		
Minimal non-isomorphic supergroups			
I	[2] $Pnna (52)$; [2] $Pmna (53)$; [2] $Pcca (54)$; [2] $Pbam (55)$; [2] $Pccn (56)$; [2] $Pbcm (57)$; [2] $Pnmm (58)$; [2] $Pbcn (60)$; [2] $Pbca (61)$; [2] $Pnma (62)$; [2] $Cmce (64)$		
II	$A12/m1 (C2/m, 12)$; [2] $C12/c1 (C2/c, 15)$; [2] $I12/c1 (C2/c, 15)$; [2] $P12/m1 (C' = \frac{1}{2}c) (P2_1/m, 11)$; [2] $P12/c1 (b' = \frac{1}{2}b) (P2/c, 13)$		

➤ Asymmetric unit

- ✓ a region of space which fills all space when all the symmetry operations of the space group are applied
- ✓ smaller than a unit cell

➤ Unit cell

- ✓ a region of space which fills all space when the translation operations are applied

Origin at $\bar{1}$

Asymmetric unit $0 \leq x \leq 1; 0 \leq y \leq \frac{1}{2}; 0 \leq z \leq 1$

Symmetry operations

(1) 1 (2) $2(0, \frac{1}{2}, 0) \ 0, y, \frac{1}{2}$ (3) $\bar{1} \ 0, 0, 0$ (4) $c \ x, \frac{1}{4}, z$

International Tables for X-ray Crystallography

➤ Symmetry operations

- ✓ (n) of the general equivalent position can be obtained from (1) x, y, z by symmetry operation number (n)
- ✓ (3) $-x, -y, -z \leftarrow \bar{1}$ with 0,0,0 as inversion point

4 c 1 (1) x, y, z (2) $\bar{x}, y + \frac{1}{2}, \bar{z} + \frac{1}{2}$ (3) $\bar{x}, \bar{y}, \bar{z}$ (4) $x, \bar{y} + \frac{1}{2}, z + \frac{1}{2}$

Origin at $\bar{1}$

Asymmetric unit $0 \leq x \leq 1; 0 \leq y \leq \frac{1}{2}; 0 \leq z \leq 1$

Symmetry operations

(1) 1 (2) $2(0, \frac{1}{2}, 0) \ 0, y, \frac{1}{2}$ (3) $\bar{1} \ 0, 0, 0$ (4) $c \ x, \frac{1}{4}, z$

Screw part
Screw axis
Location of inversion point
 c glide, glide plane $x, \frac{1}{4}, z$

International Tables for X-ray Crystallography

➤ Generators

- ✓ Symmetry operations and their sequence, selected to generate all symmetrically equivalent points of the general position from a point x,y,z
- ✓ Set of symmetry operators which when successfully multiplied yield ALL of the operators of the group
- ✓ List of symmetry operations selected that can generate all of the symmetry operations of the space group

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; (2); (3)

translations

Symmetry operations			
(1) 1	(2) $2(0, \frac{1}{2}, 0)$ $0, y, \frac{1}{2}$	(3) $\bar{1}$ $0, 0, 0$	(4) c $x, \frac{1}{2}, z$

International Tables for X-ray Crystallography

➤ Positions

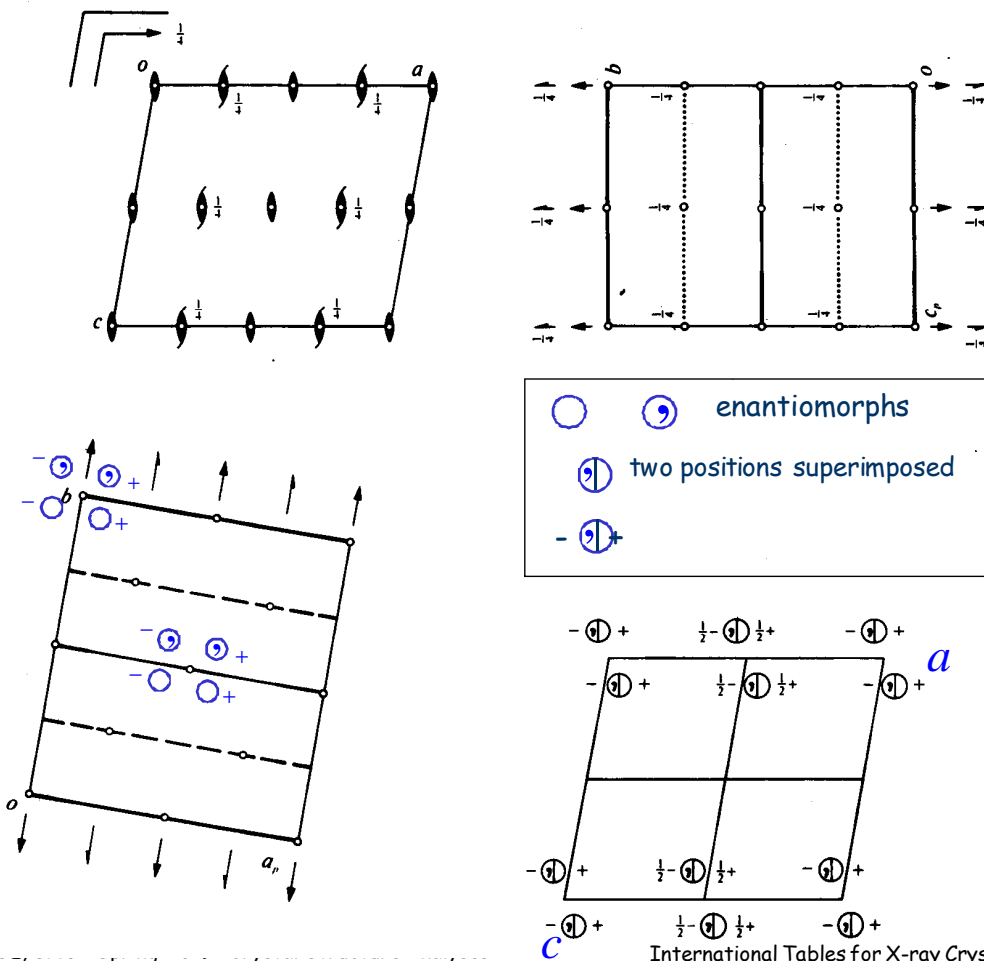
- ✓ Multiplicity (rank); # equivalent points per unit cell
- ✓ Wyckoff letter
- ✓ Site symmetry (point symmetry of the position)
- ✓ Coordinates of the equivalent positions

	Positions	Coordinates			
	Multiplicity, Wyckoff letter, Site symmetry				
General position	4 e 1	(1) x,y,z	(2) $\bar{x}, y + \frac{1}{2}, \bar{z} + \frac{1}{2}$	(3) $\bar{x}, \bar{y}, \bar{z}$	(4) $x, \bar{y} + \frac{1}{2}, z + \frac{1}{2}$
Special position	2 d $\bar{1}$	$\frac{1}{2}, 0, \frac{1}{2}$	$\frac{1}{2}, \frac{1}{2}, 0$		
	2 c $\bar{1}$	$0, 0, \frac{1}{2}$	$0, \frac{1}{2}, 0$		
	2 b $\bar{1}$	$\frac{1}{2}, 0, 0$	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$		
	2 a $\bar{1}$	$0, 0, 0$	$0, \frac{1}{2}, \frac{1}{2}$		

- The number of equivalent points in the unit cell = **multiplicity**
- A **general position** is a set of equivalent points with point symmetry (site symmetry) 1
- A **special position** is a set of equivalent points with point symmetry (site symmetry) higher than 1
- The **asymmetric unit** of a space group is the smallest part of the unit cell from which the whole cell may be filled by the operation of all the symmetry operations

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$C \frac{2}{m}$

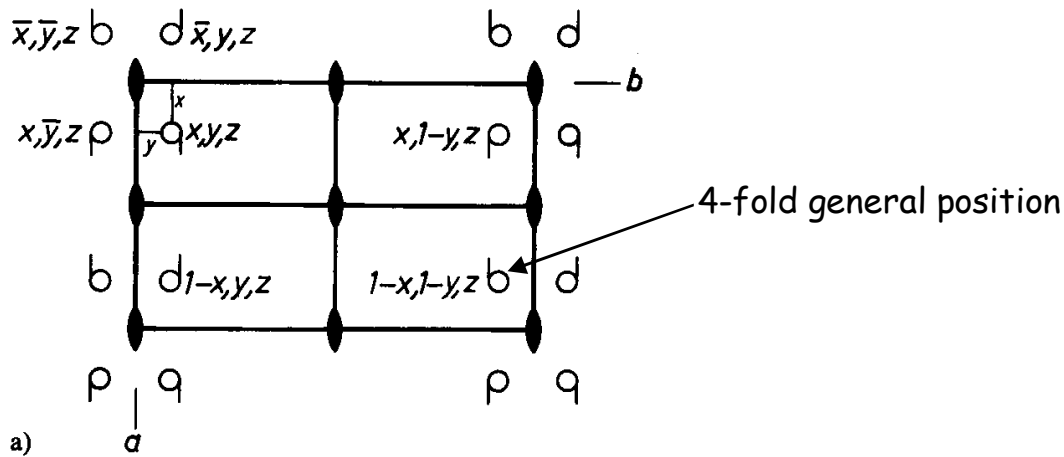


22 CHANPARK, MSE, SNU Spring-2019 Crystal Structure Analyses

Space Group - Pmm2

- for a point x, y, z (general point),
symmetry element generates $\bar{x}, y, z; x, \bar{y}, z; \bar{\bar{x}}, \bar{\bar{y}}, z$

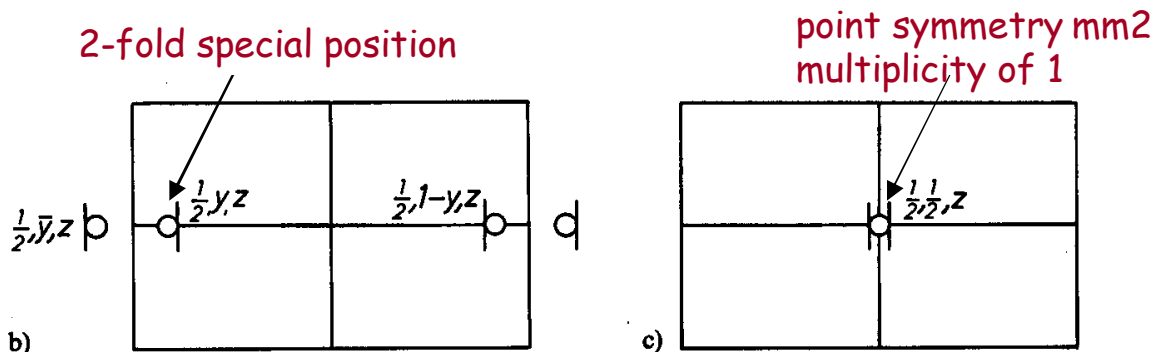
$x, y, z; \bar{x}, y, z; x, \bar{y}, z; \bar{\bar{x}}, \bar{\bar{y}}, z$ are equivalent (multiplicity of 4)



Space Group - Pmm2

- move a point x, y, z on to mirror plane at $\frac{1}{2}, y, z$
 x, y, z and $1-x, y, z$ coalesce to $\frac{1}{2}, y, z$
 $x, 1-y, z$ and $1-x, 1-y, z$ coalesce to $\frac{1}{2}, 1-y, z$
- **multiplicity of 2**

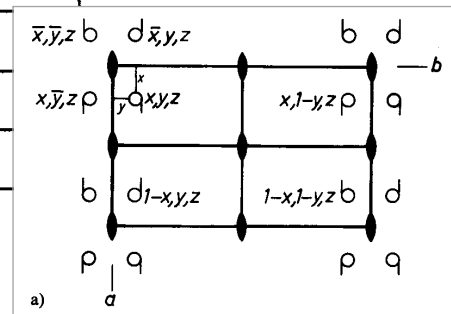
✓ as long as the point remains on the mirror plane, its multiplicity is unchanged - degree of freedom 2



A special point arises from the merging of equivalent positions

Space Group Pmm2

Position	Degrees of freedom	Multiplicity	Site symmetry	Coordinates of equivalent points
general	3	4	1	$x, y, z; \bar{x}, \bar{y}, z;$ $x, \bar{y}, z; \bar{x}, y, z$
special	2	2	m	$\frac{1}{2}, y, z; \frac{1}{2}, \bar{y}, z$
		2	m	$0, y, z; 0, \bar{y}, z$
		2	m	$x, \frac{1}{2}, z; \bar{x}, \frac{1}{2}, z$
		2	m	$x, 0, z; \bar{x}, 0, z$
	1	1	mm2	$\frac{1}{2}, \frac{1}{2}, z$
		1	mm2	$\frac{1}{2}, 0, z$
		1	mm2	$0, \frac{1}{2}, z$
		1	mm2	$0, 0, z$



Space Group - Pmm2

$Pmm2$

No. 25

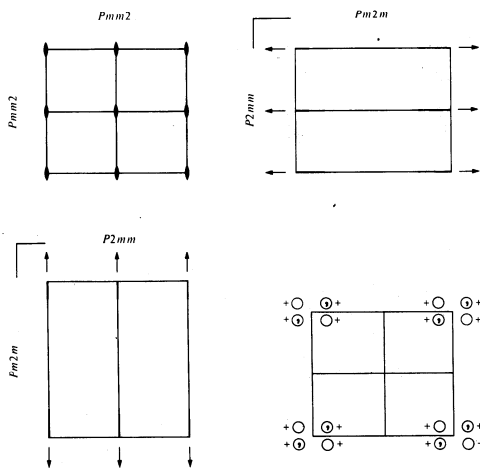
C_{2v}^1

$Pmm2$

$mm2$

Orthorhombic

Patterson symmetry $Pmmm$



Origin on $mm2$

Asymmetric unit $0 \leq x \leq \frac{1}{2}; 0 \leq y \leq \frac{1}{2}; 0 \leq z \leq 1$

Symmetry operations

(1) 1 (2) 2 $0, 0, z$ (3) m $x, 0, z$ (4) m $0, y, z$

- short space group symbol
- Schoenflies symbol
- point group
- crystal system
- number of space group
- full space group symbol
- projection of symmetry elements
- projection of general position

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; (2); (3)

Positions

Multiplicity,
Wyckoff letter,
Site symmetry

Coordinates

Reflection conditions

		(1)	(2)	(3)	(4)
4	<i>i</i> 1	x, y, z	\bar{x}, \bar{y}, z	x, \bar{y}, z	\bar{x}, y, z
2	<i>h</i> <i>m</i> ..	$\frac{1}{2}, y, z$	$\frac{1}{2}, \bar{y}, z$		
2	<i>g</i> <i>m</i> ..	$0, y, z$	$0, \bar{y}, z$		
2	<i>f</i> . <i>m</i> .	$x, \frac{1}{2}, z$	$\bar{x}, \frac{1}{2}, z$		
2	<i>e</i> . <i>m</i> .	$x, 0, z$	$\bar{x}, 0, z$		
1	<i>d</i> <i>m m</i> 2	$\frac{1}{2}, \frac{1}{2}, z$			
1	<i>c</i> <i>m m</i> 2	$\frac{1}{2}, 0, z$			
1	<i>b</i> <i>m m</i> 2	$0, \frac{1}{2}, z$			
1	<i>a</i> <i>m m</i> 2	$0, 0, z$			

General:

no conditions

Special: no extra conditions

Zinc Blende, ZnS

 $F\bar{4}3m$ (No.216)

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; $t(0, \frac{1}{2}, \frac{1}{2})$; $t(\frac{1}{2}, 0, \frac{1}{2})$; (2); (3); (5); (13)

Positions

Multiplicity,
Wyckoff letter,
Site symmetry

Coordinates

Reflection conditions

		(0,0,0)+	$(0, \frac{1}{2}, \frac{1}{2})+$	$(\frac{1}{2}, 0, \frac{1}{2})+$	$(\frac{1}{2}, \frac{1}{2}, 0)+$
96	<i>i</i> 1	(1) x, y, z	(2) \bar{x}, \bar{y}, z	(3) \bar{x}, y, \bar{z}	(4) x, \bar{y}, \bar{z}
		(5) z, x, y	(6) z, \bar{x}, \bar{y}	(7) \bar{z}, \bar{x}, y	(8) \bar{z}, x, \bar{y}
		(9) y, z, x	(10) \bar{y}, z, \bar{x}	(11) y, \bar{z}, \bar{x}	(12) \bar{y}, \bar{z}, x
		(13) y, x, z	(14) \bar{y}, \bar{x}, z	(15) y, \bar{x}, \bar{z}	(16) \bar{y}, x, \bar{z}
		(17) x, z, y	(18) \bar{x}, z, \bar{y}	(19) \bar{x}, \bar{z}, y	(20) x, \bar{z}, \bar{y}
		(21) z, y, x	(22) z, \bar{y}, \bar{x}	(23) z, y, \bar{x}	(24) \bar{z}, \bar{y}, x

General position

 h, k, l permutable

General:

 $hkl: h+k, h+l, k+l = 2n$ $0kl: k, l = 2n$ $hhl: h+l = 2n$ $h00: h = 2n$

Special: no extra conditions

48	<i>h</i> . <i>m</i>	x, x, z	\bar{x}, \bar{x}, z	\bar{x}, x, \bar{z}	x, \bar{x}, \bar{z}	z, x, x	z, \bar{x}, \bar{x}
		\bar{z}, \bar{x}, x	\bar{z}, x, \bar{x}	x, z, x	\bar{x}, z, \bar{x}	x, \bar{z}, \bar{x}	\bar{x}, \bar{z}, x
24	<i>g</i> 2. <i>m m</i>	$x, \frac{1}{2}, \frac{1}{2}$	$\bar{x}, \frac{1}{2}, \frac{1}{2}$	$\frac{1}{2}, x, \frac{1}{2}$	$\frac{1}{2}, \bar{x}, \frac{1}{2}$	$\frac{1}{2}, \frac{1}{2}, x$	$\frac{1}{2}, \frac{1}{2}, \bar{x}$
24	<i>f</i> 2. <i>m m</i>	$x, 0, 0$	$\bar{x}, 0, 0$	$0, x, 0$	$0, \bar{x}, 0$	$0, 0, x$	$0, 0, \bar{x}$
16	<i>e</i> .3 <i>m</i>	x, x, x	\bar{x}, \bar{x}, x	\bar{x}, x, \bar{x}	x, \bar{x}, \bar{x}		
4	<i>d</i> $\bar{4}3m$	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$					
4	<i>c</i> $\bar{4}3m$	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$					
4	<i>b</i> $\bar{4}3m$	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$					
4	<i>a</i> $\bar{4}3m$	$0, 0, 0$					

Special position

Zinc Blende, ZnS

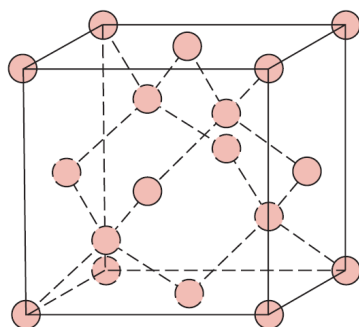
- diamond derivative structure
- Zn and S replace the C atoms in diamond
- Zn cubic close packing; S $\frac{1}{2}$ tetrahedral site
- Zn and S cubic close packing displaced by $\frac{1}{4}, \frac{1}{4}, \frac{1}{4}$

$F\bar{4}3m$ (No.216)

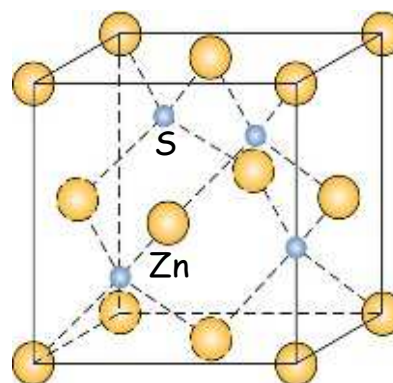
Zn: $4a, \bar{4}3m, 0,0,0$

Zn: $4c, \bar{4}3m, \frac{1}{4}, \frac{1}{4}, \frac{1}{4}$

Diamond, Si, Ge



Zinc blende structure
ZnS, SiC



Point group vs. space group

Point groups: A group of point symmetry operations, whose operation leaves at least one point unaltered. Any operation involving lattice translations is thus excluded	Space groups: A group of symmetry operations which include lattice translations
$1 \quad \bar{1}$ $2 \quad m$ $3 \quad \bar{3}$ $4 \quad \bar{4}$ $6 \quad \bar{6}$	$1 \quad \bar{1}$ $2 \quad m \quad 2_1; a, b, c, n, e, d$ $3 \quad \bar{3} \quad 3_1, 3_2$ $4 \quad \bar{4} \quad 4_1, 4_2, 4_3$ $6 \quad \bar{6} \quad 6_1, 6_2, 6_3, 6_4, 6_5$ lattice translations
a, b, c α, β, γ	a_0, b_0, c_0 α, β, γ
Order of the symmetry operations e.g. $4/m \quad 2/m \quad 2/m$ $\quad \quad \quad \quad \quad \quad \quad \quad \quad $ $\quad \quad \quad c \quad <a> \quad <110>$	Order of the symmetry operations e.g. $P4_2/m \quad 2/m \quad 2/m$ $\quad \quad \quad \quad \quad \quad \quad \quad \quad $ $\quad \quad \quad c \quad <a> \quad <110>$
General form: Set of equivalent faces each with face symmetry 1	General position: Set of equivalent points each with site symmetry 1
$\frac{f_{\text{asymmetric face unit}}}{f_{\text{sphere}}}$ multiplicity of general form	$\frac{V_{\text{asymmetric unit}}}{V_{\text{unit cell}}}$ multiplicity of general point
Multiplicity of general form of the point group	Multiplicity of the general position in all space groups with a P-lattice that are isomorphous with that point group
Special form: Set of equivalent faces each with face symmetry >1	Special position: Set of equivalent points each with site symmetry >1