# INTRODUCTION

- What is Heat Transfer ?
- Continuum Hypothesis
- Local Thermodynamic Equilibrium
- Conduction
- Radiation
- Convection
- Energy Conservation

# WHAT IS HEAT ? In a solid body

Crystal : a three-dimensional periodic array of atoms



Oscillation of atoms about their various positions of equilibrium (lattice vibration): The body possesses heat.

Conductors: free electrons ↔ Dielectics



The energy of the oscillatory motions:

the heat-energy of the body

More vigorous oscillations:

the increase in temperature of the body

### In a gas

The storage of thermal energy:

molecular translation, vibration and rotation change in the electronic state intermolecular bond energy



Internuclear separation distance (diatomic molecule) average kinetic energy

$$\boldsymbol{E}_{\boldsymbol{u}} = \frac{1}{2}\boldsymbol{m}\overline{\boldsymbol{u}_{\boldsymbol{m}}^2} \equiv \frac{3}{2}\boldsymbol{k}_{\boldsymbol{B}}\boldsymbol{T}$$

$$k_B = 1.3807 \times 10^{-23} \text{ J/K}$$

at T = 300 K, air M = 28.97 kg/kmol  $\langle u_m^2 \rangle^{1/2} = 468.0$  m/s

### HEAT TRANSFER

Heat transfer is the study of thermal energy transport within a medium or among neighboring media by

- Molecular interaction: conduction
- Fluid motion: convection
- Electromagnetic wave: radiation

resulting from a spatial variation in temperature

Energy carriers: molecule, atom, electron, ion, phonon (lattice vibration), photon (electro-magnetic wave)



(3×10<sup>7</sup> molecules at sea level, 15°C, 1atm)

- microscopic uncertainty due to molecular random motion
- macroscopic uncertainty

due to the variation associated with spatial distribution of density

In continuum, velocity and temperature vary smoothly.  $\rightarrow$  differentiable

Mean free path of air at STP (20°C, 1atm)  $\lambda_{\rm m} = 66 \text{ nm}, \langle u_m^2 \rangle^{1/2} = 468.0 \text{ m/s}$ 

bulk motion vs molecular random motion

## LOCAL THERMODYNAMIC EQUILIBRIUM



# CONDUCTION

### **Gases and Liquids**

 Due to interactions of atomic or molecular activities



- Net transfer of energy by random molecular motion
- Molecular random motion→ diffusion
- Transfer by collision of random molecular motion

### **Solids**

- Due to lattice waves induced by atomic motion
- In non-conductors (dielectrics): exclusively by lattice waves
- In conductors: translational motion of free electrons as well

### Fourier's Law



# Notation

- **Q** : amount of heat transfer [J]
- q: heat transfer rate [W],  $q' = \frac{Q}{\Delta t}$
- q'': heat transfer rate per unit area [W/m<sup>2</sup>]  $q'' = \frac{Q}{A \cdot \Delta t}$

q': heat transfer rate per unit length [W/m]

$$q' = \frac{Q}{L \cdot \Delta t}$$

q = q''A = q'L

### **Heat Flux**



Ex) 
$$T(x, y) = x + y$$
  $(0 \le x \le 1, 0 \le y \le 1)$   
 $T = \text{constant line or surface: isothermal lines or surfaces (isotherms)}$   
 $T = 0.5 \ 1 \ x$   
 $\vec{q}'' = -k\nabla T = -k\left(\frac{\partial T}{\partial x}\hat{i} + \frac{\partial T}{\partial y}\hat{j}\right) = -k\left(\hat{i} + \hat{j}\right)$   
 $= q_x'\hat{i} + q_y'\hat{j} = -k\hat{i} - k\hat{j}$   
 $q_x'' = -k, q_y'' = -k$ 

### temperature : driving potential of heat flow

heat flux : normal to isotherms

along the surface of T(x, y, z) = constant



#### **Steady-State One Dimensional Conduction**



$$q_x'' + \Delta q_x'' = q_x'' + \frac{dq_x''}{dx} \Delta x + O\left[\left(\Delta x\right)^2\right]$$

$$=-k\frac{dT}{dx}+\frac{d}{dx}\left(-k\frac{dT}{dx}\right)\Delta x+O\left[\left(\Delta x\right)^{2}\right]$$

$$\Delta q_x'' = \frac{d}{dx} \left( -k \frac{dT}{dx} \right) \Delta x + O\left[ \left( \Delta x \right)^2 \right] = 0$$

or 
$$\frac{d}{dx}\left(-k\frac{dT}{dx}\right)+O(\Delta x)=0$$

As 
$$\Delta x \to 0$$
,  $\frac{d}{dx} \left( k \frac{dT}{dx} \right) = 0$ 

When 
$$k = \text{const.}, \quad \frac{d^2 T}{dx^2} = 0$$

## RADIATION

# **Thermal Radiation**



**Characteristics of Thermal Radiation** 

- 1. Independence of existence and temperature of medium
- Ex) ice lens



black carbon paper

### 2. Acting at a distance Ex) sky radiation

- electromagnetic wave or photon
- photon mean free path
- volume or integral phenomena

conduction

- fluid: molecular random motion
- solid: lattice vibration (phonon) free electron

diffusion or differential phenomena as long as continuum holds

# 3. Spectral and Directional Dependence quanta history of path



# **Two Points of View**

### 1. Electromagnetic wave

- Maxwell's electromagnetic theory
- Useful for interaction between radiation and matter

### 2. Photons

- Planck's quantum theory
- Useful for the prediction of spectral properties of absorbing, emitting medium

# **Radiating Medium**

- Transparent medium ex: air
- Participating medium emitting, absorbing and scattering ex: CO<sub>2</sub>, H<sub>2</sub>O
- Opaque material

### Stefan-Boltzmann's law

Blackbody emissive power

$$E_b = q_{b,e}'' = \sigma T^4 [W/m^2]$$

blackbody: a perfect absorber

$$\boldsymbol{\sigma} = 5.6696 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4$$

Stefan by experiment (1879):  $E_b \sim T^4$ Boltzmann by theory (1884):  $E_b = \sigma T^4$ 

### Planck's law

(The Theory of Heat Radiation, Max Planck, 1901)

spectral distribution of hemispherical emissive power of a blackbody in vacuum

$$E_{\lambda b} = \frac{2\pi C_1}{\lambda^5 \left( e^{C_2 / \lambda T} - 1 \right)}$$
$$C_1 = h C_0^2, \ C_2 = h C_0 / k$$

C<sub>0</sub>: speed of light in vacuum
h: Planck constant
k: Boltzmann constant



$$E_{b} = \int_{0}^{\infty} \frac{2\pi C_{1}}{\lambda^{5} \left( e^{C_{2}/\lambda T} - 1 \right)} d\lambda$$
$$= \sigma T^{4}$$

For a real surface,

 $E = \varepsilon \sigma T^4$ 

*ɛ*: emissivity

Blackbody spectral emissive power

### **Surface Radiation**

#### **Ray-tracing method vs Net-radiation method**



$$q'' = J - G$$

$$J = \varepsilon \sigma T^{4} + \rho G$$

$$q'' = J - \frac{1}{\rho} \left( J - \varepsilon \sigma T^{4} \right) = \frac{1}{\rho} \left( \rho J - J + \varepsilon \sigma T^{4} \right)$$

$$= \frac{1}{\rho} \left( \varepsilon \sigma T^{4} - \varepsilon J \right) = \frac{\varepsilon}{1 - \varepsilon} \left( \sigma T^{4} - J \right)$$



### Ex) a body in an enclosure



a blackbody.

# CONVECTION

energy transfer due to bulk or macroscopic motion of fluid

bulk motion: large number of molecules moving collectively

- convection: random molecular motion
   + bulk motion
- advection: bulk motion only



- hydrodynamic (or velocity) boundary layer
- thermal (or temperature) boundary layer

at y = 0, velocity is zero: heat transfer only by molecular random motion



### When radiation is negligible,



**Convection Heat Transfer Coefficient** 

$$h = -\frac{k_f}{\left(T_s - T_{\infty}\right)} \frac{\partial T}{\partial n} \bigg|_{+} = -\frac{k_s}{\left(T_s - T_{\infty}\right)} \frac{\partial T}{\partial n} \bigg|_{-}$$

not a property: depends on geometry and fluid dynamics

- forced convection
- free (natural) convection
- external flow
- Internal flow
- laminar flow
- turbulent flow

## **ENERGY CONSERVATION** First law of thermodynamics

- control volume (open system)
- material volume (closed system)



In a time interval  $\Delta t$ :  $E_{in} + E_g - E_{out} = \Delta E_{st}$ steady-state:  $\dot{E}_{st} = 0 \rightarrow \dot{E}_{in} + \dot{E}_g - \dot{E}_{out} = 0$ 

# Surface Energy Balance $\dot{E}_{\rm in} \longrightarrow \dot{E}_{\rm out}$ $\dot{E}_{\rm in} = \dot{E}_{\rm out}$ $\begin{aligned} \mathbf{y}_{\text{cond},s}^{\text{sur.}} &= \mathbf{q}_{\text{cond},f}^{"} + \mathbf{q}_{\text{rad}}^{"} \\ &= \mathbf{q}_{\text{conv}}^{"} + \mathbf{q}_{\text{rad}}^{"} \\ &= -k_{f} \frac{\partial T}{\partial n} \\ &=$ sur. Ex) $q_{\rm cond,s}$
#### Example 1.2



Find:

- 1) Surface emissive power *E* and irradiation *G*
- 2) Pipe heat loss per unit length, q'

Assumptions:

- 1) Steady-state conditions
- 2) Radiation exchange between the pipe and the room is between a small surface in a much larger enclosure.
- 3) Surface emissivity = absorptivity



1. Surface emissive power and irradiation

 $E = \varepsilon \sigma T_s^4 = 0.8(5.67 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4)(473 \text{ K})^4 = 2,270 \text{ W/m}^2$ 

$$G = \sigma T_{sur}^4 = 5.67 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4 (298 \text{ K})^4 = 447 \text{ W/m}^2$$



2. Heat loss from the pipe

$$q_{\text{loss}} = q_{\text{conv}} + q_{\text{rad}} = hA(T_s - T_{\infty}) + \varepsilon \sigma A(T_s^4 - T_{\text{sur}}^4) \qquad A = \pi DL$$
  
=  $h(\pi DL)(T_s - T_{\infty}) + \varepsilon (\pi DL) \sigma (T_s^4 - T_{\text{sur}}^4)$   
$$q' = \frac{q_{\text{loss}}}{L} = 15 \text{ W/m}^2 \cdot \text{K} (\pi \times 0.07 \text{ m}) (200 - 25)^{\circ}\text{C}$$
  
+  $0.8(\pi \times 0.07 \text{ m}) 5.67 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4 (473^4 - 298^4) \text{ K}^4$ 

= 577 W/m + 421 W/m = 998 W/m

#### Example 1.2



 $\boldsymbol{q}_{\text{loss}} = \boldsymbol{q}_{\text{conv}} + \boldsymbol{q}_{\text{rad}}$ 

Q: Why not  $q_{loss} = q_{conv} + q_{rad} + q_{cond}$ ? Conduction does not take place?



$$q_{loss}'' = q_{cond,s}'' = q_{cond,f}'' + q_{rad}''$$
$$-k_s \frac{dT}{dr} \bigg|_s = -k_f \frac{dT}{dr} \bigg|_f + \varepsilon \sigma \left(T_s^4 - T_{sur}^4\right)$$
$$\equiv h \left(T_s - T_{\infty}\right) + \varepsilon \sigma \left(T_s^4 - T_{sur}^4\right)$$
$$q_{loss}'' = q_{conv}'' + q_{rad}'', \quad q_{cond,f}'' \equiv q_{conv}''$$

#### Example 1.4

#### Hydrogen-air Proton Exchange Membrane (PEM) fuel cell



Three-layer membrane electrode assembly (MEA)

Anode: (exothermic)  $2H_2 \rightarrow 4H^+ + 4e^-$ 

Cathode:  $O_2 + 4e^- + 4H^+ \rightarrow 2H_2O$ 

 $2\mathrm{H}_{2} + \mathrm{O}_{2} \rightarrow 2\mathrm{H}_{2}\mathrm{O}$ 

Role of Electrolytic membrane

- 1. transfer hydrogen ions
- 2. serve as a barrier to electron transfer

Membrane needs a moist state to conduct ions.

Liquid water in cathode: block oxygen from reaching cathode reaction site  $\rightarrow$  need to control  $T_c$ 

The convection heat coefficient,  $h = 10.9 \text{ W} \cdot \text{s}^{0.8} / \text{m}^{2.8} \cdot \text{K} \times V^{0.8}$ 



Find: The required cooling air velocity, V, needed to maintain steady state operation at  $T_c$ =56.4°C.

$$h = 10.9 \text{ W} \cdot \text{s}^{0.8} / \text{m}^{2.8} \cdot \text{K} \times V^{0.8}$$
  
 $\dot{E}_{g} = 11.25 \text{ W}$ 

Assumptions:

- 1) Steady-state conditions
- 2) Negligible temperature variations within the fuel cell
- 3) Large surroundings
- 4) Insulated edge of fuel cell
- 5) Negligible energy flux by the gas or liquid flows

Energy balance on the fuel cell



$$\begin{aligned} \vec{E}_{in} + \vec{E}_{g} - \vec{E}_{out} &= \Delta \vec{E}_{st} \\ \dot{\vec{E}}_{g} = \dot{\vec{E}}_{out} = q_{conv} + q_{rad} \\ \dot{\vec{E}}_{g} = 11.25 \, \mathrm{W} = q_{conv} + q_{rad} \\ q_{conv} &= hA(T_{c} - T_{\infty}) \\ q_{conv} &= \dot{\vec{E}}_{g} - q_{rad} \\ q_{rad} &= \varepsilon A\sigma (T_{c}^{4} - T_{sur}^{4}) \\ hA(T_{c} - T_{\infty}) &= \dot{\vec{E}}_{g} - \varepsilon A\sigma (T_{c}^{4} - T_{sur}^{4}) \\ h = 10.9 \, \mathrm{W} \cdot \mathrm{s}^{0.8} / \mathrm{m}^{2.8} \cdot \mathrm{K} \times V^{0.8} \\ &= \frac{\dot{\vec{E}}_{g} - \varepsilon A\sigma (T_{c}^{4} - T_{sur}^{4})}{A(T_{c} - T_{\infty})} \end{aligned}$$

V = 9.4 m/s

#### Example 1.5



Find:

Expression for time needed to melt the ice,  $t_m$ 

Assumptions:

1) Inner surface of wall is at  $T_f$  through the process.

- 2) Constant properties
- 3) Steady-states, 1-D conduction through each wall
- 4) Conduction area of one wall =  $W^2(L \ll W)$



 $\boldsymbol{h}_{sf}$  : latent heat of fusion

$$q_{\text{cond}} = kA \frac{T_1 - T_f}{L} = k \left( 6W^2 \right) \frac{T_1 - T_f}{L}$$

$$\left[6kW^2\frac{T_1-T_f}{L}\right]t_m = Mh_{sf}$$

$$\boldsymbol{t}_{m} = \frac{Mh_{sf}L}{6kW^{2}(T_{1}-T_{f})}$$



Find:

1) Cure temperature **T** for  $h = 15 \text{ W/m}^2 \cdot \text{K}$ 

2) Effect of air flow on the cure temperature for  $2 \le h \le 200 \text{ W/m}^2 \cdot \text{K}$ 

Value of h for which the cure temperature is 50°C.

Assumptions:

- 1) Steady-state conditions
- 2) Negligible heat loss from back surface of plate
- 3) Plate is very thin and a small object in large surroundings, coating absorptivity  $\alpha = \varepsilon = 0.5$  w.r.t. irradiation from the surroundings



 $2 \le h \le 200 \text{ W/m}^2 \cdot \text{K}$ 





#### WHY HEAT TRANSFER ?



## **Natural System / Temperature Distribution in the Earth**



# **Environment / Solar Radiation**



Wavelength  $\lambda$ ,  $\mu$ m

# **Energy Conversion / Gas Turbine Engine**





JT8D





CF6

## **Energy Conversion / Gas Turbine Blade Cooling**



#### Manufacturing / Ultra-Short Pulse Laser Material Processing

Steel foil

 $100\mu m$  in thickness

#### ns Machining Process



4.2 J/cm<sup>2</sup> @ 3.3 ns

#### **fs Machining Process**



0.5 J/cm<sup>2</sup> @ 200 fs





## Manufacturing / Nano-Machining

#### Atomic Force Microscope + Near Field Optics (Grigoroporos, UC Berkeley)



 Manogrids

Nanodots



Nanocurves



Nano-lithography/machining

#### **Cryo-Preservation**



Adiabatic demagnetization technique Paramagnetic salt  $T = 10^{-5}$  K

Laser Surgery



## **Electrical & Electronics / Thermal Management**



- local heat flux of 200-300 W/cm<sup>2</sup>, today
- equivalent to that of 1 Mt nuclear blast at 1 mile from ground zero
- only one order of magnitude less than the sun

## **Electrical & Electronics / Cooling Techniques**

#### **Direct Immersion**



**Heat Pipes** 



Refrigeration Cooling

Thermoelectric Coolers (TEC)







### **Electrical & Electronics / Micro Cooler**



## **Process / Nanoparticle Control Principle**

#### (M. Choi, SNU)





## **Process / Nanofluids**

#### (Argonne National Lab., USA)



 Size dependent physical properties: color, conductivity

 Large surface area:
 3 orders of magnitude greater than microfluids

• Surface structure: ~20% of atoms near the surface

Problem: rapid setting agglomeration

## **Process / Thermal Conductivity of Nanofluids**



# **Process / PDP Thermal Process**



## Process / Rapid Thermal Processing (RTP) System



## **Sensors & Actuators / Micro Thermal Flow Sensor**



Low emission, High performance Electronic gasoline injection control



## **Sensors & Actuators / Micro Thermal Flow Sensor**



Characteristics

- Independent to inlet pressure, temperature variations
- Sensitive, precise, low power consuming...

#### **Considerations**

- Conduction, convection heat transfer between substrate and fluid
- Sensor / heater array shape and material
- Transient heating

## **Sensors & Actuators / Tunable AC Thermal Anemometry**



#### **Sensors & Actuators / Scanning Thermal Microscope**



#### **Sensors & Actuators / Scanning Thermal Microscope**

## Sub-surface Thermal Image – Overhang

#### 80 nano DRAM









(b)





(d)

## **Sensors & Actuators / Scanning Thermal Microscope**

#### Sub-surface Thermal Image – Result



#### Topography

2*w* signal
## **Sensors & Actuators / Thermal Ink Jet**

- Facts about Ink Jet
  - heating rate >10<sup>8</sup> K/s
  - heat flux >  $5 \times 10^8$  W/m<sup>2</sup>



## **Real Estate to Patent**



## Paradigm Shift

