



# Clustering

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# CURE

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- [Guha, Rastogi, Shim 98]
- Propose a new hierarchical clustering algorithm
  - Use a small number of representatives
  - Note:
    - Centroid-based: use 1 point to represent a cluster => Too little information..Hyper-spherical clusters
    - MST-based: use every point to represent a cluster => Too much information..Easily mislead
- Use random sampling
- Use Partitioning
- Provide correct labeling



# CURE

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A **Representative** set of points:

- Small in number :  $c$
- Distributed over the cluster
- Each point in cluster is close to one representative
- Distance between clusters:

**smallest distance between representatives**



# CURE

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## Finding **Scattered** Representatives

- We want to
  - Distribute around the center of the cluster
  - Spread well out over the cluster
  - Capture the physical shape and geometry of the cluster
- Use **farthest point heuristic** to scatter the points over the cluster
- Shrink uniformly around the mean of the cluster



# CURE

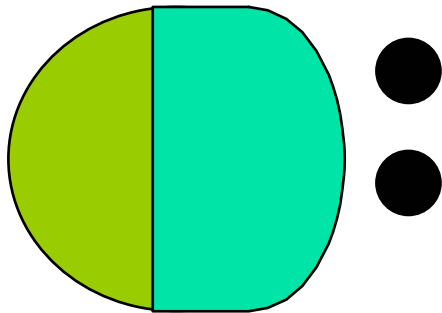
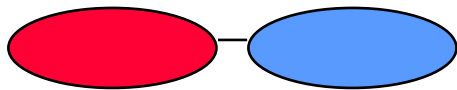
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- Random sampling
  - If each cluster has a certain number of points, with **high probability** we will sample in proportion from the cluster
  - $\epsilon n$  points in cluster translates into  $\epsilon s$  points in sample of size  $s$

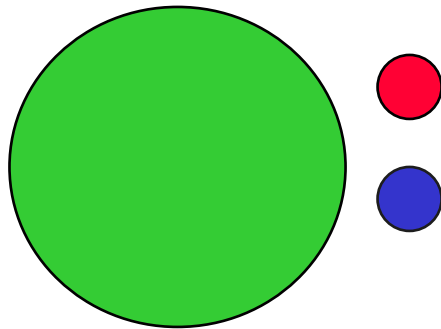
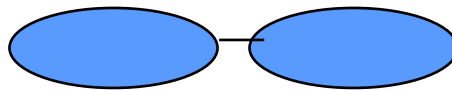
**Sample size is independent of  $n$  to represent all sufficiently large clusters**
- Labeling data on disk
  - Choose some constant number of representatives from each cluster

# CURE

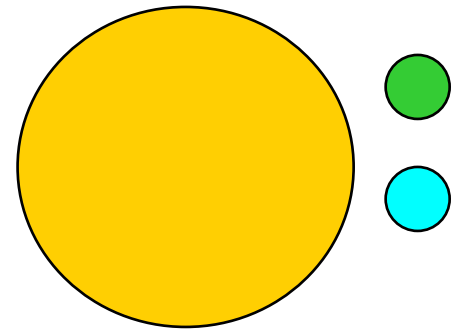
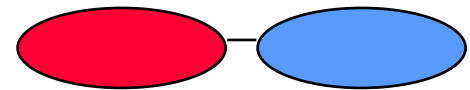
## Comparisons



**(a) Centroid**



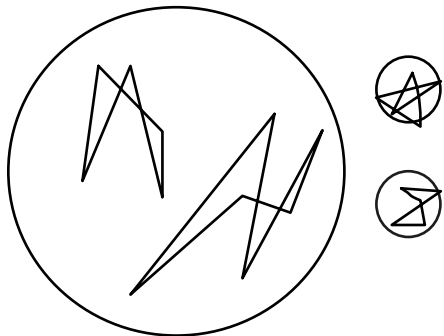
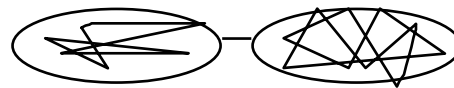
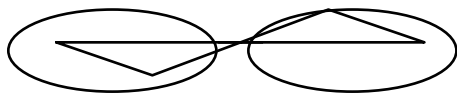
**(b) MST**



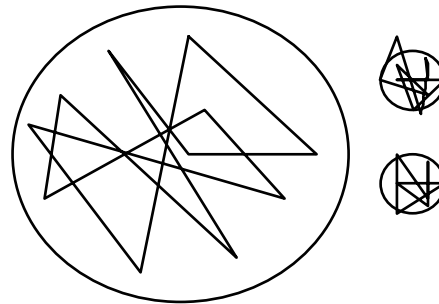
**(c) CURE**

# CURE

## Number of Representatives



**(a)  $c = 5$**



**(b)  $c = 10$**



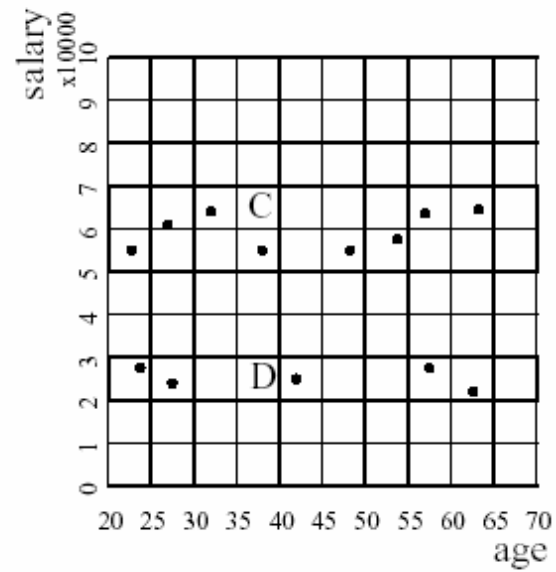
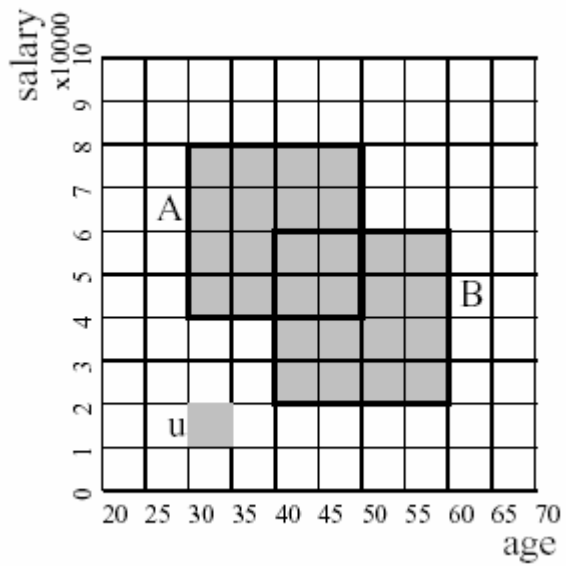
# CLIQUE

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- [Agrawal, Gehrke, Gunopulos, Raghavan 98]
- Automatically finds subspaces with high-density clusters
- Can be considered as both density-based and grid-based
  - Partition the data space  $S$  into non-overlapping rectangular units which has the same interval in each dimension
  - Calculate selectivity in each unit, which is a fraction of total data points contained in the unit
  - A unit  $u$  is dense if  $\text{selectivity}(u)$  is greater than threshold
  - Partitioning interval and density threshold are input parameter that user can define



# CLIQUE





# CLIQUE

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- Find dense units in bottom-up fashion
  - Use monotonicity : If a set of point  $S$  is a cluster in  $k$ -dimensional space, then  $S$  is also cluster in any  $(k-1)$  dimensional projections of this space
  - Having determined  $(k-1)$  dimensional dense units, the candidate  $k$  dimensional units are determined like Apriori algorithm
- Find cluster
  - After finding dense units, find connected units that would be a cluster
- Generate minimal description for the clusters
  - NP-hard problem
  - Use greedy method





# ROCK

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- [Guha, Rastogi, Shim 99]
- Hierarchical clustering algorithm for **categorical** attributes
  - Example: market basket customers
- Use novel concept of **links** for merging clusters
  - $\text{sim}(p_i, p_j)$ : **similarity function** that captures the closeness between  $p_i$  and  $p_j$
  - $p_i$  and  $p_j$  are said to be **neighbors** if  $\text{sim}(p_i, p_j) \geq \theta$
  - $\text{link}(p_i, p_j)$ : the number of **common** neighbors
- A new **goodness** measure was proposed
- Random sampling used for scale up
- Use labeling phase



# ROCK

<1, 2, 3, 4, 5>

{1, 2, 3}	{1, 4, 5}
{1, 2, 4}	{2, 3, 4}
{1, 2, 5}	{2, 3, 5}
{1, 3, 4}	{2, 4, 5}
{1, 3, 5}	{3, 4, 5}

<1, 2, 6, 7>

{1, 2, 6}
{1, 2, 7}
{1, 6, 7}
{2, 6, 7}

$$\text{sim}(T_1, T_2) = \frac{|T_1 \cap T_2|}{|T_1 \cup T_2|} \geq 0.5$$

- {1, 2, 6} and {1, 2, 7} have 5 links.
- {1, 2, 3} and {1, 2, 6} have 3 links.

# Clustering for Categorical Attributes



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- Traditional algorithms do not work well for categorical attributes
- **Jaccard coefficient** has been used for categorical attributes
  - Centroid approach cannot be used
  - Group average and MST algorithms tend to fail
  - Hard to reflect the properties of the neighborhood of the points
  - Fail to capture the natural clustering of data sets
- Viewing as points with (0/1) values of attributes fails too!



# Example (Traditional Alg.)

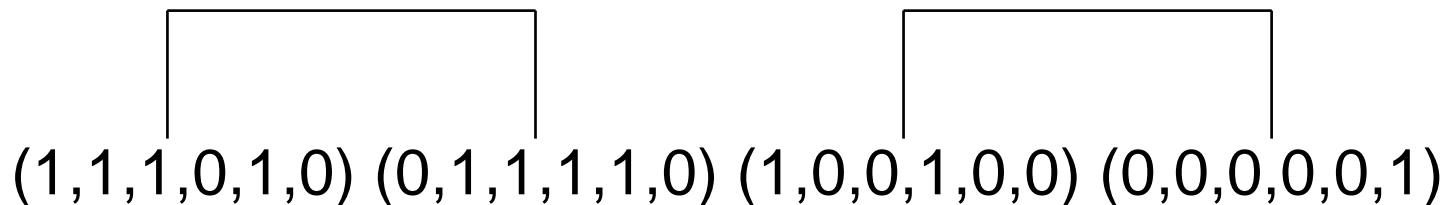
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- As the cluster size grows
  - The number of attributes appearing in mean go up
  - Their values in the mean decreases
  - Thus, very difficult to distinguish two points on few attributes

Database: {1, 2, 3, 5}    {2, 3, 4, 5}    {1, 4}    {6}

(0.5, 1, 1, 0.5, 1, 0)

(0.5, 0, 0, 0.5, 0, 0.5)





# Conclusions

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- CURE and ROCK are interesting algorithms