2019 Spring

"Phase Equilibria in Materials"

03.06.2019

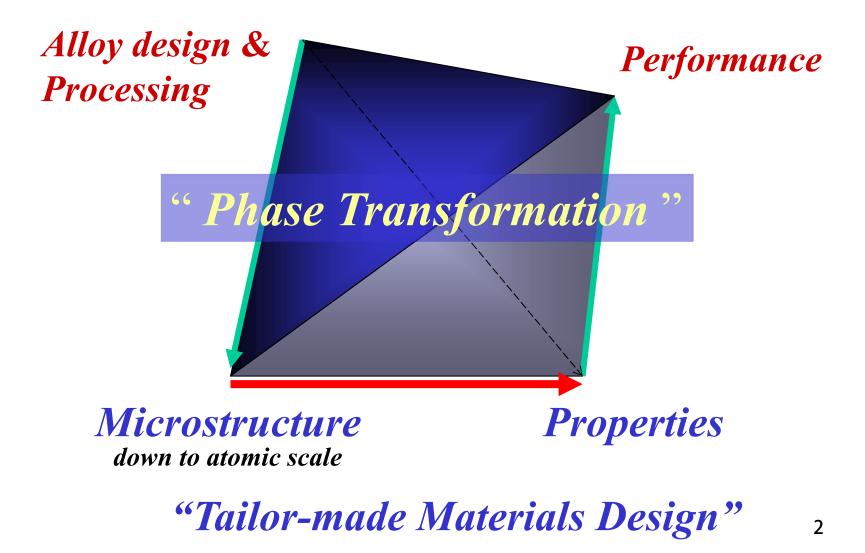
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Contents for previous class

Microstructure-Properties Relationships

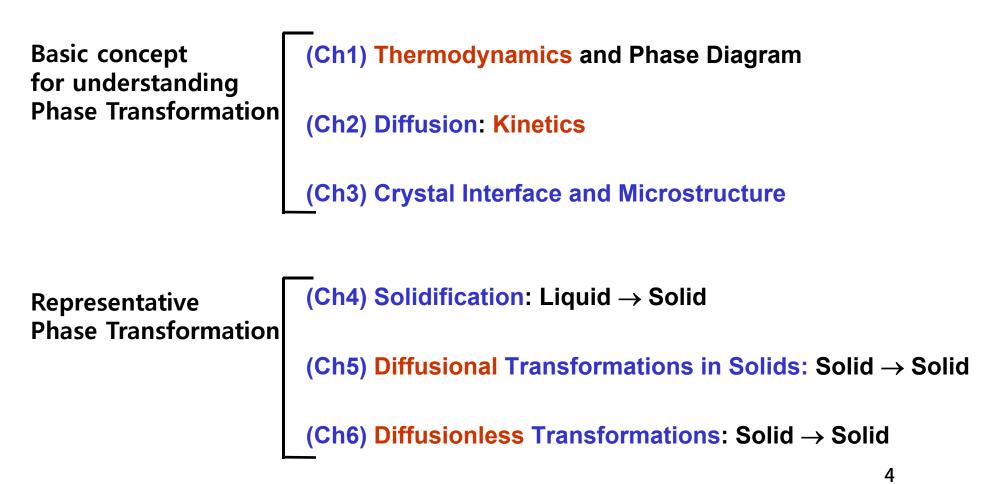


Contents for previous class

Important!!! Understanding and Controlling Phase Transformation of Materials

Contents in Phase Transformation

D.A. Porter and K.E. Eastering, "Phase Transformations in Metals and Alloys"



Contents for previous class

Phase Equilibria in Materials

Thermodynamics

Phase diagrams Binary, Ternary, Quarternary phase diagram

Contents for today's class

CHAPTER 1 Introductory Thermondynamics

- Equilibrium
- Single component system

Gibbs Free Energy as a Function of Temp. and Pressure

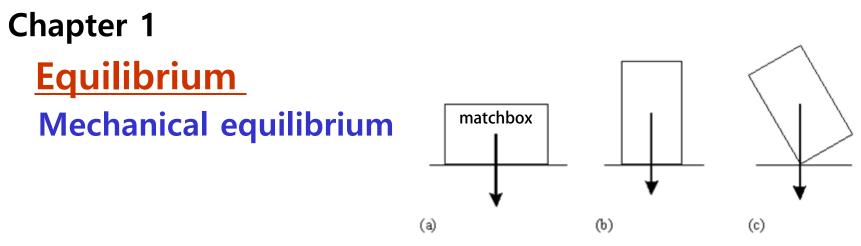
- Phase Transformation
- Solidification: Liquid → Solid

Driving force for solidification

- Classification of phase transition

First order transition/Second order transition

Q1: "thermodynamic equilibrium"? Lowest possible value of Gibb's Free Energy



: total potential energy of the system is a minimum.

Thermal equilibrium

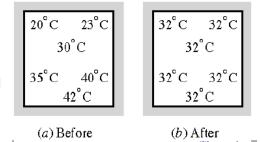
: absence of temperature gradients in the system

Chemical equilibrium

: no further reaction occurs between the reacting substances i.e. the forward and reverse rates of reaction are equal.

Thermodynamic equilibrium

: the system is under mechanical, thermal and chemical equilibrium The properties of the system-P, T, V, concentrations-do not change with time. ⁸



Thermodynamic free energy, the energy in a physical system that can be converted to do work,

When no useful work is being extracted from the sub-system,

 $dX \leq 0$

The energy *X* reaching a minimum at equilibrium, when dX=0.

If no chemical species can enter or leave the sub-system, then $\sum \mu_{iR} N_i$ can be ignored.

If furthermore the temperature of the sub-system is such that T is always equal to T_R ,

then X = E - TS + const' = A + const'

in particular:

Helmholtz free energy, the energy that can be converted into work at a constant temperature and volume

If the volume V is constrained to be constant, then

where F is the thermodynamic potential called Helmholtz free energy, F=E-TS.

Under constant volume conditions therefore, dF < 0 if a process is to go forward;

and dF=0 is the condition for equilibrium. X = E - TS + constants

X = E - TS + const' = A + const'

Helmholtz free energy : *F*=*E*−*TS*.

Useful when V is constrained during thermodynamic process.

<u>Gibbs free energy</u>, the energy that can be converted into work at a uniform temperature and pressure throughout a system

If the sub-system pressure P is constrained to be equal to the external reservoir pressure P_R ,

X = E - TS + PV + const = G + const

,where G is the Gibbs free energy, G=E-TS+PV. Therefore under constant pressure conditions, if $dG \le 0$, then the process can occur spontaneously, because the change in system energy exceeds the energy lost to entropy. dG=0 is the condition for equilibrium. This is also commonly written in terms of enthalpy, where H=E+PV. G=H-TS

> Gibbs free energy : *G*=*E* +*PV*-*TS*=*H*-*TS* Useful when P is constrained during thermodynamic process.

Chapter 1.1

Relative Stability of a System \implies <u>Gibbs Free Energy</u> G = H - TS

H : *Enthalpy* ; Measure of the heat content of the system

H = E + PV

 $H \cong E$ for Condensed System

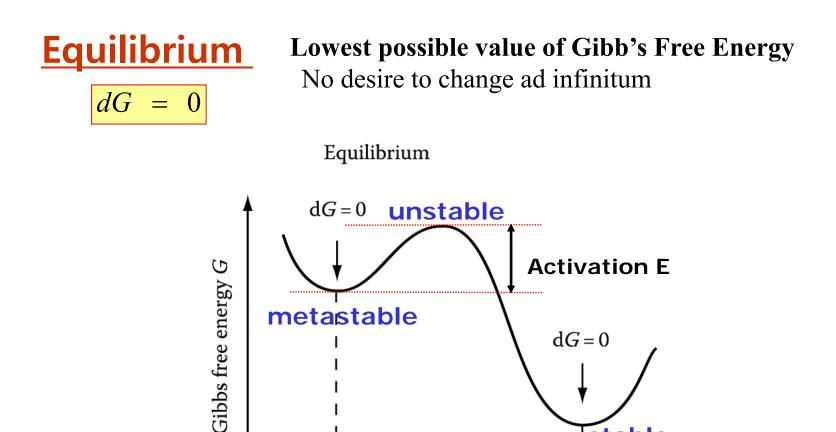
E: Internal Energy, Kinetic + Potential Energy of a atom within the system
 <u>Kinetic Energy :</u>
 Atomic Vibration (Solid, Liquid)
 Translational and Rotational Energy in liquid and gas.

 <u>Potential Energy :</u> Interactions or Bonds between the atoms within the system

T: The Absolute Temperature

S : *Entropy*, The *Randomness* of the System

Chapter 1.1



Arrangement of atoms

(B)

Phase Transformation

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stable

 $\Delta G = G_2 - G_1 < 0$

Α

Q2: What is single component system?

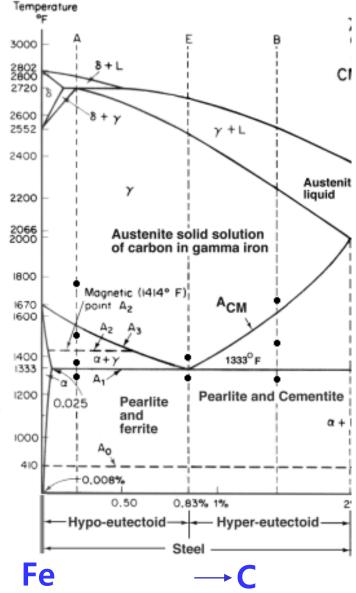


G = H - TS

One element (Al, Fe)

One type of molecule (H_2O)

Allotropic form?





1.2.1 Gibbs Free Energy as a Function of Temp. 14

* What is the role of temperature on equilibrium?

Q3: C_v vs. C_p ?

Specific heat (the quantity of heat (in joules) required to raise the temperature of substance by 1K) at constant volume VS. at constant pressure

$$H = E + PV \longrightarrow dE = \delta Q - P \cdot dV$$

When V is constant,
$$\frac{\delta Q}{dT} = \frac{dE}{dT} + P \frac{dV}{dT} O \qquad C_V = (\frac{\partial Q}{\partial T})_V = (\frac{\partial E}{\partial T})_V \qquad C_V = (\frac{\partial E}{\partial T})_V \quad or \quad E = \int C_V dT$$

Experimentally, it is easy to keep constant P (Cp) than constant V because it is difficult to make constant V (Cv) \rightarrow pressure ex) 1 atm,

When pressure is constant,

$$H \equiv E + PV \longrightarrow dH = dE + PdV + VdP$$

$$= \delta Q - \delta w + PdV + VdP$$

$$= \delta Q - PdV + PdV + VdP$$

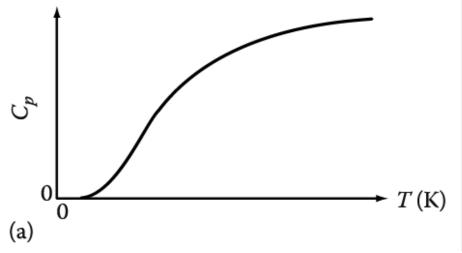
$$= \delta Q - PdV + PdV + VdP$$

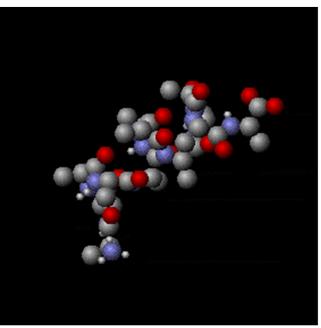
$$= \delta Q + VdP$$

In alloy work one usually consider systems at constant pressure so that enthalpy changes are more important then energy changes. $C_{\rm P}$; tempeature-dependent function

 $C_{P} = a + bT + CT^{-2}$

(empirical formula above room temp)





Molecules have internal structure because they are composed of atoms that have different ways of moving within molecules. Kinetic energy stored in these *internal degrees of freedom* contributes to a substance's specific heat capacity and not to its temperature.

Table of specific heat capacities

Substance	Phase	С р Ј / g·К	С р J / mol·K	Cv J / mol·K	Volumetric heat capacity J / cm ³ ·K
Aluminium	Solid	0.897	24.2		2.422
Copper	solid	0.385	24.47		3.45
Diamond	solid	0.5091	6.115		1.782
Gold	solid	0.1291	25.42		2.492
Graphite	solid	0.710	8.53		1.534
Iron	solid	0.450	25.1		3.537
Lithium	solid	3.58	24.8		1.912
Magnesium	solid	1.02	24.9		1.773
Silver	solid	0.233	24.9		
Water	liquid (25 °C)	4.1813	75.327	74.53	4.184
Zinc	solid	0.387	25.2		
All measurements are at 25 °C unless otherwise noted.					

* What is the role of temperature on equilibrium?

Q4: How is C_p related with H and S?

Draw the plots of (a) C_p vs. T, (b) H vs. T and (c) S vs. T.

How is C_p related with H and S?

$$C_{P} = \left(\frac{\partial H}{\partial T}\right)_{P} \quad \mathbf{H} = \mathbf{?} \quad H = \int_{298}^{T} C_{P} dT$$

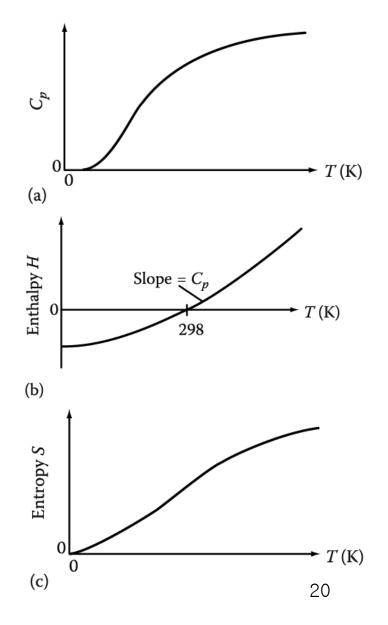
H = 0 at 298K for a pure element

in its most stable state.

: When considering a phase transformation or a chemical reaction, the important thing is not the value of the thermodynamic function, but <u>the amount of change.</u>

Enropy :
$$S = \frac{q}{T}$$

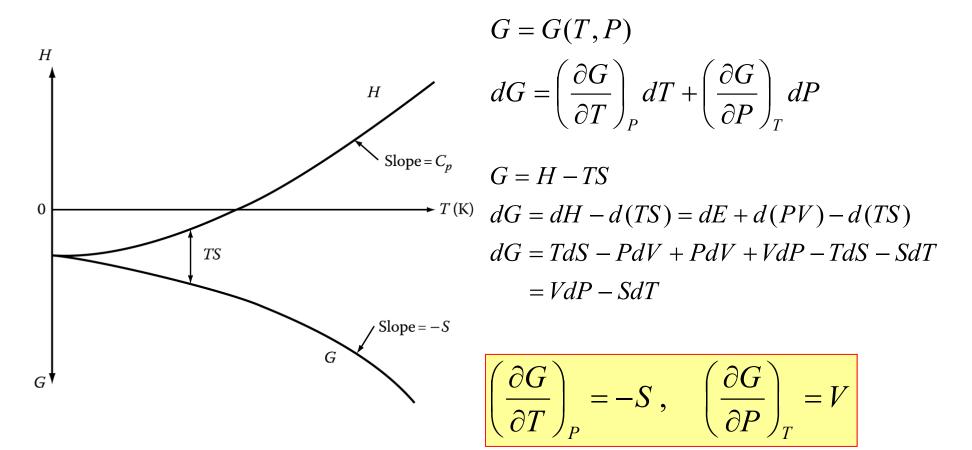
S = ? $\frac{C_P}{T} = \left(\frac{\partial S}{\partial T}\right)_P$ $S = \int_0^T \frac{C_P}{T} dT$



* What is the role of temperature on equilibrium?

Q5: How to draw the plots of H vs.T and G vs. T in single component system?

Compare the plots of H vs.T and G vs. T.



$$dG = VdP - SdT$$

$$G(P,T) = G(P_0, T_0) + \int_{P_0}^{P_1} V(T_0, P)dP - \int_{T_0}^{T_1} S(P,T)dT$$

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* What is the role of temperature on equilibrium?

Q6: G^S vs G^L as a function of temperature?

1.2.1 Gibbs Free Energy as a Function of Temp.

- Which is larger, H^L or H^S?
- H^L > H^s at all temp.
- Which is larger, S^L or S^S?
- $S^L > S^S$ at all temp.

 \rightarrow Gibbs free energy of the liquid <u>decreases more rapidly</u> with increasing temperature than that of the solid.

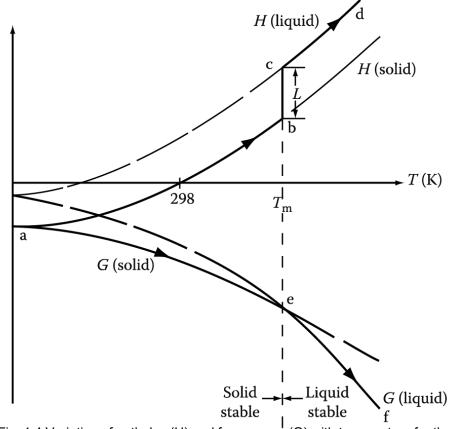
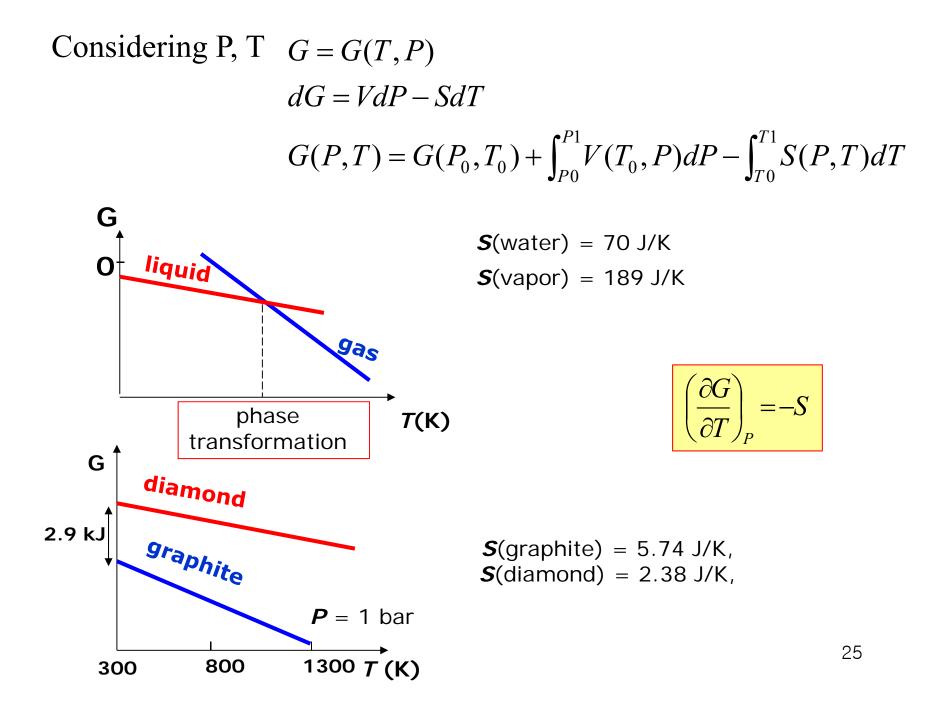


Fig. 1.4 Variation of enthalpy (H) and free energy (G) with temperature for the Solid and liquid phases of a pure metal. L is the latent heat of melting, Tm the Equilibrium melting temperature.

- Which is larger, G^L or G^S at low T?
- $G^L > G^S$ (at low Temp) and $G^S > G^L$ (at high Temp)

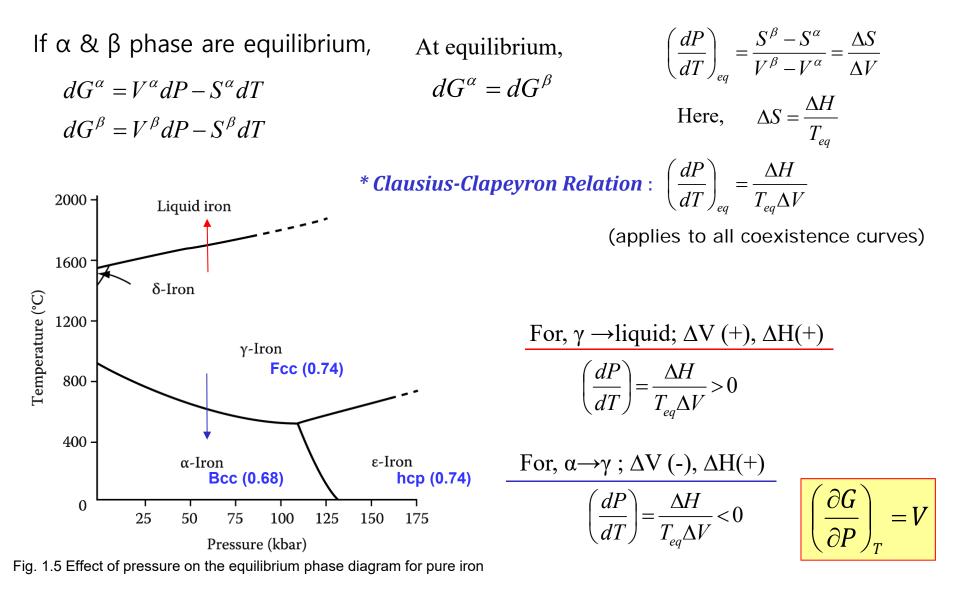


Q7: What is the role of pressure on equilibrium?

* Clausius-Clapeyron Relation : $\left(\frac{dP}{dT}\right)_{eq} = \frac{\Delta H}{T_{eq}\Delta V}$ (applies to all coexistence curves)

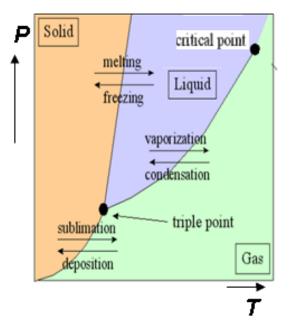
1.2.2 Pressure Effects

When the two phases with different molar volumes are in equilibrium, if the pressure changes, the equilibrium temperature T should also change with pressure.



Q8: How to classify phase transition?

"First order transition" vs "Second order transition"



The First-Order Transition

Latent heat Energy barrier Discontinuous entropy, heat capacity

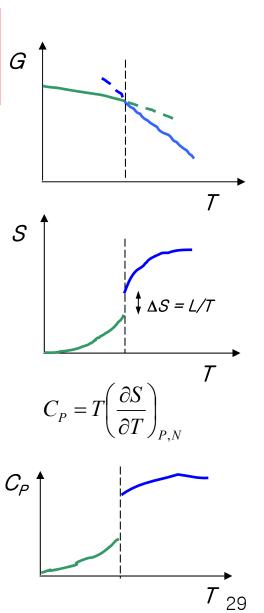
- First Order Phase Transition at T_T:
 - G is <u>continuous</u> at T_T
 - First derivatives of G (V, S, H) are discontinuous at T_T

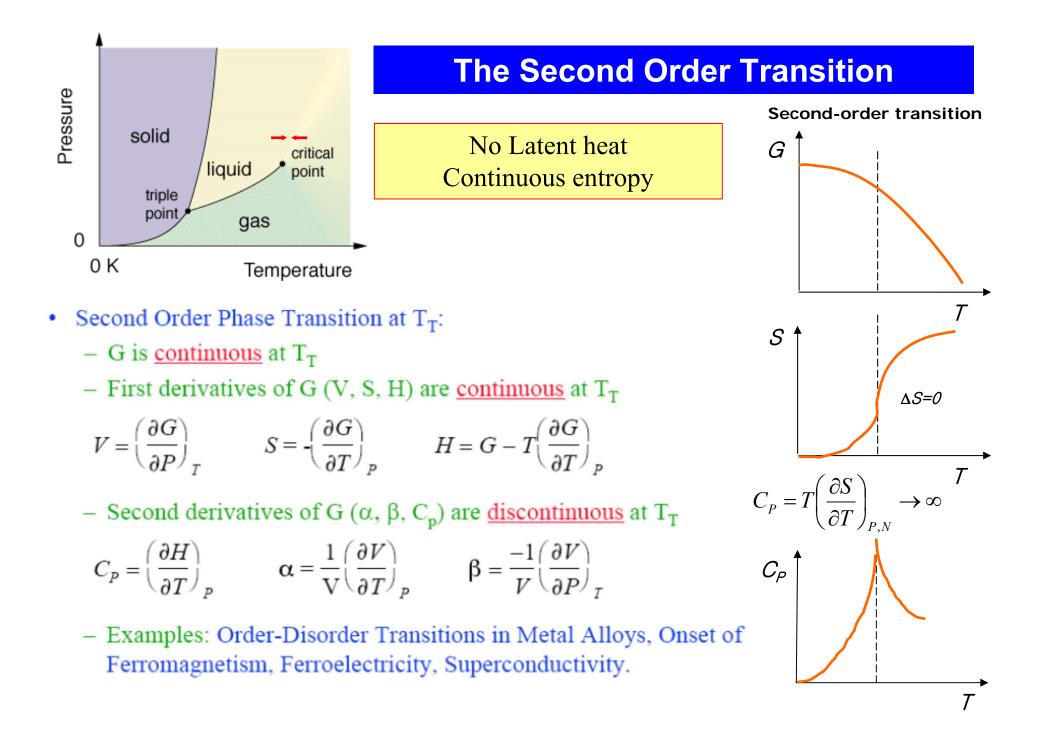
$$V = \left(\frac{\partial G}{\partial P}\right)_T \qquad S = -\left(\frac{\partial G}{\partial T}\right)_P \qquad H = G - T\left(\frac{\partial G}{\partial T}\right)_P$$

– Second derivatives of G (α , β , C_p) are <u>discontinuous</u> at T_T

$$C_{P} = \left(\frac{\partial H}{\partial T}\right)_{P} \qquad \alpha = \frac{1}{V} \left(\frac{\partial V}{\partial T}\right)_{P} \qquad \beta = \frac{-1}{V} \left(\frac{\partial V}{\partial P}\right)_{T}$$

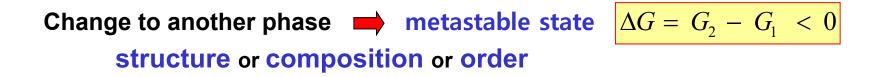
 Examples: Vaporization, Condensation, Fusion, Crystallization, Sublimation.

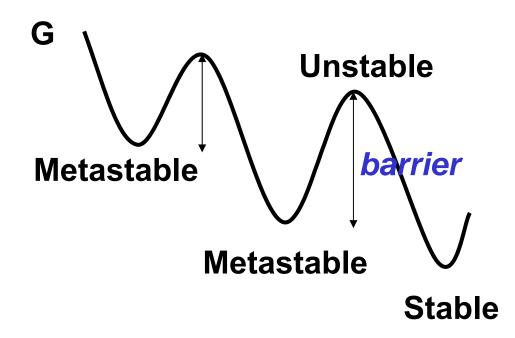




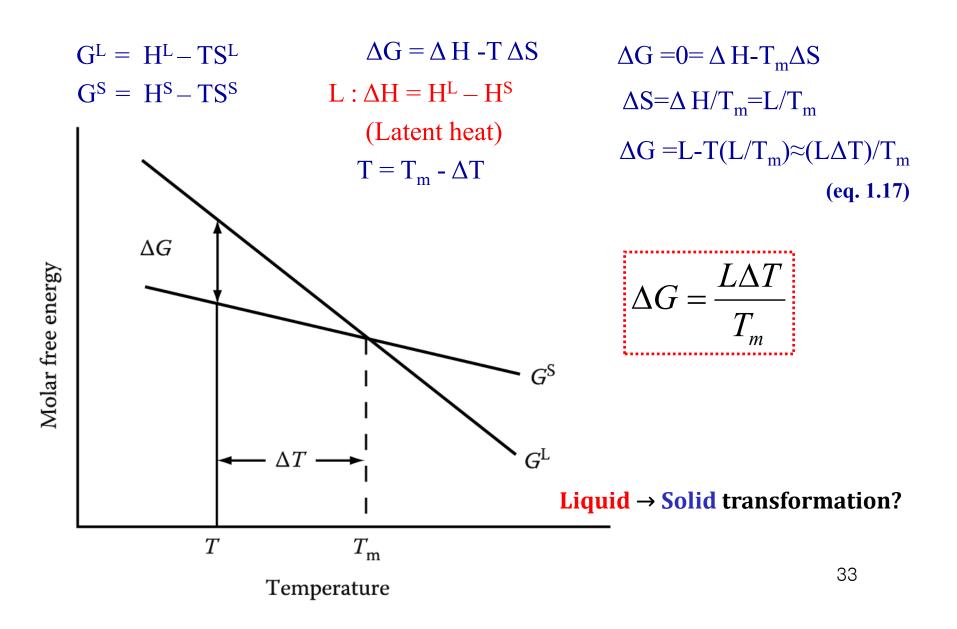
Q9: What is the driving force for "Solidification: Liquid → Solid"?

Phase Transformation

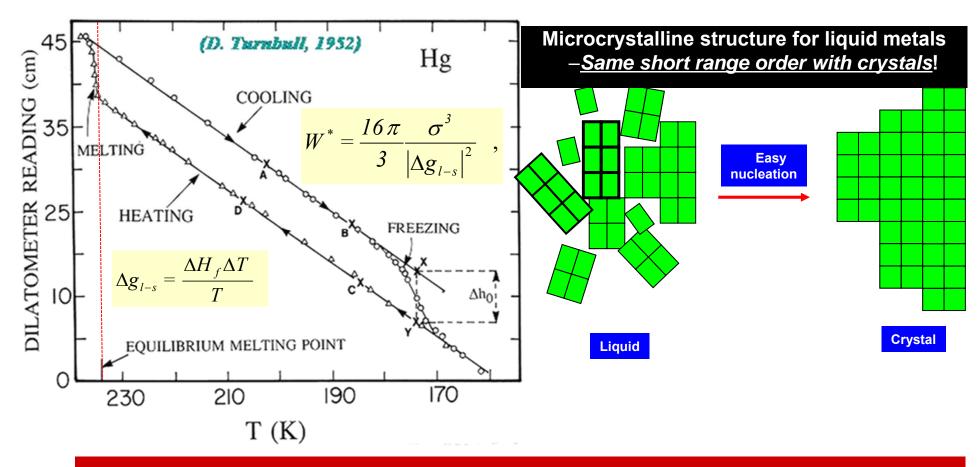




1.2.3 Driving force for solidification



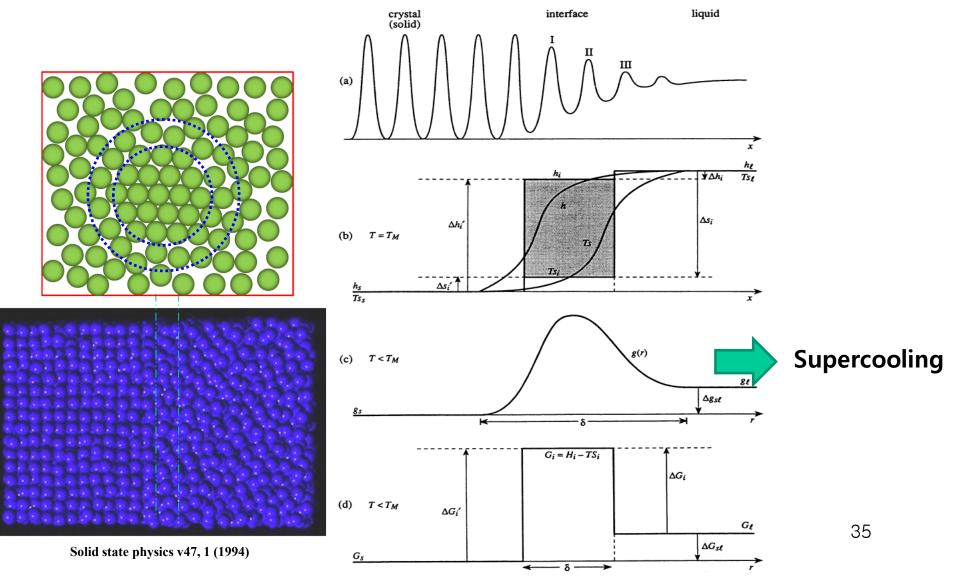
Turnbull's Insight for Supercooling



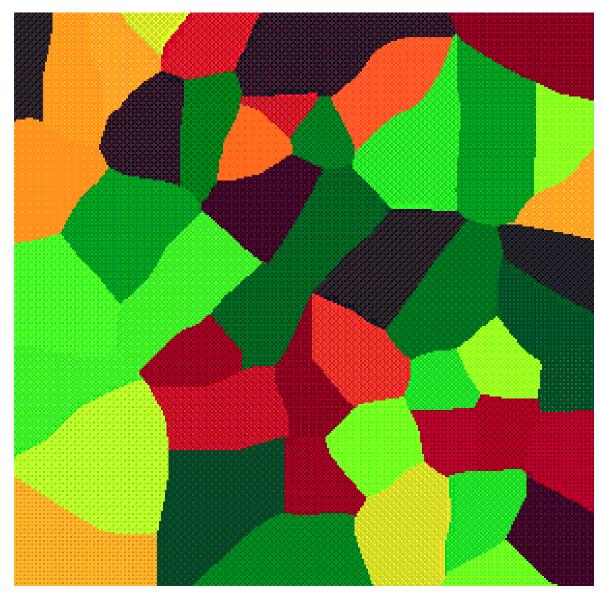
How does the liquid metals resist on the crystallization?
 What is the origin of high nucleation barrier against the crystallization?
 What is the structure of interface between liquids and crystals?
 What is the local order of liquid metals?

Turnbull's solid-liquid interface

<u>Turnbull's insight :</u> Liquid orders substantially near a crystal surface due to entropy decreasing caused by the crystal-melt interfacial tension

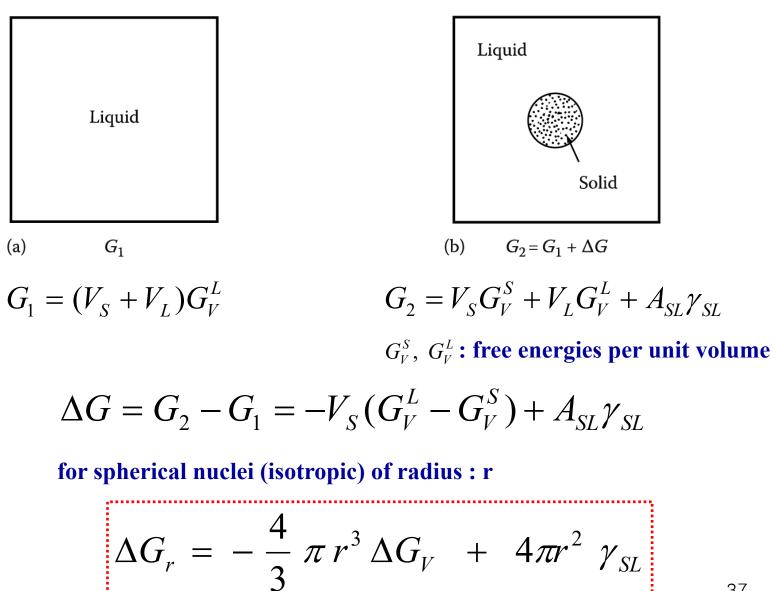


4. Solidification: Liquid — Solid



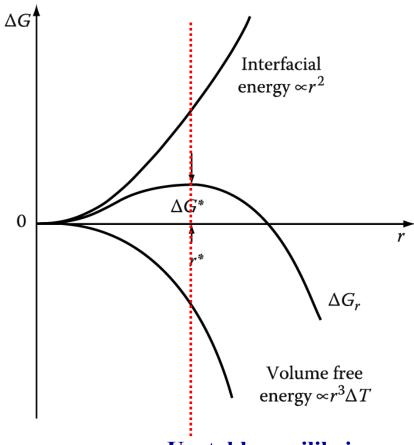
4 Fold Anisotropic Surface Energy/2 Fold Kinetics, Many Seeds

4.1.1. Homogeneous Nucleation



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4.1.1. Homogeneous Nucleation



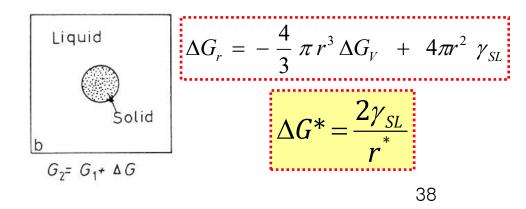
Unstable equilibrium

Fig. 4.2 The free energy change associated with homogeneous nucleation of a sphere of radius r.

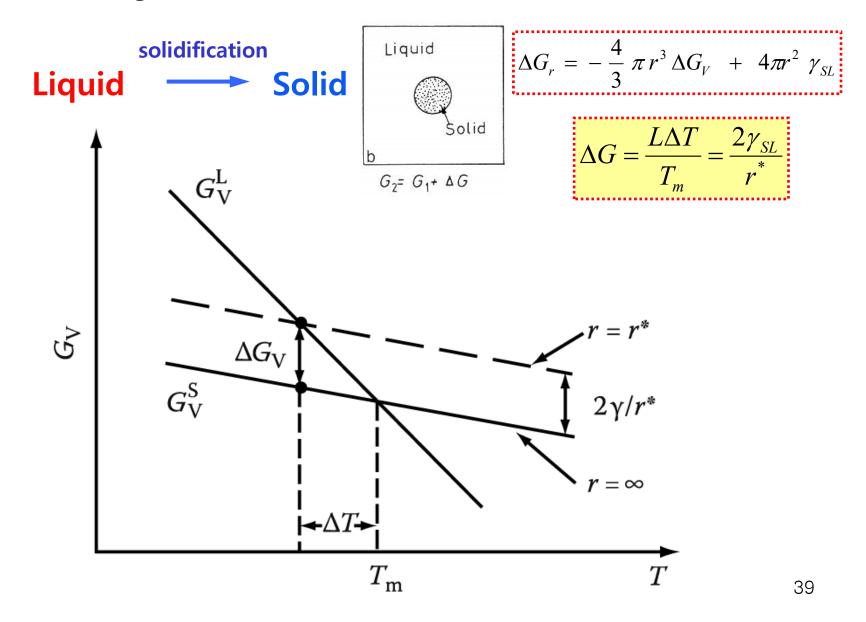
Why r^{*} is not defined by $\Delta G_r = 0$?

r < r* : unstable (lower free E by reduce size)
r > r* : stable (lower free E by increase size)
r* : critical nucleus size

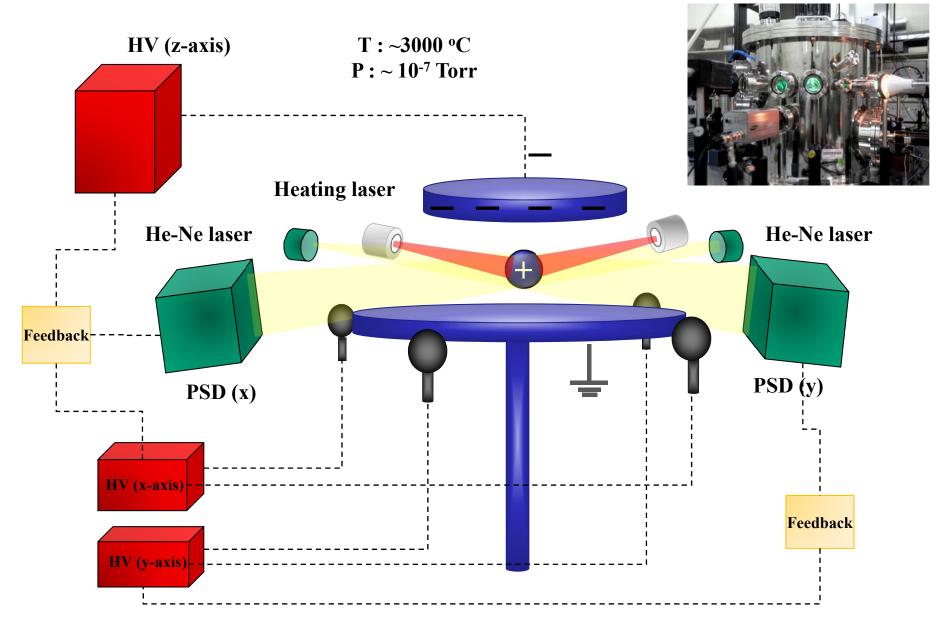




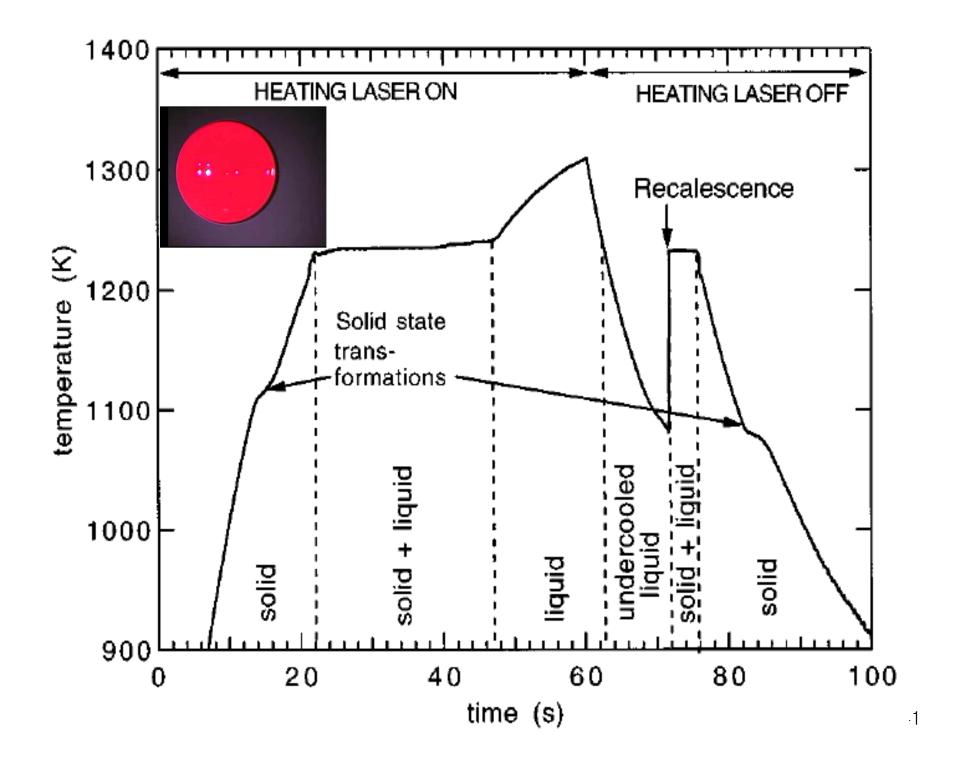
1.2.3 Driving force for solidification



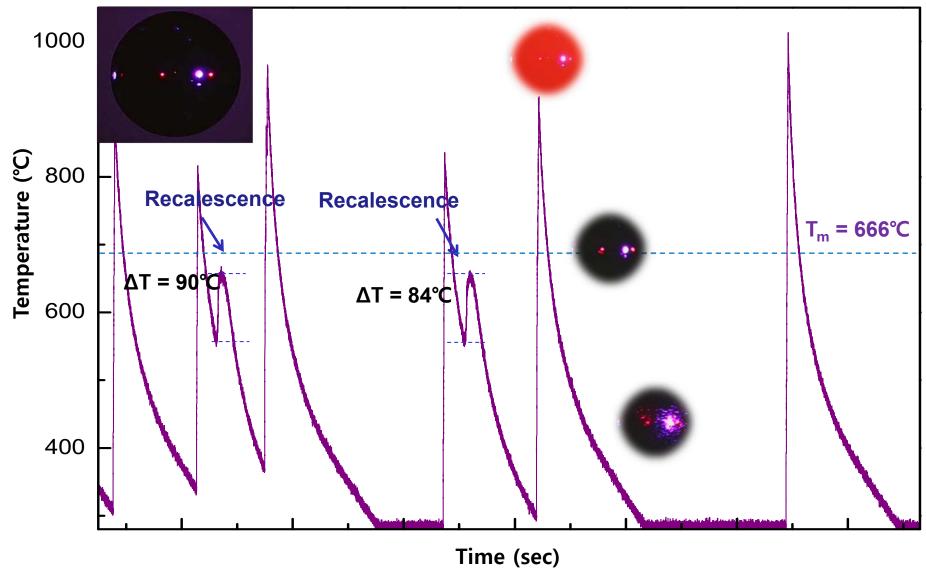
Electrostatic levitation in KRISS



KRISS material : Dr. G.W.Lee



Cyclic cooling curves of Zr_{41.2}Ti_{13.8}Cu_{12.5}Ni₁₀Be_{22.5}

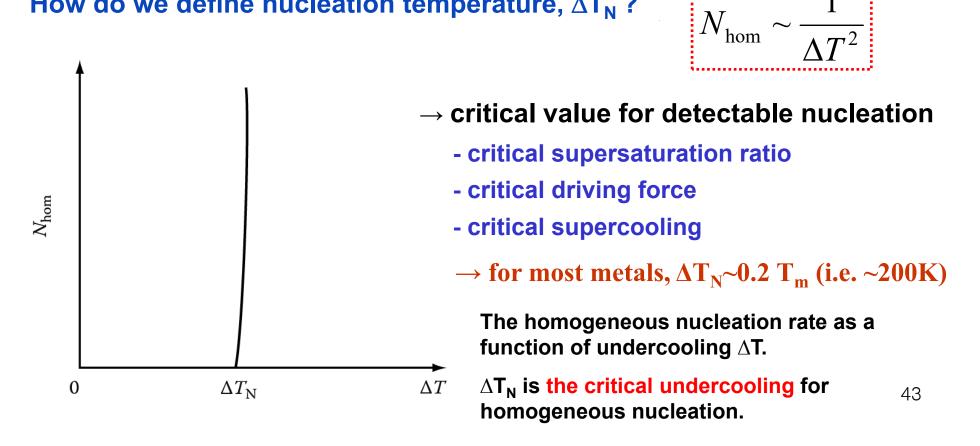


* The homogeneous nucleation rate - kinetics

$$I = \frac{nkT}{h} \exp\left(-\frac{G_A}{kT}\right) \exp\left(-\frac{16\pi\sigma_{SL}^3 T_E^2}{3L^2(\Delta T)^2 kT}\right)$$

: insensitive to Temp.





* Relationship between Maximum Supercoolings and T_m

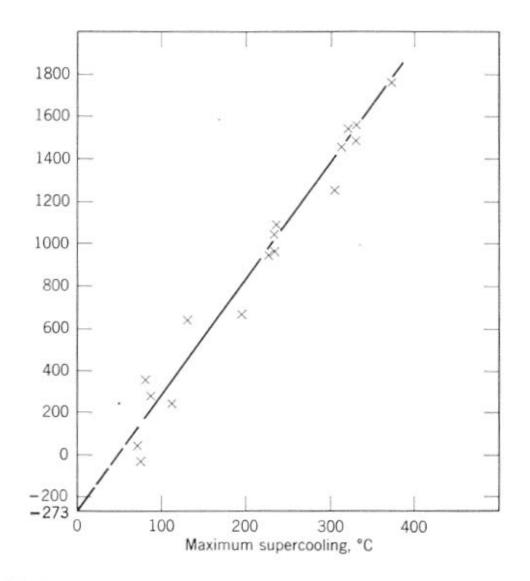


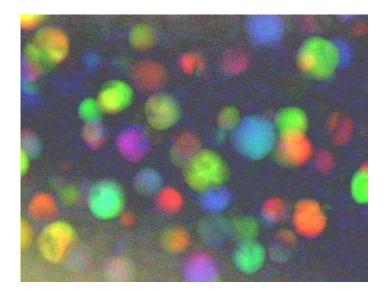
Fig. 3.7. Maximum supercooling as a function of melting point. (From *Thermo*dynamics in *Physical Metallurgy*, American Society for Metals, Cleveland, 1911, p. 11.)

Solidification: Liquid ---- Solid

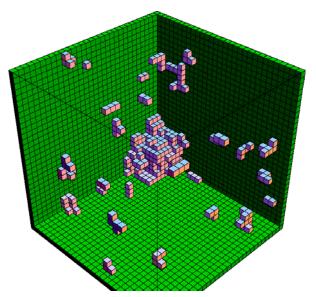
- casting & welding
- single crystal growth
- directional solidification
- rapid solidification

Nucleation in Pure Metals

- $T_{\rm m}$: $G_{\rm L}$ = $G_{\rm S}$
- Undercooling (supercooling) for nucleation: 250 K ~ 1 K
- <Types of nucleation>
- Homogeneous nucleation

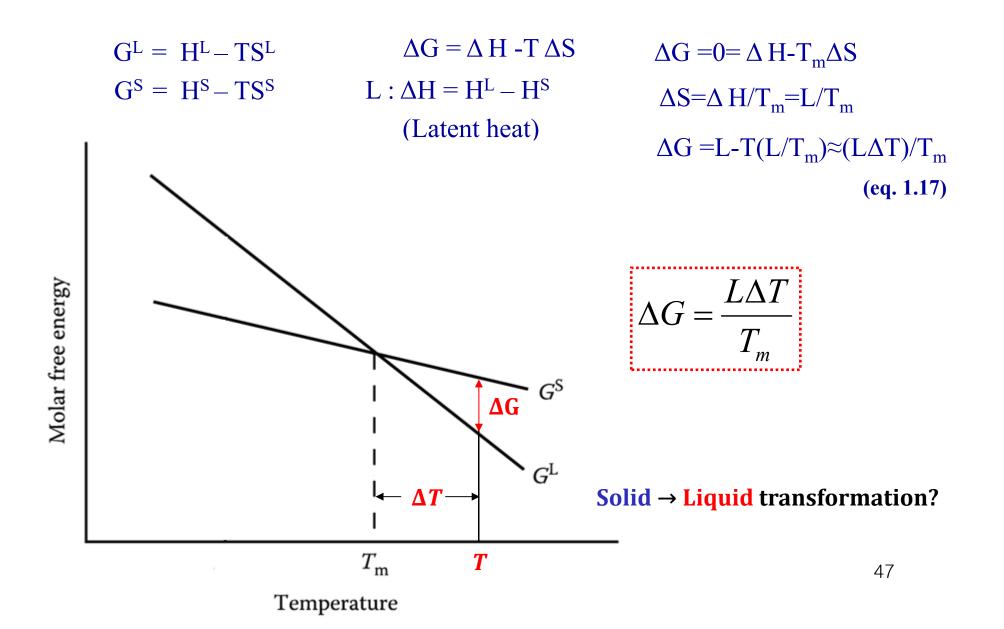


- Heterogeneous nucleation



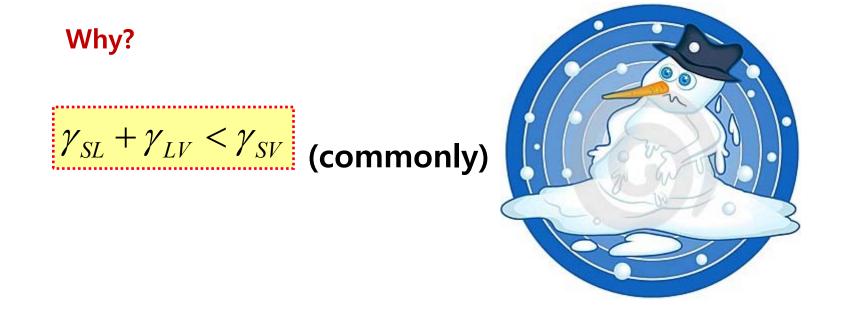
Q10: What is the driving force for "Melting: Solid → Liquid"?

* Driving force for melting



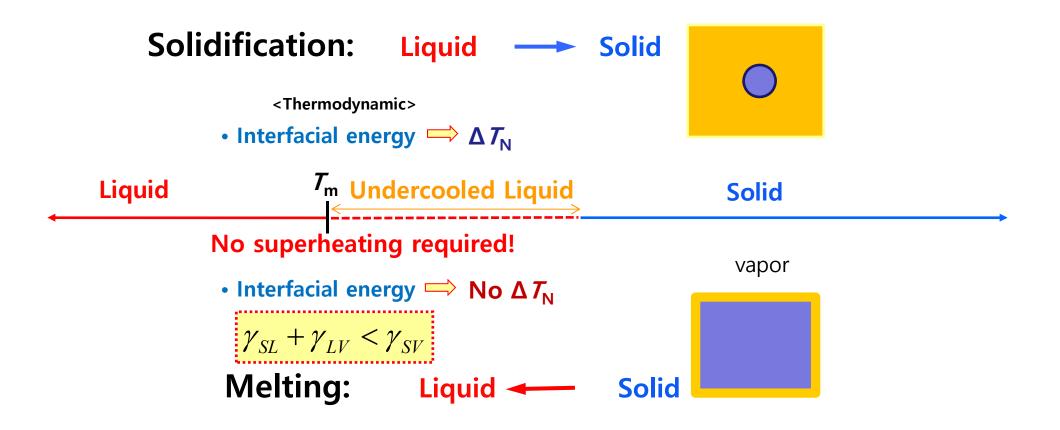
Nucleation of melting

Although nucleation during solidification usually requires some undercooling, melting invariably occurs at the equilibrium melting temperature even at relatively high rates of heating.



In general, wetting angle = 0 \implies No superheating required!

Melting and Crystallization are Thermodynamic Transitions



Contents for today's class

CHAPTER 1 Introductory Thermondynamics

- Equilibrium dG = 0

Lowest possible value of G *No desire to change ad infinitum*

- Single component system

Gibbs Free Energy as a Function of Temp. and Pressure

$$\left(\frac{\partial G}{\partial T}\right)_{P} = -S , \quad \left(\frac{\partial G}{\partial P}\right)_{T} = V$$

$$\left(\frac{dP}{dT}\right)_{eq} = \frac{\Delta H}{T_{eq}\Delta V}$$

Clausius-Clapeyron Relation

- Phase Transformation $\Delta G = C$

$$\Delta G = G_2 - G_1 < 0$$

- Classification of phase transition

First order transition: CDD/Second order transition: CCD

- Solidification: Liquid → Solid Themodynamic transition

Driving force for solidification

$$\Delta G = \frac{L\Delta T}{T_m}$$