2018 Fall

"Phase Transformation in Materials"

09.06.2018

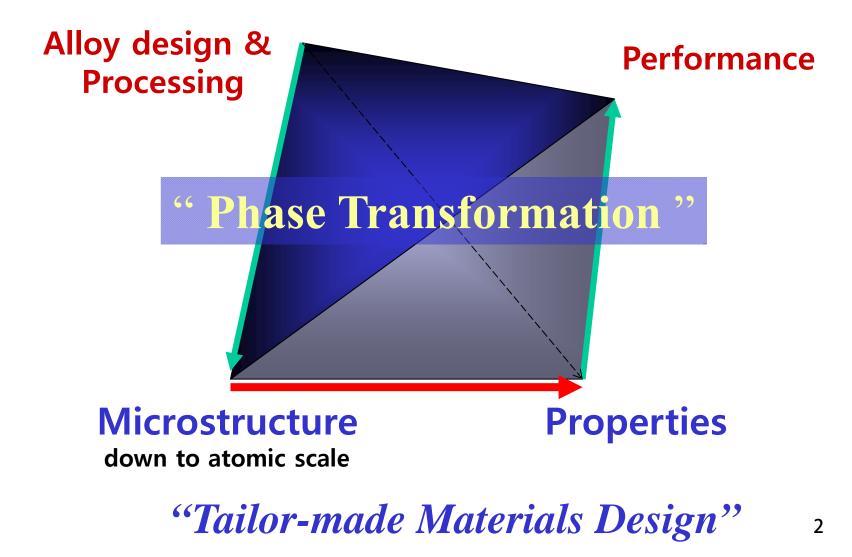
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Contents for previous class

Microstructure-Properties Relationships



Contents for previous class

Contents of this course_Phase transformation

(Ch1) Thermodynamics and Phase Diagrams

Background to understand phase transformation

(Ch2) Diffusion: Kinetics

(Ch3) Crystal Interface and Microstructure

Representative Phase transformation (Ch4) Solidification: Liquid → Solid

(Ch5) Diffusional Transformations in Solid: Solid → Solid

(Ch6) Diffusionless Transformations: Solid → Solid

Contents for today's class I

Chapter 1

Thermondynamics and Phase Diagrams

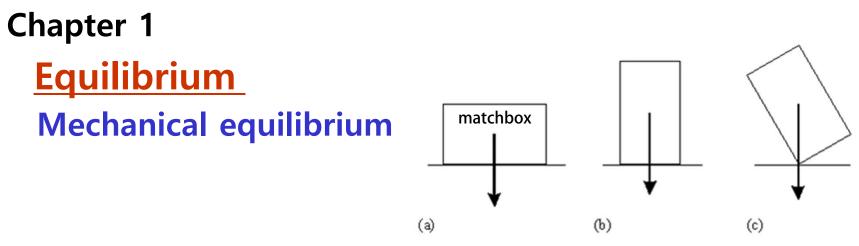
- Equilibrium
- Single component system

Gibbs Free Energy as a Function of Temp. and Pressure

- Classification of phase transition
- Driving force for solidification

Q1: "thermodynamic equilibrium"? Lowest possible value of Gibb's Free Energy

→ The main use of thermodynamics in metallurgy is to allow the prediction of whether an alloy is in equilibrium.



: total potential energy of the system is a minimum.

Thermal equilibrium

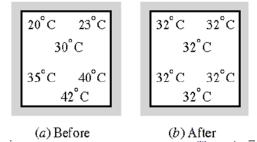
: absence of temperature gradients in the system

Chemical equilibrium

: no further reaction occurs between the reacting substances i.e. the forward and reverse rates of reaction are equal.

Thermodynamic equilibrium

: the system is under mechanical, thermal and chemical equilibrium The properties of the system-P, T, V, concentrations-do not change with time.



Chapter 1.1

Relative Stability of a System \implies <u>Gibbs Free Energy</u>

Gibbs free energy : *G*=*E* +*PV*-*TS*=*H*-*TS*

Useful when P is constrained during thermodynamic process.

H : *Enthalpy* ; Measure of the heat content of the system

Mixture of one or more phases

H = E + PV

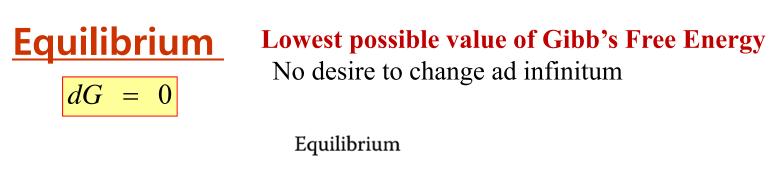
 $H \cong E$ for Condensed System

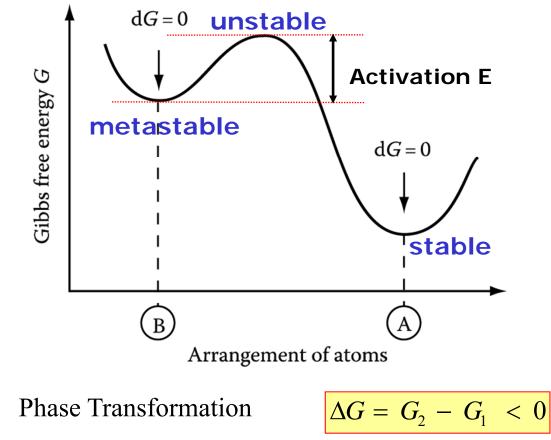
E : Internal Energy, Kinetic + Potential Energy of a atom within the system <u>Kinetic Energy :</u> Atomic Vibration (Solid, Liquid) Translational and Rotational Energy in liquid and gas. <u>Potential Energy :</u> Interactions or Bonds between the atoms within the system

T : The Absolute Temperature

S: Entropy, The Randomness of the System

Chapter 1.1





Q2: What is single component system?

Different elements or chemical compounds

1.2 Single component system

One element (Al, Fe)

One type of molecule (H_2O)

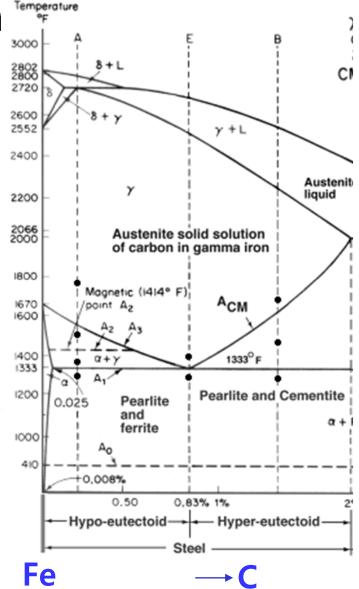
- Allotropic forms?

- How is phase stability measured?

G = H - TS



1.2.1 Gibbs Free Energy as a Function of Temp. 10



* What is the role of temperature on equilibrium?

Q3: C_v vs. C_p ?

Specific heat (the quantity of heat (in joules) required to raise the temperature of substance by 1K) at constant volume VS. at constant pressure

$$H = E + PV \longrightarrow dE = \delta Q - P \cdot dV$$

When V is constant,
$$\frac{\delta Q}{dT} = \frac{dE}{dT} + P \frac{dV}{dT} \qquad C_V = (\frac{\partial Q}{\partial T})_V = (\frac{\partial E}{\partial T})_V \qquad C_V = (\frac{\partial E}{\partial T})_V \quad \text{or} \quad E = \int C_V dT$$

Experimentally, it is easy to keep constant P (Cp) than constant V because it is difficult to make constant V (Cv) → pressure ex) 1 atm,

When pressure is constant,

$$H = E + PV \longrightarrow dH = dE + PdV + VdP$$
$$= \delta Q - \delta w + PdV + VdP$$
$$= \delta Q - PdV + PdV + VdP$$
$$= \delta Q - PdV + PdV + VdP$$
$$= \delta Q + VdP$$
$$= \delta Q + VdP$$
$$= \delta Q + VdP$$
$$H = 0 \text{ when } P \text{ is constant}$$
$$\left(\frac{dH}{dT}\right)_{P} = \left(\frac{\delta Q}{dT}\right)_{P} = C_{P}$$

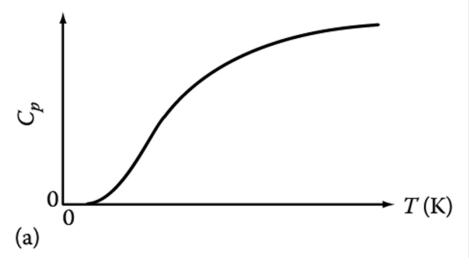
In alloy work one usually consider systems at constant pressure so that enthalpy changes are more important then energy changes.

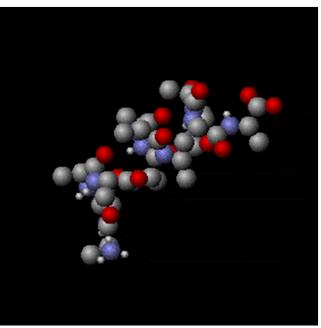
 $\int C_{p} dT$

 $C_{\rm P}$; tempeature-dependent function

 $C_P = a + bT + CT^{-2}$

(empirical formula above room temp)





Molecules have <u>internal structure</u> because they are composed of atoms that have different ways of moving within molecules. Kinetic energy stored in these <u>internal degrees of freedom</u> contributes to a substance's specific heat capacity and not to its temperature. * What is the role of temperature on equilibrium?

Q4: How is C_p related with H and S?

Draw the plots of (a) C_p vs. T, (b) H vs. T and (c) S vs. T.

How is C_p related with H and S?

$$C_{P} = \left(\frac{\partial H}{\partial T}\right)_{P} \quad \mathbf{H} = \mathbf{?} \quad H = \int_{298}^{T} C_{P} dT$$

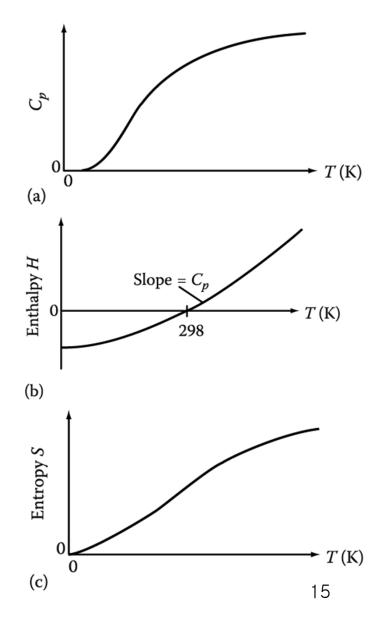
H = 0 at 298K for a pure element

in its most stable state.

: When considering a phase transformation or a chemical reaction, the important thing is not the value of the thermodynamic function, but <u>the amount of change.</u>

Enropy :
$$S = \frac{q}{T}$$

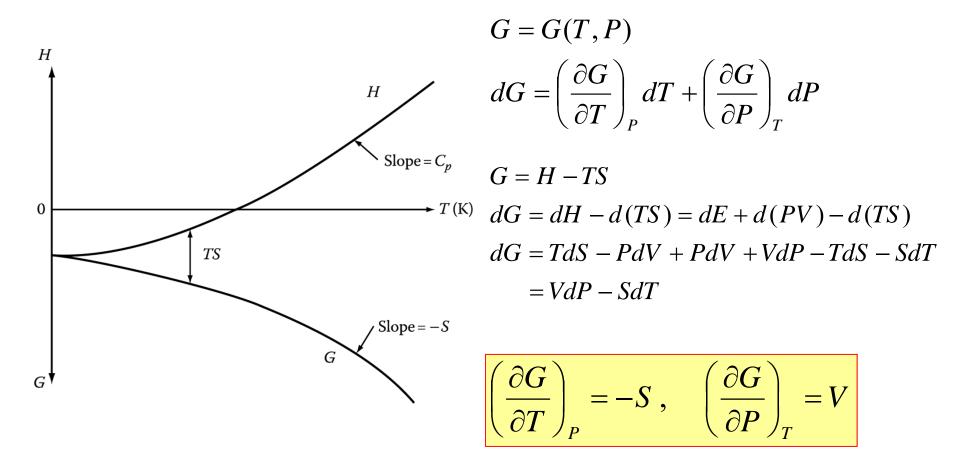
S = ? $\frac{C_P}{T} = \left(\frac{\partial S}{\partial T}\right)_P$ $S = \int_0^T \frac{C_P}{T} dT$



* What is the role of temperature on equilibrium?

Q5: How to draw the plots of H vs.T and G vs. T in single component system?

Compare the plots of H vs.T and G vs. T.



$$dG = VdP - SdT$$

$$G(P,T) = G(P_0, T_0) + \int_{P_0}^{P_1} V(T_0, P)dP - \int_{T_0}^{T_1} S(P,T)dT$$
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* What is the role of temperature on equilibrium?

Q6: G^S vs G^L as a function of temperature?

1.2.1 Gibbs Free Energy as a Function of Temp.

- Which is larger, H^L or H^S?
- H^L > H^s at all temp.
- Which is larger, S^L or S^S?
- $S^L > S^S$ at all temp.

 \rightarrow Gibbs free energy of the liquid <u>decreases more rapidly</u> with increasing temperature than that of the solid.

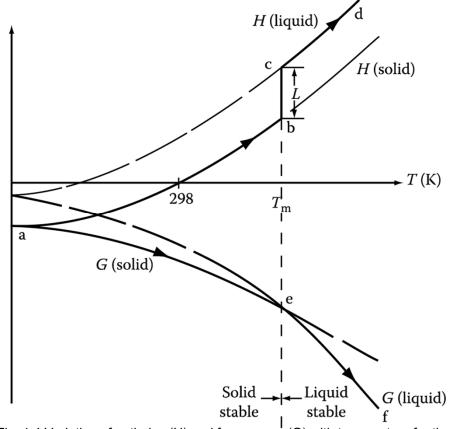
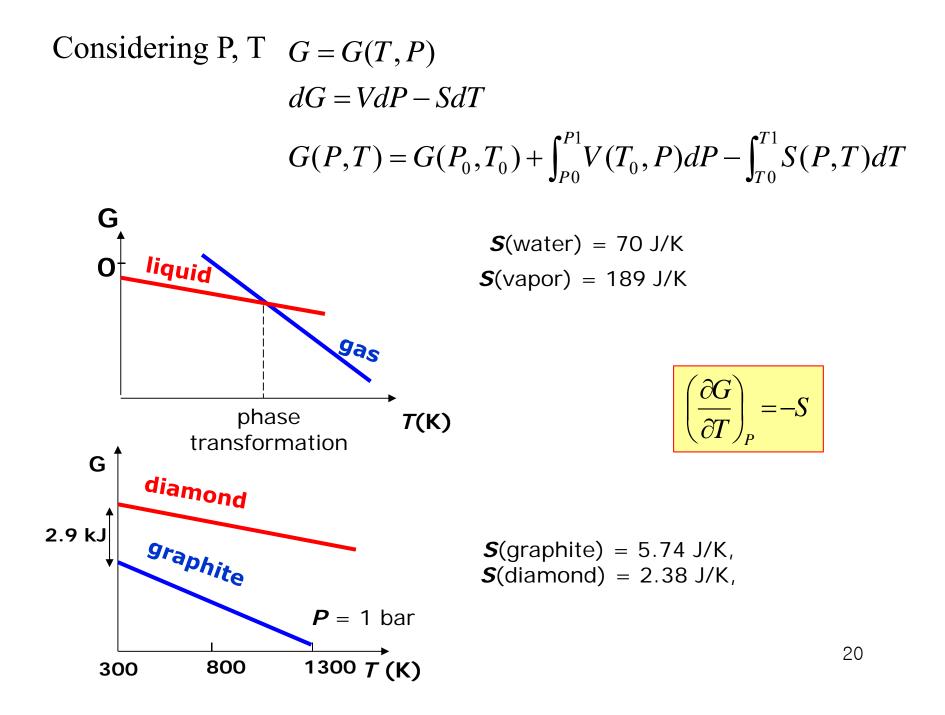


Fig. 1.4 Variation of enthalpy (H) and free energy (G) with temperature for the Solid and liquid phases of a pure metal. L is the latent heat of melting, Tm the Equilibrium melting temperature.

- Which is larger, G^L or G^S at low T?
- $G^L > G^S$ (at low Temp) and $G^S > G^L$ (at high Temp)

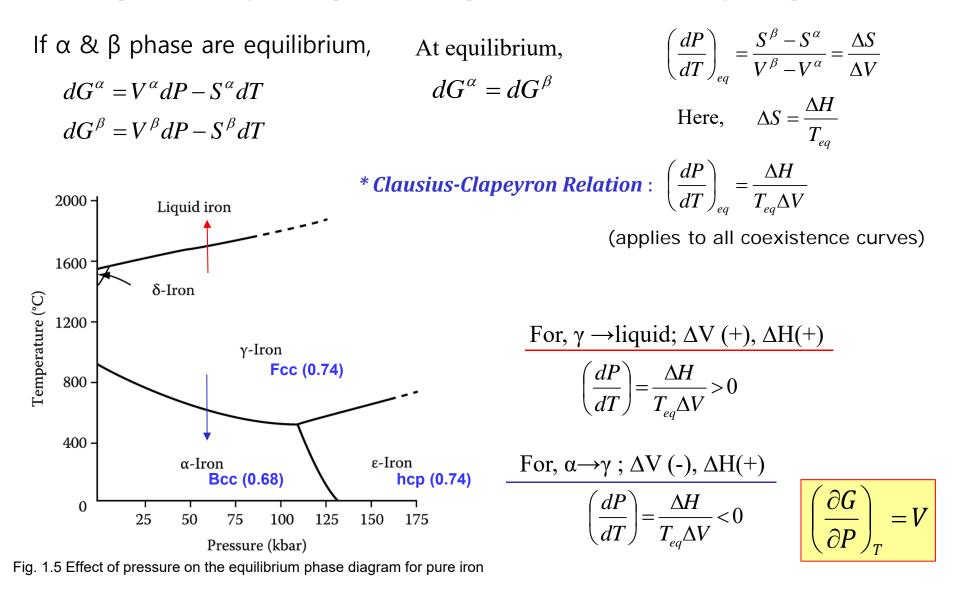


Q7: What is the role of pressure on equilibrium?

* Clausius-Clapeyron Relation : $\left(\frac{dP}{dT}\right)_{eq} = \frac{\Delta H}{T_{eq}\Delta V}$ (applies to all coexistence curves)

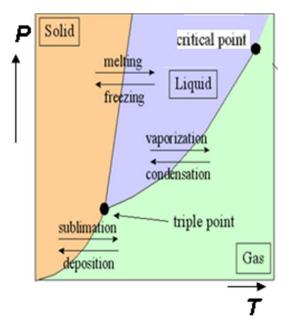
1.2.2 Pressure Effects

When the two phases with different molar volumes are in equilibrium, if the pressure changes, the equilibrium temperature T should also change with pressure.



Q8: How to classify phase transition?

"First order transition" vs "Second order transition"



The First-Order Transition

Latent heat Energy barrier Discontinuous entropy, heat capacity

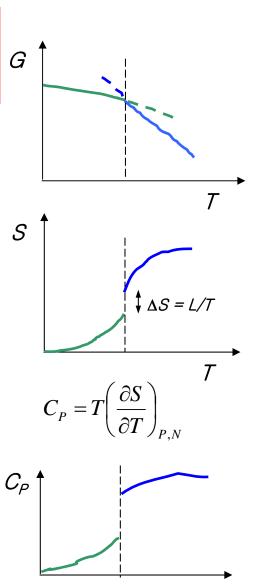
- First Order Phase Transition at T_T:
 - G is continuous at T_T
 - First derivatives of G (V, S, H) are discontinuous at T_T

$$V = \left(\frac{\partial G}{\partial P}\right)_T \qquad S = -\left(\frac{\partial G}{\partial T}\right)_P \qquad H = G - T\left(\frac{\partial G}{\partial T}\right)_P$$

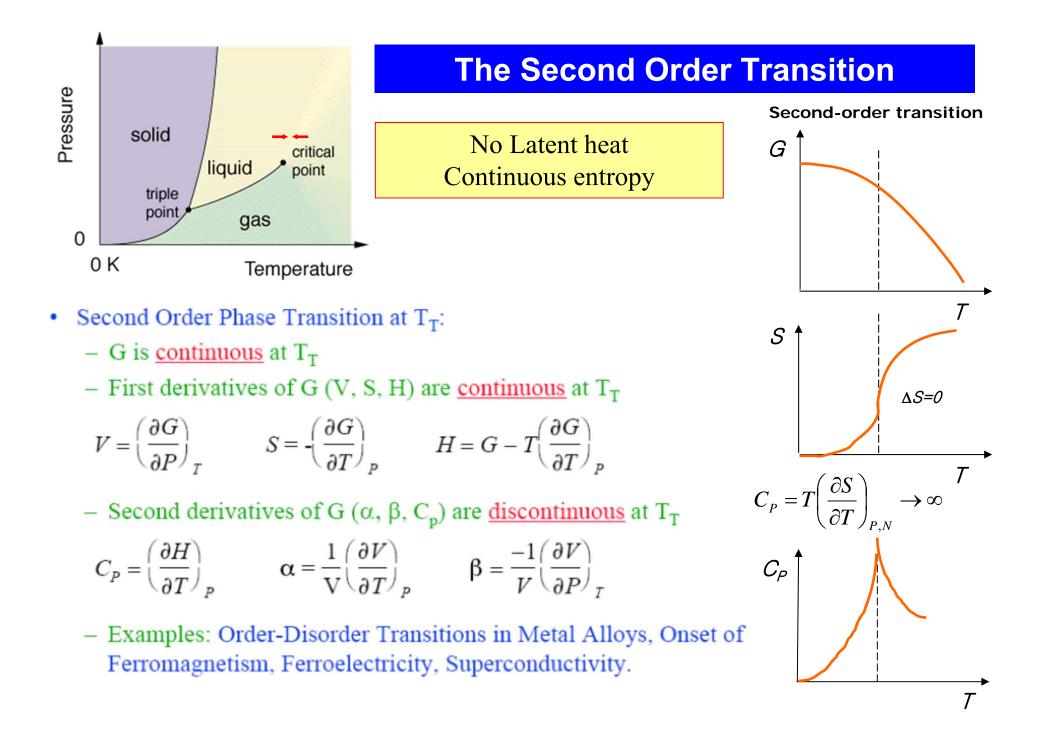
– Second derivatives of G (α , β , C_p) are <u>discontinuous</u> at T_T

$$C_{P} = \left(\frac{\partial H}{\partial T}\right)_{P} \qquad \alpha = \frac{1}{V} \left(\frac{\partial V}{\partial T}\right)_{P} \qquad \beta = \frac{-1}{V} \left(\frac{\partial V}{\partial P}\right)_{T}$$

 Examples: Vaporization, Condensation, Fusion, Crystallization, Sublimation.

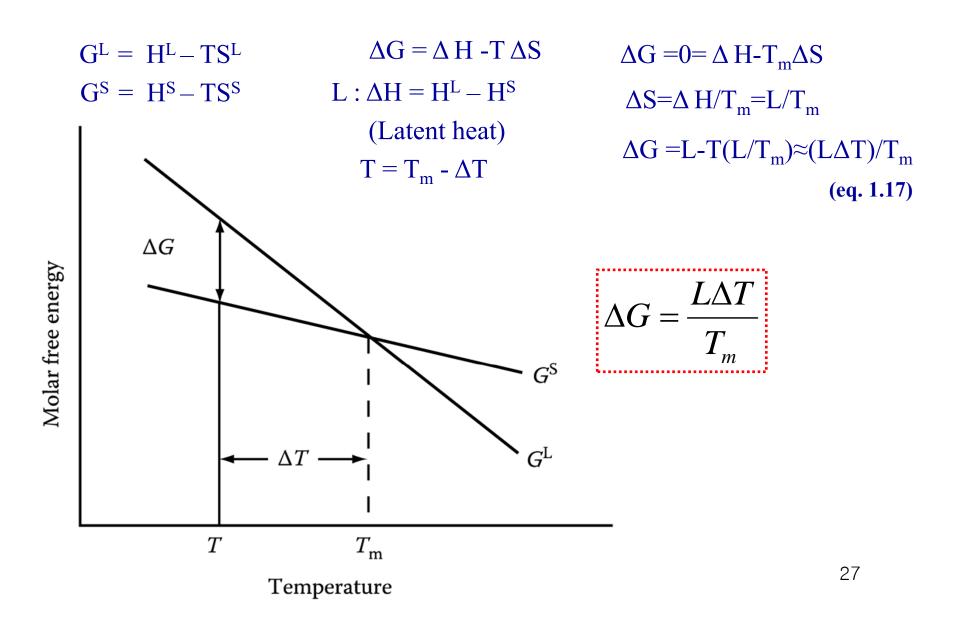


T ₂₄

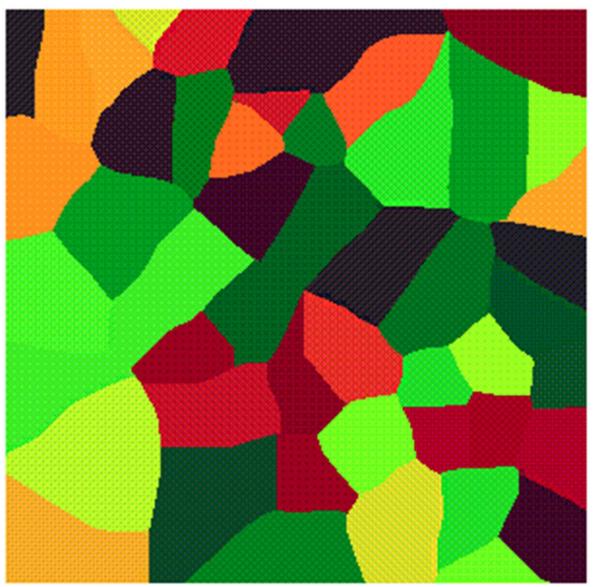


Q9: What is the driving force for "Solidification: Liquid → Solid"?

1.2.3 Driving force for solidification



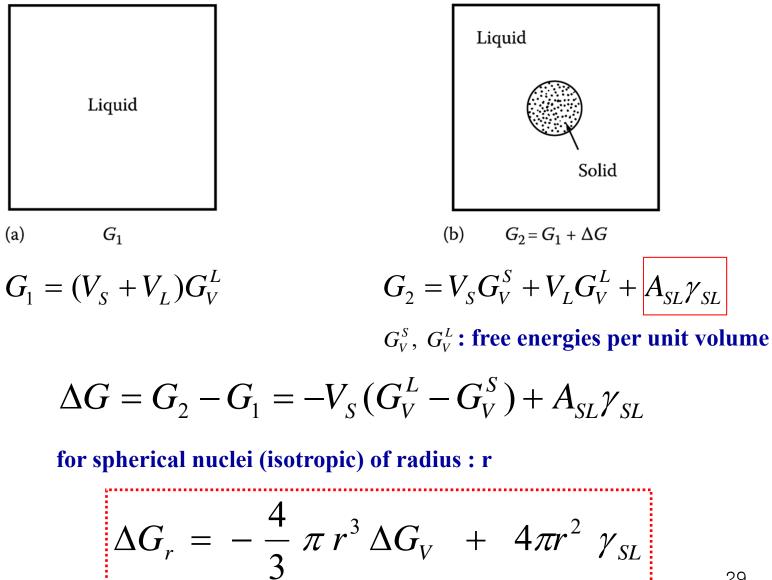




4 Fold Anisotropic Surface Energy/2 Fold Kinetics, Many Seeds

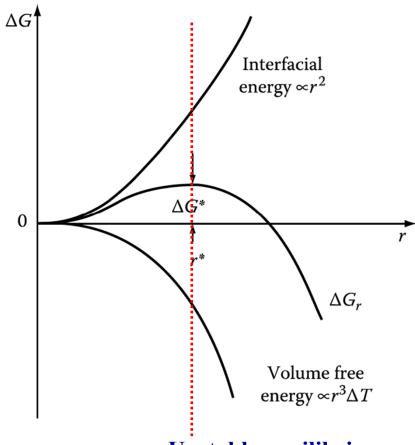
²⁸

4.1.1. Homogeneous Nucleation



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4.1.1. Homogeneous Nucleation



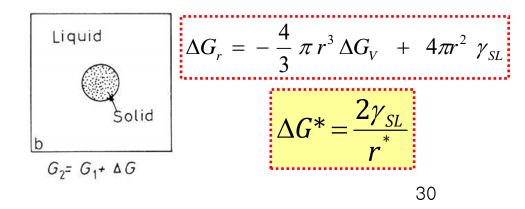
Unstable equilibrium

Fig. 4.2 The free energy change associated with homogeneous nucleation of a sphere of radius r.

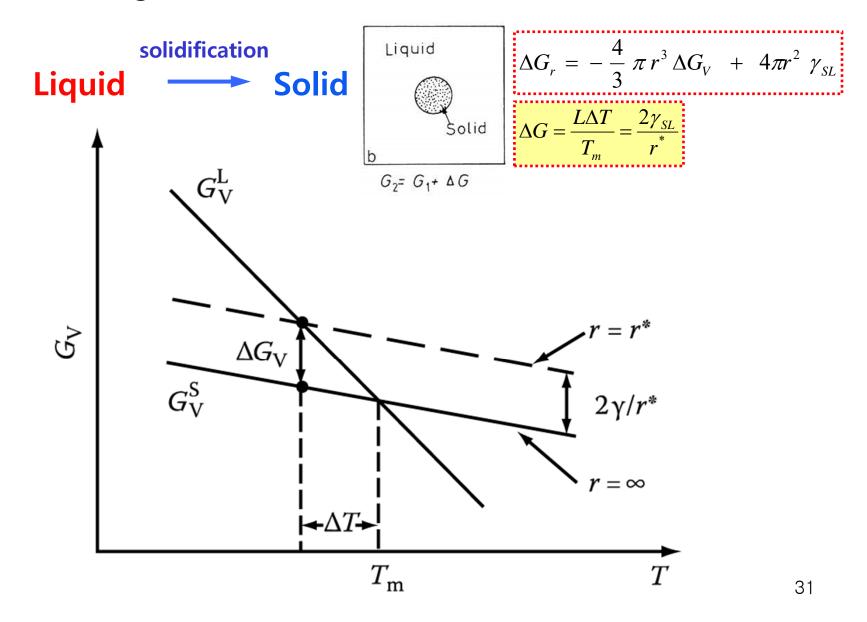
Why r^{*} is not defined by $\Delta G_r = 0$?

r < r* : unstable (lower free E by reduce size)
r > r* : stable (lower free E by increase size)
r* : critical nucleus size

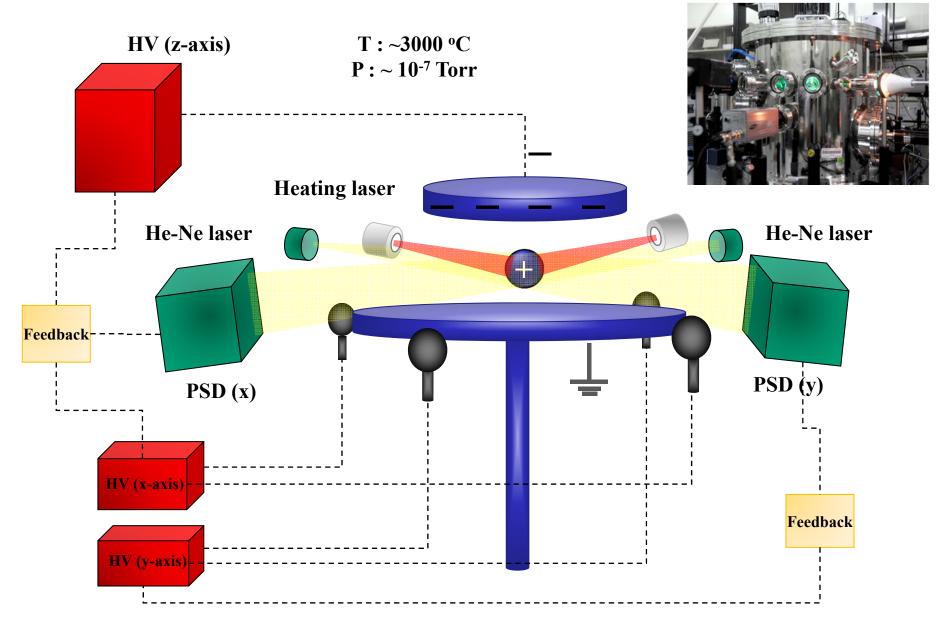




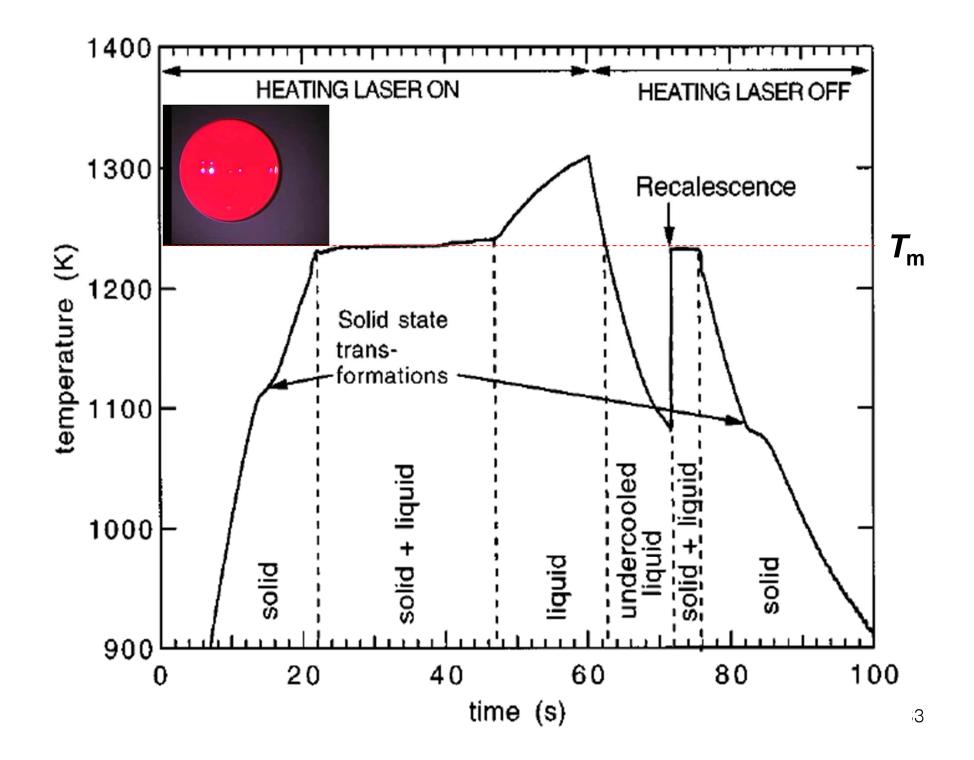
1.2.3 Driving force for solidification



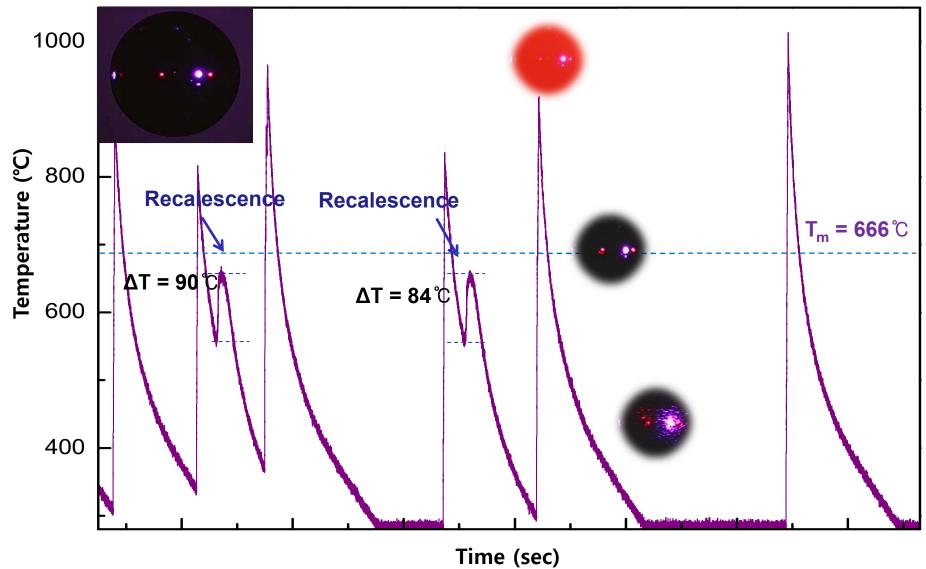
Electrostatic levitation in KRISS



KRISS material : Dr. G.W.Lee



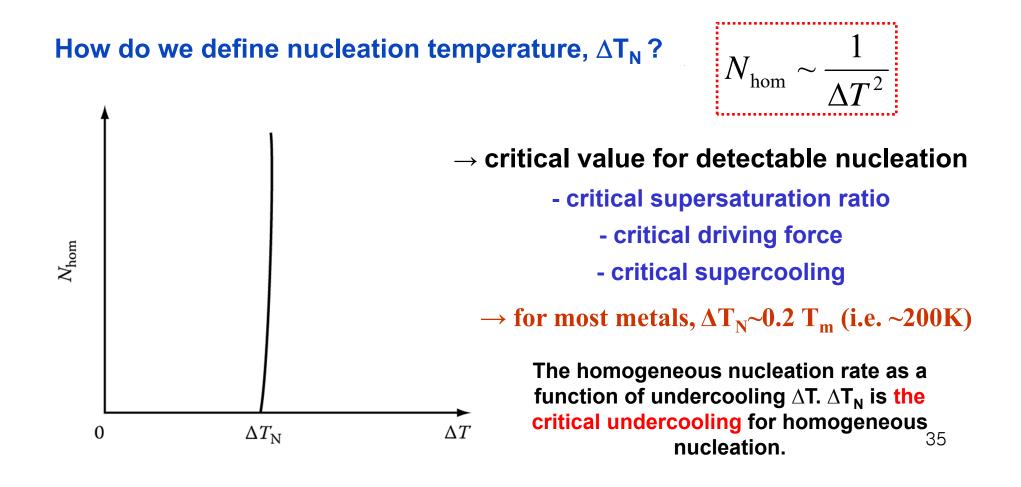
Cyclic cooling curves of $Zr_{41.2}Ti_{13.8}Cu_{12.5}Ni_{10}Be_{22.5}$



* The homogeneous nucleation rate - kinetics

$$I = \frac{nkT}{h} \exp\left(-\frac{G_A}{kT}\right) \exp\left(-\frac{16\pi\sigma_{SL}^3 T_E^2}{3L^2(\Delta T)^2 kT}\right)$$

: insensitive to Temp.



* Relationship between Maximum Supercoolings and T_m

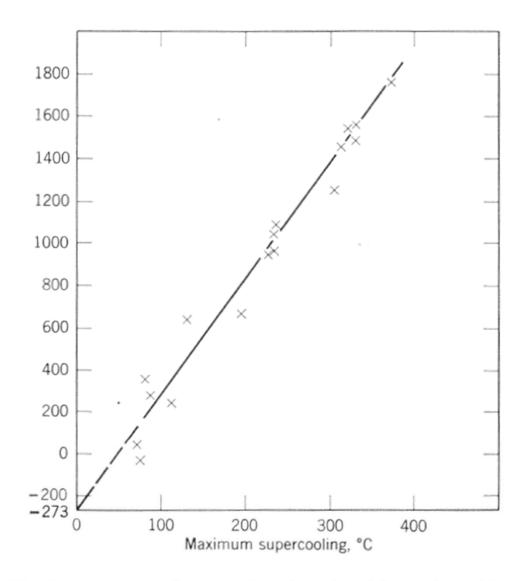


Fig. 3.7. Maximum supercooling as a function of melting point. (From *Thermo*dynamics in *Physical Metallurgy*, American Society for Metals, Cleveland, 1911, p. 11.)

Solidification: Liquid ----- Solid

- casting & welding

- single crystal growth

- directional solidification

- rapid solidification

Nucleation in Pure Metals

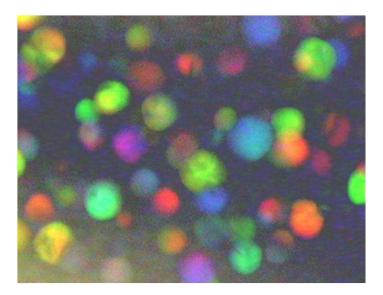
 $T_{\rm m}$: $G_{\rm L}$ = $G_{\rm S}$

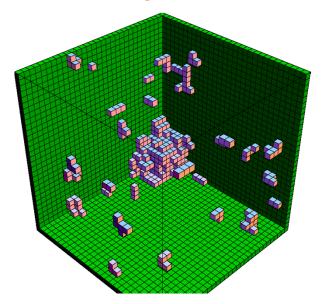
- Undercooling (supercooling) for nucleation: 250 K ~ 1 K

<Types of nucleation>

- Homogeneous nucleation

- Heterogeneous nucleation





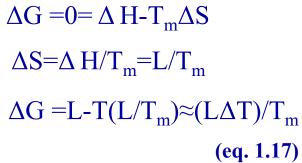
Q10: What is the driving force for "Melting: Solid → Liquid"?

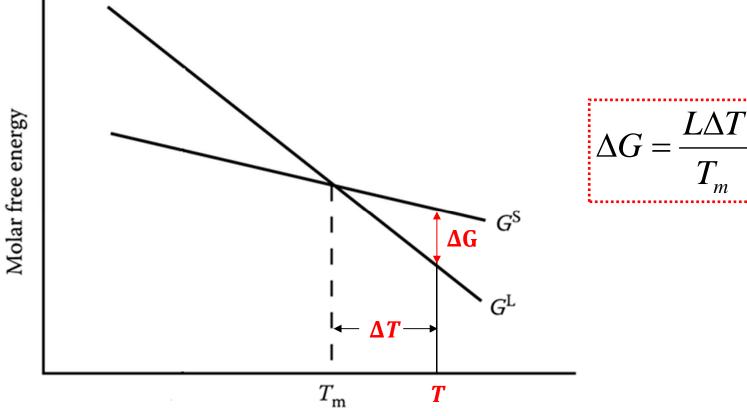
* Driving force for melting



 $\Delta G = \Delta H - T \Delta S$ $G^{S} = H^{S} - TS^{S}$ $L : \Delta H = H^{L} - H^{S}$

(Latent heat)



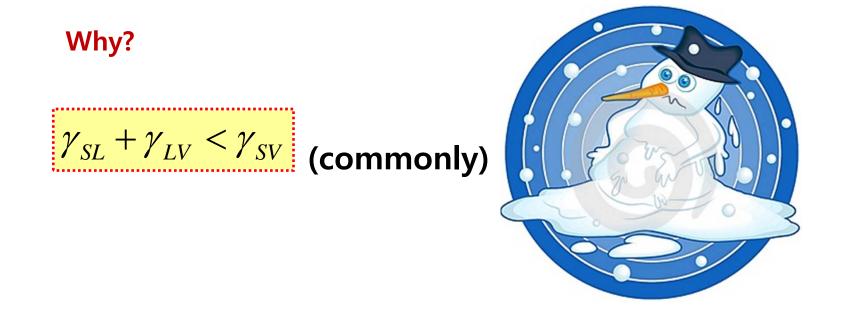


Temperature

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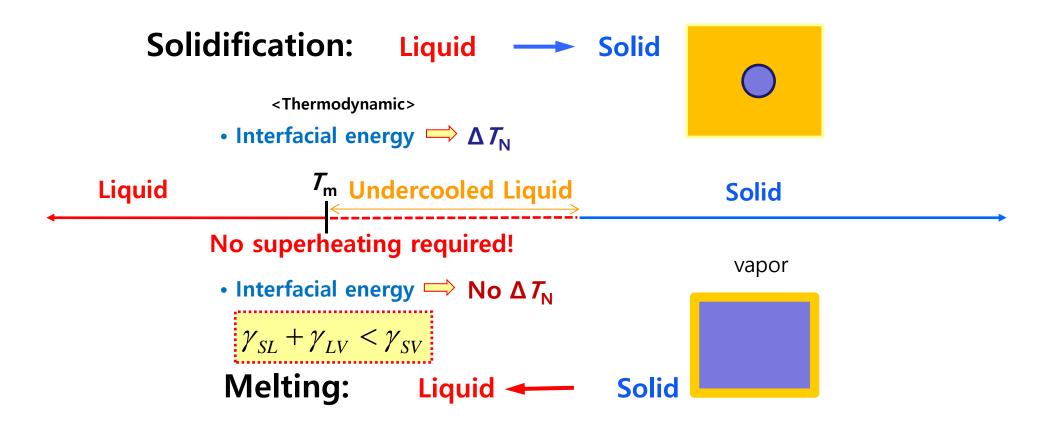
Nucleation of melting

Although nucleation during solidification usually requires some undercooling, melting invariably occurs at the equilibrium melting temperature even at relatively high rates of heating.



In general, wetting angle = 0 No superheating required!

Melting and Crystallization are Thermodynamic Transitions



Contents for today's class

Chapter 1

Thermondynamics and Phase Diagrams

- Equilibrium dG = 0

Phase Transformation

< 0

Lowest possible value of G
$$\Delta G = G_2 - G_1$$

No desire to change ad infinitum

- Single component system

Gibbs Free Energy as a Function of Temp. and Pressure

$$\left(\frac{\partial G}{\partial T}\right)_{P} = -S , \quad \left(\frac{\partial G}{\partial P}\right)_{T} = V \qquad \left(\frac{dP}{dT}\right)_{eq} = \frac{\Delta H}{T_{eq}\Delta V}$$
Clau

Clausius-Clapeyron Relation

- Classification of phase transition

First order transition: CDD/Second order transition: CCD

- Driving force for solidification

$$G = \frac{L\Delta T}{T_m}$$
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