

4. Amplifiers

Operational Amplifier
Instrumentation Amplifier
Grounding
Isolation



Amplifier Properties



Operational Amp.

1947 – Ragazza : Diff. Equation Solver

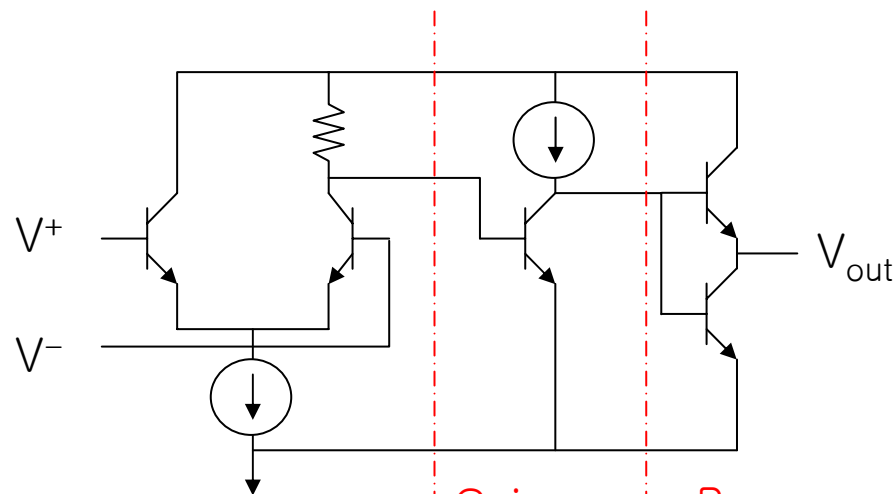
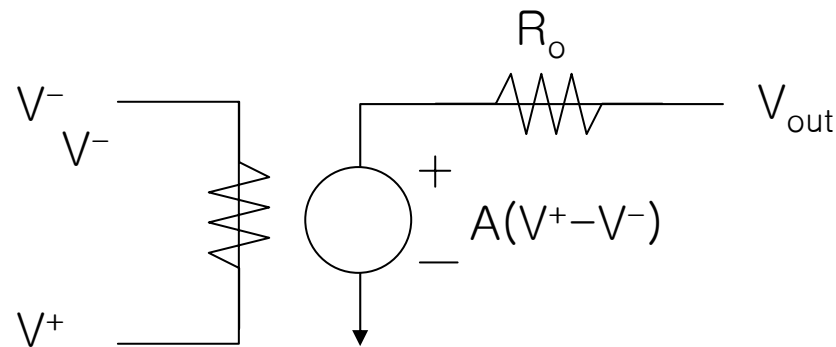
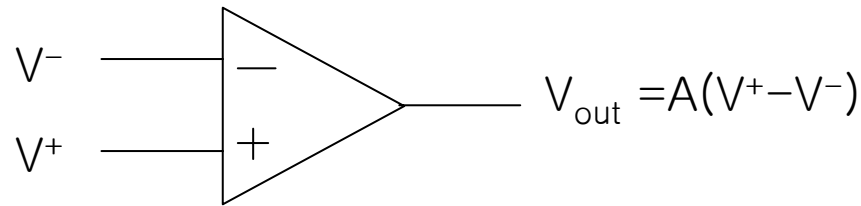
1962 – Module형 OP Amp.

1970 – Chip

Ideal Op. Amp.	ideally	means
gain(open-loop)	∞	$\geq 10^4$
open-loop BW	∞	Dominant Pole at 10Hz
CMRR	∞	$\geq 70\text{dB}$
Ri	∞	$\geq 10\text{M}\Omega$
Ro	0	$< 500\Omega$
I B	0	$< 0.5\mu\text{A}$
Vos	0	$< 10\text{mV}$
Ios	0	$< 0.2\mu\text{A}$



How do we achieve these properties?



Differential stage

Gain stage

Power gain

741인 경우

(Stage 1) $R=1.6M\Omega$
Gain=1200

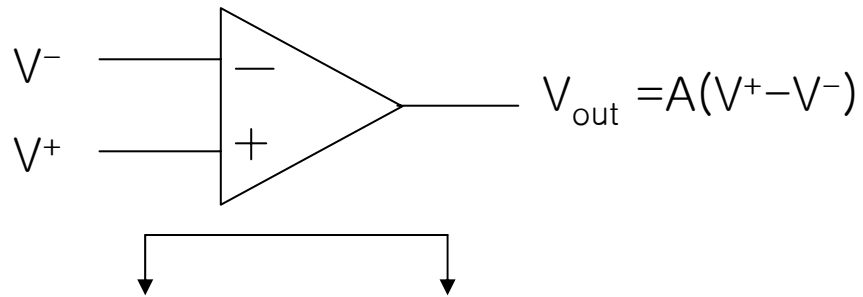
(Stage 2) V_{tg} gain=220

(Stage 3) $R_o=60\Omega$
 V_{tg} gain=1

Overall Gain=108dB



Two rules

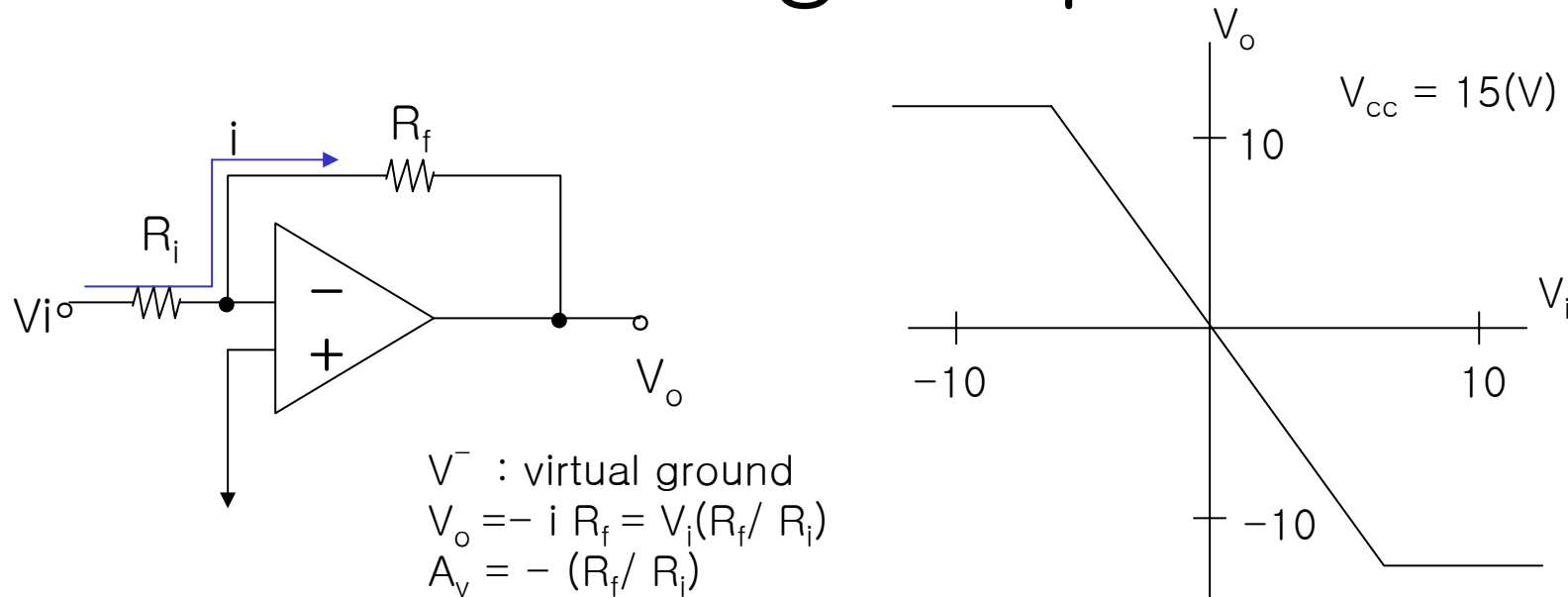


Rule 1: Op Amp의 output이 Linear Stage에 있을 때,
두 input은 동 전위에 있다. (Virtual Ground)

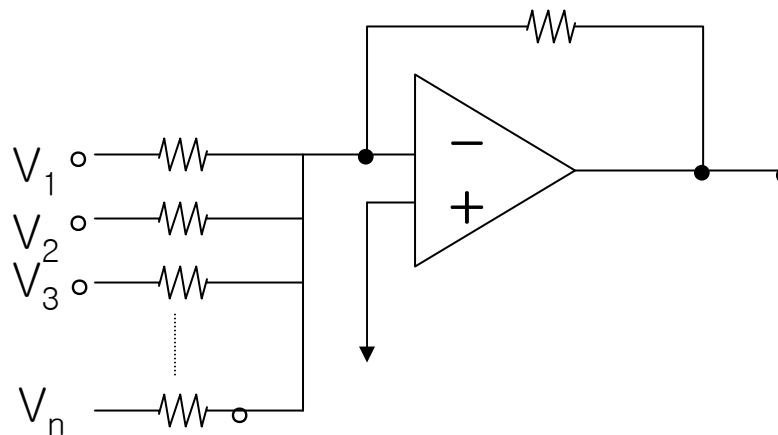
Rule 2: Op Amp의 input 단자에 입력되는 전류는 없다.
(infinite input impedance)



Inverting Amp.

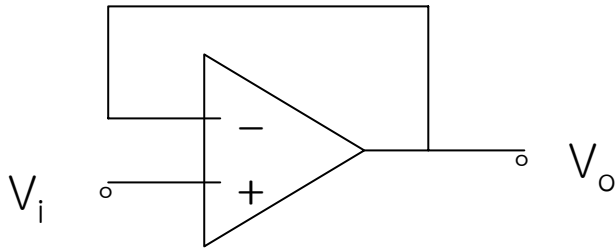


■ Summing



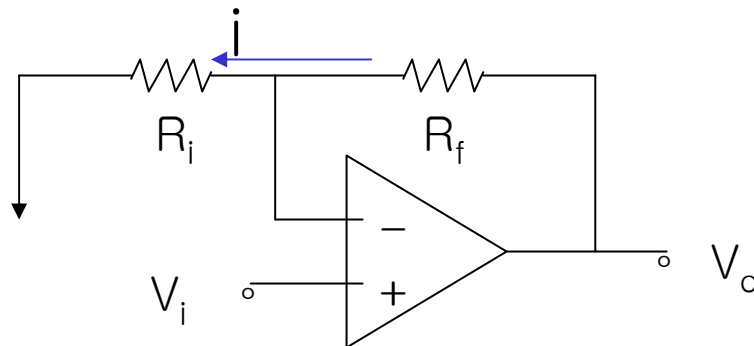
Non Inverting Amp.

- Follower



Buffer, Impedance Converter

- Non-inverting Amp.



$$\begin{aligned} V_o &= i \cdot (R_i + R_f) \\ V_i &= i \cdot R_i \end{aligned}$$

$$\Rightarrow A_v = \frac{R_i + R_f}{R_i}$$

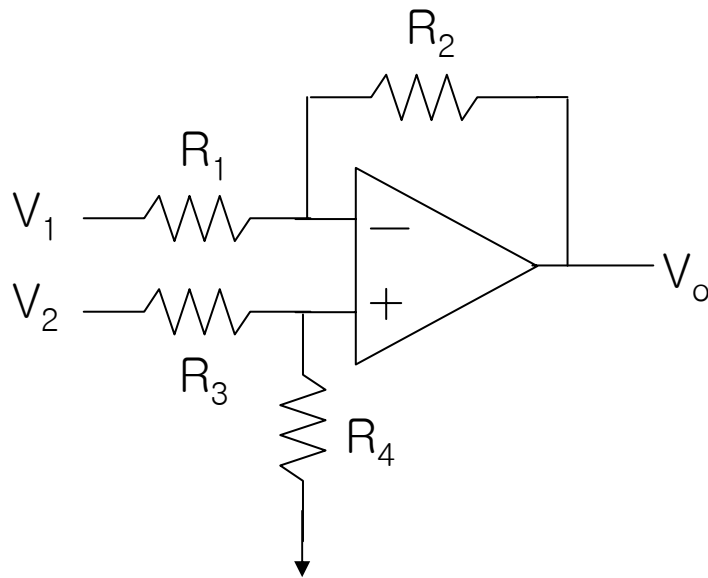


Instrumentation Amp

- High gain DC complied differential amp with single ended output.

High Z_{in} , CMRR

Used to Amplify small differential signals from transducer where there may be a large common signal.



$$V^+ = V_2 \cdot \frac{R_4}{R_3 + R_4}, \quad V^- = (V_o - V_1) \frac{R_1}{R_1 + R_2} + V_1$$

$V^+ = V^-$ 로부터

$$V_o = \frac{R_4}{R_3 + R_4} \left(1 + \frac{R_2}{R_1} \right) V_2 - \frac{R_2}{R_1} V_1$$

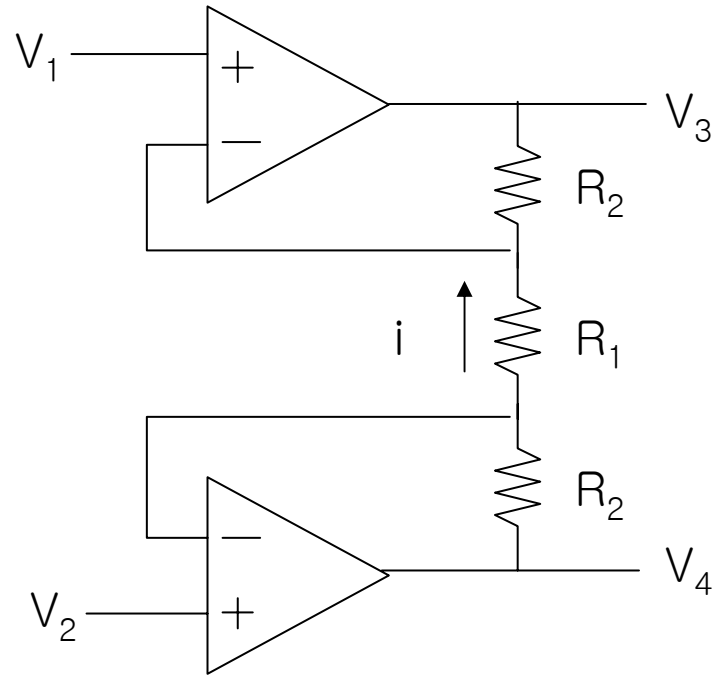
$$\text{if } \frac{R_3}{R_4} = \frac{R_1}{R_2} \rightarrow V_o = \frac{R_2}{R_1} (V_2 - V_1), \quad G_d = \frac{R_2}{R_1}$$

Common mode $V_1 = V_2 \rightarrow V_o = 0 \rightarrow G_c = 0$

CMRR = G_d / G_c



For High Input Impedance



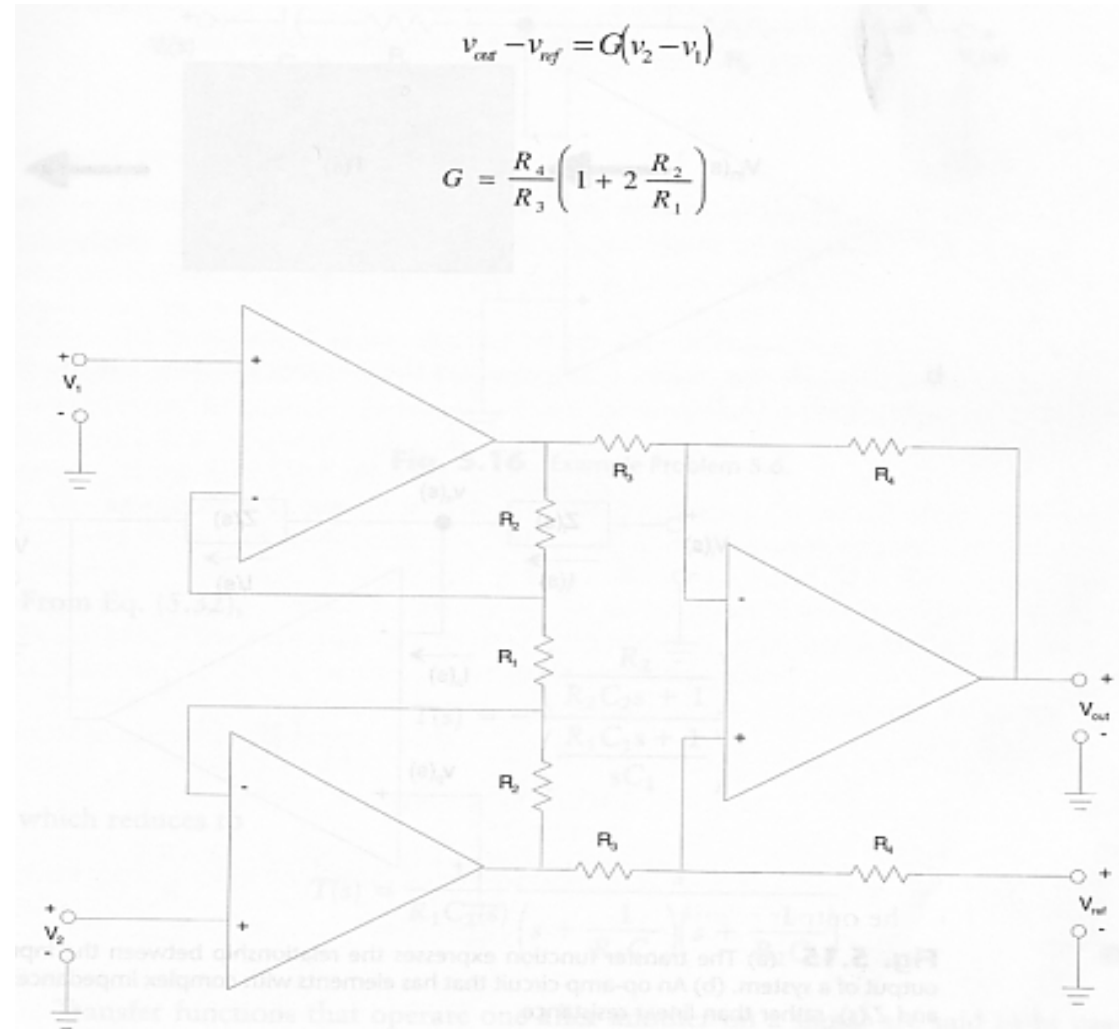
If $V_1 = V_2$ (CMG)
 $\rightarrow i = 0$
 $\rightarrow V_1 = V_2 = V_3 = V_4$
 $\rightarrow G_c$ (CMG) = 0

If $V_1 \neq V_2$ (DMG)
 $\rightarrow i = (V_2 - V_1) / R_1$

$$\frac{V_4 - V_3}{V_2 - V_1} = \frac{R_1 + 2R_2}{R_1} = 1 + 2 \cdot \frac{R_2}{R_1}$$

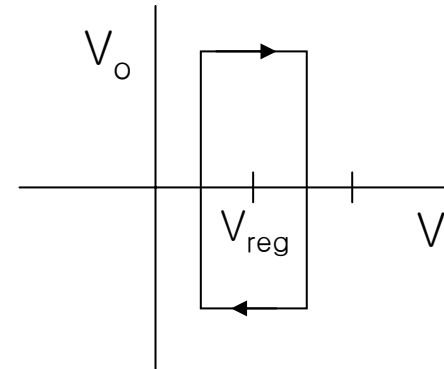
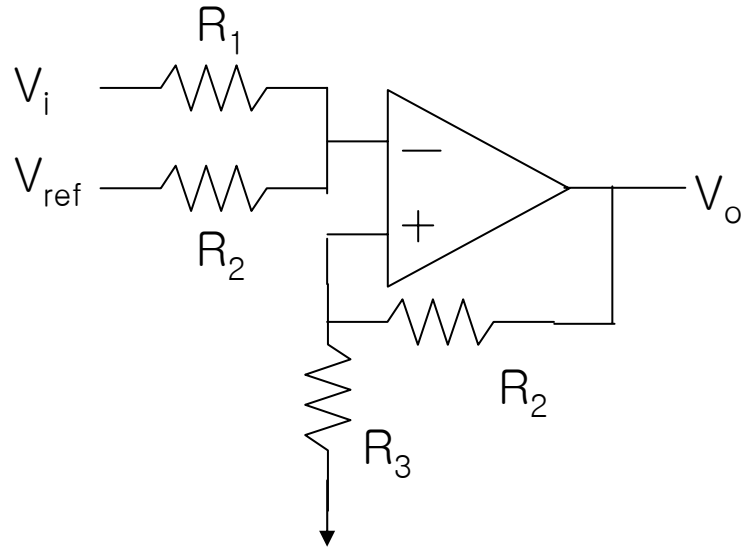


Complete Design of Instrumentation Amp.

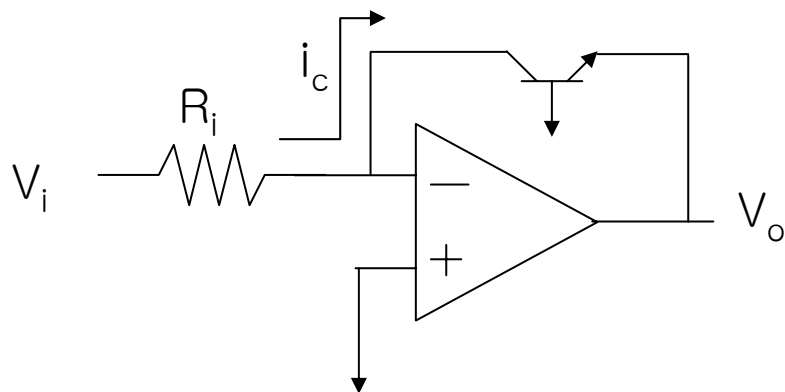


Circuits

<Comparator>



<Log Amp>

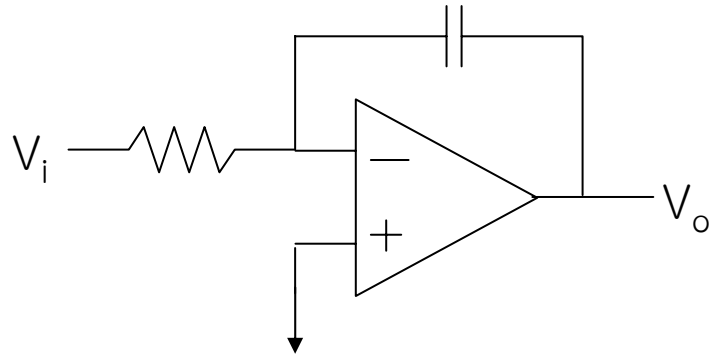


$$V_{BE} = 0.06 \log \frac{I_c}{I_s}, \quad V_{BE} = -V_o$$

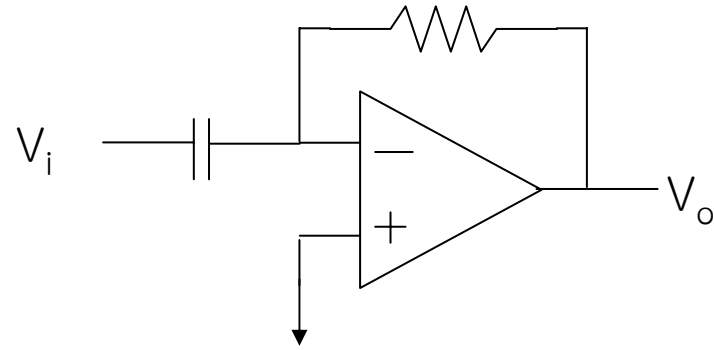
$$I_c = \frac{V_i}{R_i} \rightarrow V_o = -V_{BE} \propto -\log V_i$$



<Integrator>

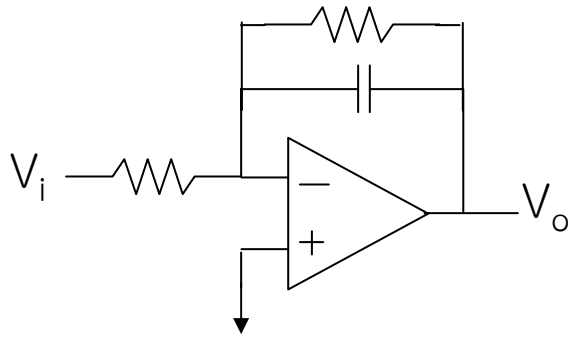


<Differentiator>

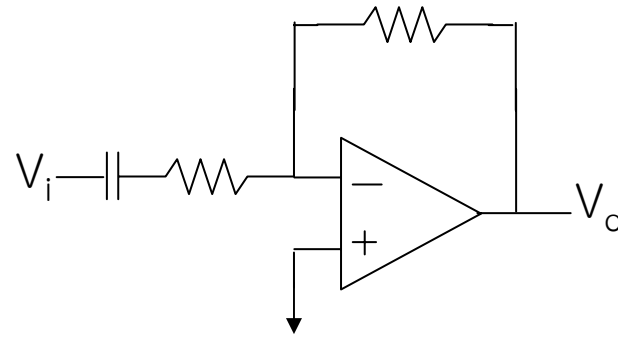


Slope detector (if cascaded by a comparator)

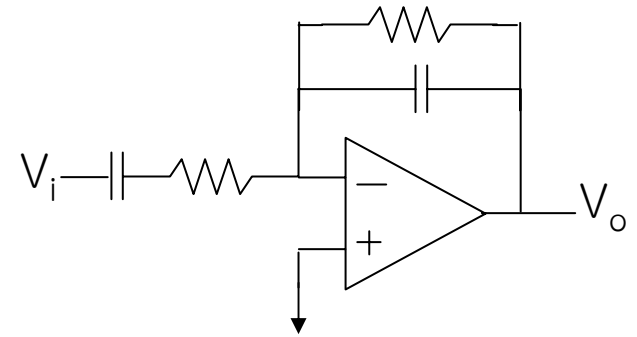
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Low pass



High pass

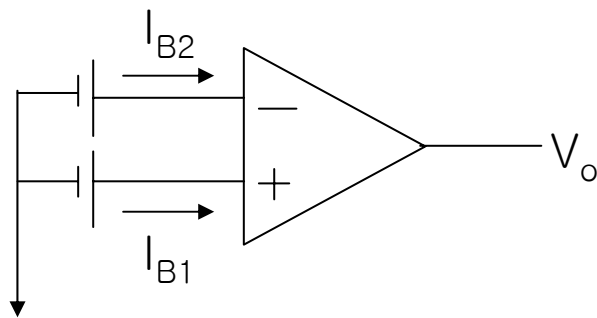


Band pass

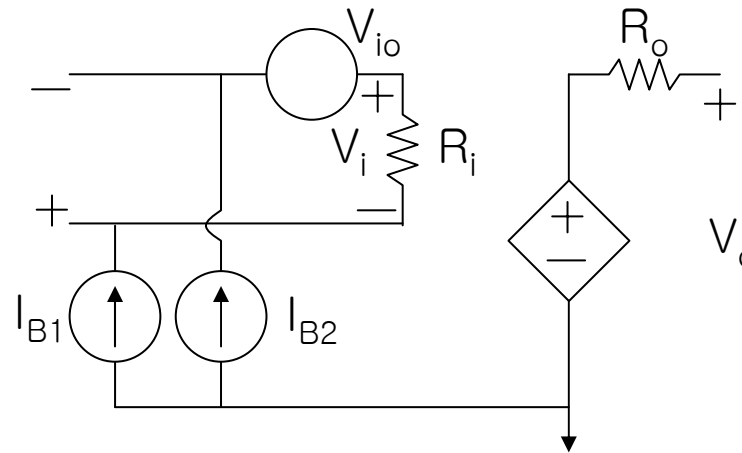


Bias currents and Input current offset

- Input Bias Currents I_{B1}, I_{B2} exist to bias the frontend transistors.



~20uA 741



30pA to JFET input

- Input offset current (I_{io})

$$I_{io} = I_{B1} - I_{B2}$$



Input and Output Voltage Offsets

– Input offset voltage (V_{io})

V_{be} 의 작은 차이가 원인

V_{io} is temperature dependent ($-2.2\text{mV}/\text{C}$)

This temperature dependency is too large to accept. Use differential configuration to compensate. ($3.3\mu\text{V}/\text{C}$)

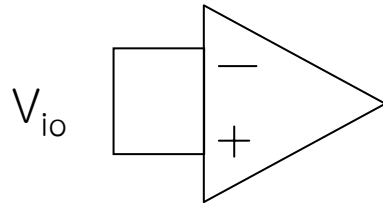
– Output offset voltage (V_{os})

DC voltage present at two output terminals when two input terminals are grounded. This is independent of amplifier gain. Usually seen as a drift at unity gain.



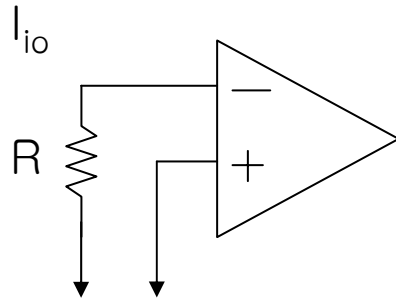
Measurements of Offsets

– Input offset voltage measurement



– Short input. (At high gain, the output offset voltage can be negligible compared to the input offset voltage multiplied by the gain.)

– Bias current measurement



Measure output divided by Gain This gives the input offset voltage.

– Short two inputs to GND, one through R

$$\left(\frac{V_{out}}{Gain} - V_{io} \right) \cdot \frac{1}{R} = I_{b1}$$

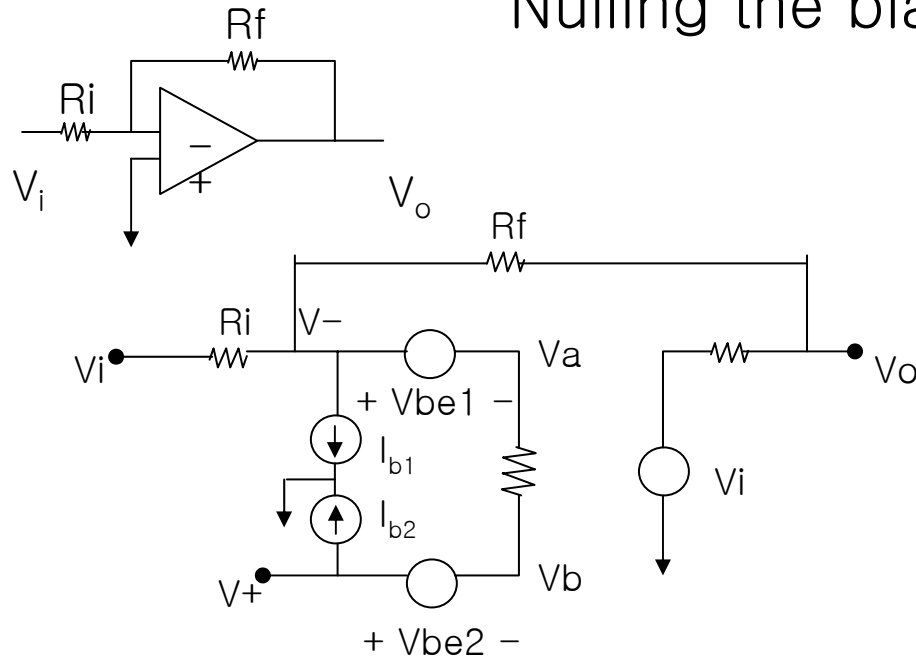
Repeat this for the other terminal for I_{b2}

$$I_{io} = I_{b1} - I_{b2}$$

$$I_b = \frac{1}{2}(I_{b1} + I_{b2})$$



Nulling the bias current



Assume

$$V^+ = V^-$$

$$I_{b1} = I_{b2} = I_b$$

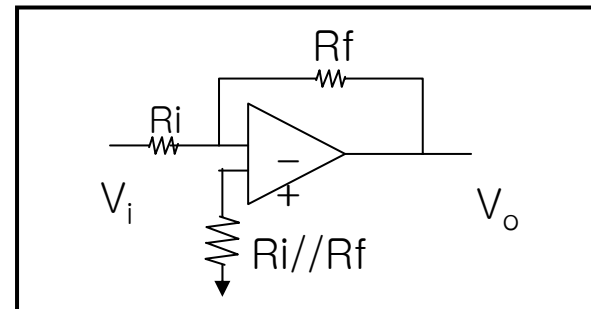
$$\frac{V_o - V^-}{R_f} + \frac{V_i - V^-}{R_i} = I_b \quad (\text{eq 1})$$

Ideally we want, $V_o/R_f = -V_i/R_i$ (eq 2)

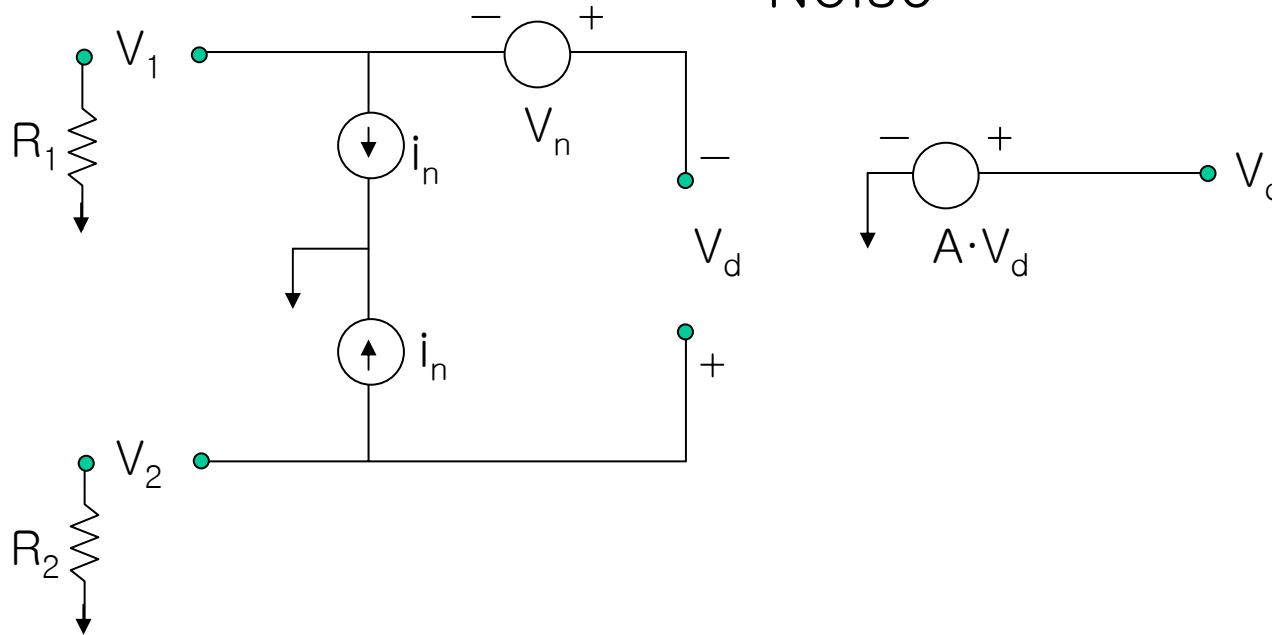
Comparing eq 1 and 2,

$$I_b + V^+ / (R_f // R_i) = 0$$

This condition can be satisfied by the next circuit.



Noise



i_n : noise current sources in rms

$$A/\sqrt{\text{Hz}}$$

V_n : noise voltage sources in rms

$$V/\sqrt{\text{Hz}}$$

$$V_t \cong \sqrt{[V_n^2 + (i_n R_1)^2 + (i_n R_2)^2 + 4kTR_1 + 4kTR_2] \text{BW}}$$

i_n , V_n given by specs

- Bipolars
- FETs: smaller i_n —especially JFETs



Input Impedance

(1) The case of a Follower

$R_i = R_i (\text{op amp}) \times A_{OL} : \text{very large}$

$$2\text{M}\Omega \times 10^5 = 100\text{G}\Omega$$

But Bias currents can reduce R_i .

For this reason, OP amp with FET (especially JFET) input is preferred for applications where high input impedance is required, such as in single neural cell recordings.

(2) inverter

$R_i = R_i (\text{op amp})$



– output impedance

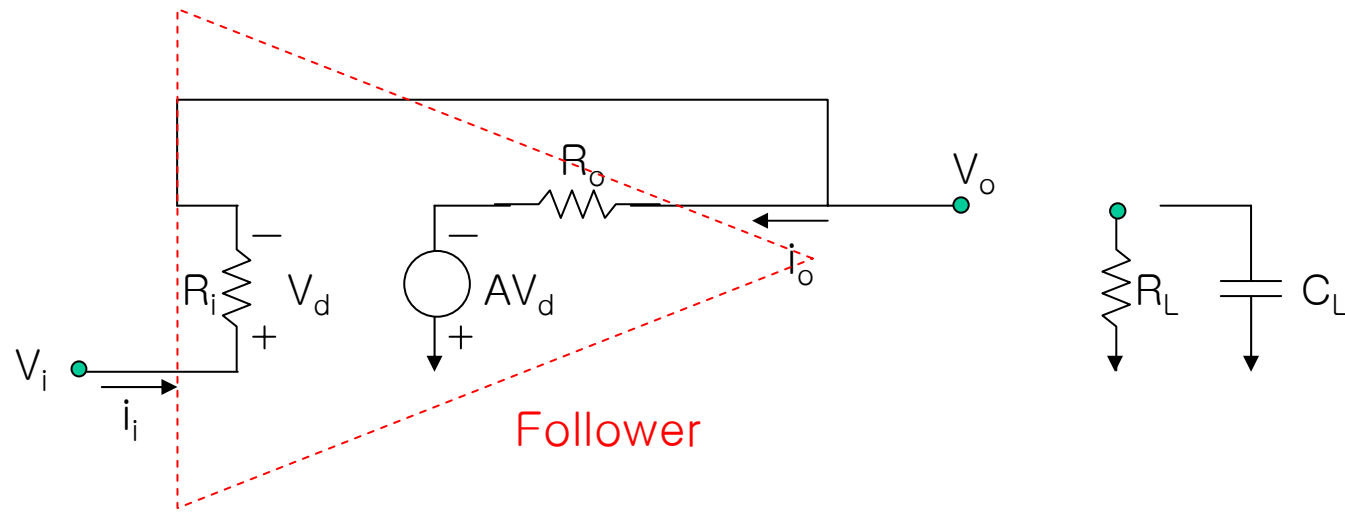
(1) Follower인 경우

$$R_o = R_o (\text{op amp}) / A_{OL}$$
$$40 / 10^5 = 0.4 \text{m}\Omega$$

(2) inverter인 경우

$$R_o = R_o (\text{op amp})$$





For R_i

$$\Delta V_o = AV_d = A(\Delta V_i - \Delta V_o)$$

$$\Delta V_o = \frac{A}{A+1} \Delta V_i$$

$$\Delta i_i = \frac{\Delta V_d}{R_i} = \frac{\Delta V_i - \Delta V_o}{R_i} = \frac{\Delta V_i}{(A+1)R_i}$$

$$\rightarrow R_i = \frac{\Delta V_i}{\Delta i_i} = (A+1)R_i = A \cdot R_i$$

For R_o

$$\begin{aligned} \Delta V_d = \Delta V_o &= A \Delta V_d + \Delta i_o R_o \\ &= -A \Delta V_o + \Delta i_o R_o \end{aligned}$$

$$\rightarrow (A+1) \Delta V_o = \Delta i_o R_o$$

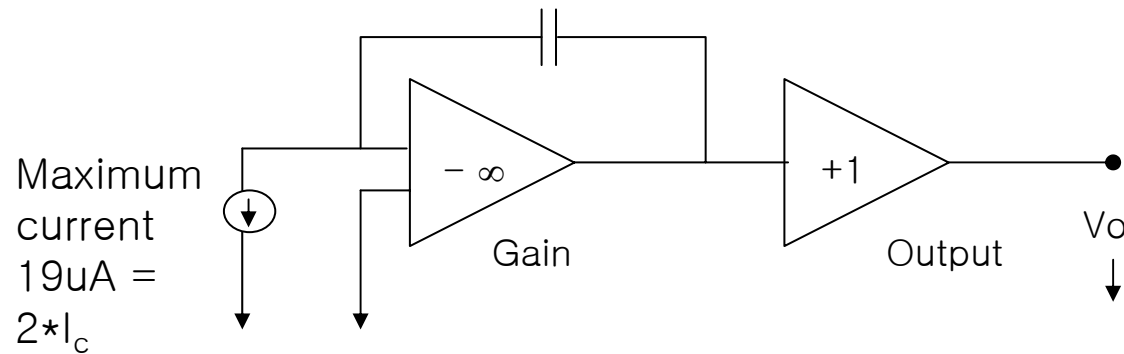
$$\rightarrow R_o = \frac{\Delta V_o}{\Delta i_o} = \frac{R_o}{A+1} = \frac{R_o}{A}$$



Slew Rate

- Maximum rate of output voltage change

741 model

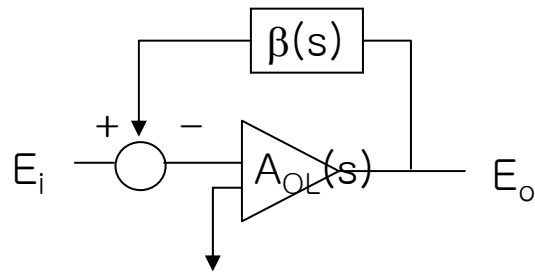


$$2 \cdot I_c \text{ charging } C_c : \text{Slew rate} \\ = dV_o/dt = 2I_c/C_c = 0.63\text{V}/\mu\text{s}$$

C_c : freq. Compensation 을 위해 삽입된 Miller Cap.



Frequency Stability



$$A_{CL}(S) = E_o/E_i = A_{OL}(S)/(1 + A_{OL}(s) \beta(s))$$
$$= A_{OL}(s)/(1 + A_L(S))$$

Instability : $A_L(s) = A_{OL}(s)B(s) = 1 \angle 180 = -1$ 일 때.

Critical condition : $A_{OL}(j\omega) = \{1/\beta(j\omega)\} \angle 180$

즉,

$|A_{OL}(j\omega)| = 1/|\beta(j\omega)|$ 이고 $\Phi_{OL} - \Phi_{CL} = 180^\circ$

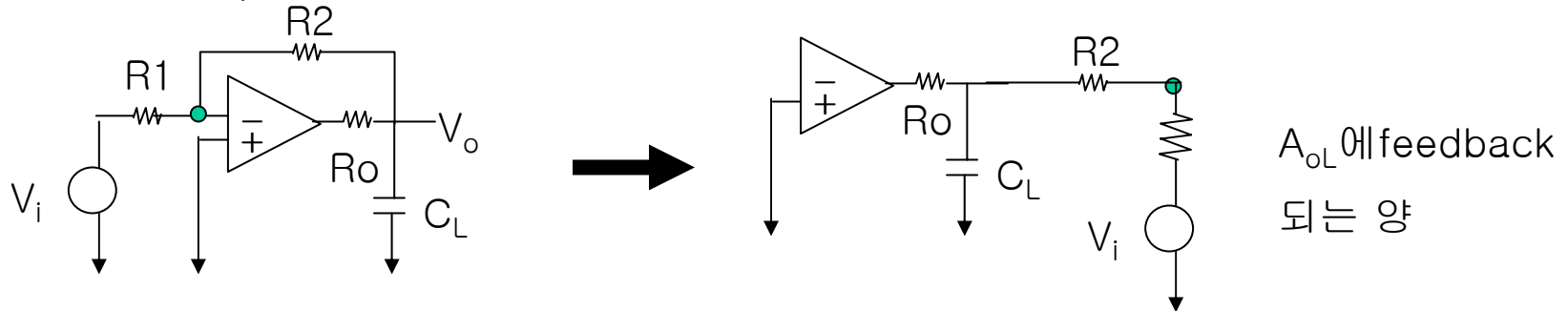
가 되는 freq.에서 oscillation



Frequency Stability

- 흔히 우리는 $|A_L(j\omega)| = |A_{oL}(j\omega)\beta(j\omega)| = 1$ 이 되는 ω 를 구하고 이 때의 $A_L(j\omega)$ 의 phase를 보아, 이것이 $+180^\circ$ 로부터 떨어진 정도를 측정하며 이를 Φ_M (Phase margin) 이라고 한다.
 - $\Phi_M \sim 90^\circ$ 정도일 때 stable system
 - Φ_M 은 크면 클수록 유리하다.

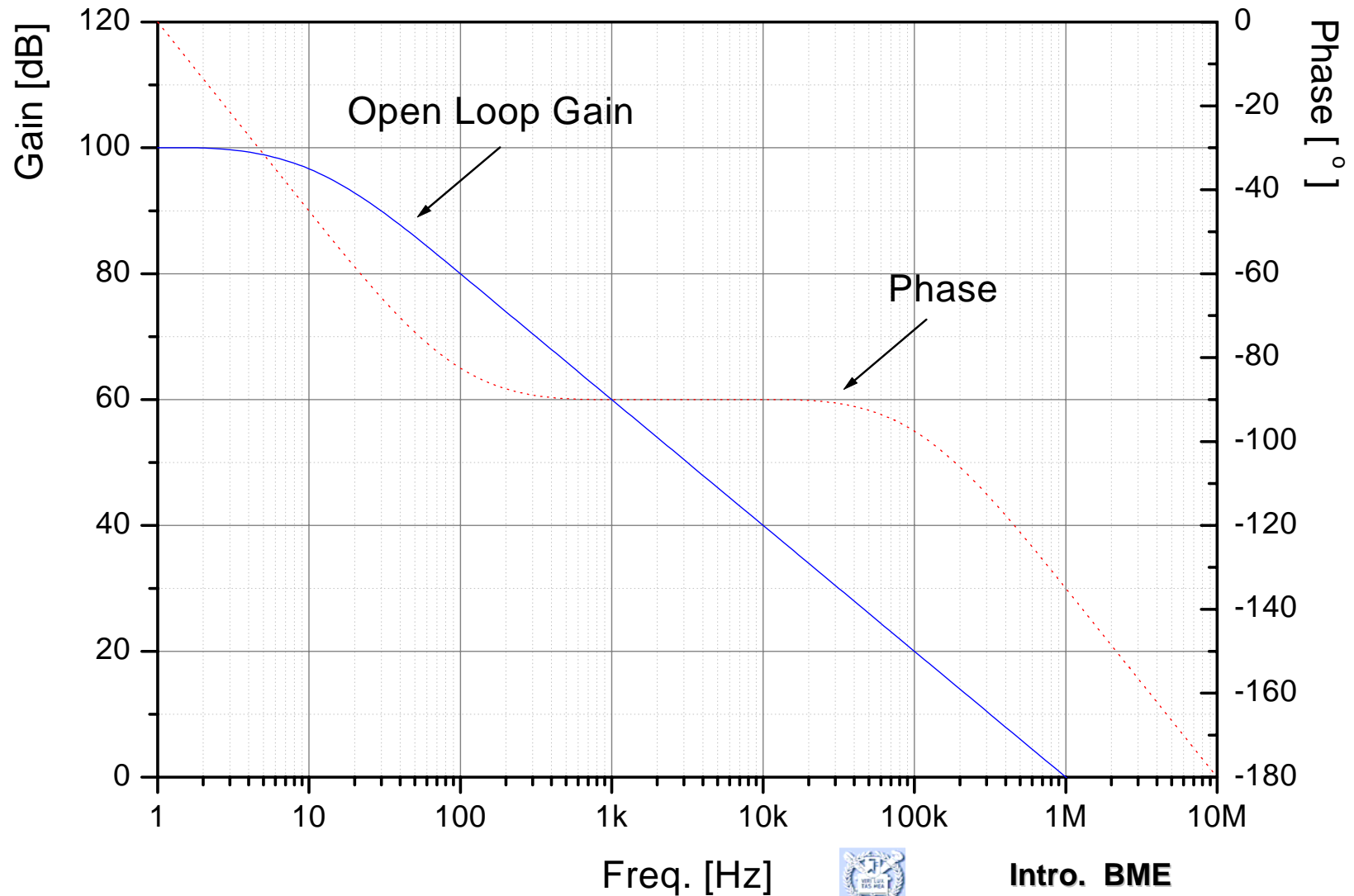
- OP Amp 의 경우



$C_L=0$, V_i 가 없을 때,
 $\beta = R_1/(R_o+R_2+R_1) \approx R_1/(R_2+R_1)$
 즉 $A_{oL}(j\omega)$ 에 $\beta = R_1/(R_2+R_1)$ 을 곱해 $A_L(j\omega)$ 를 구하고
 이의 Bode Diagram 에서 Φ_M 을 구한다



Frequency Stability



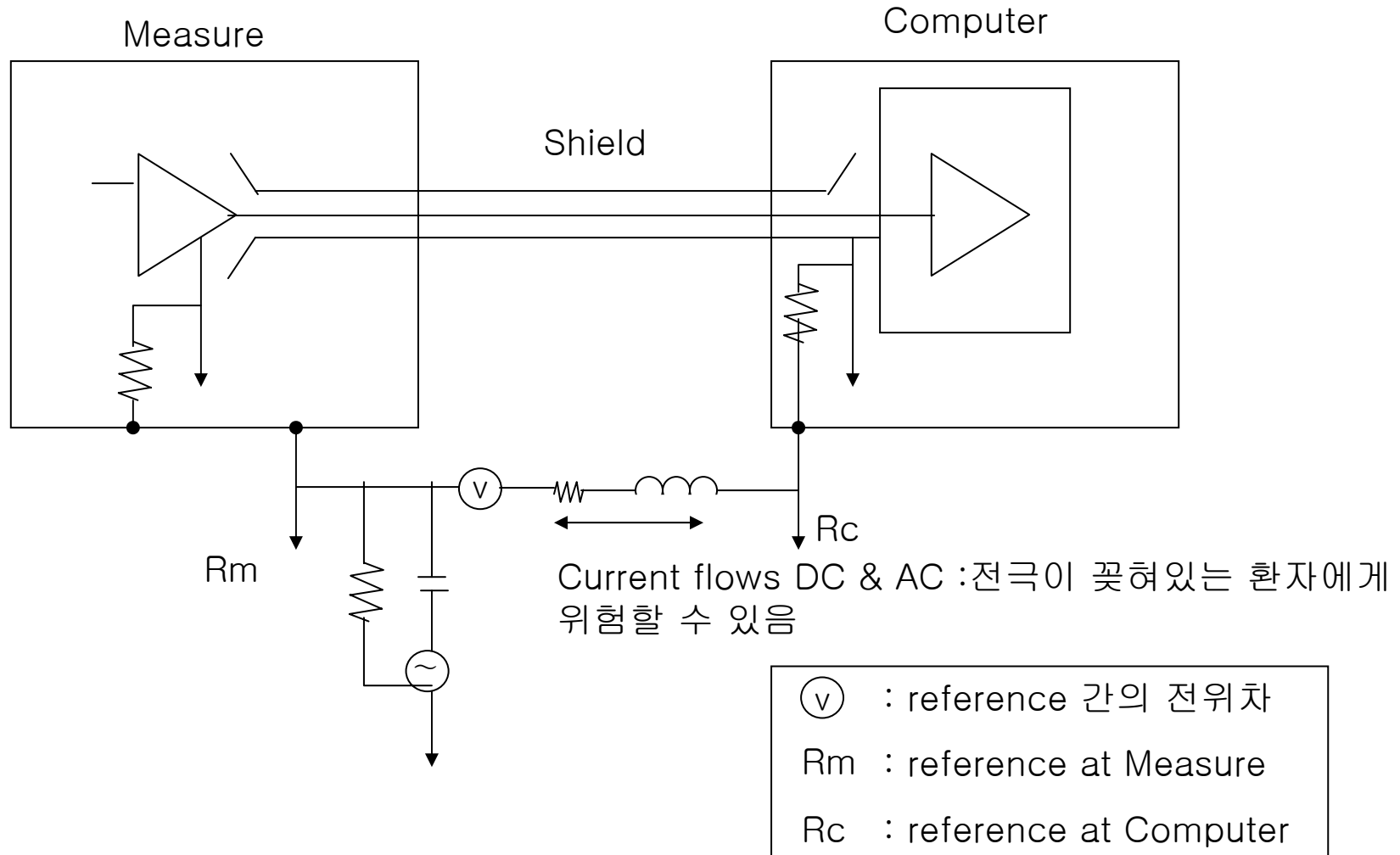
Interference

- Noise : random
- Interference : not random, comes from a known source
- Dominant interference : 60Hz
 - Thru. ① AC capacitive coupling
 ② AC inductive coupling
 ③ Ground loops
 - Solutions
 - (1) Elimination at the source
 - Use of Instrumentation Amps and Isolation Amps.
 - Star Ground (one true ground)
 - (2) (Adaptive) Filtering



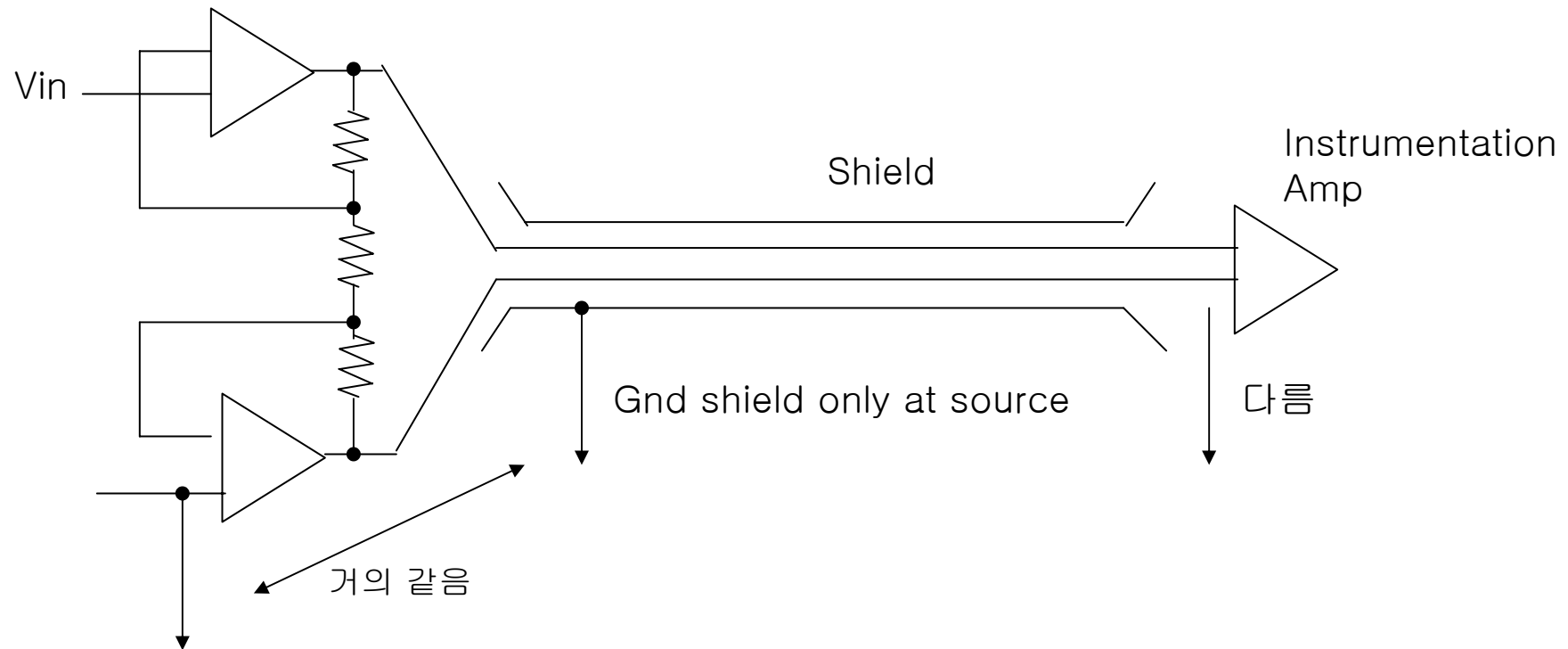
Grounding & Instrumentation Amp.

- Ground Loop is a problem.



Grounding & Instrumentation Amp.

- Solution(I) : Differential Transmission



모든 noise는 common mode로 처리



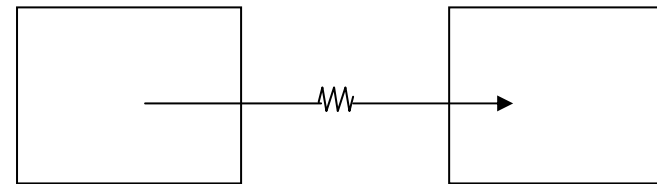
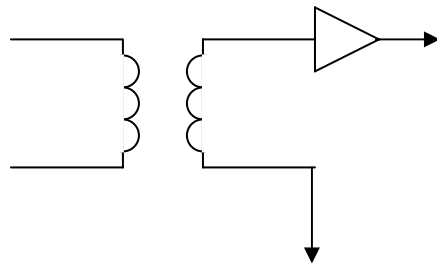
Grounding & Instrumentation Amp.

- Ground Loop => safety
ECG 측정시 ground loop current는 전극이 꽂혀있는 환자를 통하여 흐르게 되므로 위험
- Bias current => safety
특별히 I_B 가 작은 소자
Ex) AD55L max $I_B = 75\text{fA}$
AD00L max $I_B = 10\text{fA}$
- Ground Loop => SNR을 낮춤
- Careful grounding is needed



Grounding & Instrumentation Amp.

- Solution(II) : Isolation between Measure and Computer stations.
 - By transformer



Optics, RF

- Optical coupling : optical isolator : (LED/LD)–PD 조합
- Radio link
 - Signal – Modulator – Transmitter ...– Receiver – Demodulator





Low Cost, Miniature Isolation Amplifiers

AD202/AD204

FEATURES

- Small Size: 4 Channels/Inch
- Low Power: 35 mW (AD204)
- High Accuracy: $\pm 0.025\%$ max Nonlinearity (K Grade)
- High CMR: 130 dB (Gain = 100 V/V)
- Wide Bandwidth: 5 kHz Full-Power (AD204)
- High CMV Isolation: ± 2000 V pk Continuous (K Grade) (Signal and Power)

Isolated Power Outputs

Uncommitted Input Amplifier

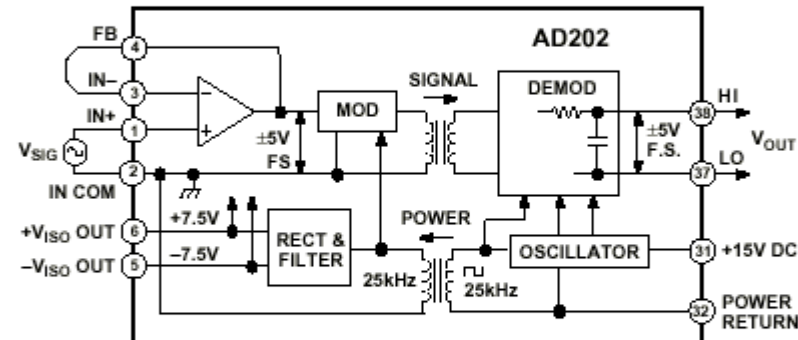
APPLICATIONS

- Multichannel Data Acquisition
- Current Shunt Measurements
- Motor Controls
- Process Signal Isolation
- High Voltage Instrumentation Amplifier

GENERAL DESCRIPTION

The AD202 and AD204 are general purpose, two-port, transformer-coupled isolation amplifiers that may be used in a broad range of applications where input signals must be measured, these industry standard isolation amplifiers offer a complete isolation function, with both signal and power isolation provided

FUNCTIONAL BLOCK DIAGRAM



Isolation mode rejection ratio(IMRR):105dB@60Hz

ing. For applications requiring a low profile, the DIP package provides a height of just 0.350".

High Accuracy: With a maximum nonlinearity of $\pm 0.025\%$ for the AD202K/AD204K ($\pm 0.05\%$ for the AD202J/AD204J) and low drift over temperature, the AD202 and AD204 provide high isolation without loss of signal integrity.

Low Power: Power consumption of 35 mW (AD204) and 75 mW (AD202), over the full signal range makes these isolators power budgets.



Intro. BME