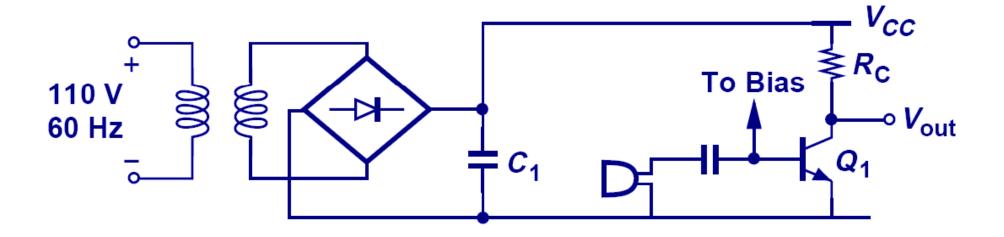
Chapter 10 Differential Amplifiers

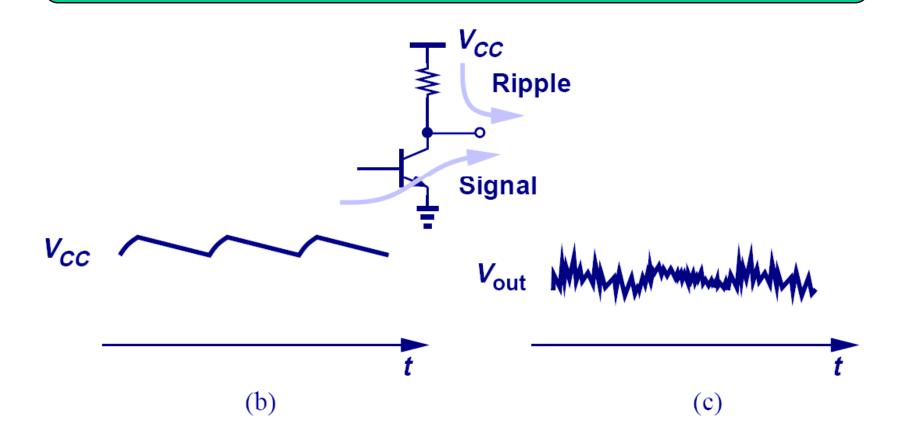
- > 10.1 General Considerations
- > 10.2 Bipolar Differential Pair
- > 10.3 MOS Differential Pair
- 10.4 Cascode Differential Amplifiers
- > 10.5 Common-Mode Rejection
- 10.6 Differential Pair with Active Load

Audio Amplifier Example



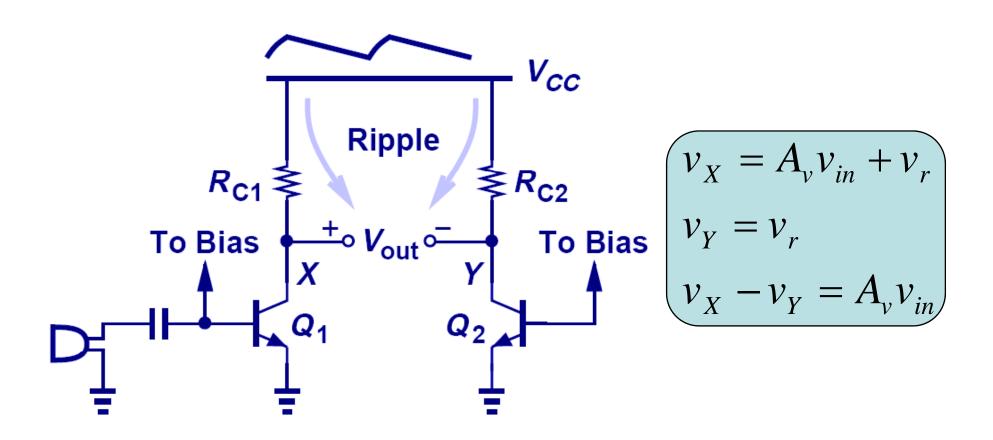
An audio amplifier is constructed above that takes on a rectified AC voltage as its supply and amplifies an audio signal from a microphone.

"Humming" Noise in Audio Amplifier Example



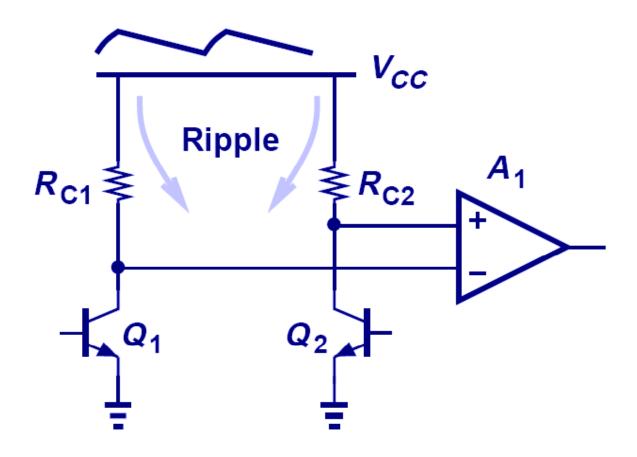
► However, V_{CC} contains a ripple from rectification that leaks to the output and is perceived as a "humming" noise by the user.

Supply Ripple Rejection



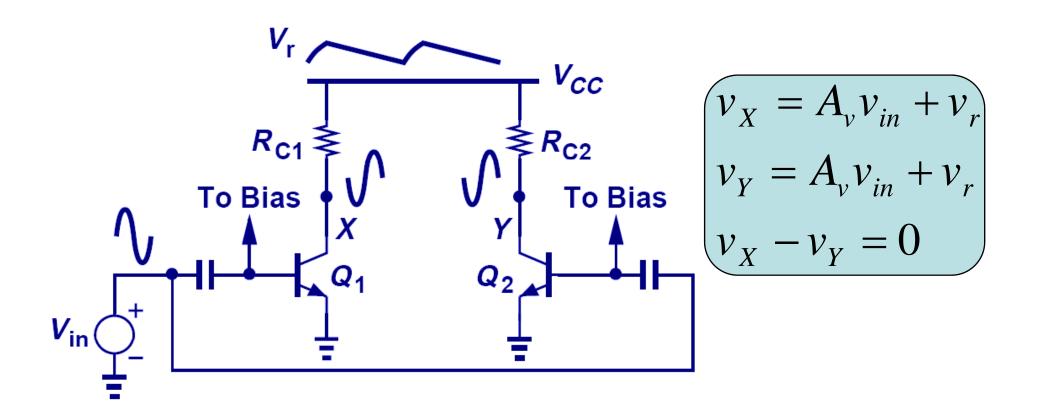
Since both node X and Y contain the ripple, their difference will be free of ripple.

Ripple-Free Differential Output



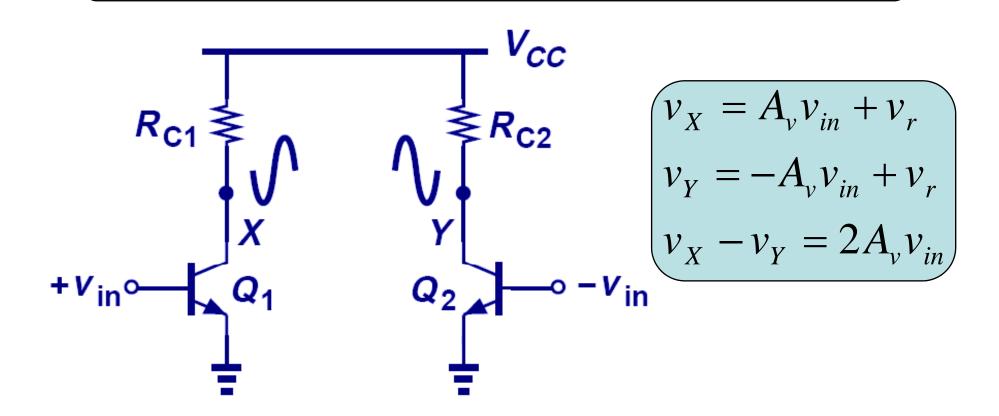
Since the signal is taken as a difference between two nodes, an amplifier that senses differential signals is needed.

Common Inputs to Differential Amplifier



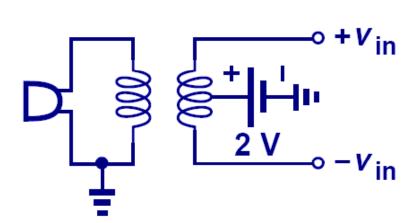
Signals cannot be applied in phase to the inputs of a differential amplifier, since the outputs will also be in phase, producing zero differential output.

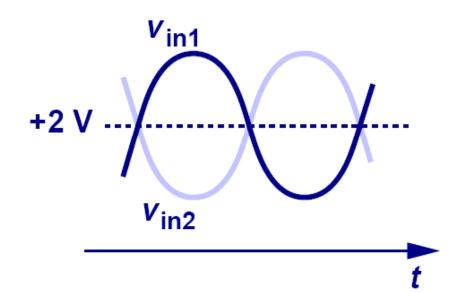
Differential Inputs to Differential Amplifier



When the inputs are applied differentially, the outputs are 180° out of phase; enhancing each other when sensed differentially.

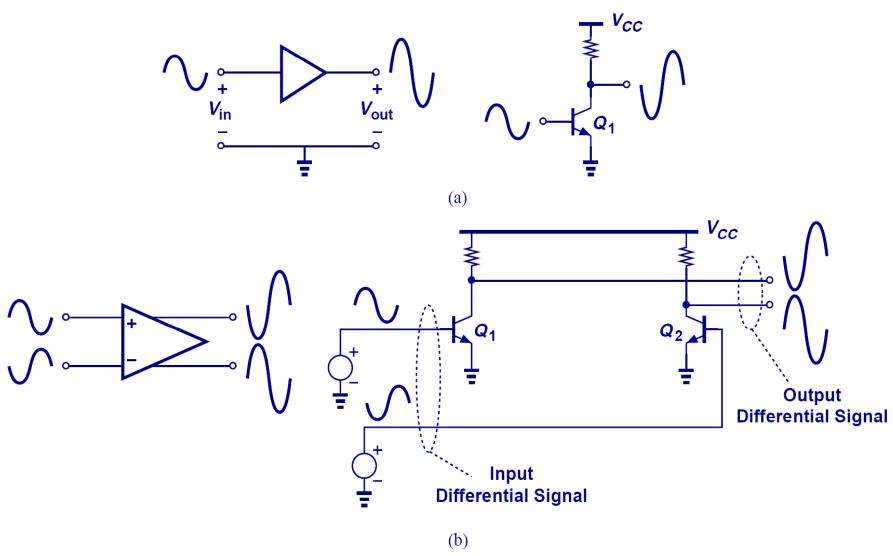
Differential Signals



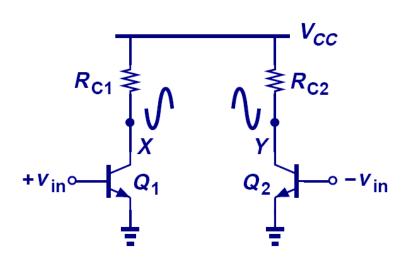


- > A pair of differential signals can be generated, among other ways, by a transformer.
- ➤ Differential signals have the property that they share the same average value to ground and are equal in magnitude but opposite in phase.

Single-ended vs. Differential Signals



Determine the common-mode level at the output of the circuit shown in Fig. 10.3(b).



In the absence of signals,

$$V_X = V_Y = V_{CC} - R_C I_C$$

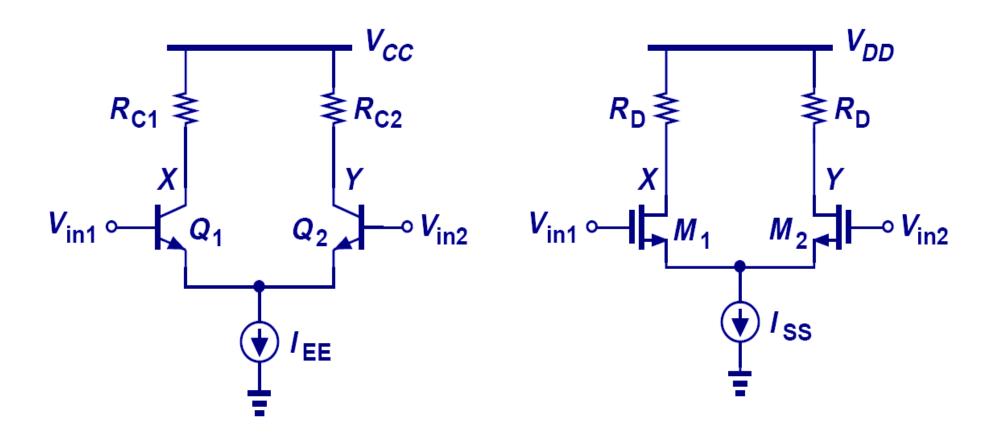
where $R_C = R_{C1} = R_{C2}$ and

 I_C denotes the bias current of Q_1 and Q_2

Thus,
$$V_{CM} = V_{CC} - R_C I_C$$

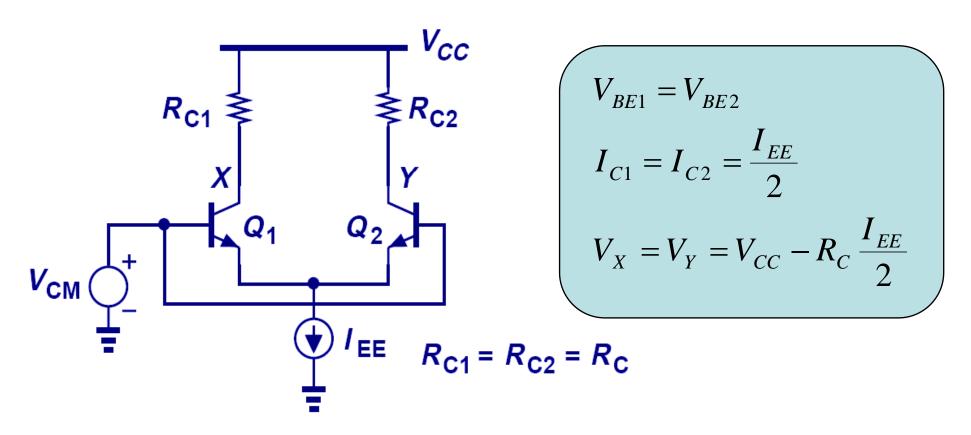
Interestingly, the ripple affects V_{CM} but not the differential output.

Differential Pair



➤ With the addition of a tail current, the circuits above operate as an elegant, yet robust differential pair.

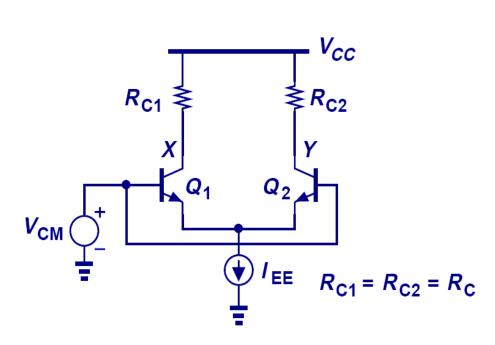
Common-Mode Response



To avoid saturation, the collector voltages must not fall below the base voltages:

$$V_{CC} - R_C \frac{I_{EE}}{2} \ge V_{CM}$$

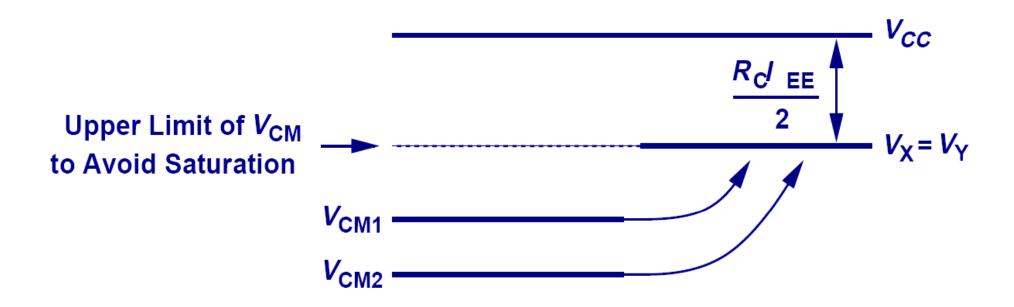
ightharpoonup A bipolar differential pair employs a load resistance of 1 kΩ and a tail current of 1 mA. How close to V_{CC} can V_{CM} be chosen?



$$V_{CC} - V_{CM} \ge R_C \frac{I_{EE}}{2}$$
$$\ge 0.5 \text{V}$$

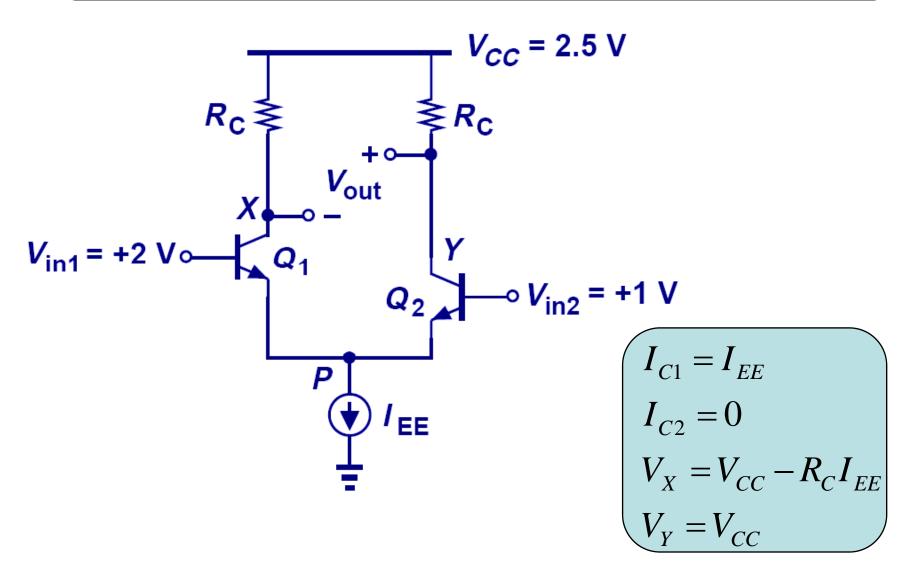
That is, V_{CM} must remain below V_{CC} by at least 0.5 V.

Common-Mode Rejection

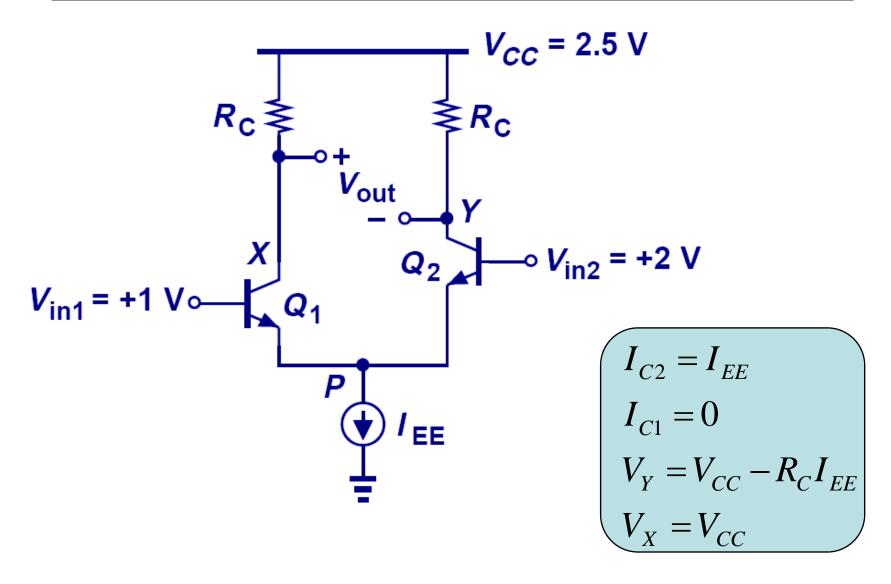


Due to the fixed tail current source, the input commonmode value can vary without changing the output commonmode value.

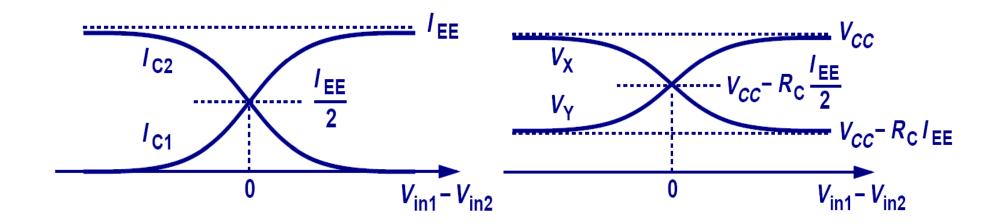
Differential Response I



Differential Response II

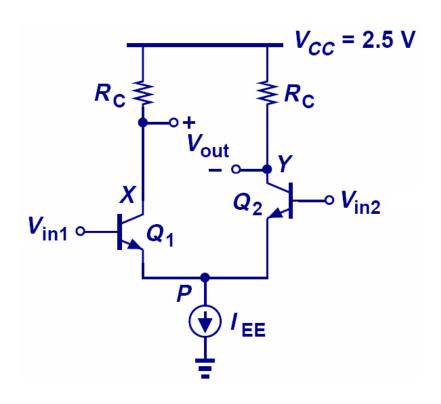


Differential Pair Characteristics



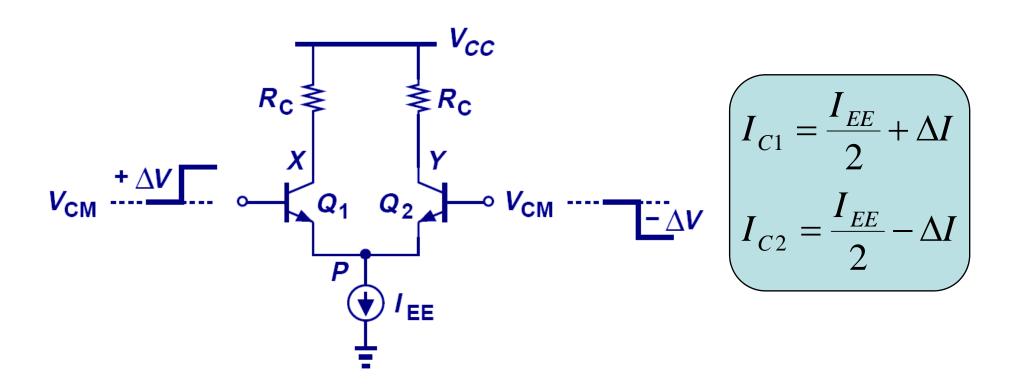
None-zero differential input produces variations in output currents and voltages, whereas common-mode input produces no variations.

 \triangleright A bipolar differential pair employs a tail current of 0.5 mA and a collector resistance of 1 kΩ. What is the maximum allowable base voltage if the differential input is large enough to completely steer the tail current? Assume V_{cc} =2.5V.



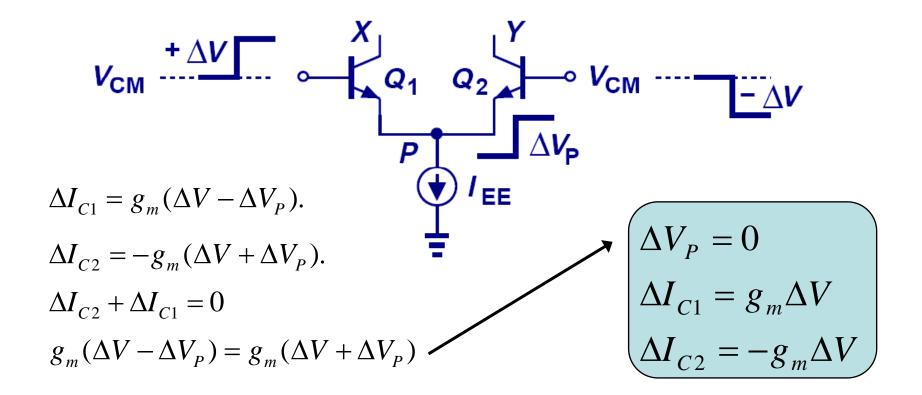
Because I_{EE} is completely steered, $V_{CC} - R_C I_{EE} = 2 \ V$ at one collector. To avoid saturation, $V_R \le 2 \ V$.

Small-Signal Analysis



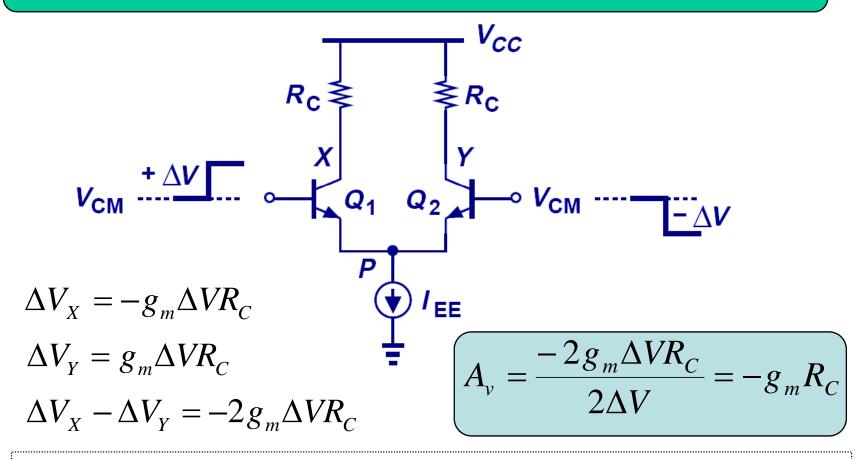
Since the input to Q_1 and Q_2 rises and falls by the same amount, and their bases are tied together, the rise in I_{C1} has the same magnitude as the fall in I_{C2} .

Virtual Ground



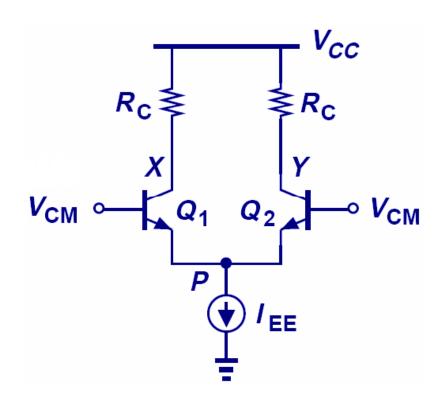
For small changes at inputs, the g_m's are the same, and the respective increase and decrease of l_{C1} and l_{C2} are the same, node P must stay constant to accommodate these changes. Therefore, node P can be viewed as AC ground.

Small-Signal Differential Gain



Since the output changes by $-2g_m\Delta VR_C$ and input by $2\Delta V$, the small signal gain is $-g_mR_C$, similar to that of the CE stage. However, to obtain same gain as the CE stage, power dissipation is doubled.

Design a bipolar differential pair for a gain of 10 and a power budget of 1mW with a supply voltage of 2V.



$$V_{CC} = 2 \text{ V}$$

$$\Rightarrow I_{EE} = \frac{1 \text{ mW}}{2 \text{ V}} = 0.5 \text{ mA}$$

$$\Rightarrow g_m = \frac{I_C}{V_T} = \frac{I_{EE}/2}{V_T} = \frac{0.25 \text{ mA}}{26 \text{ mV}} = \frac{1}{104 \Omega}$$

$$\Rightarrow R_C = \frac{|A_v|}{g_m} = 1040 \Omega$$

Compare the power dissipation of a bipolar differential pair with that of a CE stage if both circuits are designed for equal voltage gains, collector resistances, and supply voltages.

Differential pair

$$|A_{V,\text{diff}}| = g_{m1.2}R_C$$

CE stage

$$\mid A_{V,CE} \mid = g_m R_C$$

$$g_{m1,2}R_C = g_m R_C$$

$$I_{CC} I_C$$

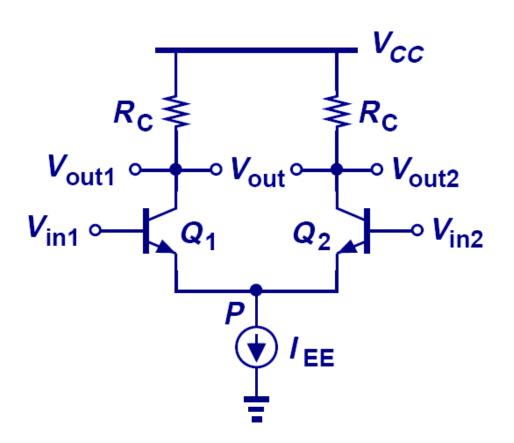
$$\frac{I_{EE}}{2V_T} = \frac{I_C}{V_T}$$

$$I_{EE} = 2I_C$$

$$P_{D,diff} = V_C I_{EE} = 2V_C I_C$$

$$P_{D,CE} = V_C I_C$$

Large Signal Analysis



$$V_{in1} - V_{in2} = V_{BE1} - V_{BE2}$$

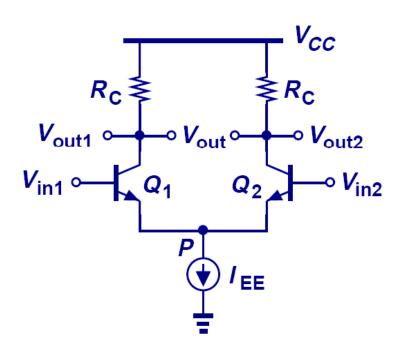
$$= V_T \ln \frac{I_{C1}}{I_{S1}} - V_T \ln \frac{I_{C2}}{I_{S2}}$$
and $I_{C1} + I_{C2} = I_{EE}$

$$\Rightarrow I_{C2} \exp \frac{V_{in1} - V_{in2}}{V_T} + I_{C2} = I_{EE}$$

$$\Rightarrow I_{C2} = \frac{I_{EE}}{1 + \exp \frac{V_{in1} - V_{in2}}{V_T}}$$

$$\Rightarrow I_{C1} = \frac{I_{EE} \exp \frac{V_{in1} - V_{in2}}{V_T}}{1 + \exp \frac{V_{in1} - V_{in2}}{V_T}}$$

➤ Determine the differential input voltage that steers 98% of the tail current to one transistor.



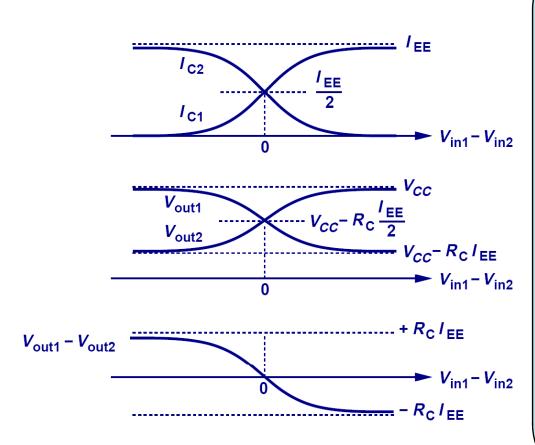
$$I_{C1} = 0.02I_{EE}$$

$$\approx I_{EE} \exp \frac{V_{in1} - V_{in2}}{V_{T}}$$

$$V_{in1} - V_{in2} \approx -3.91 \cdot V_T.$$

We often say a differential input of $4 \cdot V_T$ is sufficient to turn one side of the bipolar pair nearly off.

Input/Output Characteristics



$$V_{out1} = V_{CC} - R_C I_{C1}$$

$$= V_{CC} - R_C \frac{I_{EE} \exp \frac{V_{in1} - V_{in2}}{V_T}}{1 + \exp \frac{V_{in1} - V_{in2}}{V_T}}$$

$$V_{out2} = V_{CC} - R_C I_{C2}$$

$$= V_{CC} - R_C \frac{I_{EE}}{1 + \exp \frac{V_{in1} - V_{in2}}{V_T}}$$

$$V_{out1} - V_{out2} = R_C I_{EE} \frac{1 - \exp \frac{V_{in1} - V_{in2}}{V_T}}{1 + \exp \frac{V_{in1} - V_{in2}}{V_T}}$$

$$= -R_C I_{EE} \tanh \frac{V_{in1} - V_{in2}}{2 \cdot V_T}$$

Sketch the output waveforms of the bipolar differential pair in Fig. 10.14(a) in response to the sinusoidal inputs shown in Figs. 10.14(b) and (c). Assume Q_1 and Q_2 remain in the forward active region.

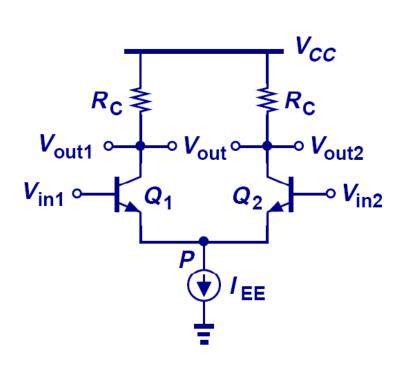
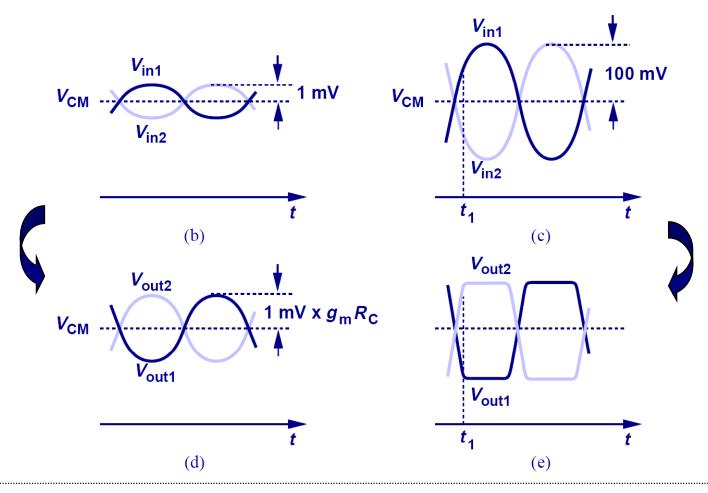


Figure 10.14 (a)

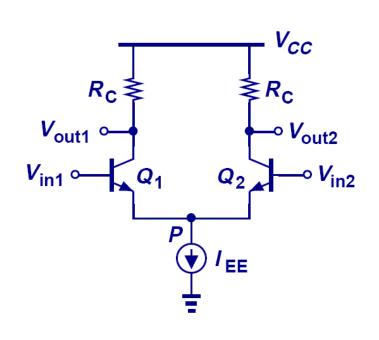
 $V_{\rm in1}$ 1 mV V_{in2} (b) $V_{\rm in1}$ 100 mV $V_{\rm in2}$ (c)

Example 10.9 (cont'd)



> The left column operates in linear region, whereas the right column operates in nonlinear region.

Small-Signal Model

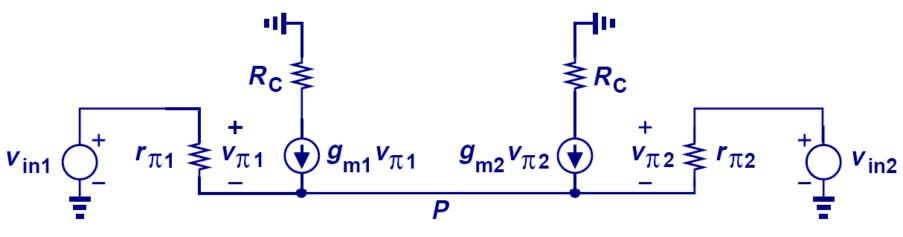


$$v_{in1} - v_{\pi 1} = v_P = v_{in2} - v_{\pi 2}$$

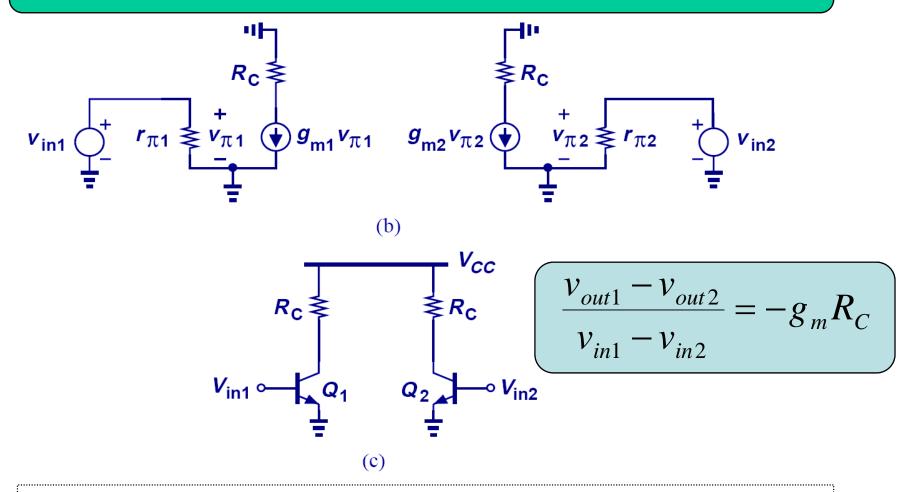
$$\frac{v_{\pi 1}}{r_{\pi 1}} + g_{m1}v_{\pi 1} + \frac{v_{\pi 2}}{r_{\pi 2}} + g_{m2}v_{\pi 2} = 0.$$

With
$$r_{\pi 1} = r_{\pi 2}$$
 and $g_{m1} = g_{m2}$ $v_{\pi 1} = -v_{\pi 2}$
Since $v_{in1} = -v_{in2}$, $2v_{in1} = 2v_{\pi 1}$.

$$\therefore v_P = v_{in1} - v_{\pi 1}$$
$$= 0$$



Half Circuits



Since V_P is grounded, we can treat the differential pair as two CE "half circuits", with its gain equal to one half circuit's single-ended gain.

Compute the differential gain of the circuit shown in Fig. 10.16(a), where ideal current sources are used as loads to maximize the gain.

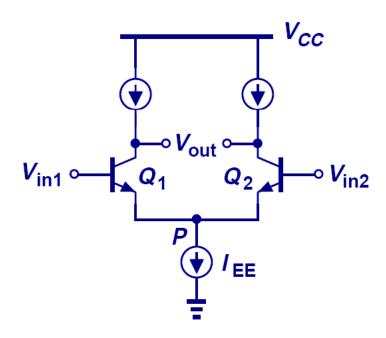
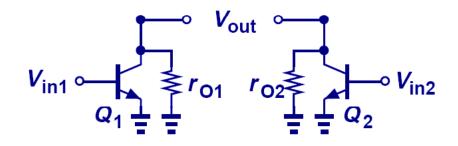
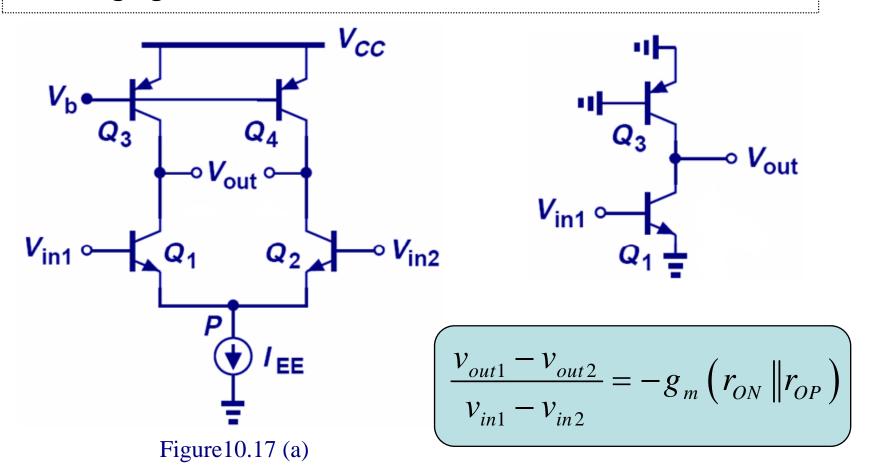


Figure 10.16 (a)



$$\frac{v_{out1} - v_{out2}}{v_{in1} - v_{in2}} = -g_m r_0$$

Figure 10.17(a) illustrates an implementation of the topology shown in Fig. 10.16(a). Calculate the differential voltage gain.



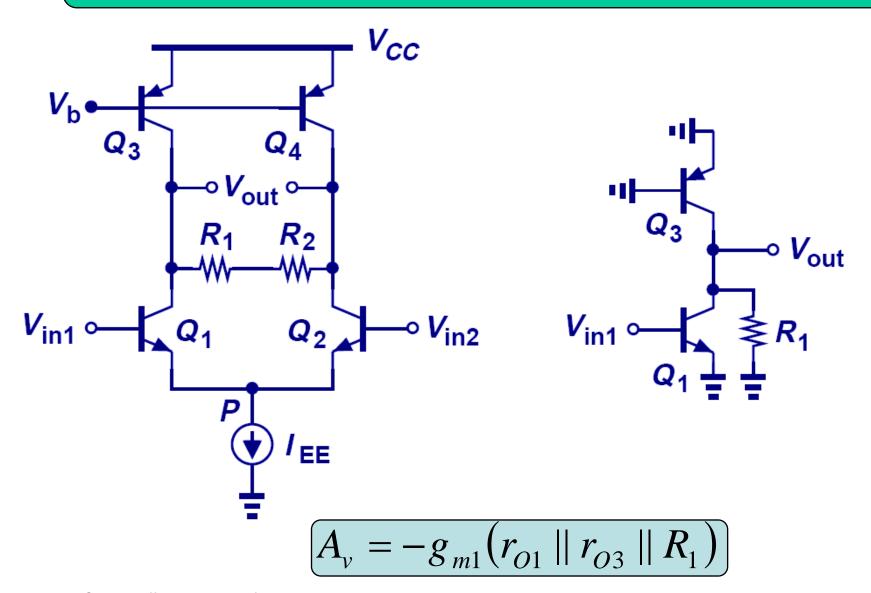
Extension of Virtual Ground

$$\int \Delta V A \sim \frac{R_1}{M} \frac{R_2}{X} \sim B \quad \Delta V$$

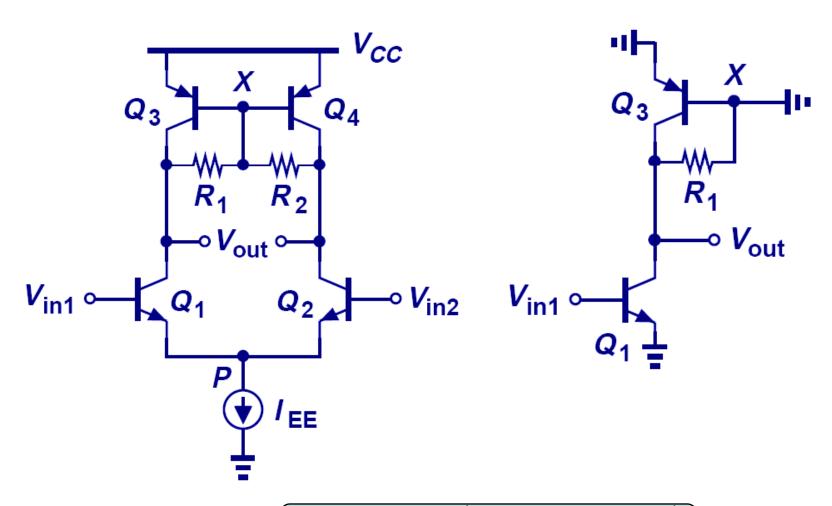
$$V_X = 0$$

It can be shown that if $R_1 = R_2$, and points A and B go up and down by the same amount respectively, V_X does not move. This property holds for any other node that appears on the axis of symmetry.

Half Circuit Example I

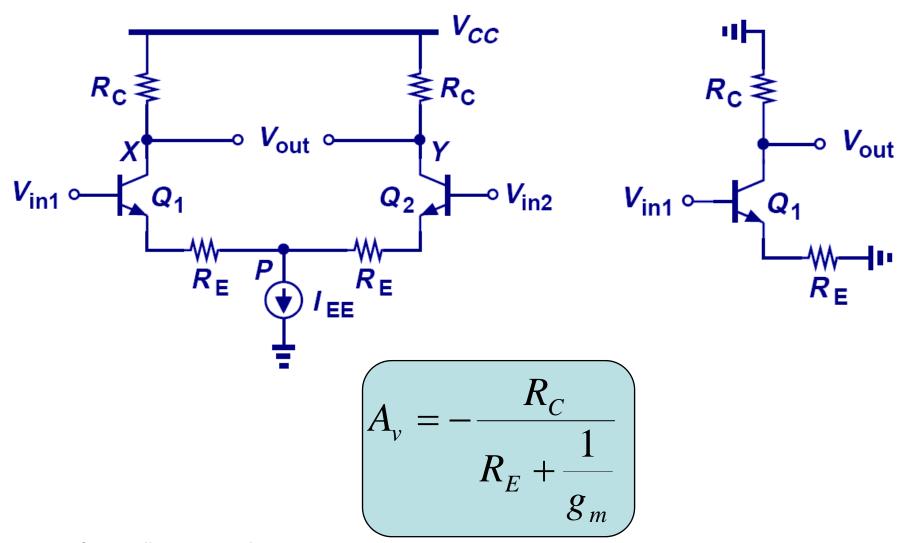


Half Circuit Example II

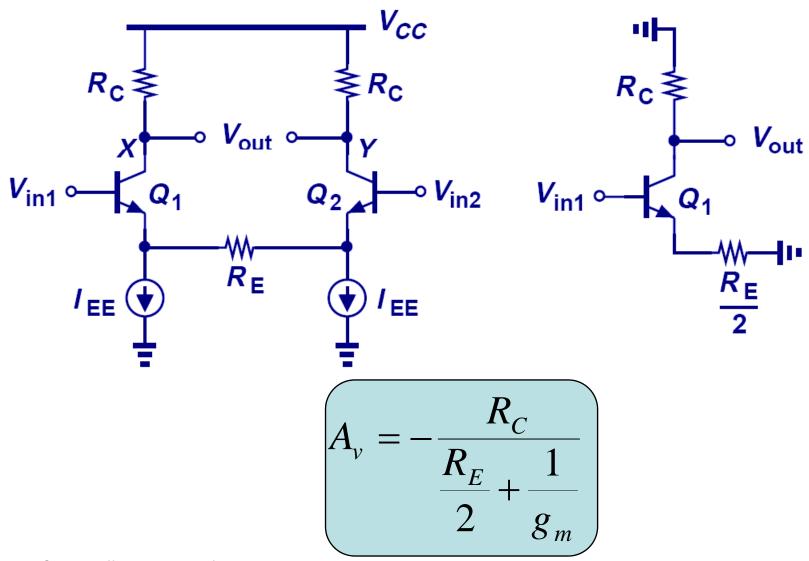


$$\left[A_{v} = -g_{m1}(r_{O1} || r_{O3} || R_{1})\right]$$

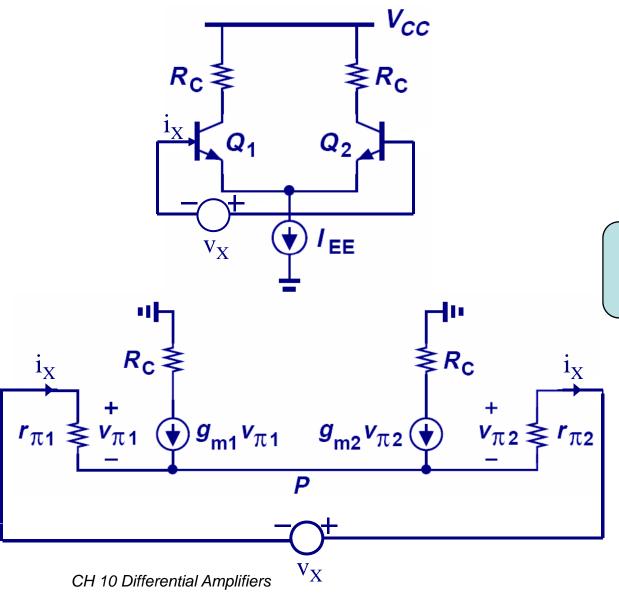
Half Circuit Example III



Half Circuit Example IV



I/O Impedances



$$\frac{v_{\pi 1}}{r_{\pi 1}} = i_X = -\frac{v_{\pi 2}}{r_{\pi 2}}$$

$$v_X = v_{\pi 1} - v_{\pi 2}$$

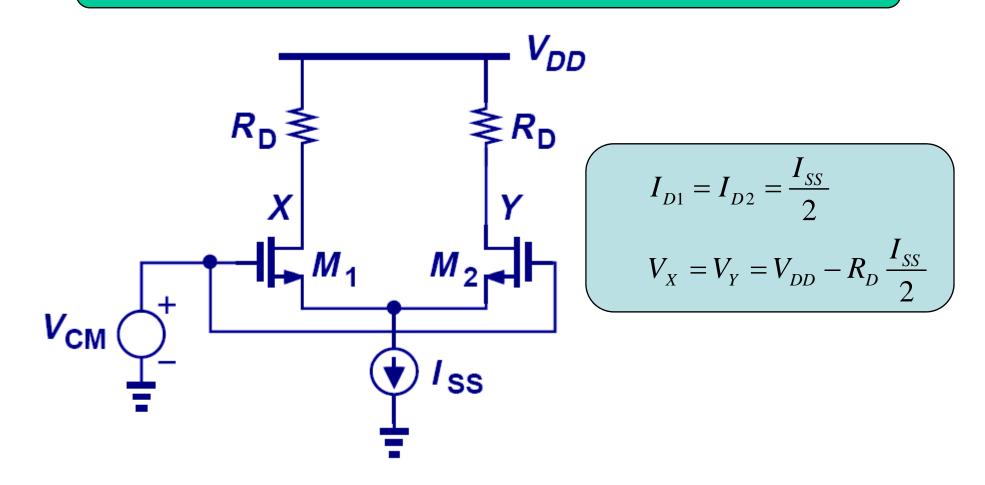
$$= 2r_{\pi 1}i_X$$

$$\Rightarrow R_{in} = \frac{v_X}{i_X} = 2r_{\pi 1}$$

In a similar manner,

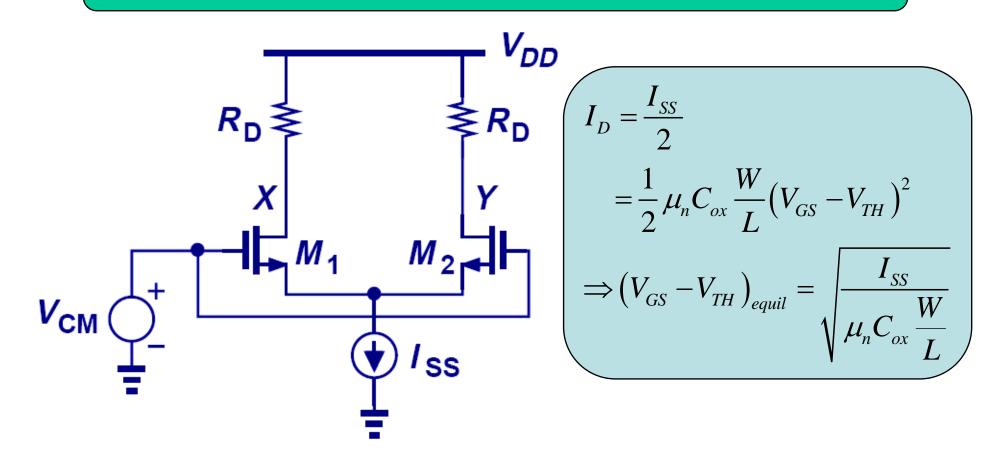
$$R_{out} = 2R_{c}$$

MOS Differential Pair's Common-Mode Response



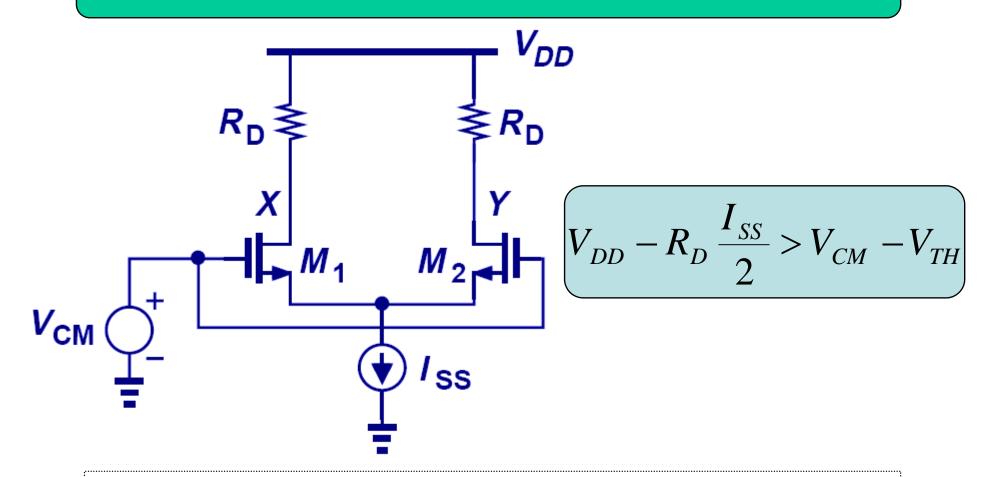
 \triangleright Similar to its bipolar counterpart, MOS differential pair produces zero differential output as V_{CM} changes.

Equilibrium Overdrive Voltage



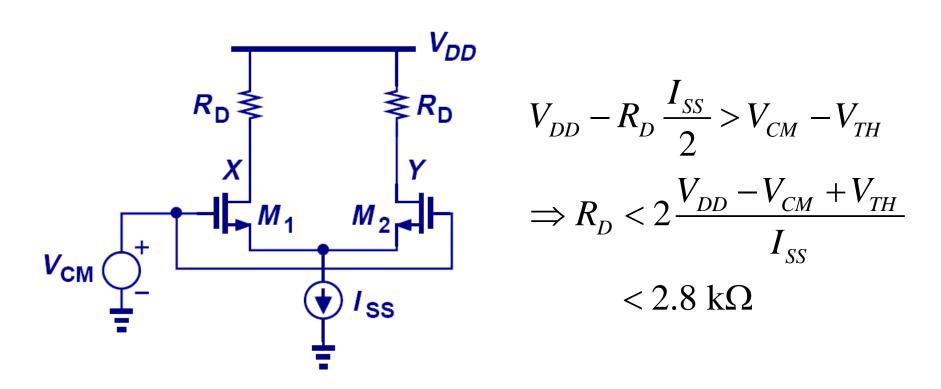
➤ The equilibrium overdrive voltage is defined as the overdrive voltage seen by M₁ and M₂ when both of them carry a current of I_{SS}/2.

Minimum Common-mode Output Voltage

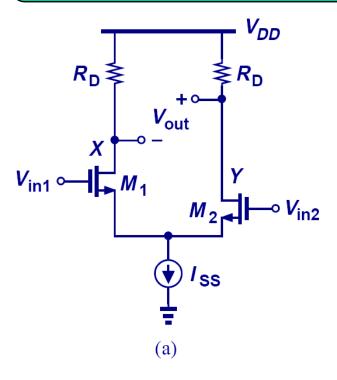


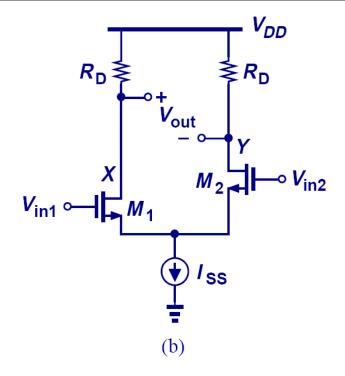
- \triangleright In order to maintain M_1 and M_2 in saturation, the common-mode output voltage cannot fall below the value above.
- This value usually limits voltage gain.

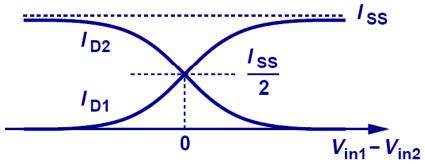
A MOS differential pair is driven with an input CM level of 1.6V. If I_{SS} =0.5mA, V_{TH} =0.5 V, and V_{DD} =1.8 V, what is the maximum allowable load resistance?

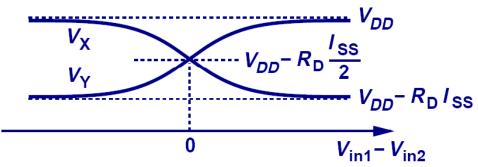


Differential Response



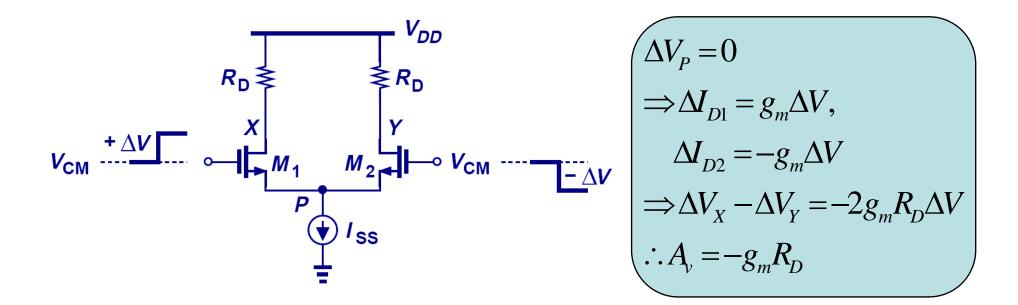






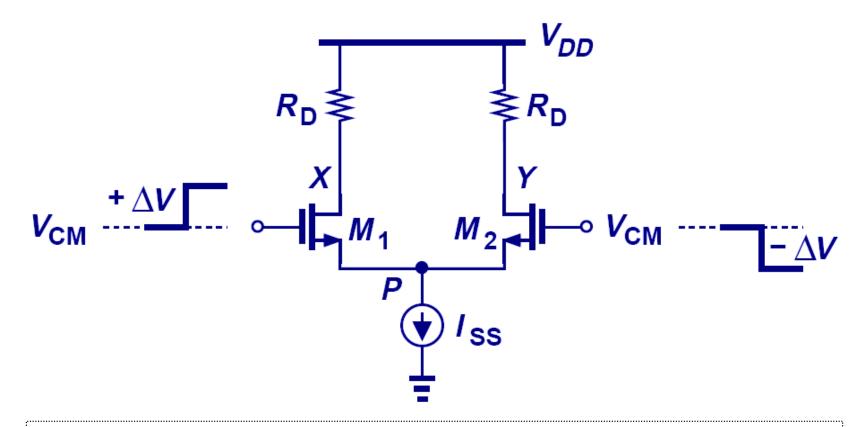
(c)

Small-Signal Response



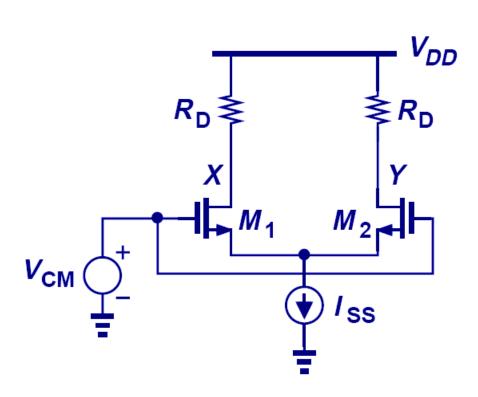
Similar to its bipolar counterpart, the MOS differential pair exhibits the same virtual ground node and small signal gain.

Power and Gain Tradeoff



In order to obtain the source gain as a CS stage, a MOS differential pair must dissipate twice the amount of current. This power and gain tradeoff is also echoed in its bipolar counterpart.

Posign an NMOS differential pair for a voltage gain of 5 and a power budget of 2 mW subject to the condition that the stage following the differential pair requires an input CM level of at least 1.6V. Assume $\mu_n C_{ox}$ =100 μA/V², λ =0, and V_{DD} = 1.8 V.



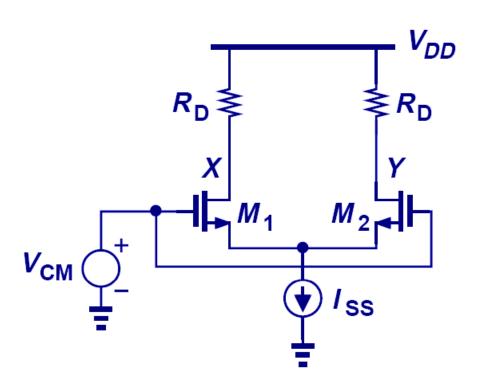
$$I_{SS} = \frac{2 \text{ mW}}{1.8 \text{ V}} = 1.11 \text{ mA}$$

$$R_{D} \qquad V_{CM,out} = V_{DD} - R_{D} \frac{I_{SS}}{2} \ge 1.6 \text{ V}$$

$$\Rightarrow R_{D} \le 360 \Omega$$
For $R_{D} = 360 \Omega$,
$$g_{m} = \frac{A_{v}}{R_{D}} = \frac{5}{360 \Omega} = \sqrt{2\mu_{n}C_{ox} \frac{W}{L} \frac{I_{SS}}{2}}$$

$$\Rightarrow \frac{W}{L} = 1738$$

What is the maximum allowable input CM level in the previous example if V_{TH} =0.4 V?



To guarantee that M_1 and M_2 operate in saturation,

$$\begin{split} V_{CM,in} < V_{DD} - R_D \, \frac{I_{SS}}{2} + V_{TH} \\ < V_{CM,out} + V_{TH} \, . \end{split}$$

Thus,

$$V_{CM,in} < 2 \text{ V}$$

The common-source stage and the differential pair shown in Fig. 10.28 incorporate equal load resistors. If the two circuits are designed for the same voltage gain and the same supply voltage, discuss the choice of (a) transistor dimensions for a given power budget, (b) power dissipation for given transistor dimensions.

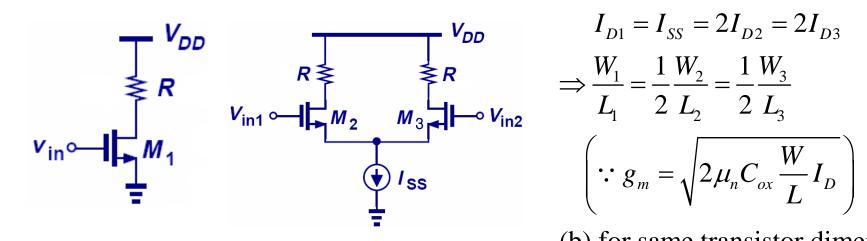


Figure 10.28

(a) for same power budget,

$$I_{D1} = I_{SS} = 2I_{D2} = 2I_{D3}$$

$$\Rightarrow \frac{W_1}{L_1} = \frac{1}{2} \frac{W_2}{L_2} = \frac{1}{2} \frac{W_3}{L_3}$$

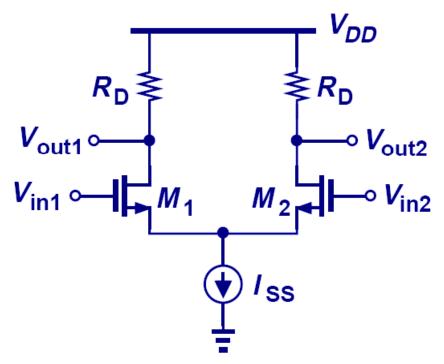
$$\left(\because g_m = \sqrt{2\mu_n C_{ox} \frac{W}{L} I_D}\right)$$

(b) for same transistor dimensions,

$$I_{SS} = 2I_{D1}$$

$$\Rightarrow P_{diff} = 2P_{CS}$$

MOS Differential Pair's Large-Signal Response



Goal is to obtain I_{D1} - I_{D2}

$$V_{in1} - V_{GS1} = V_{in2} - V_{GS2}.$$

$$I_{D1} + I_{D2} = I_{SS}.$$

$$I_{D} = (1/2)\mu_{n}C_{ox}(W/L)(V_{GS} - V_{TH})^{2}.$$

$$\Rightarrow V_{GS} = V_{TH} + \sqrt{\frac{2I_{D}}{\mu_{n}C_{ox}}\frac{W}{L}}.$$

$$\Rightarrow V_{in1} - V_{in2} = V_{GS1} - V_{GS2}$$

$$= \sqrt{\frac{2}{\mu_n C_{ox} \frac{W}{L}}} (\sqrt{I_{D1}} - \sqrt{I_{D2}}).$$

MOS Differential Pair's Large-Signal Response (cont'd)

$$(V_{in1} - V_{in2})^{2} = \frac{2}{\mu_{n} C_{ox}} \frac{W}{L} (I_{D1} + I_{D2} - 2\sqrt{I_{D1}I_{D2}})$$

$$= \frac{2}{\mu_{n} C_{ox}} \frac{W}{L} (I_{SS} - 2\sqrt{I_{D1}I_{D2}}).$$

$$\Rightarrow 4\sqrt{I_{D1}I_{D2}} = 2I_{SS} - \mu_{n} C_{ox} \frac{W}{L} (V_{in1} - V_{in2})^{2}$$

$$\Rightarrow 16I_{D1}I_{D2} = \left[2I_{SS} - \mu_{n} C_{ox} \frac{W}{L} (V_{in1} - V_{in2})^{2}\right]^{2}$$

$$\Rightarrow 16I_{D1}(I_{SS} - I_{D1}) = \left[2I_{SS} - \mu_{n} C_{ox} \frac{W}{L} (V_{in1} - V_{in2})^{2}\right]^{2}$$

MOS Differential Pair's Large-Signal Response (cont'd)

$$\Rightarrow 16I_{D1}^{2} - 16I_{SS}I_{D1} + \left[2I_{SS} - \mu_{n}C_{ox}\frac{W}{L}(V_{in} - V_{in2})^{2}\right]^{2} = 0$$

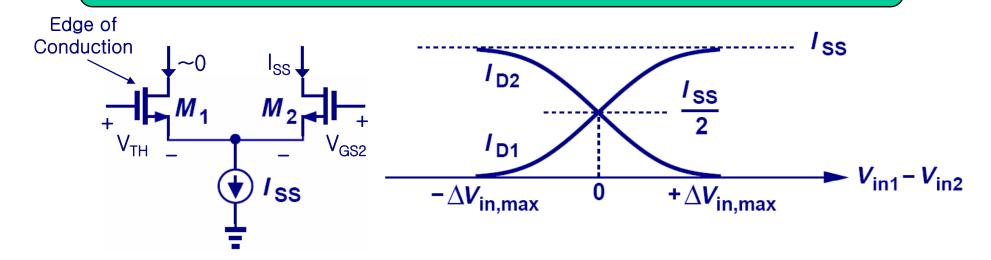
$$\Rightarrow I_{D1} = \frac{I_{SS}}{2} \pm \frac{1}{4}\sqrt{4I_{SS}^{2} - \left[\mu_{n}C_{ox}\frac{W}{L}(V_{in1} - V_{in2})^{2} - 2I_{SS}\right]^{2}}$$

$$= \frac{I_{SS}}{2} + \frac{V_{in1} - V_{in2}}{4}\sqrt{\mu_{n}C_{ox}\frac{W}{L}\left[4I_{SS} - \mu_{n}C_{ox}\frac{W}{L}(V_{in1} - V_{in2})^{2}\right]}$$

$$\Rightarrow I_{D2} = \frac{I_{SS}}{2} + \frac{V_{in2} - V_{in1}}{4}\sqrt{\mu_{n}C_{ox}\frac{W}{L}\left[4I_{SS} - \mu_{n}C_{ox}\frac{W}{L}(V_{in2} - V_{in1})^{2}\right]}$$
(:: the symmetry of the circuit)

$$\left(I_{D1} - I_{D2} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in1} - V_{in2}) \sqrt{\frac{4I_{SS}}{\mu_n C_{ox} \frac{W}{L}} - (V_{in1} - V_{in2})^2}\right)$$

Maximum Differential Input Voltage



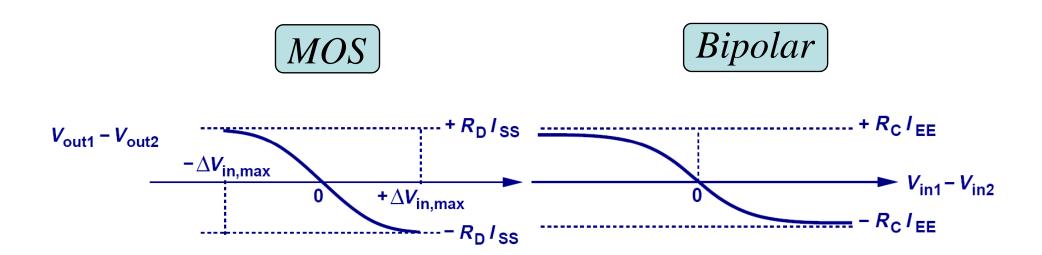
$$V_{GS1} = V_{TH}$$

$$V_{GS2} = V_{TH} + \sqrt{\frac{2I_{SS}}{\mu_n C_{ox} \frac{W}{L}}}$$

$$\left| |V_{in1} - V_{in2}|_{\text{max}} = \sqrt{\frac{2I_{SS}}{\mu_n C_{ox} \frac{W}{L}}} = \sqrt{2} \left(V_{GS} - V_{TH} \right)_{equil}$$

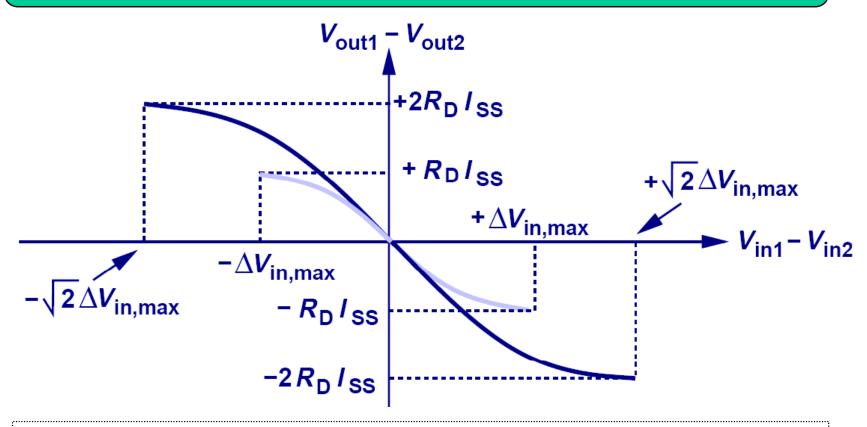
There exists a finite differential input voltage that completely steers the tail current from one transistor to the other. This value is known as the maximum differential input voltage.

Contrast Between MOS and Bipolar Differential Pairs



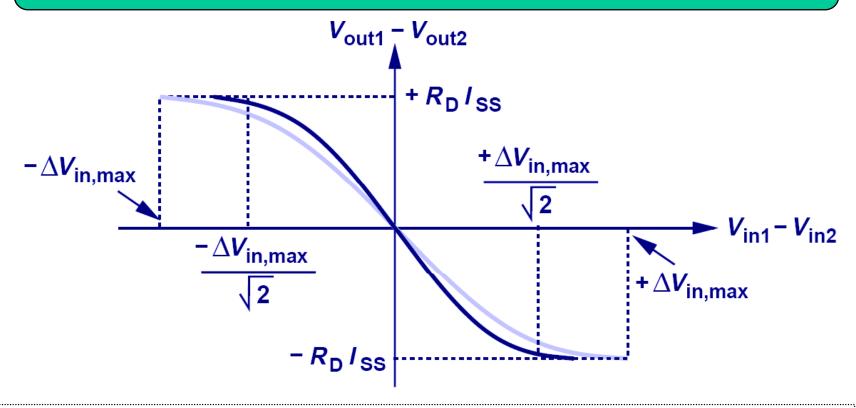
In a MOS differential pair, there exists a finite differential input voltage to completely switch the current from one transistor to the other, whereas, in a bipolar pair that voltage is infinite.

The effects of Doubling the Tail Current



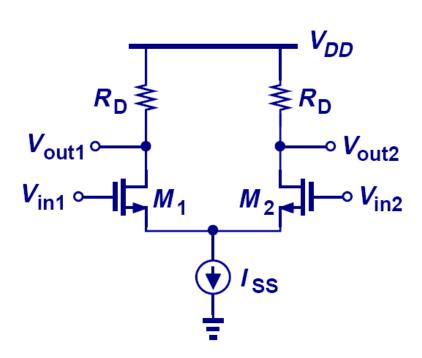
Since I_{SS} is doubled and W/L is unchanged, the equilibrium overdrive voltage for each transistor must increase by $\sqrt{2}$ to accommodate this change, thus $\Delta V_{in,max}$ increases by $\sqrt{2}$ as well. Moreover, since I_{SS} is doubled, the differential output swing will double.

The effects of Doubling W/L



Since W/L is doubled and the tail current remains unchanged, the equilibrium overdrive voltage will be lowered by $\sqrt{2}$ to accommodate this change, thus $\Delta V_{in,max}$ will be lowered by as well. Moreover, the differential output swing will remain unchanged since neither I_{SS} nor R_D has changed

Design an NMOS differential pair for a power budget of 3 mW and $\Delta V_{in,max}$ =500 mV. Assume $\mu_n C_{ox}$ =100 μ A/V² and V_{DD} =1.8 V.



$$I_{SS} = \frac{3 \text{ mW}}{1.8 \text{ V}} = 1.67 \text{ mA}$$

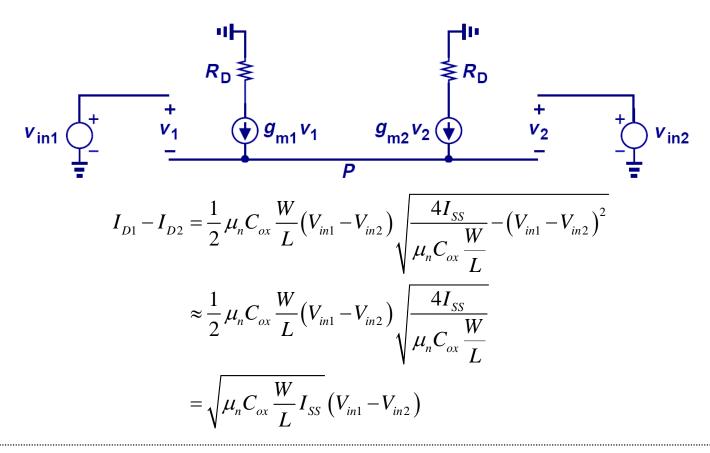
$$V_{DD}$$
 $I_{SS} = \frac{3 \text{ mW}}{1.8 \text{ V}} = 1.67 \text{ mA}$

$$R_{D}$$
From $|V_{in1} - V_{in2}|_{\text{max}} = \sqrt{\frac{2I_{SS}}{\mu_n C_{ox} \frac{W}{L}}}$

$$\frac{W}{L} = \frac{2I_{SS}}{\mu_n C_{ox} \Delta V_{in, max}^2} = 133.6$$

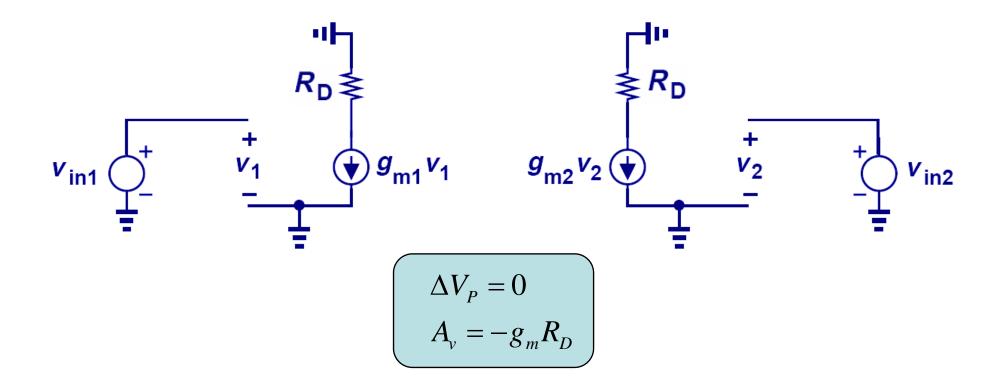
 R_D is determined by the required voltage gain.

Small-Signal Analysis of MOS Differential Pair



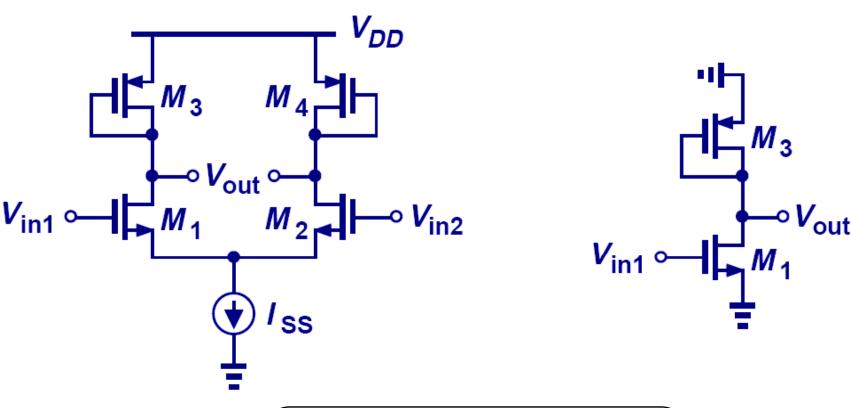
When the input differential signal is small compared to $[4I_{SS}/\mu_nC_{ox}(W/L)]^{1/2}$, the output differential current is linearly proportional to it, and small-signal model can be applied.

Virtual Ground and Half Circuit



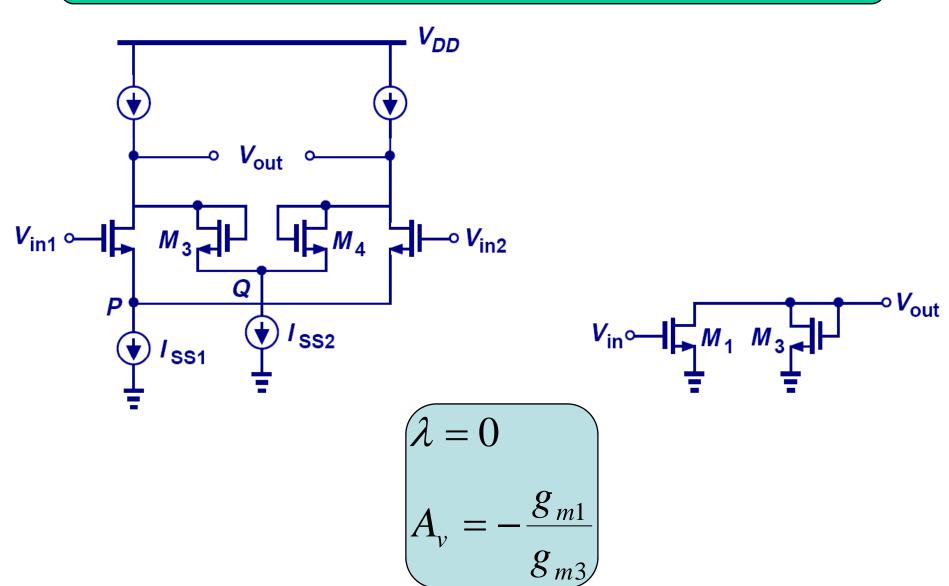
Applying the same analysis as the bipolar case, we will arrive at the same conclusion that node P will not move for small input signals and the concept of half circuit can be used to calculate the gain.

MOS Differential Pair Half Circuit Example I



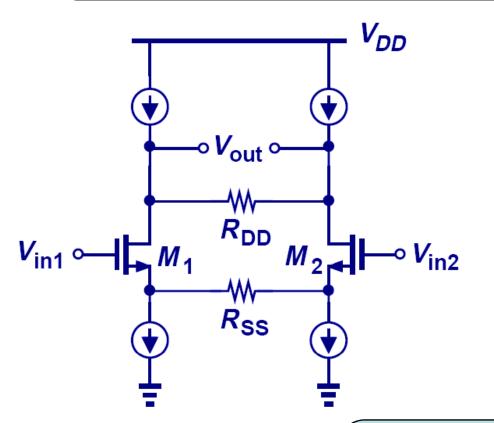
$$\left(\begin{array}{c} \lambda \neq 0 \\ A_{v} = -g_{m1} \left(\frac{1}{g_{m3}} \parallel r_{O3} \parallel r_{O1} \right) \end{array} \right)$$

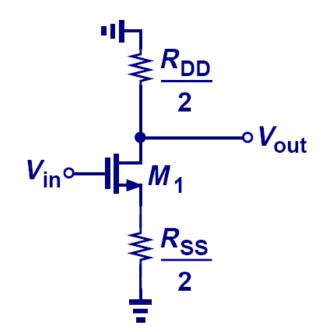
MOS Differential Pair Half Circuit Example II



CH 10 Differential Amplifiers

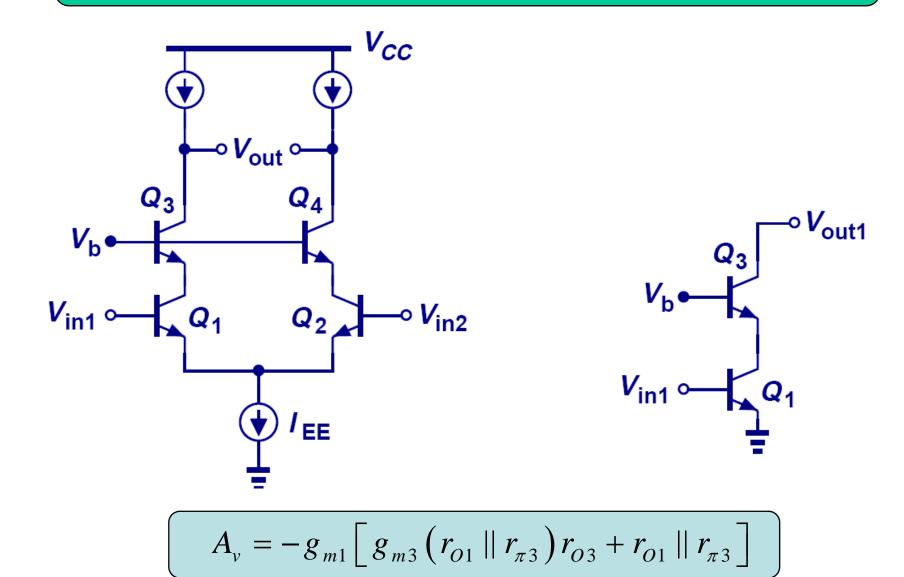
MOS Differential Pair Half Circuit Example III



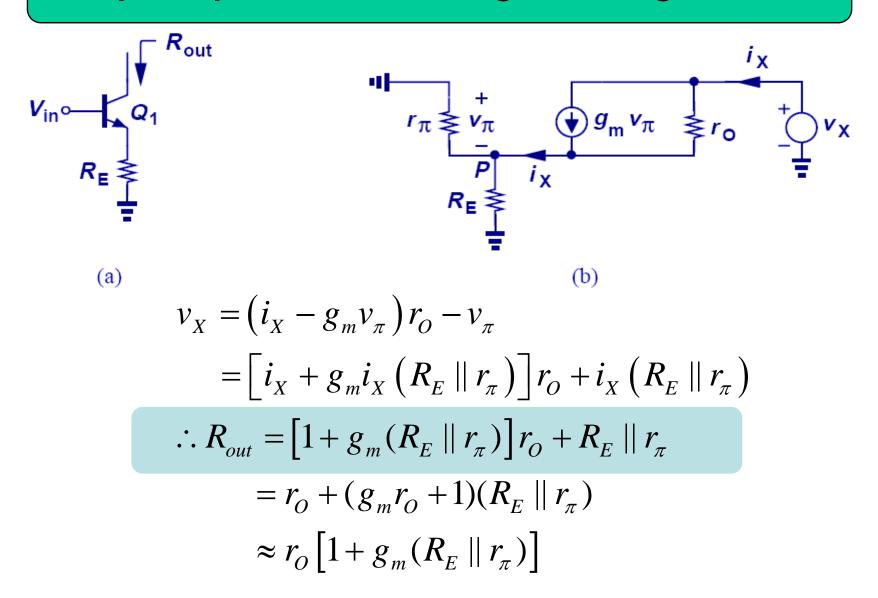


$$\begin{pmatrix} \lambda = 0 \\ A_{v} = -\frac{R_{DD}/2}{R_{SS}/2 + 1/g_{m}} \end{pmatrix}$$

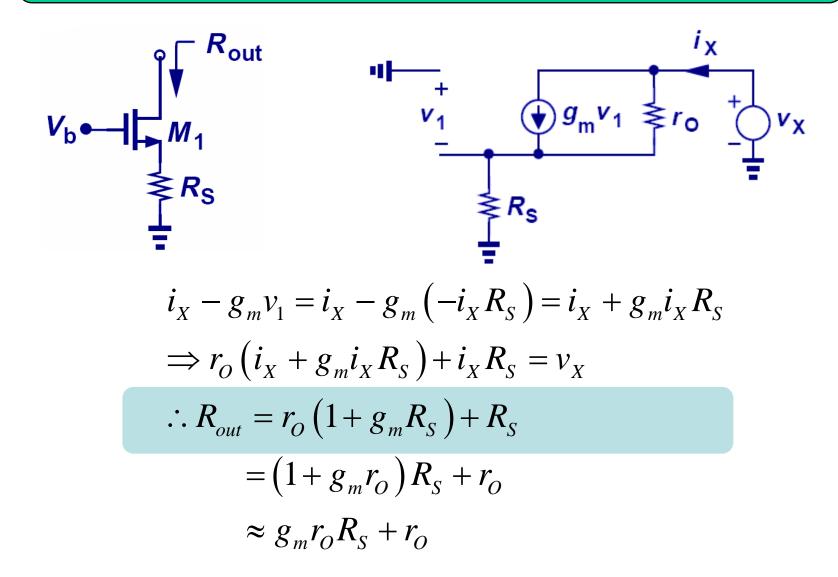
Bipolar Cascode Differential Pair



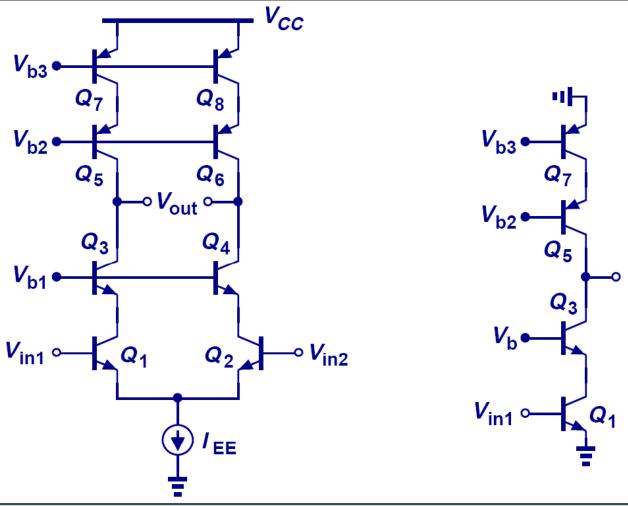
Output Impedance of CE Stage with Degeneration



Output Impedance of CS Stage with Degeneration

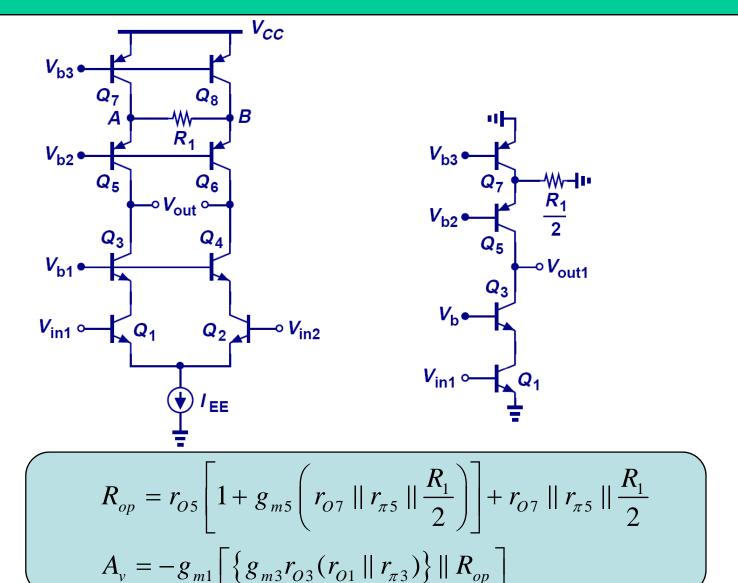


Bipolar Telescopic Cascode

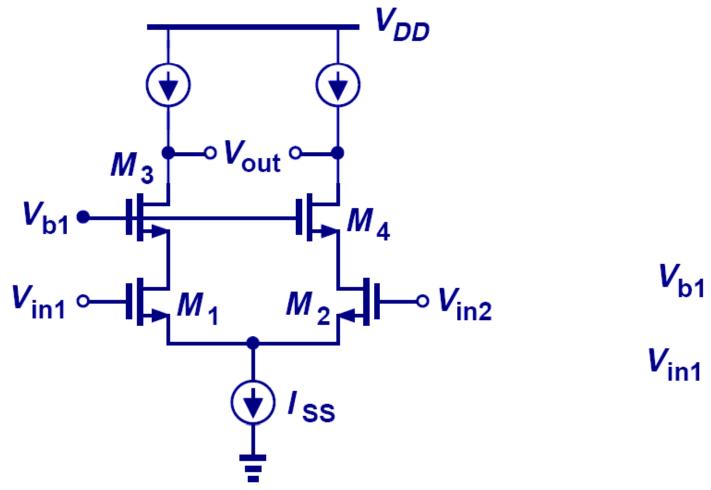


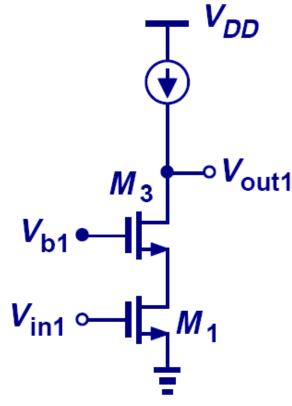
$$A_{v} \approx -g_{m1}[g_{m3}r_{O3}(r_{O1} || r_{\pi3})] || [g_{m5}r_{O5}(r_{O7} || r_{\pi5})]$$

Example: Bipolar Telescopic Parasitic Resistance



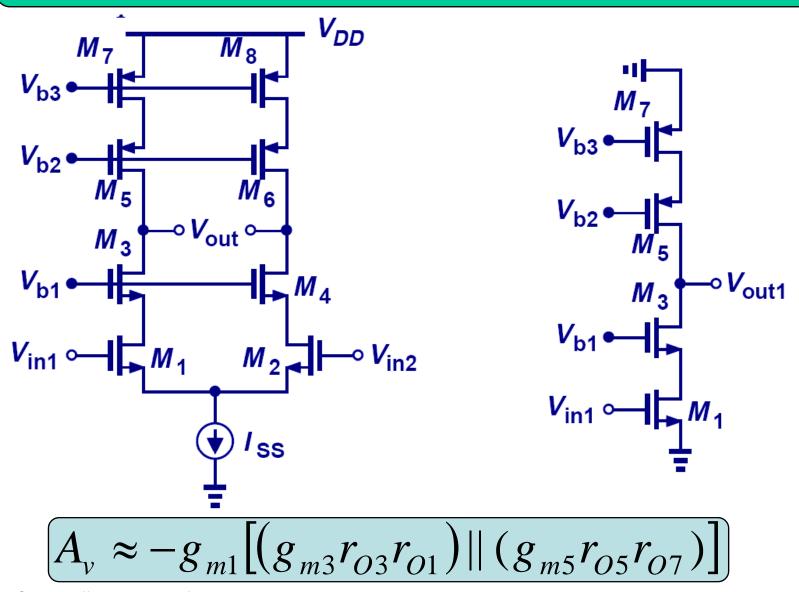
MOS Cascode Differential Pair



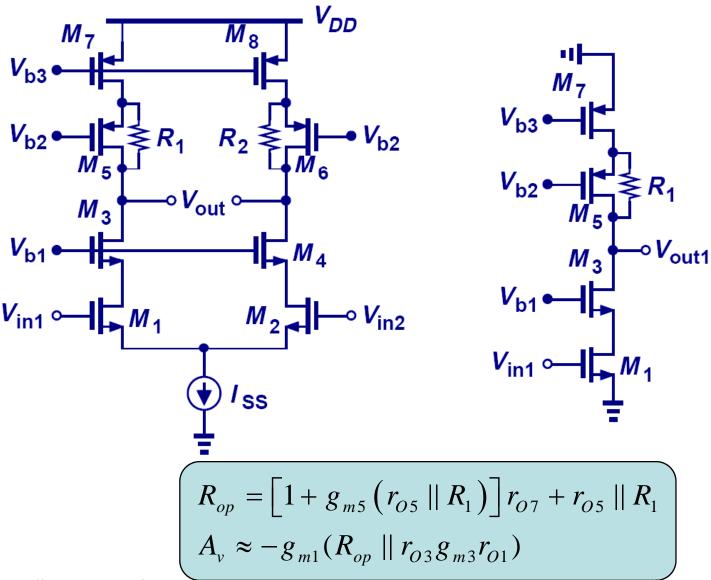


$$\left[A_{v} \approx -g_{m1}r_{O3}g_{m3}r_{O1}\right]$$

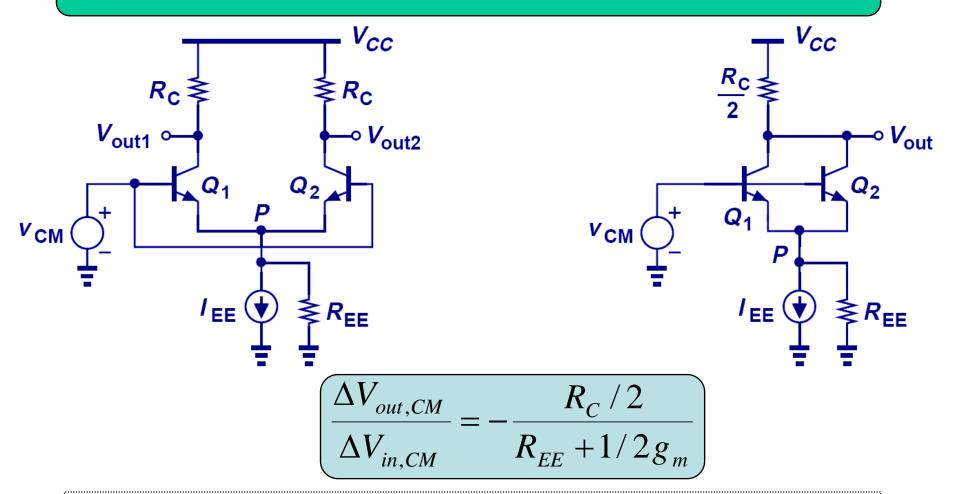
MOS Telescopic Cascode



Example: MOS Telescopic Parasitic Resistance

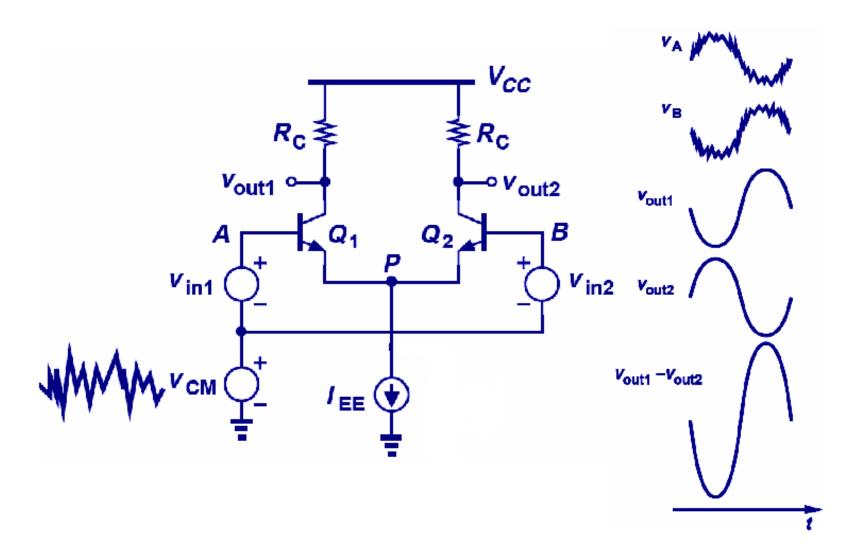


Effect of Finite Tail Impedance

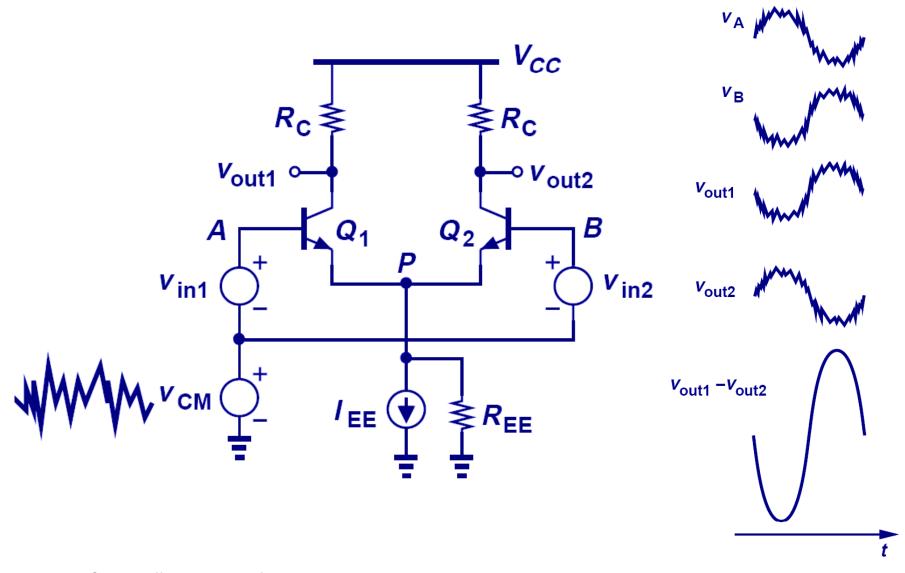


▶ If the tail current source is not ideal, then when a input CM voltage is applied, the currents in Q₁ and Q₂ and hence output CM voltage will change.

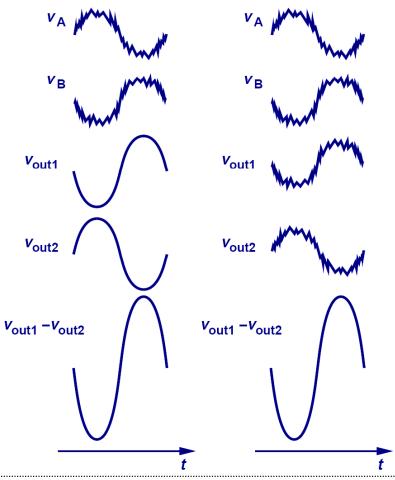
Input CM Noise with Ideal Tail Current



Input CM Noise with Non-ideal Tail Current

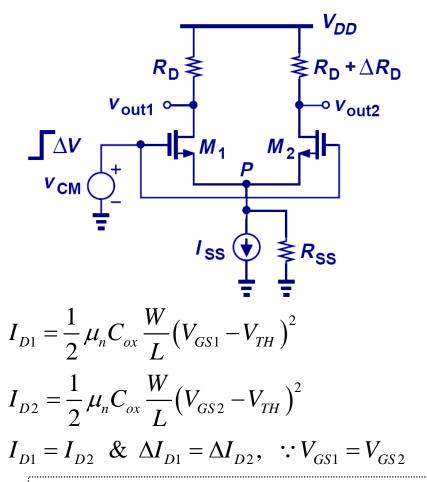


Comparison



As it can be seen, the differential output voltages for both cases are the same. So for small input CM noise, the differential pair is not affected.

CM to DM Conversion, A_{CM-DM}



$$\Delta V_{CM} = \Delta V_{GS} + 2\Delta I_D R_{SS}$$

$$= \Delta I_D \left(\frac{1}{g_m} + 2R_{SS} \right), \quad \because \Delta V_{GS} = \frac{\Delta I_D}{g_m}$$

$$\Rightarrow \Delta I_D = \frac{\Delta V_{CM}}{\frac{1}{g_m} + 2R_{SS}}$$

$$\therefore \Delta V_{out} = \Delta V_{out1} - \Delta V_{out2}$$

$$= \Delta I_D R_D - \Delta I_D (R_D + \Delta R_D)$$

$$= -\Delta I_D \Delta R_D$$

$$= \frac{\Delta V_{CM}}{1/g_m + 2R_{SS}} \Delta R_D$$

$$\Rightarrow \Delta I_D = \frac{\Delta V_{CM}}{\frac{1}{g_m} + 2R_{SS}} \Delta R_D$$

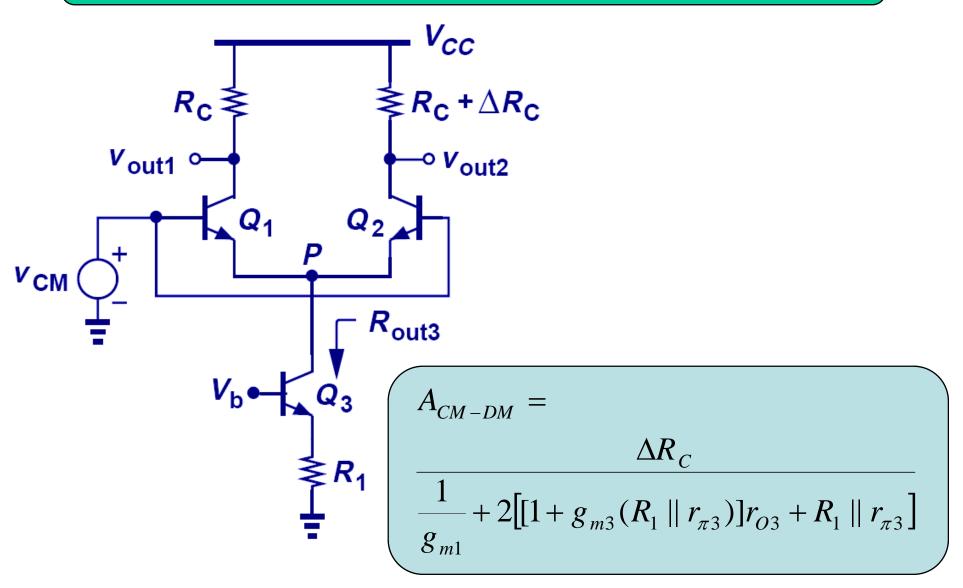
$$\Rightarrow \Delta I_D = \frac{\Delta V_{CM}}{\frac{1}{g_m} + 2R_{SS}} \Delta R_D$$

$$\Rightarrow \Delta I_D = \frac{\Delta V_{CM}}{\frac{1}{g_m} + 2R_{SS}} \Delta R_D$$

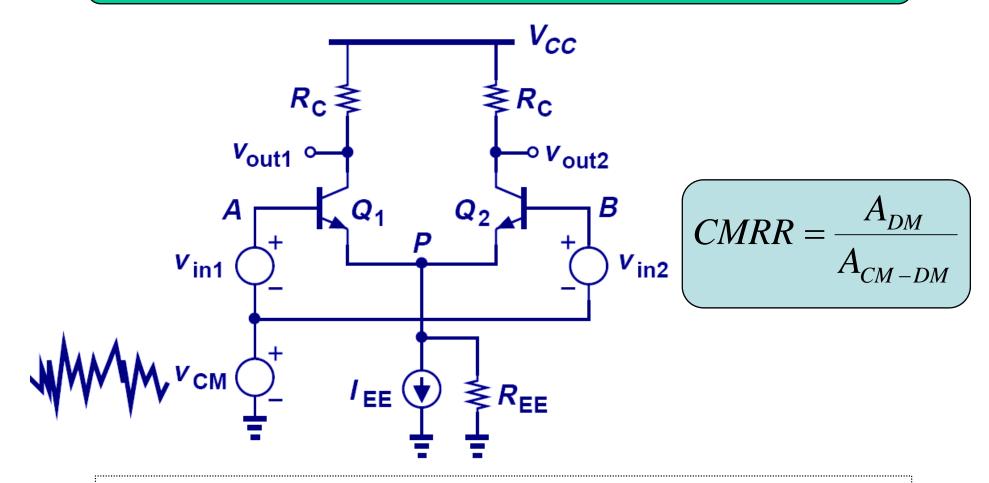
$$\Rightarrow \Delta I_D = \frac{\Delta V_{CM}}{\frac{1}{g_m} + 2R_{SS}} \Delta R_D$$

➤ If finite tail impedance and asymmetry are both present, then the differential output signal will contain a portion of input common-mode signal.

Example: A_{CM-DM}



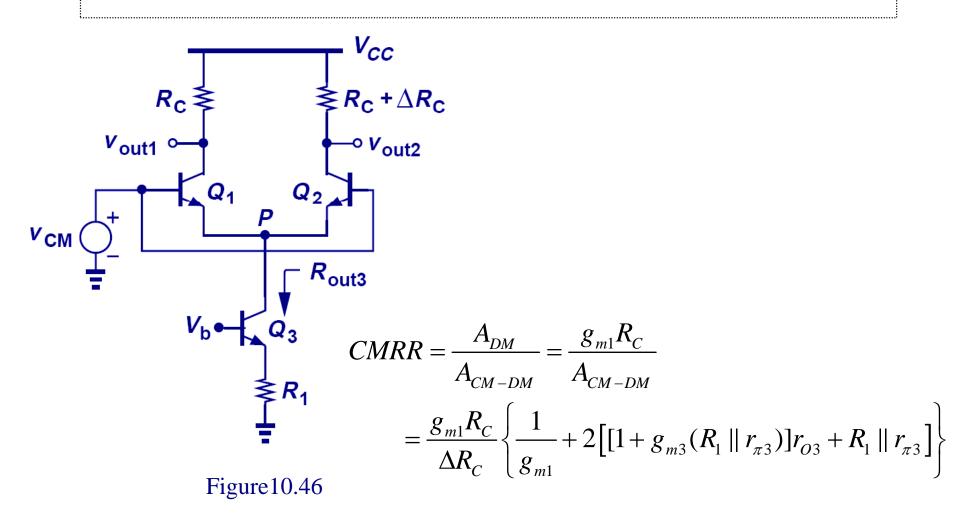
CMRR



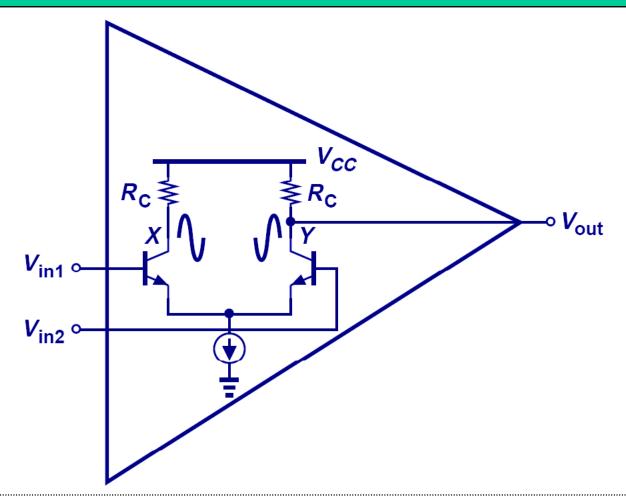
CMRR defines the ratio of wanted amplified differential input signal to unwanted converted input common-mode noise that appears at the output.

Example 10.28

Calculate the CMRR of the circuit in Fig. 10.46.

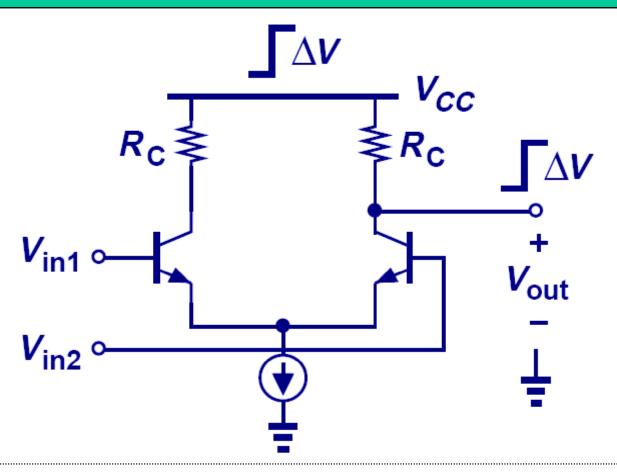


Differential to Single-ended Conversion



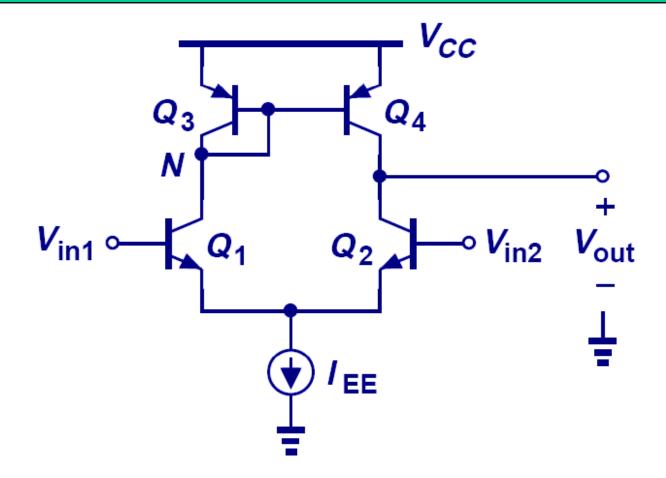
Many circuits require a differential to single-ended conversion, however, the above topology is not very good.

Supply Noise Corruption



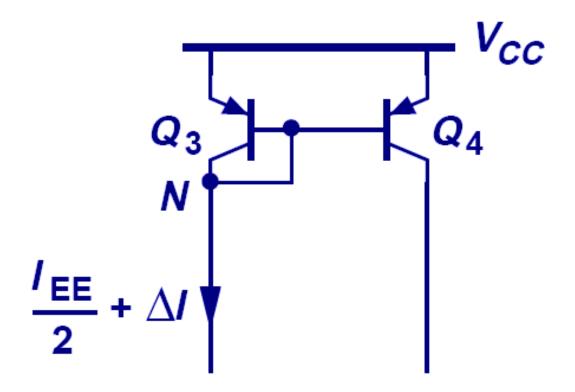
➤ The most critical drawback of this topology is supply noise corruption, since no common-mode cancellation mechanism exists. Also, we lose half of the signal.

Better Alternative



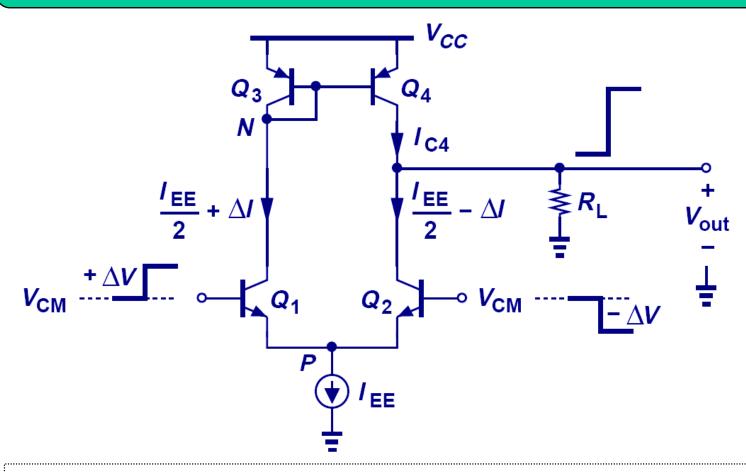
> This circuit topology performs differential to single-ended conversion with no loss of gain.

Active Load



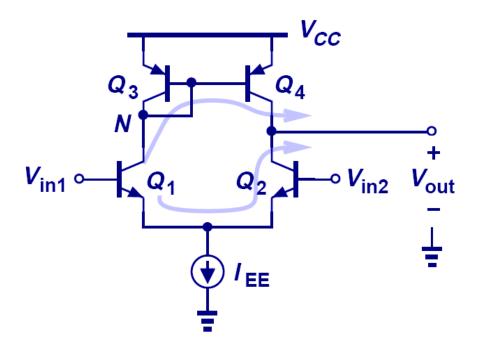
- With current mirror used as the load, the signal current produced by the Q_1 can be replicated onto Q_4 .
- ➤ This type of load is different from the conventional "static load" and is known as an "active load".

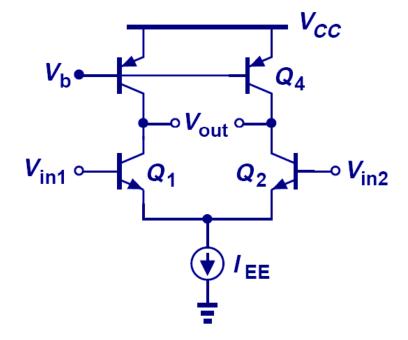
Differential Pair with Active Load



The input differential pair decreases the current drawn from R_L by ΔI and the active load pushes an extra ΔI into R_L by current mirror action; these effects enhance each other.

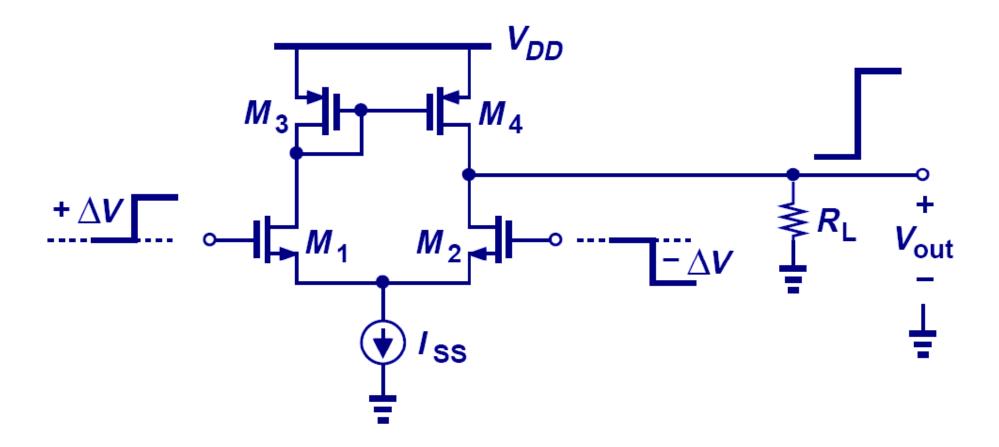
Active Load vs. Static Load





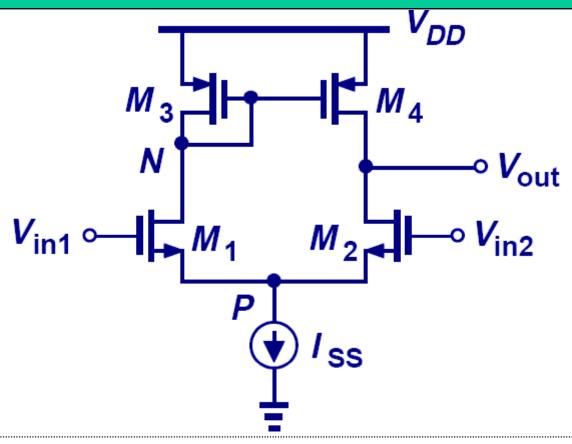
➤ The load on the left responds to the input signal and enhances the single-ended output, whereas the load on the right does not.

MOS Differential Pair with Active Load



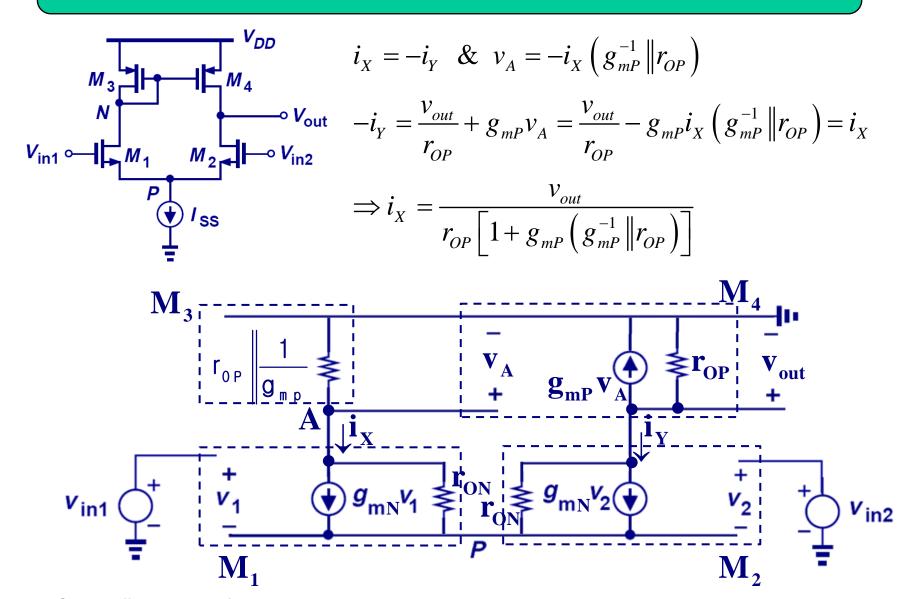
➤ Similar to its bipolar counterpart, MOS differential pair can also use active load to enhance its single-ended output.

Asymmetric Differential Pair



➤ Because of the vastly different resistance magnitude at the drains of M₁ and M₂, the voltage swings at these two nodes are different and therefore node P cannot be viewed as a virtual ground.

Quantitative Analysis - Approach 1



Quantitative Analysis - Approach 1 - cont'd

$$-v_{A} + (i_{X} - g_{mN}v_{1})r_{ON} - (i_{Y} - g_{mN}v_{2})r_{ON} + v_{out} = 0$$

$$\Rightarrow -v_{A} + 2i_{X}r_{ON} - g_{mN}r_{ON}(v_{in1} - v_{in2}) + v_{out} = 0$$

$$\therefore v_{1} - v_{2} = v_{in1} - v_{in2} \quad \& \quad i_{X} = -i_{Y}$$

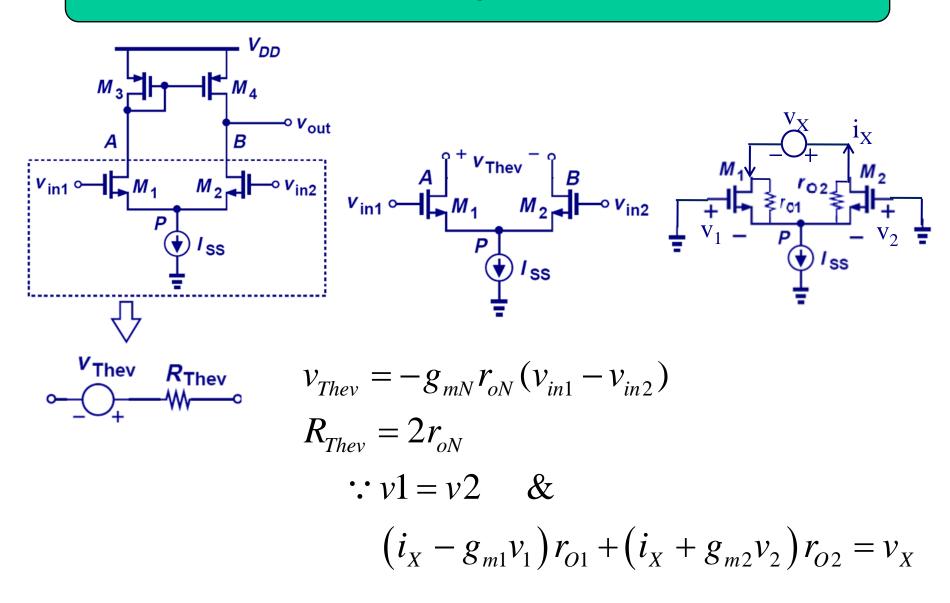
Substituting for v_A and i_X ,

$$\frac{v_{out}}{r_{OP} \left[1 + g_{mP} \left(g_{mP}^{-1} \| r_{OP}\right)\right]} \left(g_{mP}^{-1} \| r_{OP}\right) + 2r_{ON} \frac{v_{out}}{r_{OP} \left[1 + g_{mP} \left(g_{mP}^{-1} \| r_{OP}\right)\right]} + v_{out} = g_{mN} r_{ON} \left(v_{in1} - v_{in2}\right)$$

$$\Rightarrow \frac{v_{out}}{v_{in1} - v_{in2}} = g_{mN} r_{ON} \frac{r_{OP} \left[1 + g_{mP} \left(g_{mP}^{-1} \| r_{OP}\right)\right]}{2r_{ON} + 2r_{OP}}$$

$$\approx g_{mN} \left(r_{ON} \| r_{OP}\right)$$

Quantitative Analysis - Approach 2

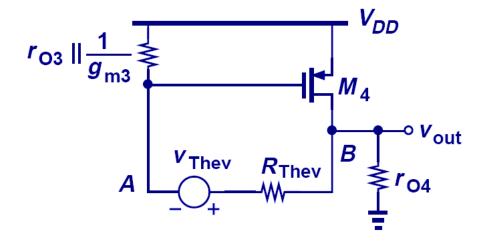


Quantitative Analysis - Approach 2 - cont'd

$$v_{A} = \frac{\frac{1}{g_{m3}} \| r_{O3}}{\frac{1}{g_{m3}} \| r_{O3} + R_{Thev}} (v_{out} + v_{Thev})$$

$$r_{O3} \| \frac{1}{g_{m3}} \| r_{O3} + R_{Thev} \| r_{O3} \| \frac{1}{g_{m3}} \| r_{O3} \| r_{O3} \| \frac{1}{g_{m3}} \| r_{O3} \|$$

$$g_{m4}v_A + \frac{v_{out}}{r_{O4}} + \frac{v_{out} + v_{Thev}}{\frac{1}{g_{m3}}} = 0$$



$$\Rightarrow \left(\frac{1}{g_{m3}} \| r_{O3} + \frac{1}{\frac{1}{g_{m3}}} \| r_{O3} + \frac{1}{\frac{1}{g_{m3}}} \| r_{O3} + R_{Thev} + \frac{1}{\frac{1}{g_{m3}}} \| r_{O3} + R_{Thev} \right) + \frac{v_{out}}{r_{O4}} = 0$$

$$\Rightarrow \frac{2}{R_{Thev}} (v_{out} + v_{Thev}) + \frac{v_{out}}{r_{O4}} = 0$$

$$\Rightarrow v_{out} \left(\frac{1}{r_{ON}} + \frac{1}{r_{OP}}\right) = \frac{g_{mN} r_{ON} (v_{in1} - v_{in2})}{r_{ON}}$$

$$\Rightarrow \frac{v_{out}}{v_{out}} = g_{mN} (r_{ON} \| r_{OP})$$

Example 10.29

Prove that the voltage swing at node A is much less than that at the output.

