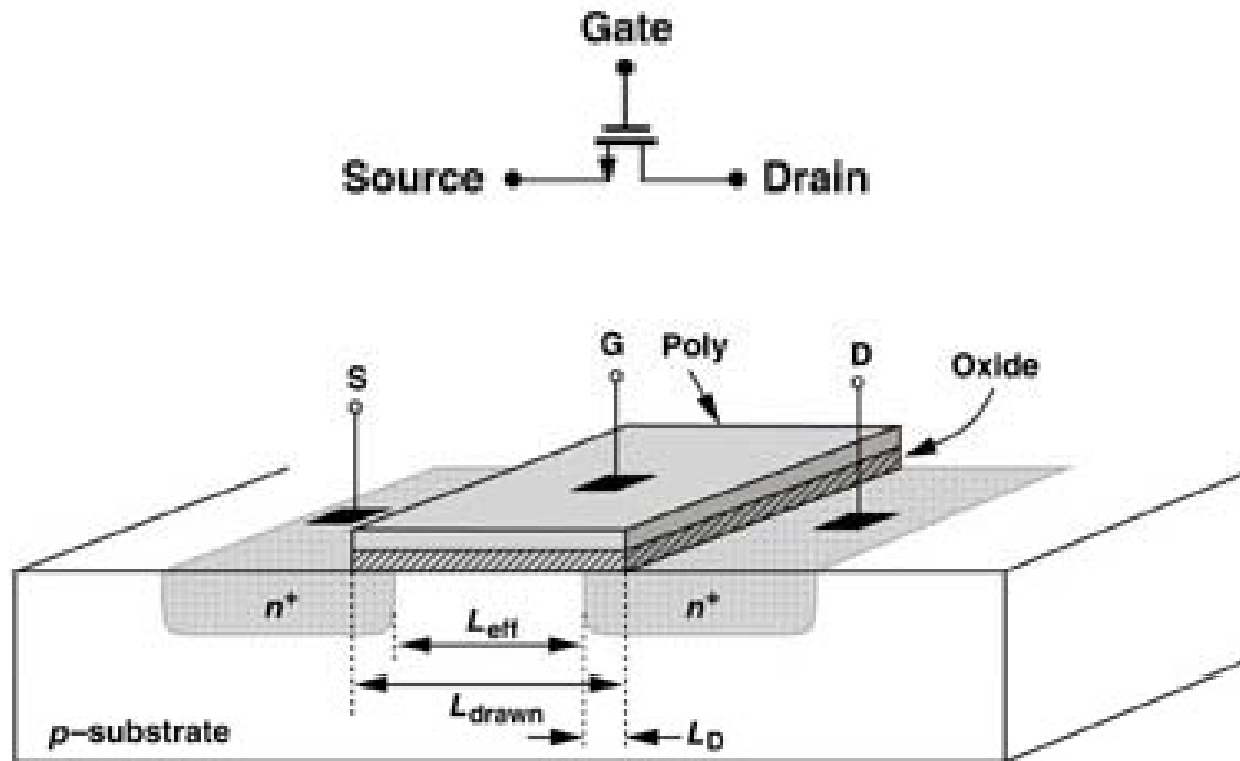


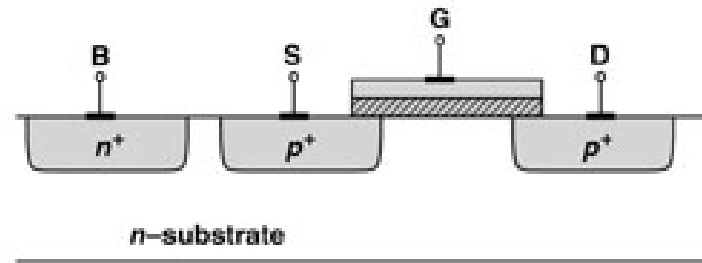
Chapter 2

Basic MOS Device Physics

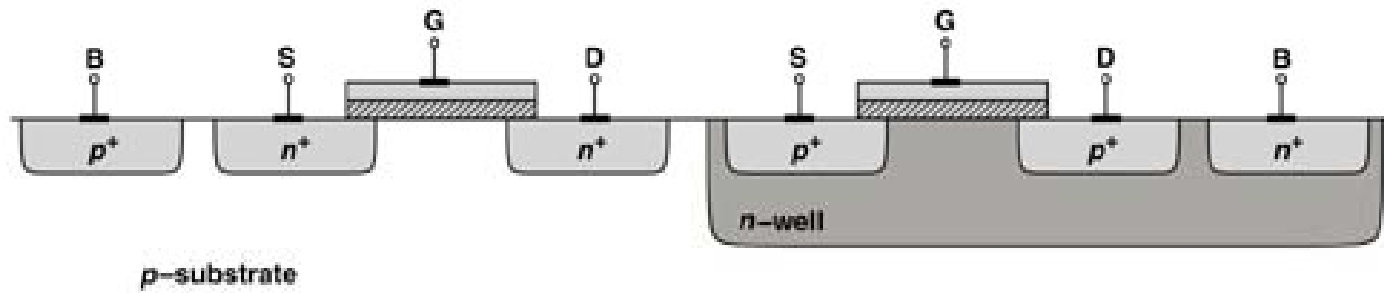
MOS Device Structure



NMOS and PMOS with Well

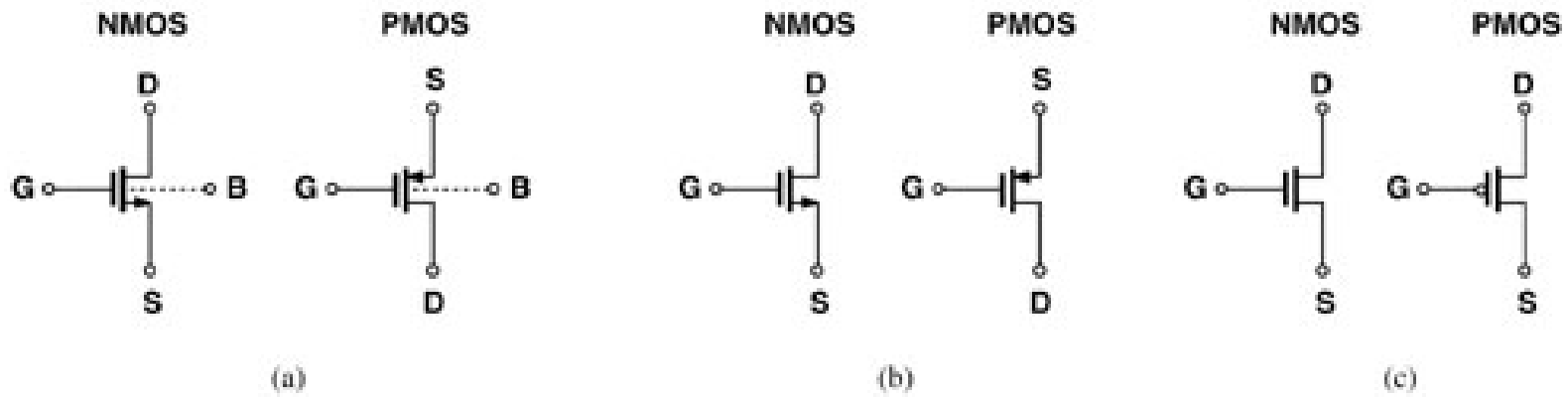


(a)

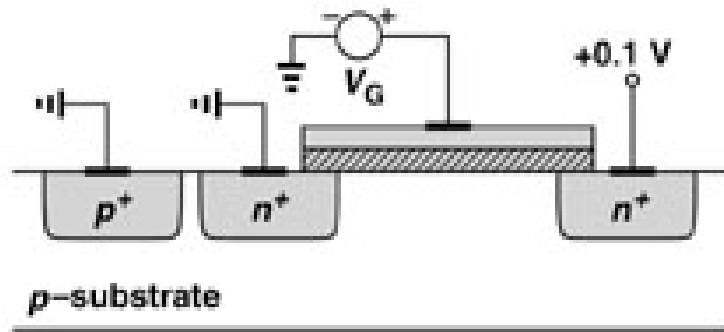


(b)

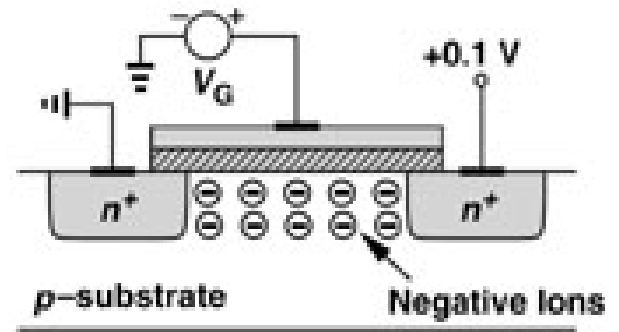
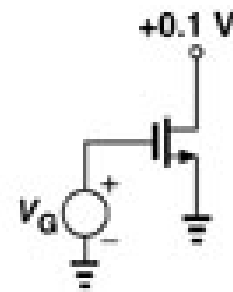
MOS Symbols



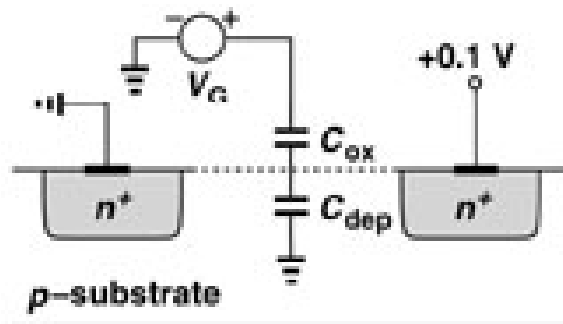
MOS Channel Formation



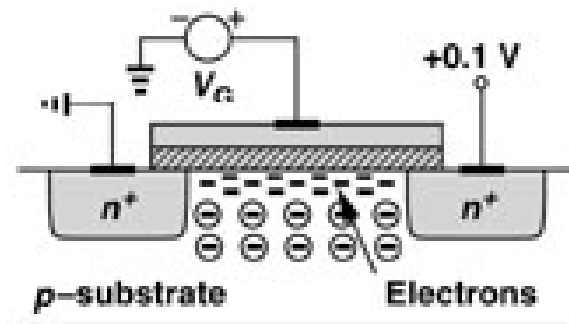
(a)



(b)

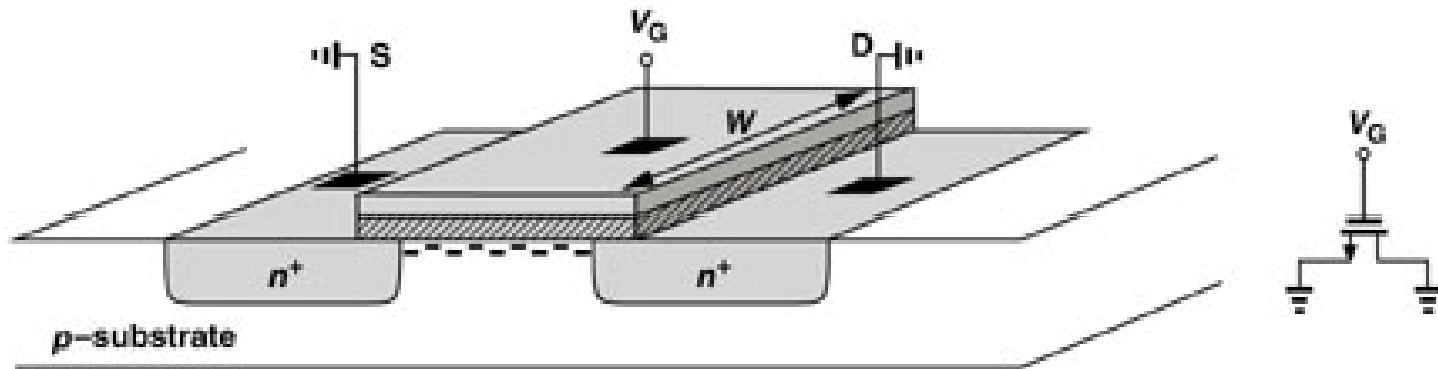


(c)

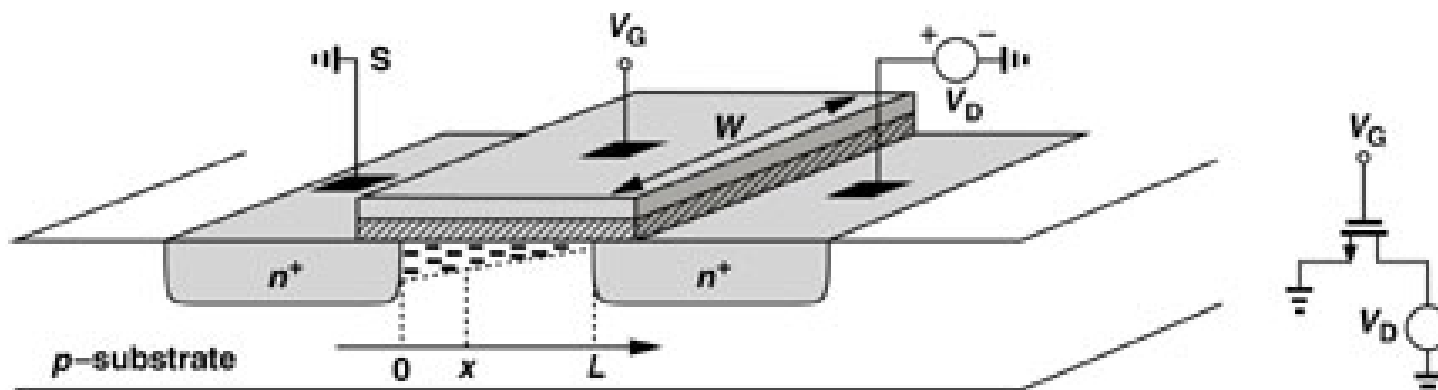


(d)

I/V Characteristics

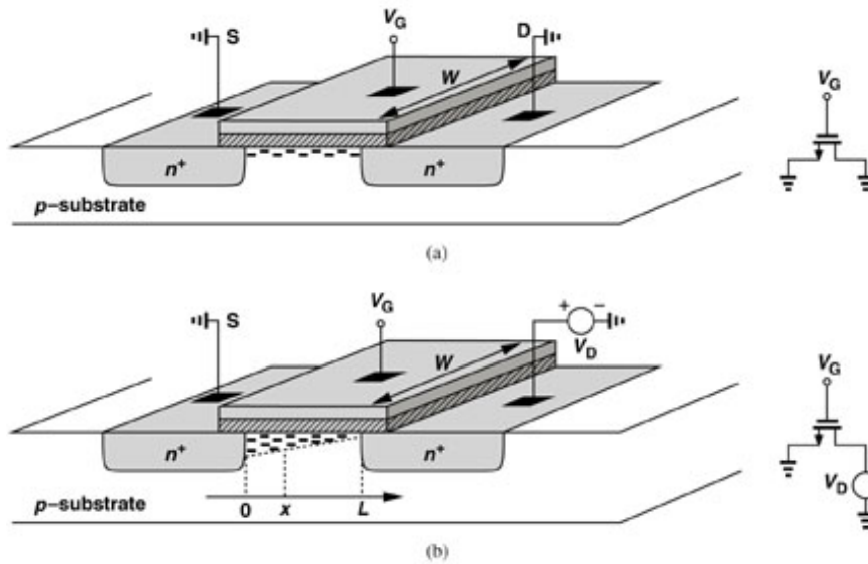


(a)



(b)

I/V Characteristics



$$I = Q_d \cdot v$$

$$Q_d = WC_{ox}(V_{GS} - V_{TH})$$

$$Q_d(x) = WC_{ox}(V_{GS} - V(x) - V_{TH})$$

I/V Characteristics (cont.)

$$I_D = -WC_{ox}[V_{GS} - V(x) - V_{TH}]v$$

Given $v = \mu E$ and $E(x) = -\frac{dV(x)}{dx}$

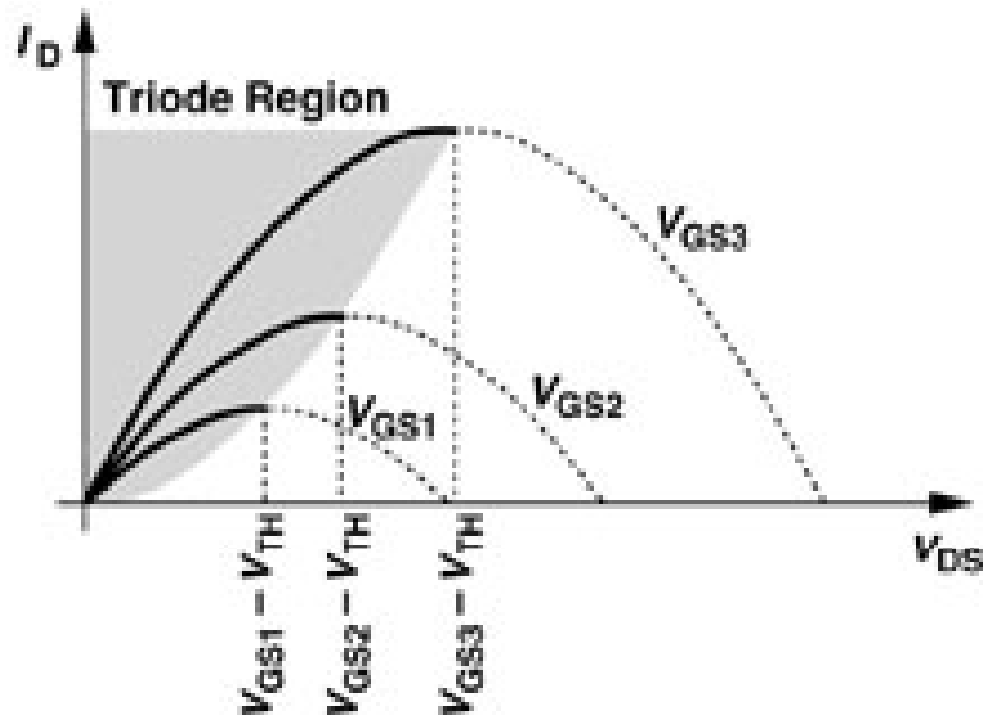
$$I_D = WC_{ox}[V_{GS} - V(x) - V_{TH}]\mu_n \frac{dV(x)}{dx}$$

$$\int_{x=0}^L I_D dx = \int_{V=0}^{V_{DS}} WC_{ox}\mu_n [V_{GS} - V(x) - V_{TH}] dV$$

$$I_D = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

I/V Characteristics (cont.)

$$I_D = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

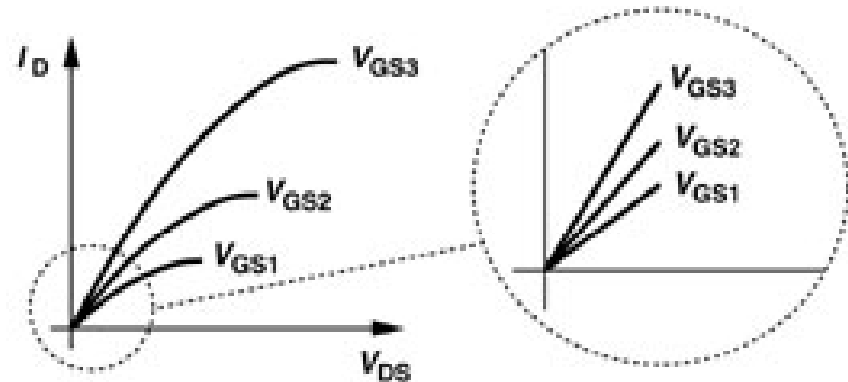


Operation in Triode Region

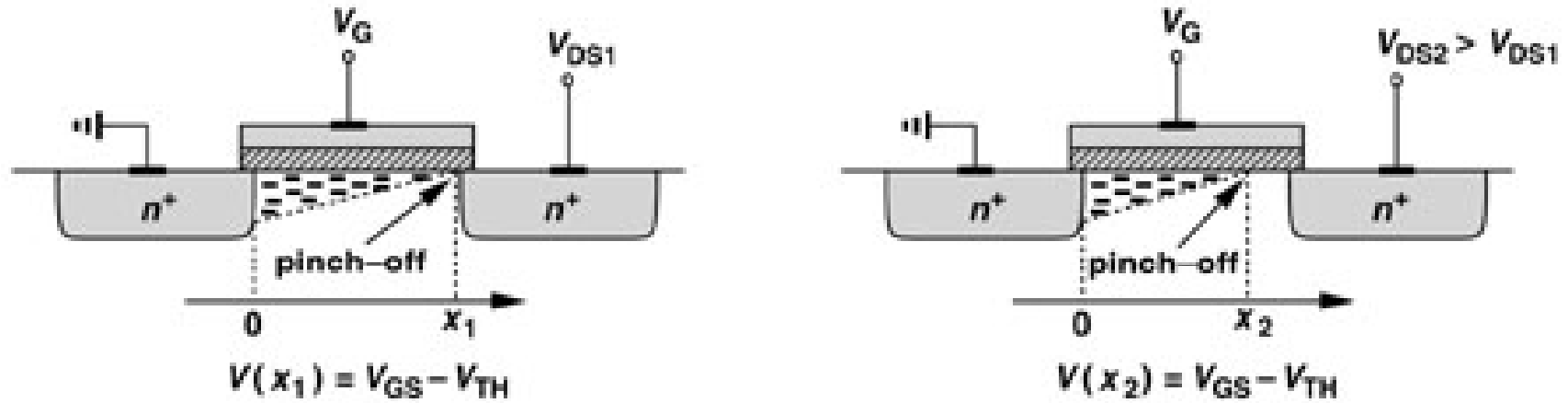
$$I_D = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

$$I_D = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH}) V_{DS}, \quad V_{DS} \ll 2(V_{GS} - V_{TH})$$

$$R_{ON} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})}$$



Operation in Active (Saturation) Region

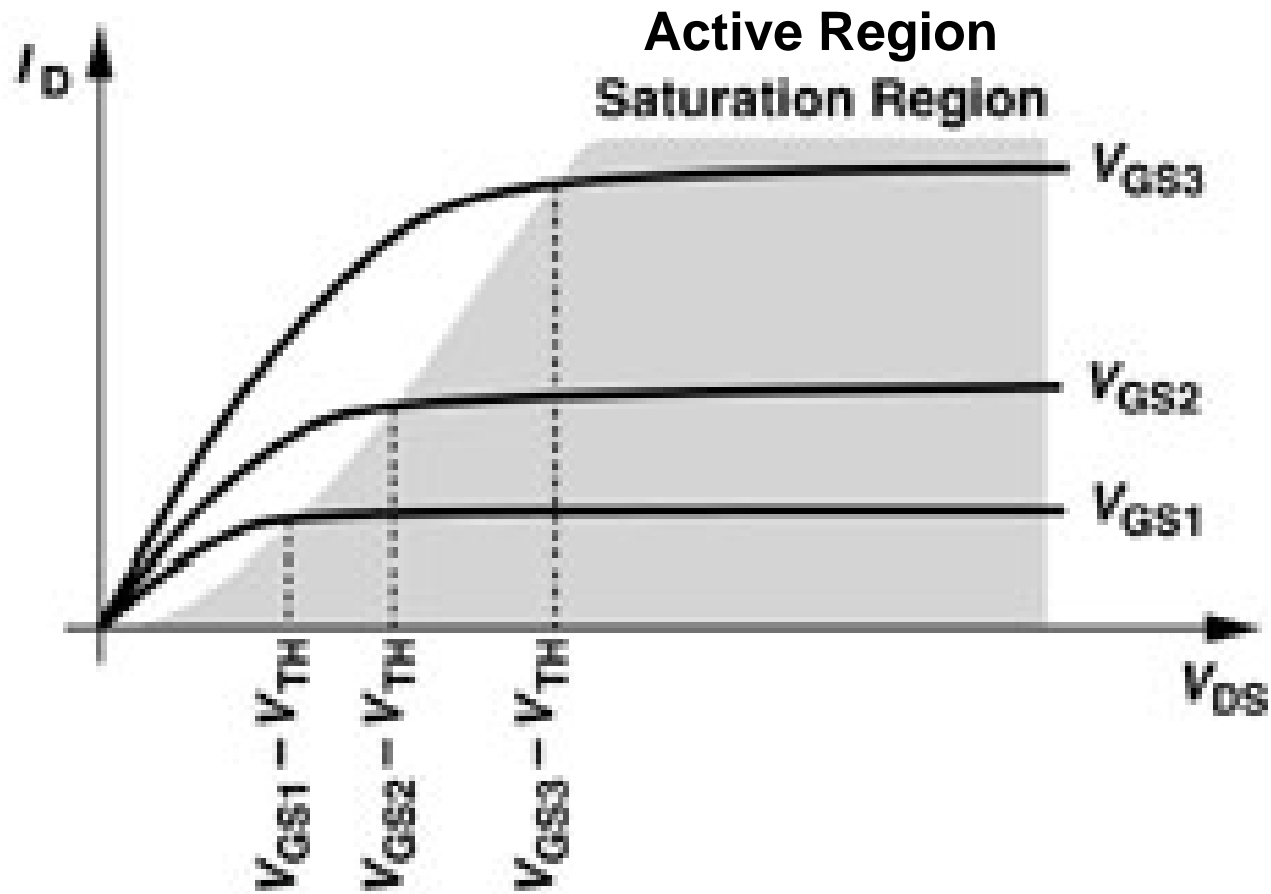


$$I_D = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

$$V'_{DS} = V_{GS} - V_{TH} \quad (\text{Pinch-off})$$

$$I_D = \frac{\mu_n C_{ox}}{2} \frac{W}{L} (V_{GS} - V_{TH})^2$$

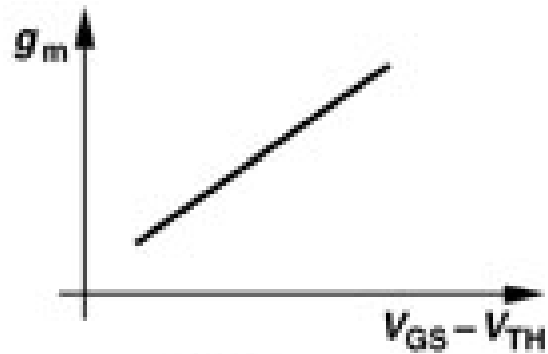
Active Region (cont.)



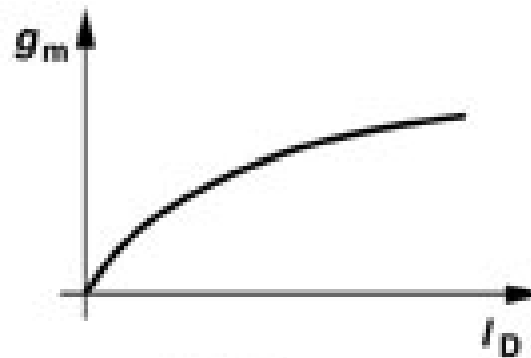
Transconductance, g_m

$$g_m = \left. \frac{\partial I_D}{\partial V_{GS}} \right|_{V_{DS} \text{ constant}}$$
$$= \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})$$

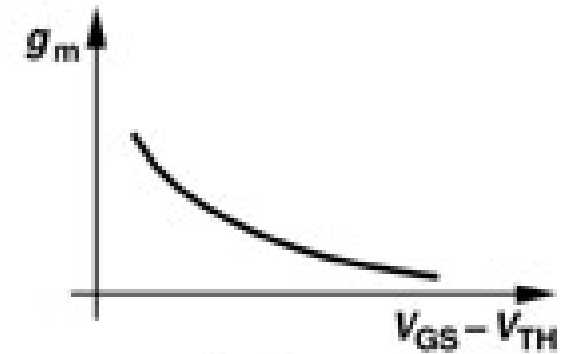
$$g_m = \sqrt{2 \mu_n C_{ox} \frac{W}{L} I_D}$$
$$= \frac{2 I_D}{V_{GS} - V_{TH}}$$



W/L Constant

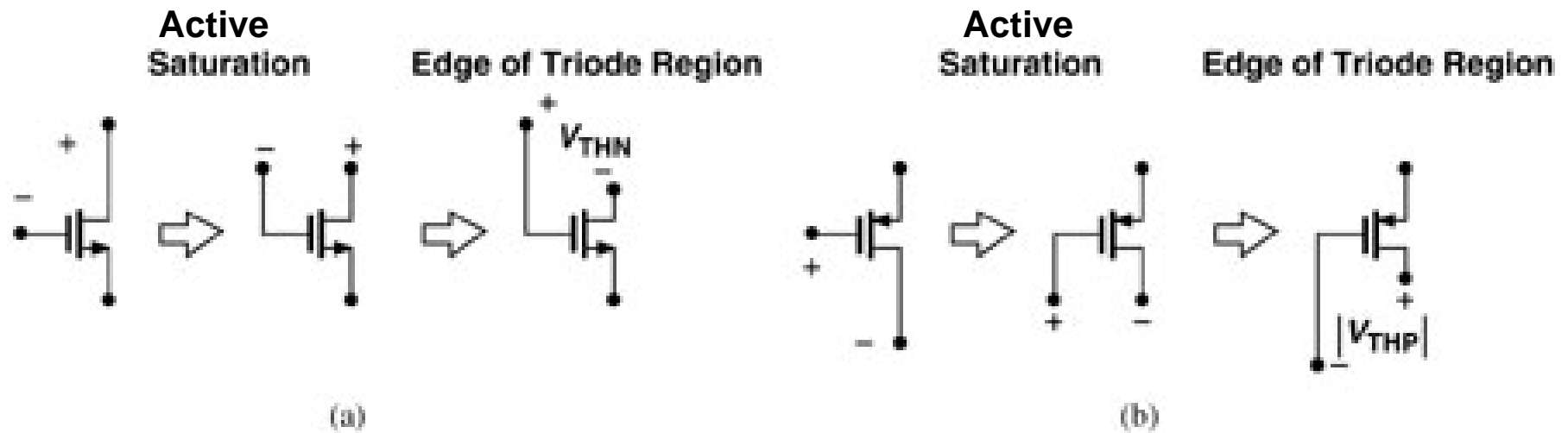


W/L Constant



I_D Constant

Triode and Active Region Transition



Threshold Voltage and Body Effect

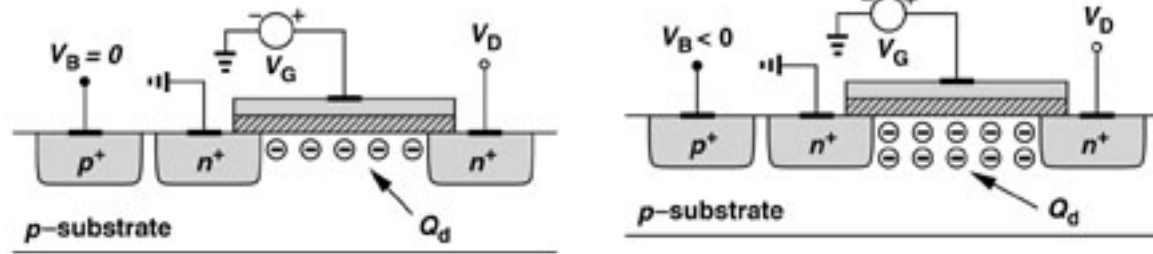
$$V_{TH} = \Phi_{MS} + 2\Phi_F + \frac{Q_{dep}}{C_{ox}}, \text{ where}$$

$$\Phi_{MS} = \Phi_{gate} - \Phi_{silicon}$$

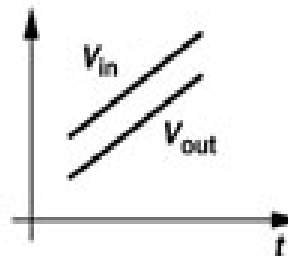
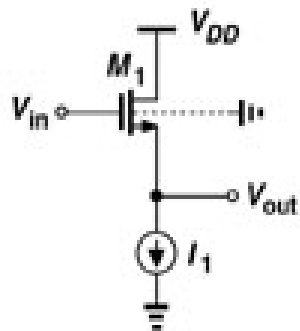
$$\Phi_F = \left(\frac{kT}{q}\right) \ln\left(\frac{N_{sub}}{n_i}\right)$$

$$Q_{dep} = \sqrt{4q \epsilon_{si} |\Phi_F| N_{sub}}$$

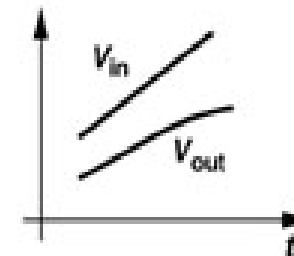
Threshold Voltage and Body Effect (cont.)



$$V_{TH} = V_{TH0} + \gamma \left(\sqrt{2\Phi_F + V_{SB}} - \sqrt{2\Phi_F} \right), \quad \gamma = \frac{\sqrt{2q\epsilon_{si}N_{sub}}}{C_{ox}}$$

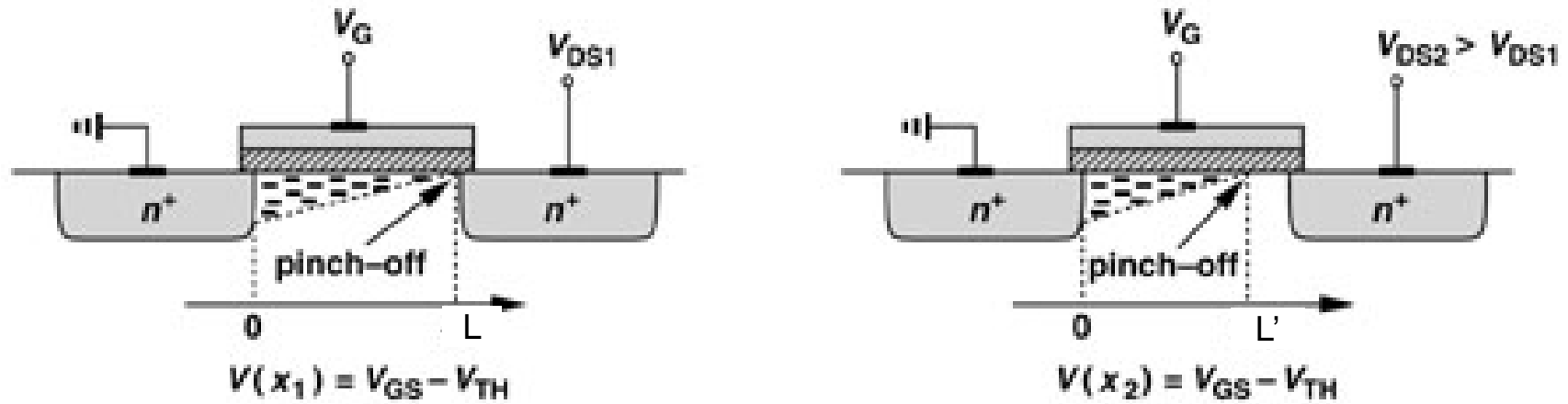


No Body Effect



With Body Effect

Channel Length Modulation



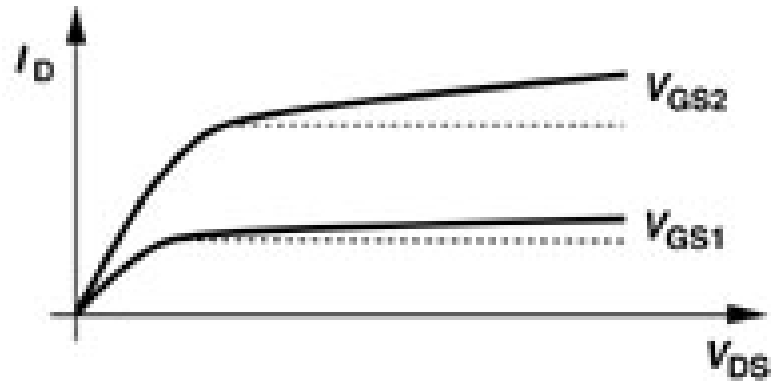
$$L' = L - \Delta L$$

$$1/L' = \frac{1}{L} (1 + \Delta L/L)$$

$$1/L' = \frac{1}{L} (1 + \lambda V_{DS}), \quad \lambda V_{DS} = \Delta L/L$$

$$I_D = \frac{\mu_n C_{ox}}{2} \frac{W}{L} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})$$

Channel Length Modulation (cont.)



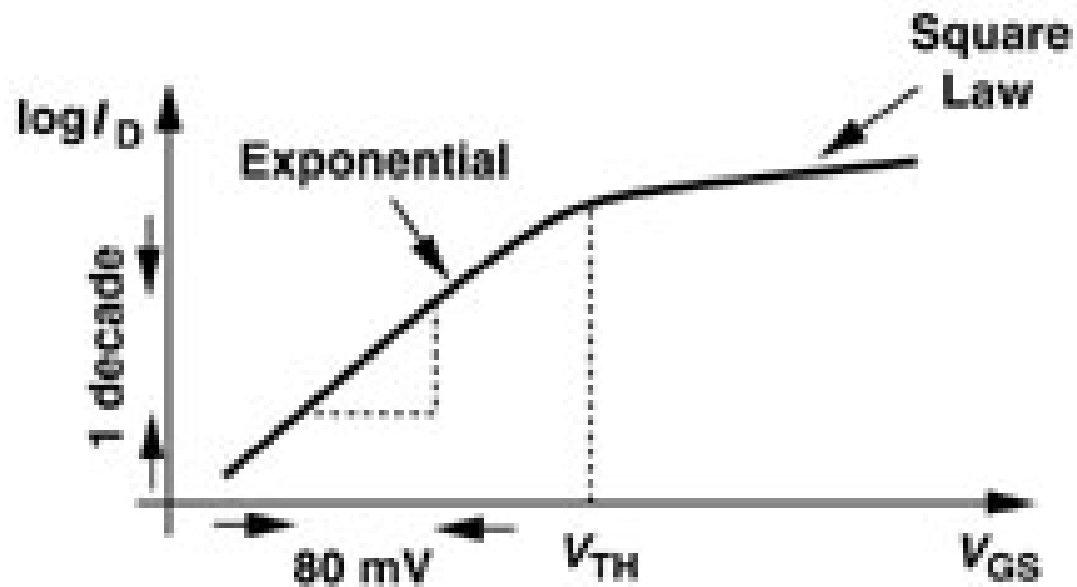
$$g_m = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})(1 + \lambda V_{DS})$$

$$g_m = \sqrt{\frac{2 \mu_n C_{ox} \frac{W}{L} I_D}{(1 + \lambda V_{DS})}}$$

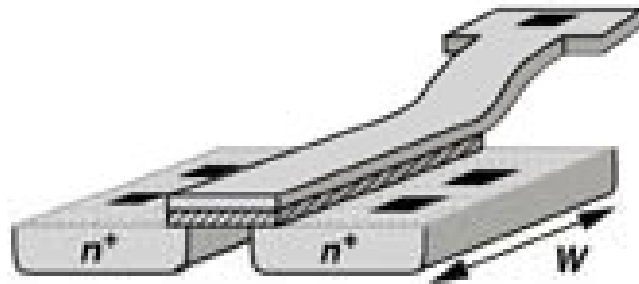
$$g_m = \frac{2I_D}{V_{GS} - V_{TH}}, \quad (\text{unchanged})$$

Subthreshold Conduction

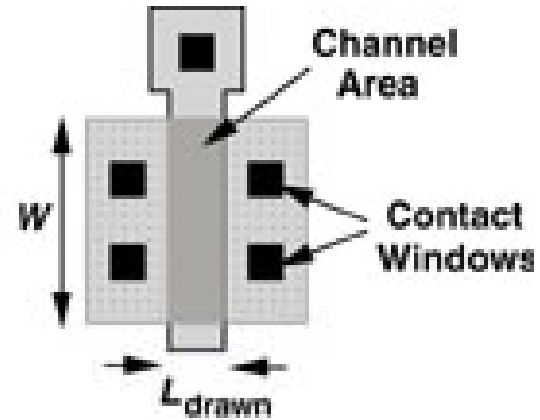
$$I_D = I_0 \exp\left(\frac{V_{GS}}{\zeta kT/q}\right)$$



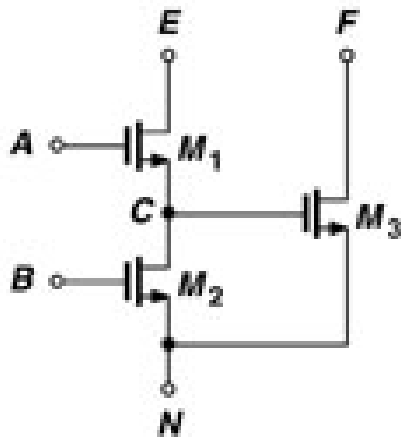
MOS Layout



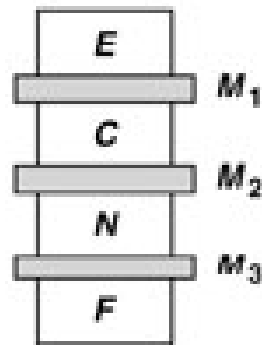
(a)



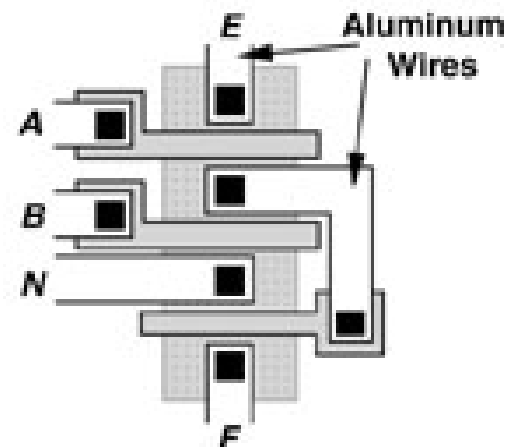
(b)



(a)

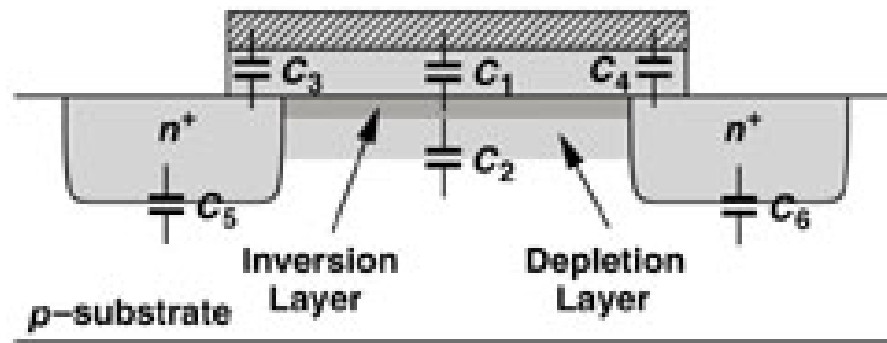
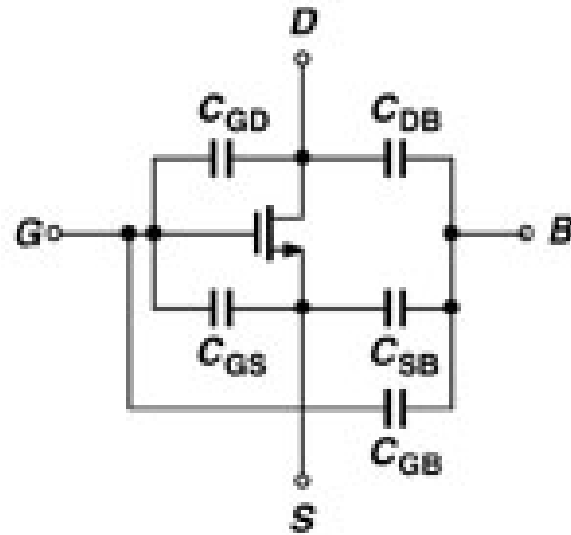


(b)

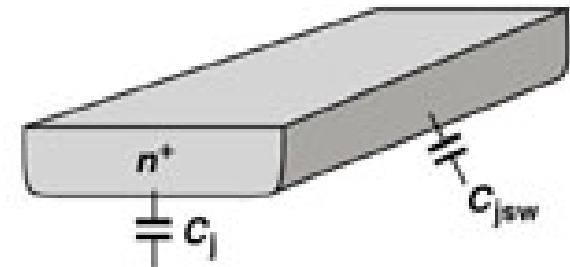


(c)

Device Capacitances

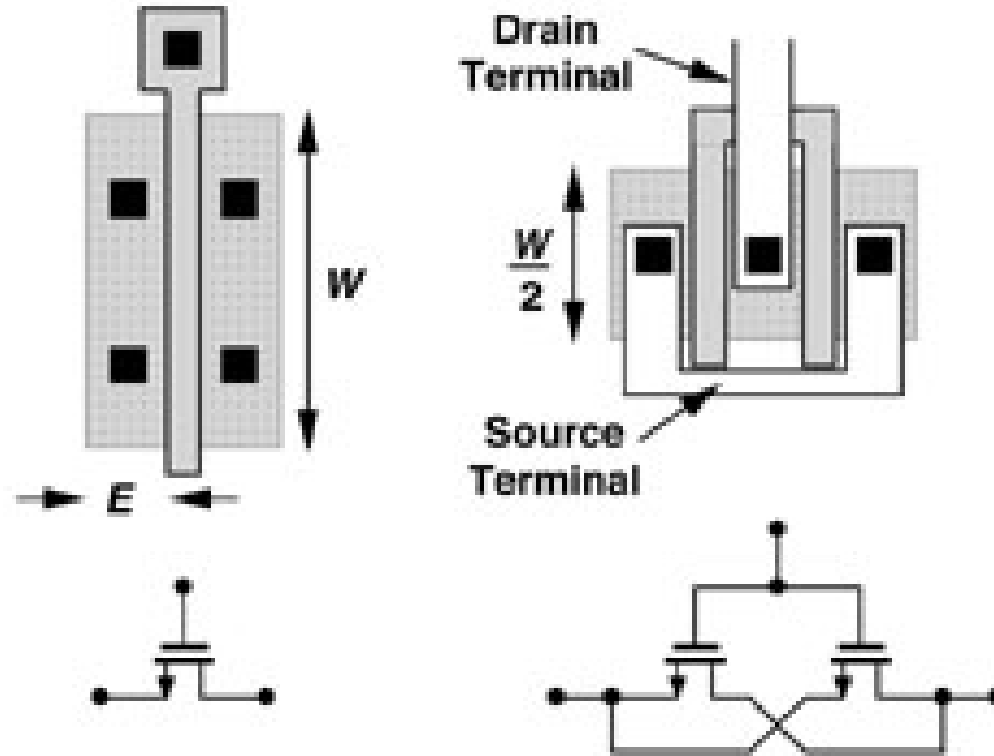


(a)

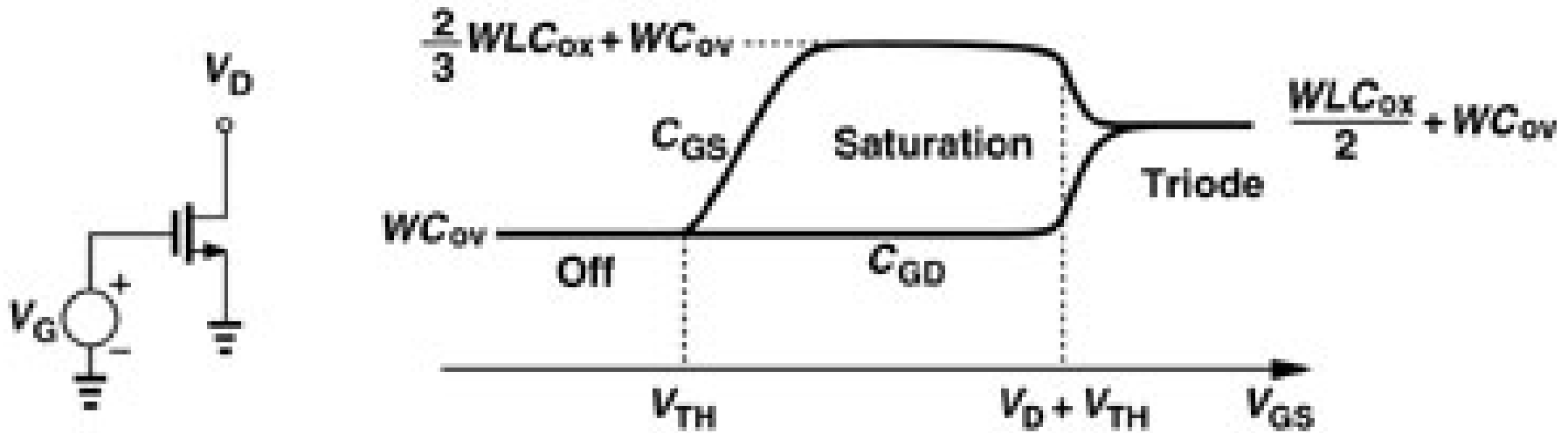


(b)

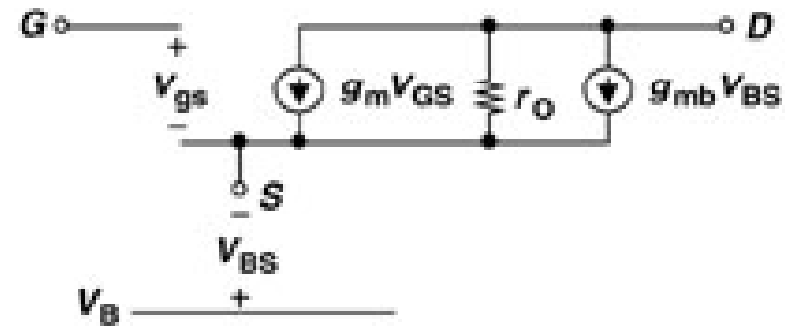
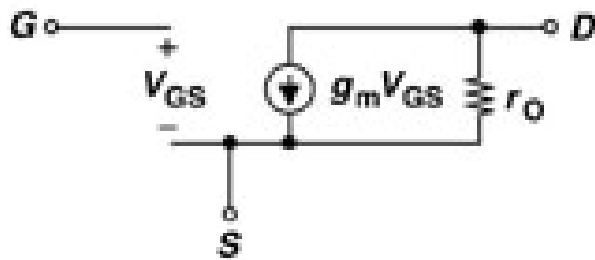
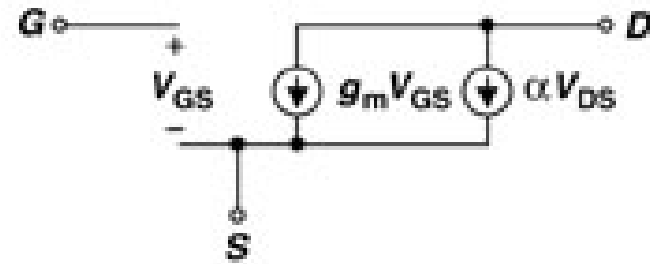
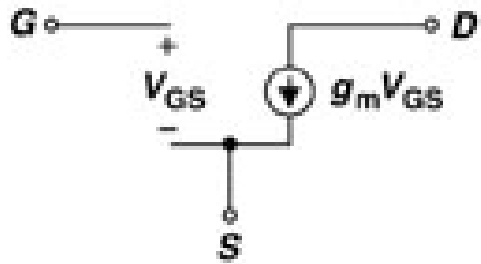
Layout for Low Capacitance



G-S and G-D Capacitance



MOS Small Signal Models



$$r_o = \frac{\partial \mathcal{N}_{DS}}{\partial I_D} = \frac{1}{\partial I_D / \partial \mathcal{N}_{DS}} = \frac{1}{\frac{\mu_n C_{ox}}{2} \frac{W}{L} (V_{GS} - V_{TH})^2 \lambda} = \frac{1}{\lambda I_D}$$

Bulk Transconductance, g_{mb}

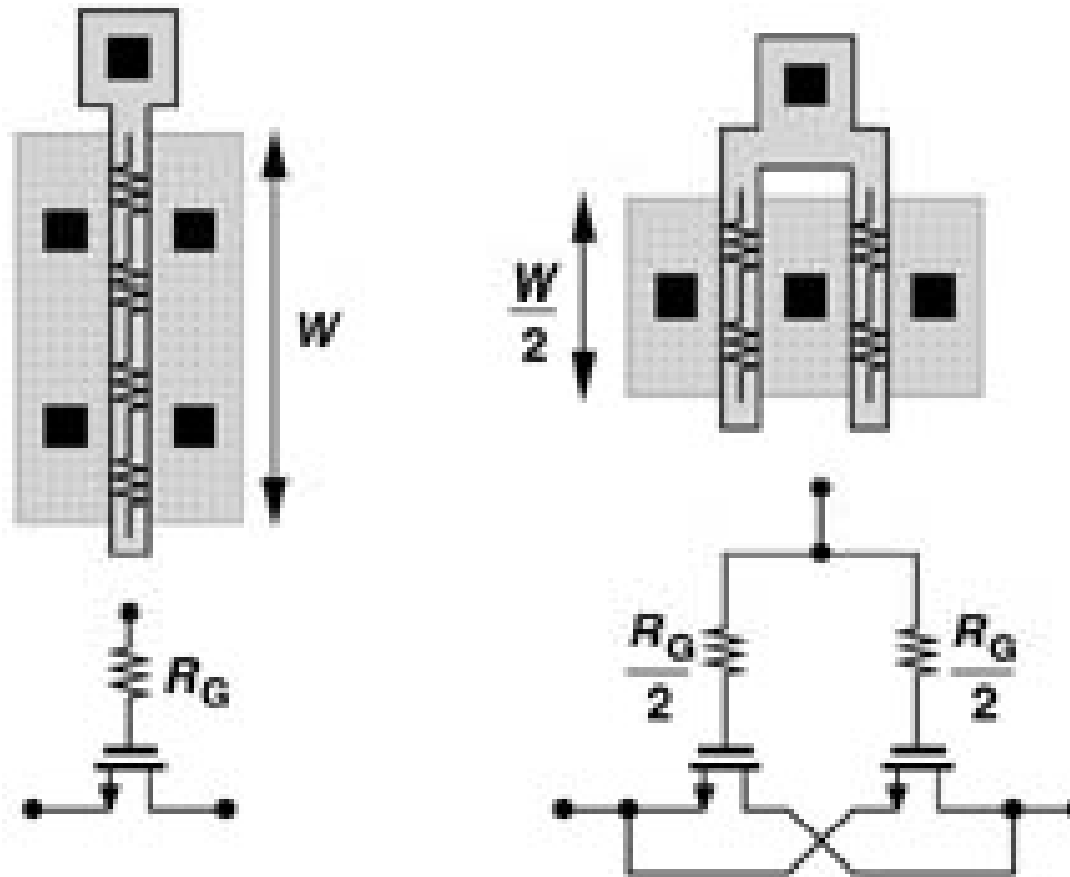
$$g_{mb} = \frac{\tilde{a}_D}{\mathcal{N}_{BS}} = \frac{\mu_n C_{ox}}{2} \frac{W}{L} (V_{GS} - V_{TH}) \left(\frac{-\partial \mathcal{N}_{TH}}{\partial \mathcal{N}_{BS}} \right)$$

Also,

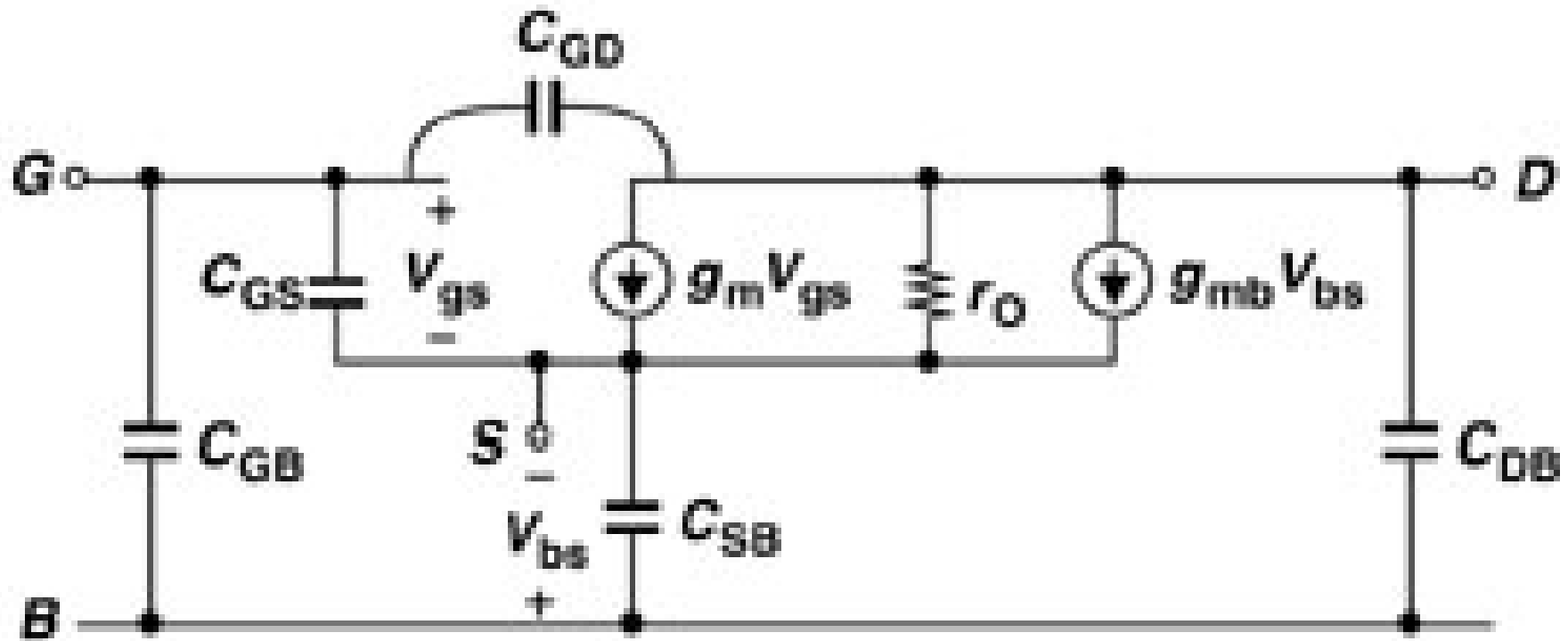
$$\frac{\partial \mathcal{N}_{TH}}{\partial \mathcal{N}_{BS}} = \frac{-\partial \mathcal{N}_{TH}}{\partial \mathcal{N}_{SB}} = -\frac{\gamma}{2} (2\Phi_F + V_{SB})^{-1/2}$$

$$g_{mb} = g_m \frac{\gamma}{2\sqrt{2\Phi_F + V_{SB}}} = \eta g_m$$

Gate Resistance



MOS Small Signal Model with Capacitance



C-V of NMOS

