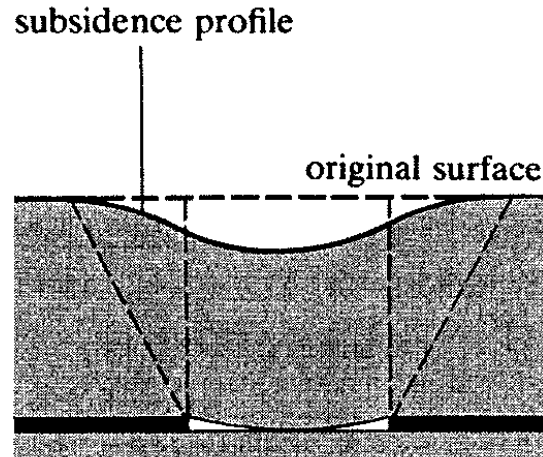


# **16. Mining-induced surface subsidence**

# 16.1 Types and effects of mining-induced subsidence

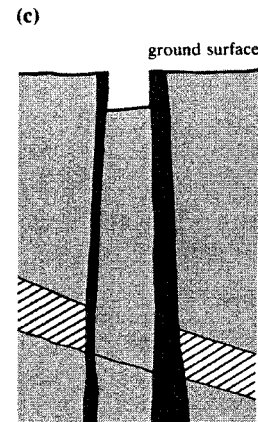
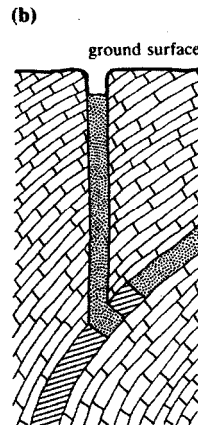
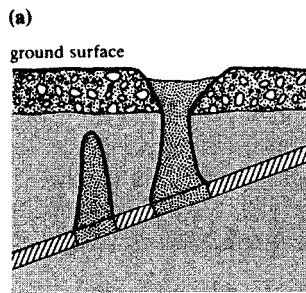
- Subsidence
  - Lowering of the ground surface following underground extraction of an orebody.
  - Types: continuous (trough) subsidence and discontinuous subsidence
- Continuous subsidence
  - Smooth surface subsidence without any step changes
  - Displacement is of elastic orders in magnitude.
  - Associated with the extraction of thin, horizontal or flat-dipping orebodies overlain by weak, non-brittle sedimentary strata.



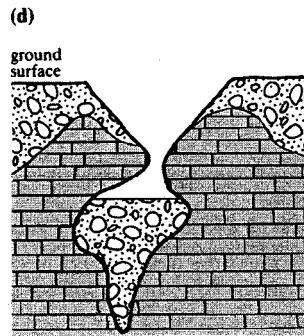
# 16.1 Types and effects of mining-induced subsidence

- Discontinuous subsidence

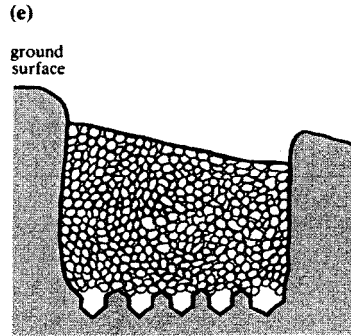
- Large surface displacement over limited surface area with steps or discontinuities in the surface profile.
- Crown holes: arising from the collapse of the roofs of generally abandoned and shallow open workings (a).
- Chimney caving (piping, funneling, sinkholes): involves the progressive migration of an unsupported mining cavity to the surface with a similar size and shape of the original excavation (b).
- Plug subsidence: sudden chimney formation controlled by structural features such as a dyke or a fault (c).



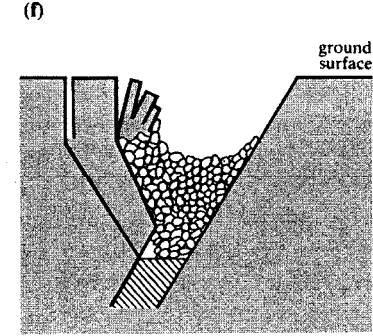
# 16.1 Types and effects of mining-induced subsidence



**Solution cavities**



**Block caving**

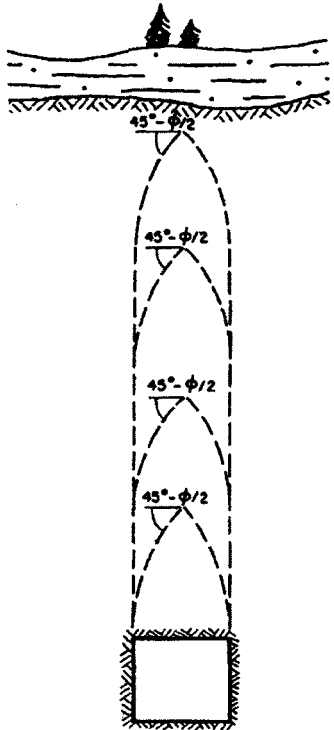


**Hanging wall caving**

- Discontinuous subsidence affects smaller area but causes more disastrous consequences.
- Prediction of the subsidence profile of continuous subsidence, and occurrence and areal extent of discontinuous subsidence are important to the planning of mining operations.

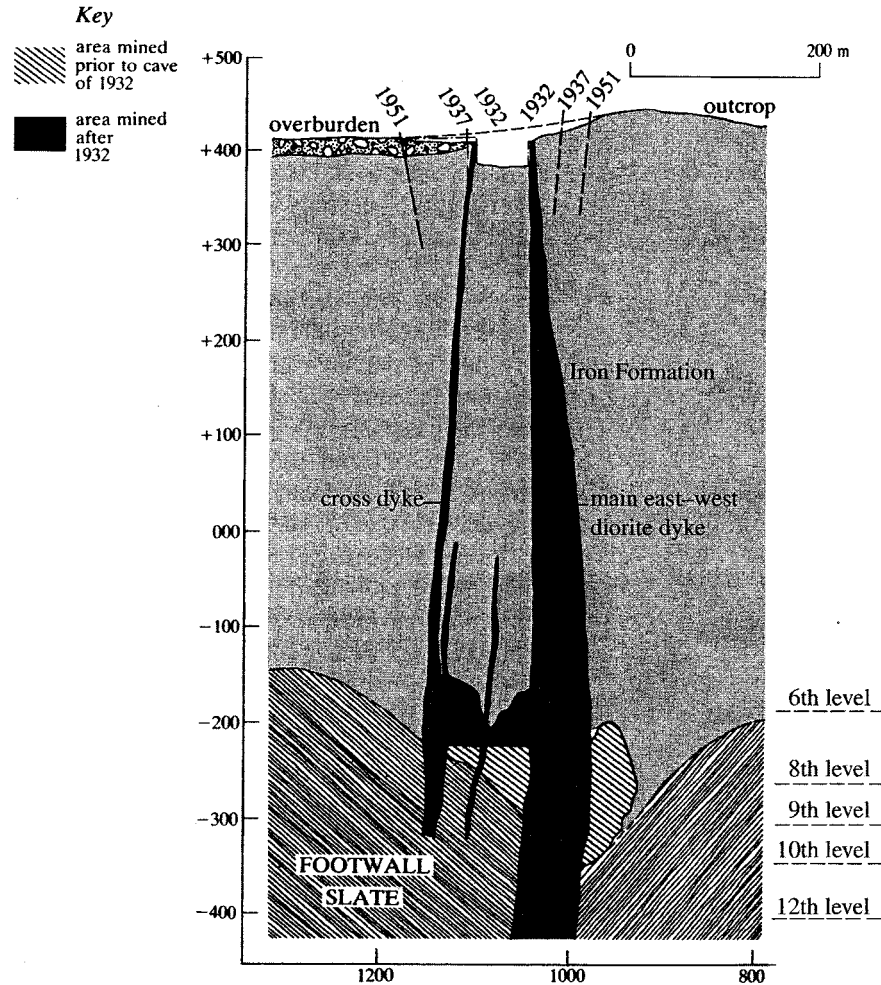
# 16.2 Chimney caving

- Chimney caving mechanisms



- 1) Progressive mechanism in weathered or weak rock or in previously caved rock
  - Fallen materials bulk and fill the stope void to prevent further subsidence unless the stope is initially large and open or the materials are drawn from it.
- 2) Progressive mechanism controlled by regular discontinuities
- 3) Plug subsidence mechanism controlled by one or more major structural features: shows rigid body displacement without breaking up or dilation and it is not affected by draw control.

# 16.2 Chimney caving



**Plug subsidence  
controlled by dykes**

# 16.2 Chimney caving

- Limiting equilibrium analysis of chimney caving

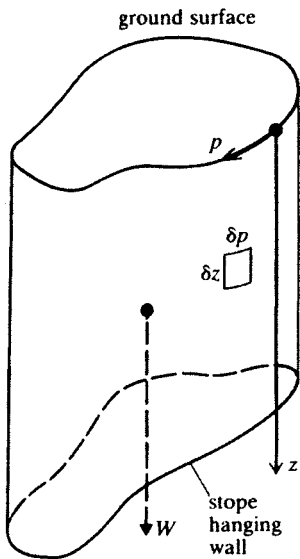
## 1) General block geometry

- Helpful in estimating ultimate collapse conditions of chimney caving by the 1<sup>st</sup> and 3<sup>rd</sup> mechanism

- Factor of safety: 
$$\frac{Q}{W} = \frac{\int_0^p \int_0^z \tau dz dp}{W}$$

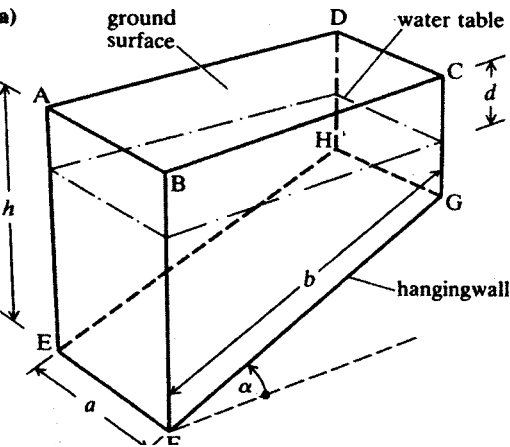
- Applying Coulomb shear strength with groundwater pressure:

$$Q = \int_0^p \int_0^z \{c' + [k\gamma z - u(z, p)] \tan \phi'\} dz dp$$

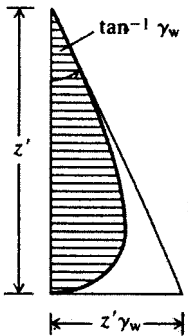


# 16.2 Chimney caving

## 2) Rectangular block geometry



(b)



- Groundwater pressure force:  $\frac{\gamma_w z^2}{3} = \frac{\gamma_w (z-d)^2}{3}$

- Total weight:  $W = \gamma ab \cos \alpha \left( h - \frac{b \sin \alpha}{2} \right)$

- Shear resistance:  $Q = 2Q_{BCGF} + Q_{DCGH} + Q_{ABFE}$

For  $0 \leq d \leq h - b \sin \alpha$

$$Q_{BCGF} = \int_0^{b \cos \alpha} \left[ \int_0^z (c' + k \gamma z \tan \phi') dz - \frac{\gamma_w (z-d)^2}{3} \tan \phi' \right] dx$$

$$= Q_1 - \frac{\gamma_w \tan \phi'}{3} b \cos \alpha \left[ \begin{array}{l} h^2 - hb \sin \alpha + \frac{b^2}{3} \sin^2 \alpha \\ -d(2h - b \sin \alpha - d) \end{array} \right]$$

where

$$Q_1 = \frac{b \cos \alpha}{2} \left[ c(2h - b \sin \alpha) + k \gamma \tan \phi' \left( h^2 - hb \sin \alpha + \frac{b^2}{3} \sin^2 \alpha \right) \right]$$



# 16.2 Chimney caving

$$Q_{DCGH} = a \left[ c' (h - b \sin \alpha) + \frac{k\gamma}{2} \tan \phi' (h - b \sin \alpha)^2 - \frac{\gamma_w \tan \phi'}{3} (h - b \sin \alpha - d)^2 \right]$$

$$Q_{ABFE} = a \left[ c' h + \frac{k\gamma h^2}{2} \tan \phi' - \frac{(h - d)^2}{3} \gamma_w \tan \phi' \right] \quad \text{for } 0 \leq d \leq h$$

For  $h - b \sin \alpha \leq d \leq h$

$$Q_{BCGF} = Q_1 - \frac{\gamma_w \tan \phi' (h - d)^3}{9 \tan \alpha}$$

$$Q_{DCGH} = a \left[ c' (h - b \sin \alpha) + \frac{k\gamma}{2} \tan \phi' (h - b \sin \alpha)^2 \right] \quad \text{for } h - b \sin \alpha \leq d$$

$$Q_{ABFE} = a \left[ c' h + \frac{k\gamma h^2}{2} \tan \phi' - \frac{(h - d)^2}{3} \gamma_w \tan \phi' \right] \quad \text{for } 0 \leq d \leq h$$

For  $h \leq d$

$$Q_{BCGF} = Q_1$$

$$Q_{DCGH} = a \left[ c' (h - b \sin \alpha) + \frac{k\gamma}{2} \tan \phi' (h - b \sin \alpha)^2 \right] \quad \text{for } h - b \sin \alpha \leq d$$

$$Q_{ABFE} = a \left[ c' h + \frac{k\gamma h^2}{2} \tan \phi' \right]$$

# 16.2 Chimney caving

- Factor of safety:

For  $h \leq d$

$$F = F_1 = \frac{2c'(a + b \cos \alpha)}{\gamma ab \cos \alpha} + \frac{k \tan \phi'}{2h - b \sin \alpha} \left\{ \frac{h^2 + (h - b \sin \alpha)^2}{b \cos \alpha} + \frac{2}{a} \left[ h(h - b \sin \alpha) + \frac{b^2 \sin^2 \alpha}{3} \right] \right\}$$

For  $h - b \sin \alpha \leq d \leq h$

$$F = F_1 - \frac{2\gamma_w (h - d)^2 \tan \phi'}{3\gamma b (2h - b \sin \alpha)} \left[ \sec \alpha + \frac{2(h - d)}{3a \sin \alpha} \right]$$

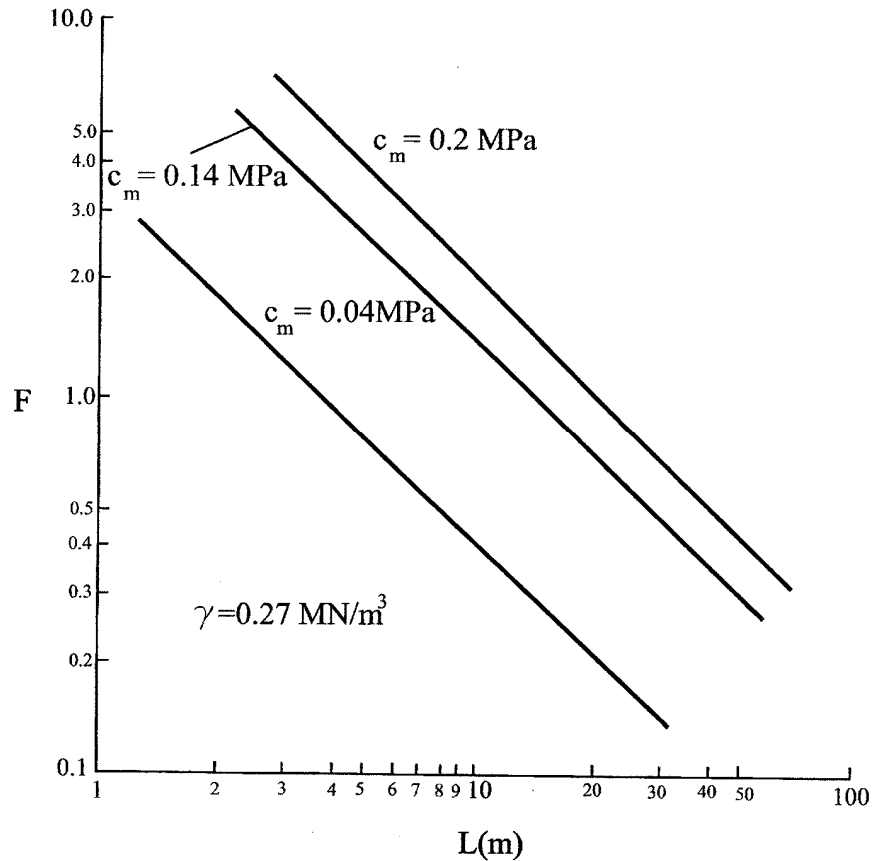
For  $0 \leq d \leq h - b \sin \alpha$

$$F = F_1 - \frac{2\gamma_w \tan \phi'}{3\gamma (2h - b \sin \alpha)} \left\{ \frac{h^2 + (h - b \sin \alpha)^2 - 2d(2h - b \sin \alpha - d)}{b \cos \alpha} + \frac{2}{3a} \left[ 3h(h - b \sin \alpha) + b^2 \sin^2 \alpha - 3d(2h - b \sin \alpha - d) \right] \right\}$$

- Critical span is obtained by setting  $F=1$  (refer to example at p.492)
- Safety factor decreases as the span increases, mining depth decreases,  $k$  decreases and unit weight of overburden increases.

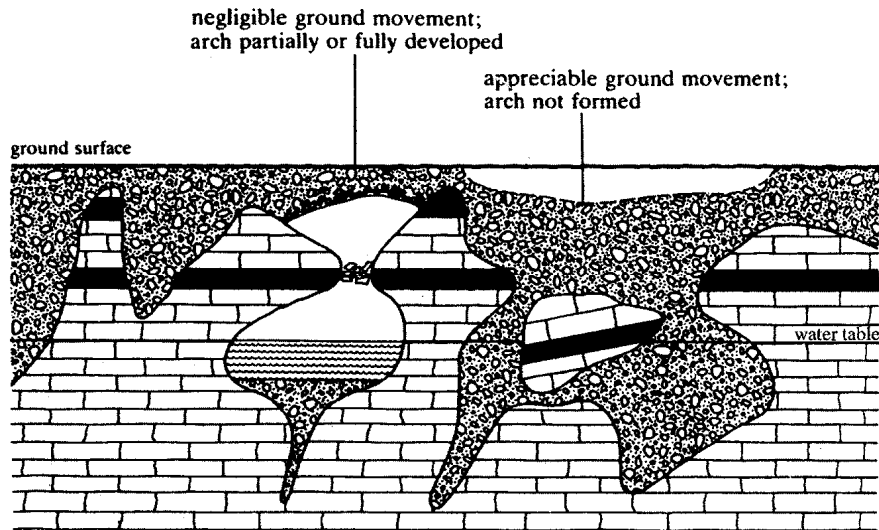
# 16.2 Chimney caving

- Relationship between stope span (L), rock mass cohesion ( $c_m$ ), and safety factor



# 16.3 Sinkholes in carbonate rocks

- Carbonate rocks: including  $\text{CO}_3^{2-}$  ion, weak and soluble in acid water, ex) limestone, dolomite
- Karst topography: landscape shaped by the dissolution of a layer or layers of soluble bedrock, usually carbonate rocks  
ex) doline, polje...
- Cavities develop in carbonate rocks generally above the water table where surface acid water flows downwards.

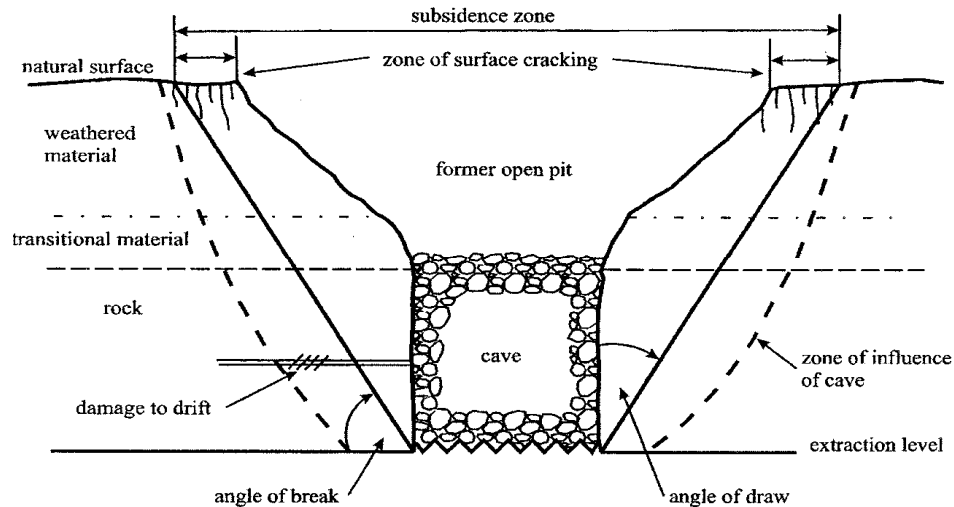


## 16.3 Sinkholes in carbonate rocks

- Basic concept of sinkhole: a sinkhole will form when the equilibrium of a stable arch of material above the void is disturbed.
  
- Sinkhole formation mechanism postulated by Jennings et al (1965).
  - a) Adjacent stiff materials for abutment exist.
  - b) Arching must develop in the residuum.
  - c) A void must exist or develop below the arched residuum.
  - d) A reservoir must exist below the arch to accept the material transported by flowing water.
  - e) Disturbing force by water, for example, is required to collapse the roof.
  
- Development of sinkhole can be accelerated by artificially lowering the water table: a large sinkhole will not develop where the water table is high.

# 16.4 Discontinuous subsidence associated with caving methods of mining

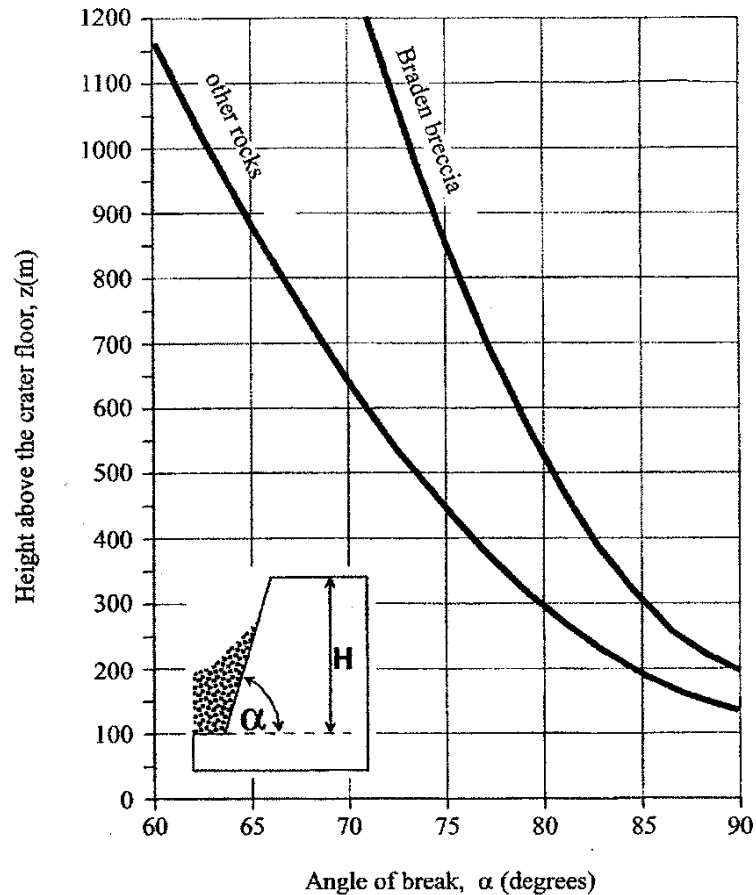
- Block caving
  - Factors influencing the extent of surface geometry: the dip, shape, strength of orebody; strength of surrounding rock and overburden; structural features such as faults and dykes; mining depth and in situ stress; surface slope; prior surface mining; placement of fill; nearby underground excavations
  - Angle of break (subsidence): angle between the horizontal undercut level and the extremity of surface cracks (complement of the angle of draw)



# 16.4 Discontinuous subsidence associated with caving methods of mining

- Zone of influence: a zone outside the zone of angle of draw where a small-scale or micro-deformation occurs (c.f. a zone of angle of draw showing the large-scale or macro-deformation)
  
- Prediction of the limits of the zone of influence:
  - 1) Project the orebody perimeters to the surface to establish the caving area.
  - 2) Estimate the angle of break using an empirical method.
  - 3) Calibrate the estimate against observed angles of break in this or similar mines.
  - 4) Check the estimated angle of break using other methods
  - 5) Modify the current estimate of the angle of break to reflect local geological features.
  - 6) Use numerical modeling to check the angle of break and to estimate stress and displacements.

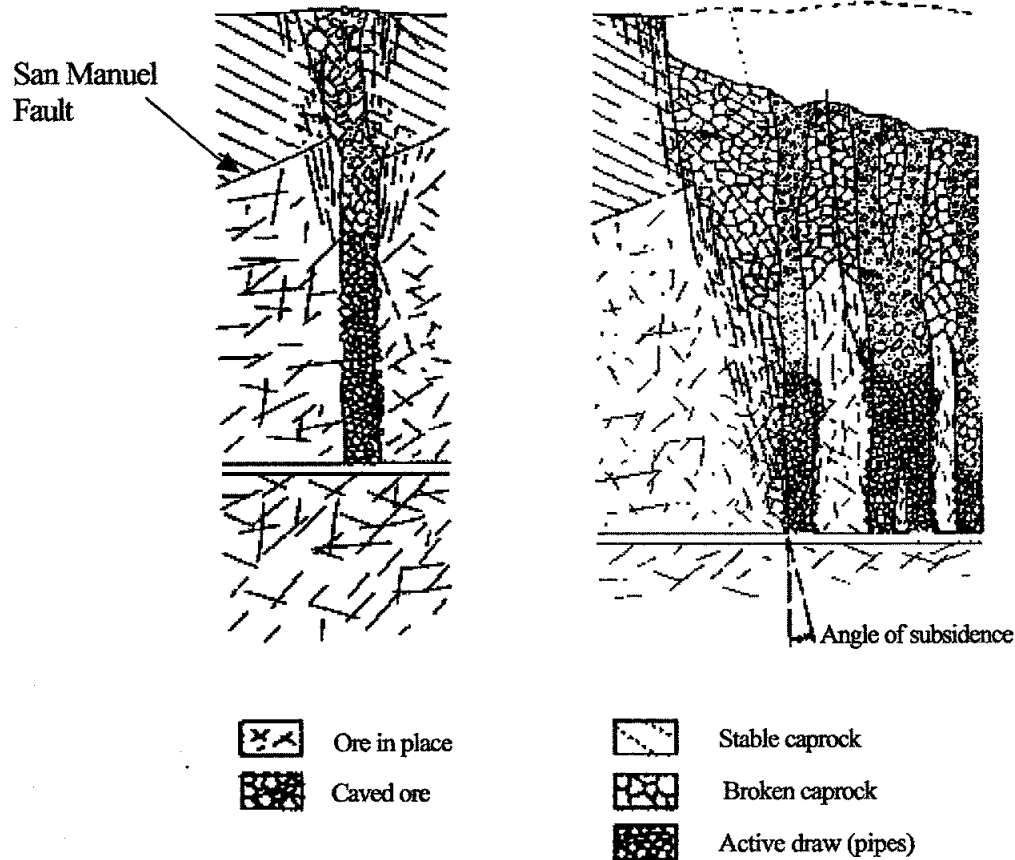
# 16.4 Discontinuous subsidence associated with caving methods of mining



**Braden breccia is stronger than other rocks**



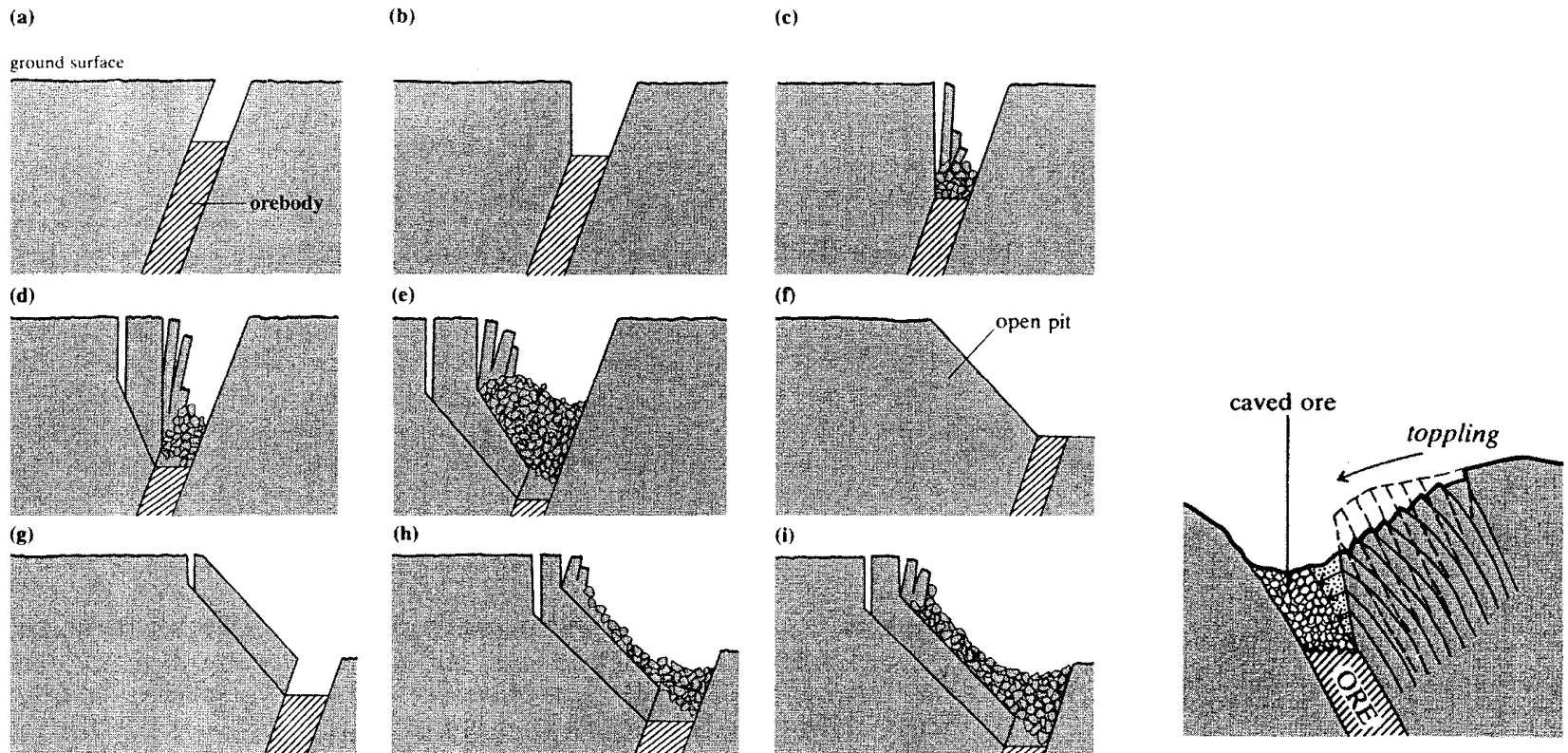
# 16.4 Discontinuous subsidence associated with caving methods of mining



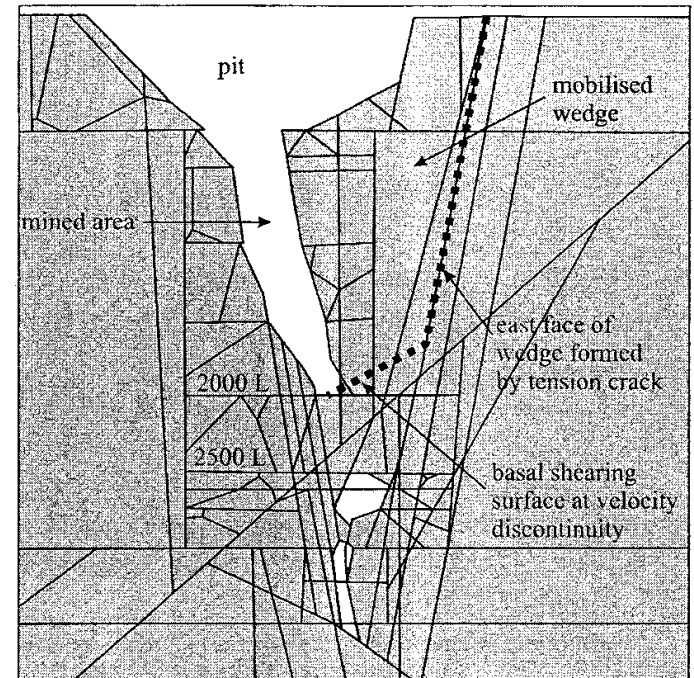
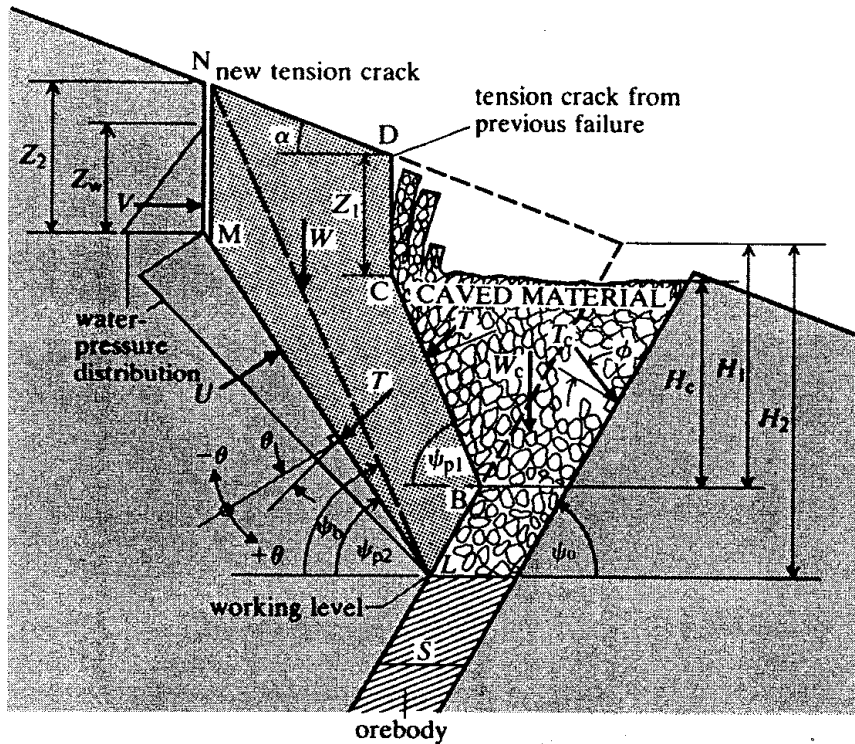
**Development of surface subsidence at San Manuel mine, Arizona, USA**

# 16.4 Discontinuous subsidence associated with caving methods of mining

- Progressive hangingwall caving



# 16.4 Discontinuous subsidence associated with caving methods of mining

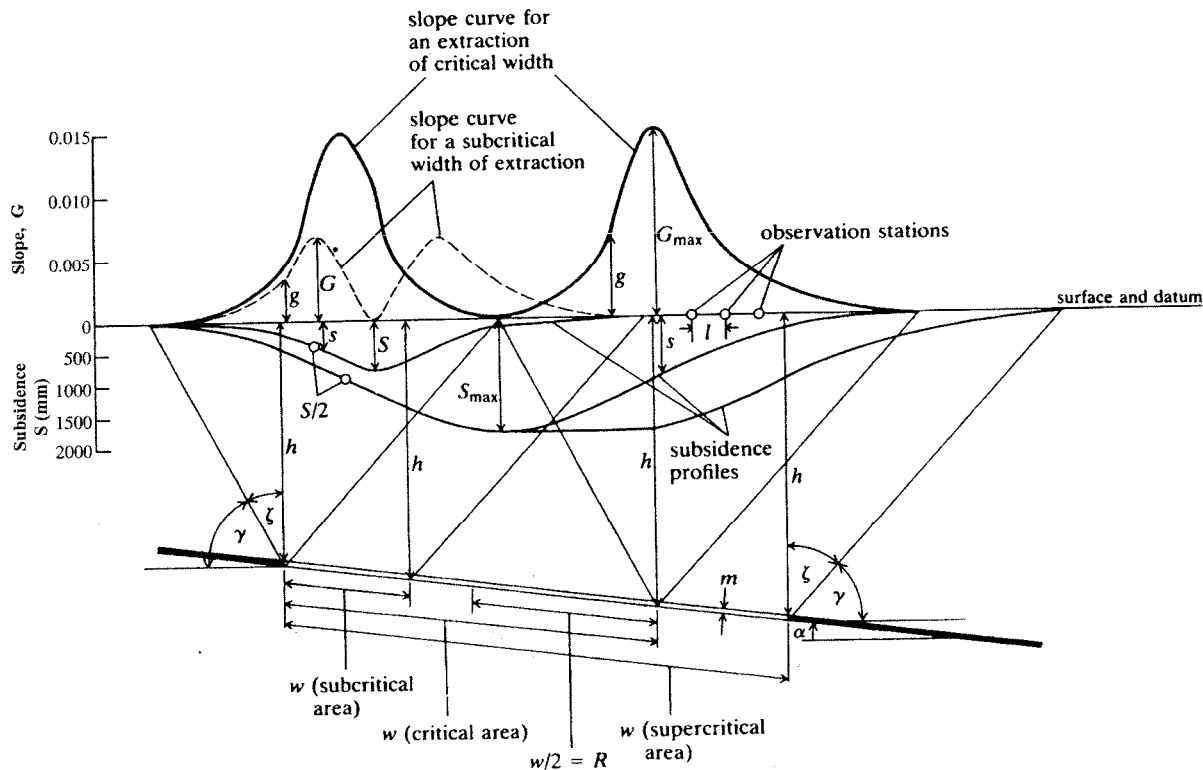


**Ideal model for limiting equilibrium analysis**

**3DEC model for Kidd mine, Canada**

# 16.5 Continuous subsidence due to the mining of tabular orebodies

- Concepts and definitions
  - Critical area is an extraction area of which maximum subsidence value is the overall maximum possible for the given ore seam.



# 16.5 Continuous subsidence due to the mining of tabular orebodies

- Subcritical area is an extraction area of which maximum subsidence value is less than the overall maximum possible for the given ore seam.
- Supercritical area is an extraction area of which maximum subsidence value is the overall maximum possible for the given ore seam and is maintained over a finite width rather than at a point.
- Angle of draw ( $\zeta$ ): an angle between a vertical line and a line from the seam base to a point of zero surface subsidence; lower for stronger rocks.
- Critical area of a horizontal seam at depth  $h$ :

$$W_c = 2h \tan \zeta$$

- Primary parameters of interest:
  - the maximum subsidence ( $S_{max}$ )
  - the maximum ground tilt ( $G_{max}$ )
  - the maximum tensile and compressive ground strains ( $+E_{max}$  and  $-E_{max}$ )
  - the minimum radius of ground curvature ( $R_{min}$ )

# 16.5 Continuous subsidence due to the mining of tabular orebodies

- Empirical prediction methods
  - The empirical methods by National Coal Board (UK) have been the most comprehensive and widely used methods for many years (*Subsidence Engineers' Handbook*):

$$+E_{\max} = 1000 \times K_1 \times S_{\max} / h$$

$$-E_{\max} = 1000 \times K_2 \times S_{\max} / h$$

$$G_{\max} = 1000 \times K_3 \times S_{\max} / h$$

$$1/R_{\min} = K_3 \times E_{\max} / h \quad (\text{max. curvature})$$

- NCB's methods met with variable success in other parts of the world because of the site-specific nature of the empirical methods.
- Concepts developed by the NCB have been found to be applicable elsewhere.

# 16.5 Continuous subsidence due to the mining of tabular orebodies

- Profile function by hyperbolic tangent function:

$$s(x) = \frac{1}{2} S_{\max} \left[ 1 - \tanh\left(\frac{bx}{h}\right) \right]$$

where  $b$  is a constant controlling the slope at the inflection point.

- Surface slope or tilt:

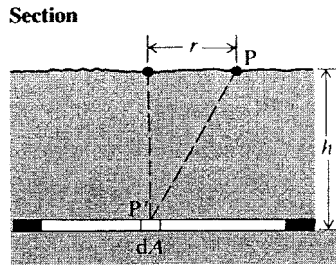
$$g = \frac{ds}{dx} = \frac{bS_{\max}}{2h} \operatorname{sech}^2\left(\frac{bx}{h}\right)$$

For  $b = 5$ , the maximum slope at the inflection point ( $x = 0$ ) is

$$G = \frac{2.5S_{\max}}{h}$$

# 16.5 Continuous subsidence due to the mining of tabular orebodies

- Influence functions are used to describe the surface subsidence caused by the extraction of an element  $dA$ .



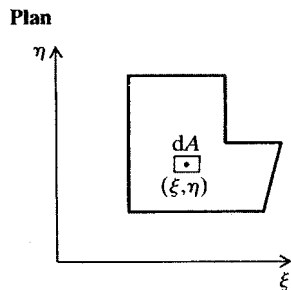
$$p(r) = w(\xi, \eta) f(r), \quad r = \sqrt{(x - \xi)^2 + (y - \eta)^2}$$

$$s(x, y) = \iint_A w(\xi, \eta) f\left(\sqrt{(x - \xi)^2 + (y - \eta)^2}\right) d\xi d\eta$$

One of the most widely used functions is

$$p(r) = \frac{nS_{\max}}{B^2} \exp\left[-n\pi\left(\frac{r}{B}\right)^2\right]$$

where  $n$  is a parameter characterizing the strata properties, and  $B$  is the critical radius of extraction,  $B = h \tan \zeta$



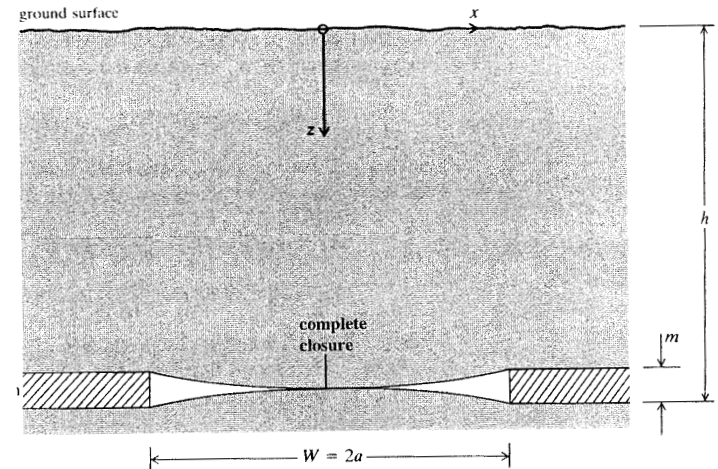


# 16.5 Continuous subsidence due to the mining of tabular orebodies

- Trough subsidence analyzed as elastic deformation
- The strata above deep tabular deposits may deform elastically.
- Surface subsidence of a completely closed excavation shows that the max. settlement is independent of the elastic constants of rock mass.
- Berry (1963)'s calculation of subsidence in a transversely isotropic media:

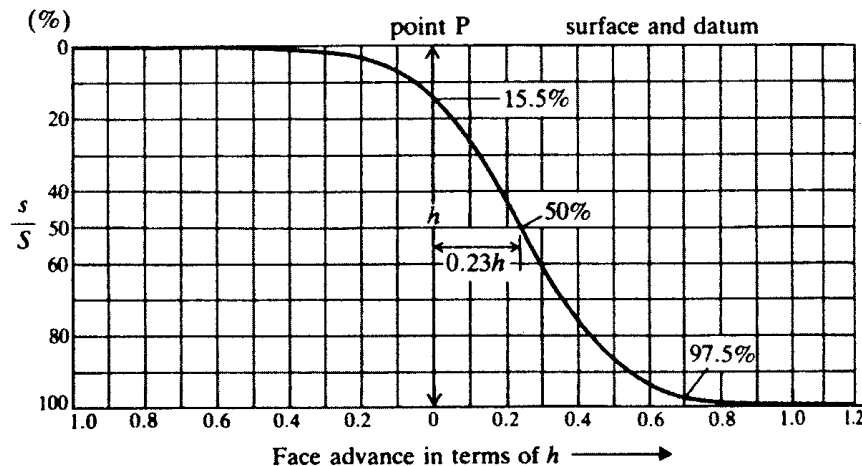
$$s(x) = \frac{m}{\pi(\alpha_1 - \alpha_2)} \left[ \alpha_1 \tan^{-1} \frac{2ah_1}{x^2 - a^2 + h_1^2} - \alpha_2 \tan^{-1} \frac{2ah_2}{x^2 - a^2 + h_2^2} \right]$$

where  $h_{1,2} = h/\alpha_{1,2}$  and  $\alpha_{1,2}$  are real values



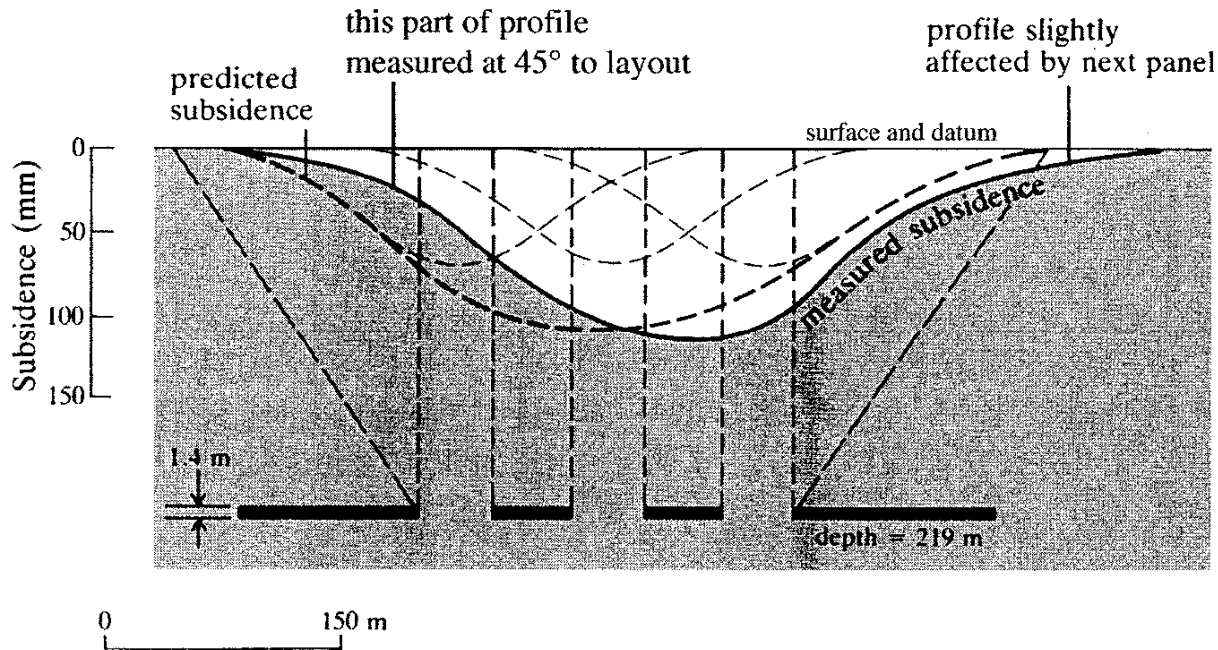
# 16.5 Continuous subsidence due to the mining of tabular orebodies

- Numerical methods
  - Numerical methods can eliminate some simplifying assumptions used for analytical approaches such as Berry's analysis.
  - FEM, BEM, FDM etc. have been adopted for the analysis
- Relation of subsidence to face position and time
  - Typical longitudinal subsidence at point P:



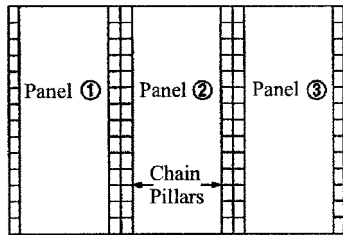
# 16.5 Continuous subsidence due to the mining of tabular orebodies

- Design measures to limit subsidence effects
  - Giving up the extraction (70%) reduces the subsidence (80%).

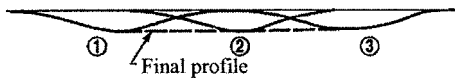


# 16.5 Continuous subsidence due to the mining of tabular orebodies

- Relation between pillar width and subsidence

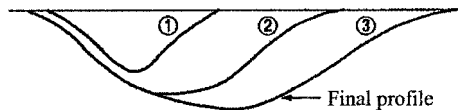


(a) Plan of longwall layout



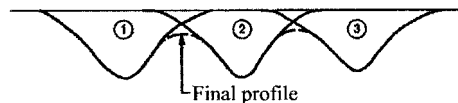
(b) Subsidence profile - shallow and smooth

Narrow panels ( $w/h < 0.33$ ) with wide pillars ( $w_p/h > 0.2$ )



(c) Subsidence profile - deep and smooth

Narrow panels ( $w/h < 0.33$ ) with narrow pillars ( $w_p/h = 0.06$ )



(d) Subsidence profile - deep and wavy

Wide panels ( $w/h > 0.6$ ) with wide pillars ( $w_p/h > 0.1$ )

# 16.5 Continuous subsidence due to the mining of tabular orebodies

- **Harmonic extraction** means a phased removal of the mineral by adopting at least two faces which advance at calculated distance apart. It makes the ground surface lowered smoothly and horizontal strains minimized.