2.1.6 Formal Potentials

χ : activity coefficient

- As the ionic strength becomes greater, the behavior of an individual ion is influenced by its nearby neighbors.
- The ionic strength depends on the concentration and charge number: μ

$$u = \frac{1}{2} \sum_{i=1}^{n} c_i z_i^2$$

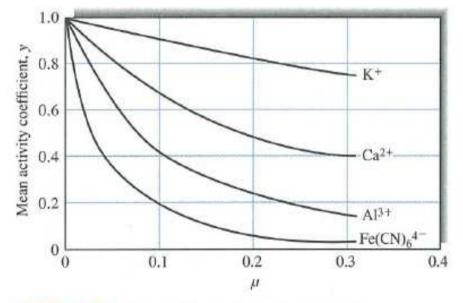
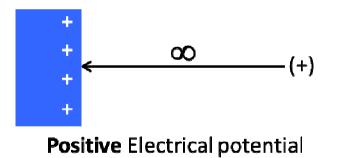
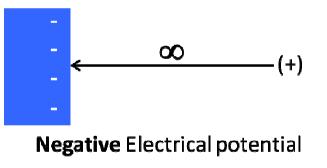


FIGURE a2-1 Effect of ionic strength on activity coefficients.

- The potential at any particular point within a phase, $\phi(x, y, z)$
 - → defined as the work required to bring a unit positive charge, without material interactions, from an infinite distance to point (x, y, z).
 - \rightarrow independent of the path of the test charge





- The work is done against a coulombic field;
- \rightarrow hence we can express the potential generally as

$$\phi(x, y, x) = \int_{\infty}^{x, y, z} - \mathscr{E} \cdot d\mathbf{1}$$

where

S: the electric field strength vector (i.e., the force exerted on a unit charge at any point)dl: an infinitesimal tangent to the path in the direction of movement.

• The difference in potential between points (x', y', z') and (x, y, z) is then

$$\phi(x', y', z') - \phi(x, y, z) = \int_{x, y, z}^{x', y', z'} - \mathscr{C} \cdot d\mathbf{1}$$

- When no current passes through a conducting phase,
- \rightarrow there is no net movement of charge carriers,
- \rightarrow So the electric field at all interior points = 0.

$$\phi(x', y', z') - \phi(x, y, z) = \int_{x, y, z}^{x', y', z'} - \mathscr{C} \cdot d\mathbf{1}$$

- From the above equation,
- \rightarrow the difference in potential between any two points in the interior of the phase = 0
- \rightarrow Thus the entire phase is an equipotential volume under these conditions.
- \rightarrow Its potential, ϕ , is known as the inner potential (or Galvani potential) of the phase.

- Consider a situation
- \rightarrow where there is a charged metal sphere of macroscopic size, perhaps a mercury droplet 1 mm in diameter, surrounded by a layer of uncharged electrolyte a few millimeters in thickness.
- \rightarrow This assembly is suspended in a vacuum.

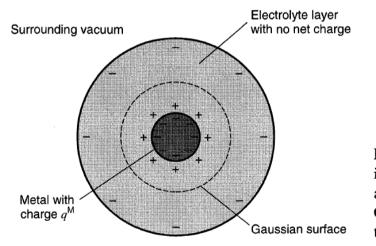
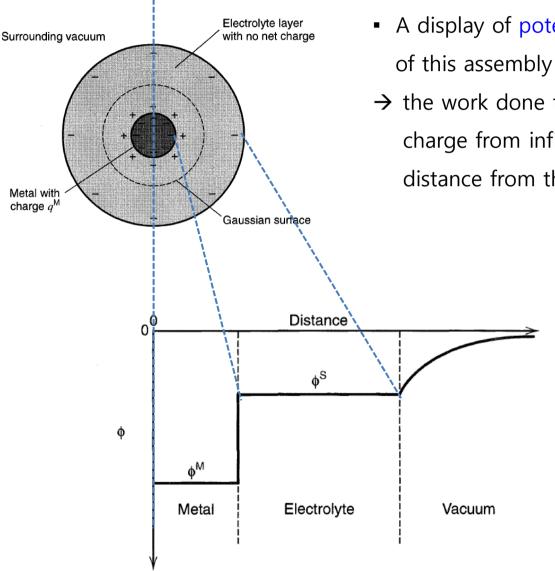


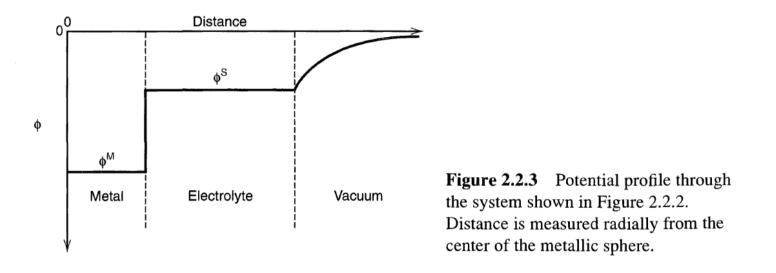
Figure 2.2.2 Cross-sectional view of the interacti56on between a metal sphere and a surrounding electrolyte layer. The Gaussian enclosure is a sphere containing the metal phase and part of the electrolyte.

2.2.2 Interactions Between Conducting Phases



- A display of potential vs. distance from the center of this assembly
- → the work done to bring a unit positive test charge from infinitely far away to a given distance from the center.
 - Within the electrolyte, *s* is zero everywhere,
 - → so there is no work in moving the test charge, and the potential is constant at ϕ^{S} .
 - At the metal-solution interface, there is a strong field because of the double layer

2.2.2 Interactions Between Conducting Phases



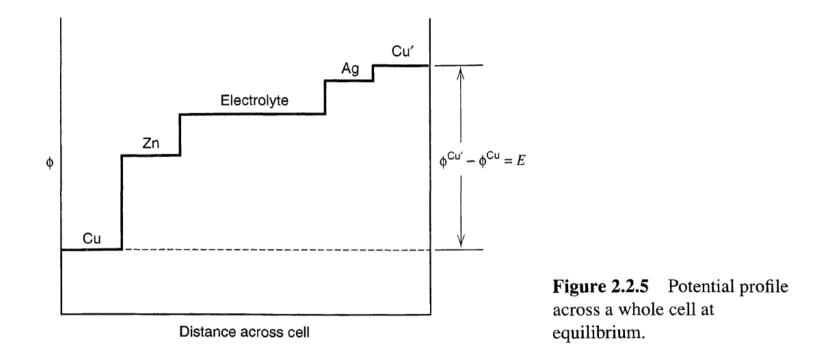
- The difference $\Delta \phi$ ($\phi^{M} \phi^{S}$), called the interfacial potential difference,
 - → depends on the charge imbalance at the interface and the physical size of the interface.

- Unfortunately, Δφ cannot be measured for a single interface by voltmeters
 → voltmeters require two electrodes
- Consider $\Delta \varphi$ at the interface Zn/Zn²⁺, Cl⁻.
 - \rightarrow We want to measure the $\Delta \phi$
 - → Need to construct the electrochemical cell including several interfaces

Cu/Zn/Zn²⁺,Cl⁻/AgCl/Ag/Cu'

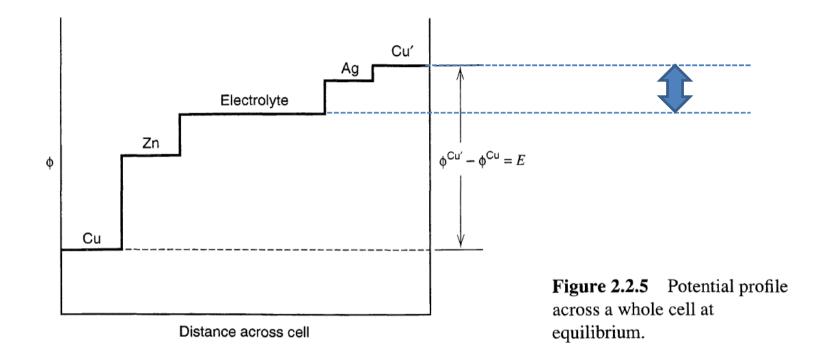
2.2.3 Measurement of Potential Differences

• The potential profile through the cell is expected as shown in the figure of:



- A measured cell potential (E)
 - \rightarrow a sum of several interfacial differences, none of which we can evaluate independently

2.2.3 Measurement of Potential Differences



• The silver/electrolyte junction can be fixed if the activities of the participants in its halfreaction remain fixed (Reference electrode).

 \rightarrow it is possible to focus on a single interfacial potential difference between zinc and the electrolyte

- Let us consider the interface Zn/Zn²⁺, Cl⁻ (aqueous) and focus on zinc ions in metallic zinc and in solution.
 - \rightarrow In the metal Zn²⁺: fixed in a lattice of positive zinc ions, with free electrons permeating the structure
 - \rightarrow In solution Zn²⁺: hydrated and interacted with Cl⁻
- The energy state of Zn²⁺ depends on
- i) the chemical environment by short-range forces
 - \rightarrow chemical potential: μ_i^{α} for species i in phase α
- ii) the energy required to bring the +2 charge to the location in question, disregarding the chemical effects
 - \rightarrow proportional to the potential ϕ at the location
 - $\rightarrow z_i F \varphi^{\alpha}$ for species i with charge z_i in phase α

2.2.4 Electrochemical Potentials

• Introduce the electrochemical potential $\overline{\mu}_{i}^{\alpha}$ for species i with charge z_{i} in phase α

$$\overline{\mu}_{i}^{\alpha} = \mu_{i}^{\alpha} + z_{i}F\phi^{\alpha}$$

- The chemical potential μ_i^{α} is defined as

$$\mu_{i}^{\alpha} = \left(\frac{\partial G}{\partial n_{i}}\right)_{T,P,n_{j\neq i}}$$

 \rightarrow where n_i is the number of moles of i in phase α .

- The electrochemical potential $\overline{\mu}_{i}^{\alpha}$ is defined as

$$\overline{\mu}_{i}^{\alpha} = \left(\frac{\partial \overline{G}}{\partial n_{i}}\right)_{T,P,n_{j\neq i}}$$

 \rightarrow where the electrochemical free energy differs from the chemical free energy, G, by the inclusion of effects from the large-scale electrical environment

(a) Properties of the Electrochemical Potential

- 1. For an uncharged species: $\overline{\mu}_{i}^{\alpha} = \mu_{i}^{\alpha}$ $\overline{\mu}_{i}^{\alpha} = \mu_{i}^{\alpha} + z_{i}F\phi^{\alpha}$
- 2. For any substance: $\mu_i^{\alpha} = \mu_i^{0\alpha} + RT \ln a_i^{\alpha}$
 - → where $\mu_i^{0\alpha}$ is the standard chemical potential, and a_i^{α} is the activity of species i in phase α .
- 3. For a pure phase at unit activity (e.g., solid Zn, AgCl, Ag, or H_2 at unit fugacity):

$$\overline{\mu}_{i}^{\alpha} = \mu_{i}^{0\alpha} \qquad \mu_{i}^{\alpha} = \mu_{i}^{0\alpha} + RT \ln a_{i}^{\alpha}$$

- 4. For electrons in a metal (z = -1): $\overline{\mu}_{e}^{\alpha} = \mu_{e}^{0\alpha} F\phi^{\alpha}$ $\mu_{i}^{\alpha} = \mu_{i}^{0\alpha} + RT \ln a_{i}^{\alpha}$ \rightarrow activity effects can be disregarded
- 5. For equilibrium of species i between phases α and β : $\overline{\mu}_{i}^{\alpha} = \overline{\mu}_{i}^{\beta}$

(b) Reactions in a Single Phase

• Consider the acid-base equilibrium within a single conducting phase:

(ϕ is constant everywhere)

$$HOAc \rightleftharpoons H^+ + OAc^-$$

• At the equilibrium

$$\overline{\mu}_{HOAc} = \overline{\mu}_{H^+} + \overline{\mu}_{OAc^-}$$
$$\mu_{HOAc} = \mu_{H^+} + F\phi + \mu_{OAc^-} - F\phi$$
$$\mu_{HOAc} = \mu_{H^+} + \mu_{OAc^-}$$

- The φ terms drop out of relations involving electrochemical potentials, and only chemical potentials remain.
 - \rightarrow ϕ exerts no effect on a chemical equilibrium.

(c) Reactions Involving Two Phases Without Charge Transfer

- Let us now examine the solubility equilibrium

AgCl (crystal, c) \rightleftharpoons Ag⁺ + Cl⁻ (solution, s),

One can consider separate equilibria involving Ag⁺ and Cl⁻ in solution and in the solid.

$$\overline{\mu}_{Ag}^{AgCl} = \overline{\mu}_{Ag}^{s} + \overline{\mu}_{Cl}^{s} + \overline{\mu}_{Cl}$$

$$\mu_{\rm AgCl}^{0{\rm AgCl}} - \mu_{\rm Ag^+}^{0{\rm s}} - \mu_{\rm Cl^-}^{0{\rm s}} = RT \ln \left(a_{\rm Ag^+}^{\rm s} a_{\rm Cl^-}^{\rm s}\right) = RT \ln K_{\rm sp}$$

: where K_{sp} is the solubility product

- Note that the ϕ^s and ϕ^{AgCl} terms canceled
- Since the final result depends only on chemical potentials
 - → The equilibrium is unaffected by the potential difference across the interface.
 - → This is a general feature of interphase reactions without transfer of charge
- However, when charge transfer does occur,

 \rightarrow the ϕ terms will not cancel and the interfacial potential difference strongly affects the chemical process.

(d) Formulation of a Cell Potential

• Consider the cell written in the form of: Cu/Zn/Zn²⁺,Cl⁻/AgCl/Ag/Cu'

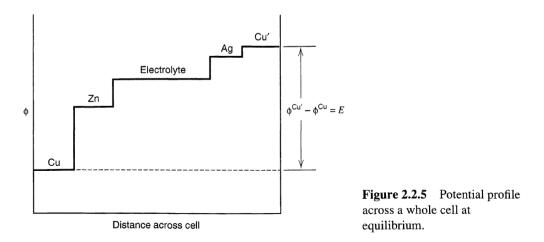
$$\operatorname{Zn} + 2\operatorname{AgCl} + 2e(\operatorname{Cu}') \rightleftharpoons \operatorname{Zn}^{2+} + 2\operatorname{Ag} + 2\operatorname{Cl}^{-} + 2e(\operatorname{Cu})$$

• At the equilibrium

$$\overline{\mu}_{Zn}^{Zn} + 2\overline{\mu}_{AgCl}^{AgCl} + 2\overline{\mu}_{e}^{Cu'} = \overline{\mu}_{Zn^{2+}}^{s} + 2\overline{\mu}_{Ag}^{Ag} + 2\overline{\mu}_{Cl^{-}}^{s} + 2\overline{\mu}_{e}^{Cu}$$

$$2(\overline{\mu}_{e}^{Cu'} - \overline{\mu}_{e}^{Cu}) = \overline{\mu}_{Zn^{2+}}^{s} + 2\overline{\mu}_{Ag}^{Ag} + 2\overline{\mu}_{Cl^{-}}^{s} - \overline{\mu}_{Zn}^{Zn} - 2\overline{\mu}_{AgCl}^{AgCl}$$

$$2(\overline{\mu}_{e}^{Cu'} - \overline{\mu}_{e}^{Cu}) = -2F(\phi^{Cu'} - \phi^{Cu}) = -2FE$$



$$\overline{\mu}_{Zn}^{Zn} + 2\overline{\mu}_{AgCl}^{AgCl} + 2\overline{\mu}_{e}^{Cu'} = \overline{\mu}_{Zn^{2+}}^{s} + 2\overline{\mu}_{Ag}^{Ag} + 2\overline{\mu}_{Cl}^{s} + 2\overline{\mu}_{e}^{Cu}$$

$$2(\overline{\mu}_{e}^{Cu'} - \overline{\mu}_{e}^{Cu}) = \overline{\mu}_{Zn^{2+}}^{s} + 2\overline{\mu}_{Ag}^{Ag} + 2\overline{\mu}_{Cl}^{s} - \overline{\mu}_{Zn}^{Zn} - 2\overline{\mu}_{AgCl}^{AgCl}$$

$$2(\overline{\mu}_{e}^{Cu'} - \overline{\mu}_{e}^{Cu}) = -2F(\phi^{Cu'} - \phi^{Cu}) = -2FE$$

$$-2FE = \mu_{Zn^{2+}}^{0s} + RT \ln a_{Zn^{2+}}^{s} + 2F\phi^{s} + 2\mu_{Ag}^{0Ag} + 2\mu_{Ag}^{0s} - 4RT \ln a_{Cl}^{s} - 2F\phi^{s} - \mu_{Zn}^{0Zn} - 2\mu_{AgCl}^{0AgCl}$$

$$\Delta G^{0} = \mu_{Zn^{2+}}^{0s} + 2\mu_{Cl}^{0s} + 2\mu_{Ag}^{0Ag} - \mu_{Zn}^{0Zn} - 2\mu_{Agcl}^{0AgCl}$$

$$-2FE = \Delta G^{0} + RT \ln a_{Zn^{2+}}^{s} (a_{Cl}^{s})^{2}$$

$$\Delta G^{0} = -2FE^{0}$$

$$E = E^{0} - \frac{RT}{2F} \ln(a_{Zn}^{s})^{2} + (a_{Cl}^{s})^{2},$$

: which is the Nernst equation for the cell.

Determine. Cell rxn? Its emf? Spontaneous?

Pt/H₂/Na⁺, OH⁻ (0.1 M)//Na⁺, OH⁻ (0.1 M)/O₂/Pt

$$O_2 + 2H_2O + 4e \rightleftharpoons 4OH^- \qquad 0.401$$

$$2H_2O + 2e \rightleftharpoons H_2 + 2OH^- \qquad -0.828$$

$$E = E^{0} + \frac{0.0257}{n} \ln \frac{a_{0}^{\nu_{0}}}{a_{R}^{\nu_{R}}} = E^{0} + \frac{0.0591}{n} \log \frac{a_{0}^{\nu_{0}}}{a_{R}^{\nu_{R}}}$$

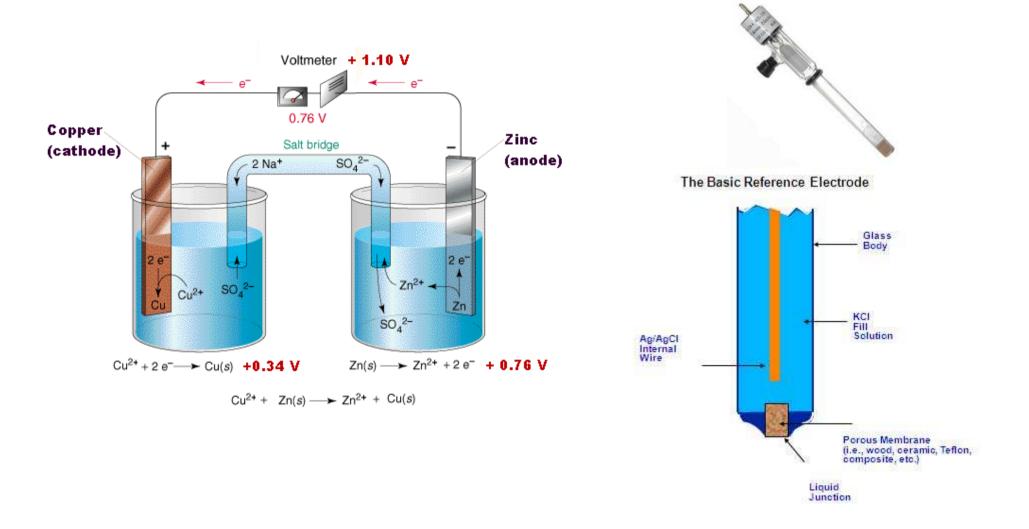
2.3.1 Potential Differences at an Electrolyte-Electrolyte Boundary

2.3 LIQUID JUNCTION POTENTIALS

- To this point, the potential differences in equilibrium electrochemical systems are considered by thermodynamics.
- However, many real cells are not at equilibrium,
- \rightarrow The electrochemical cells include different electrolytes around the two electrodes.
- → An interface between the two solutions where mass transport processes work to mix the solutes.
- → Examples: salt bridge, reference electrode
- Unless the solutions are the same initially,
- → the liquid junction will not be at equilibrium, because net flows of mass occur continuously across it.

2.3.1 Potential Differences at an Electrolyte-Electrolyte Boundary

• Examples for liquid junction: salt bridge, reference electrode



2.3.1 Potential Differences at an Electrolyte-Electrolyte Boundary

• For example,

$$Cu/Zn/Zn^{2+}/Cu^{2+}/Cu'$$

 $\alpha \beta$

• The corresponding equilibrium processes can be described as:

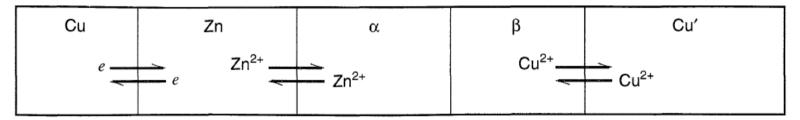


Figure 2.3.1 Schematic view of the phases in cell (2.3.1). Equilibrium is established for certain charge carriers as shown, but at the liquid junction between the two electrolyte phases α and β , equilibrium is not reached.

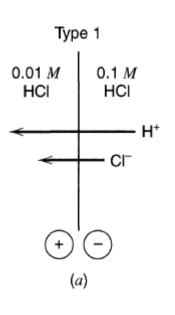
• The overall cell potential (sum of several interfacial differences) at null current is then

$$E = (\phi^{\mathsf{C}\mathsf{u}'} - \phi^{\beta}) - (\phi^{\mathsf{C}\mathsf{u}} - \phi^{\alpha}) + (\phi^{\beta} - \phi^{\alpha}) \quad \Longrightarrow \quad \phi^{\mathsf{C}\mathsf{u}'} - \phi^{\mathsf{C}\mathsf{u}} = E$$

 $E = (\phi^{\mathrm{Cu}'} - \phi^{\beta}) - (\phi^{\mathrm{Cu}} - \phi^{\alpha}) + (\phi^{\beta} - \phi^{\alpha})$

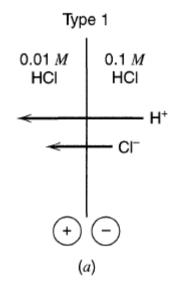
the interfacial potential differences at the copper and zinc electrodes the potential difference
between the electrolytes,
→ Liquid junction potential.

2.3.2 Types of Liquid Junctions

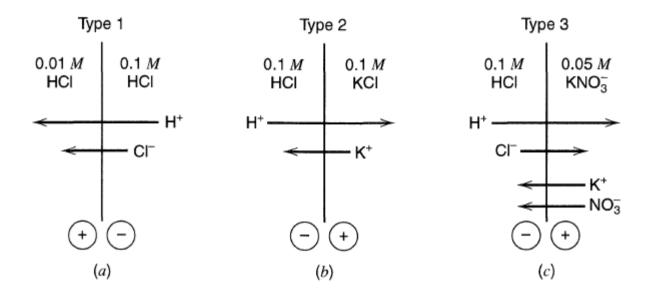


- Consider the boundary shown in the figure
- At the junction, there is a steep concentration gradient in H⁺ and Cl⁻
 → Hence both ions tend to diffuse from right to left.
- Since the H⁺ has a much larger mobility than Cl⁻,
 - \rightarrow H⁺ initially penetrates the dilute phase at a higher rate.
- This process gives
 - → a positive charge to the dilute phase and a negative charge to the concentrated one,
 - \rightarrow Results in that a boundary potential difference develops.
- However, the corresponding electric field then retards the movement of H⁺ and speeds up the passage of Cl⁻
- → until the two cross the boundary at equal rates (migration vs diffusion).

2.3.2 Types of Liquid Junctions



- Thus, there is a detectable steady-state potential,
 - \rightarrow which is not due to an equilibrium process
 - \rightarrow From its origin, this interfacial potential is sometimes called a diffusion potential.
- Even though the boundary region cannot be at equilibrium,
 - \rightarrow it has a composition that is effectively constant over long time period



- Classify liquid junctions into three types:
- 1. Figure (a): Two solutions of the same electrolyte at different concentrations
- 2. Figure (b): Two solutions at the same concentration with different electrolytes having an ion in common
- 3. Figure (c): Two solutions not satisfying conditions 1 or 2

Conductance, Transference Numbers, and Mobility

• Consider the cell:

 $\bigcirc Pt/H_2(1 \text{ atm})/H^+, Cl^-/H^+, Cl^-/H_2(1 \text{ atm})/Pt' \oplus \\ (a_1) (a_2) (a_2) (a_2) (a_2) (a_2) (a_3) (a_3)$

• When the cell operates galvanically,

 \rightarrow an oxidation occurs at the left electrode,

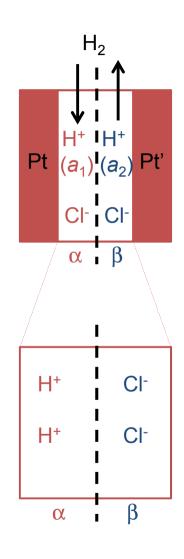
 $H_2 \rightarrow 2H^+(\alpha) + 2e(Pt)$

- And a reduction happens on the right,

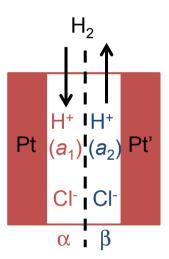
 $2\mathrm{H}^+(\beta) + 2e(\mathrm{Pt}') \rightarrow \mathrm{H}_2$

- Therefore, there is a tendency to build up

 \rightarrow a positive charge in the α phase and a negative charge in β .

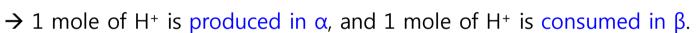


Given that $a_1 = 0.01 \text{ M}$, $a_2 = 0.1 \text{ M}$, *emf*?



2.3.2 Types of Liquid Junctions

- This tendency is overcome by the movement of ions (electroneutrality):
 - \rightarrow H⁺ to the right and Cl⁻ to the left.
- For each mole of electrons passed,



- → The total amount of H⁺ and Cl⁻ migrating across the boundary between α and β must equal 1 mole.
- The fractions of the current carried by H⁺ and Cl⁻

→ are called their transference numbers (or transport numbers).

• If we let t_+ be the transference number for H^+ and t_- be that for Cl^- , then clearly,

$$t_{+} + t_{-} = 1$$

 \rightarrow In general, for an electrolyte containing many ions, i,

$$\sum_{i} t_{i} = 1$$

H+

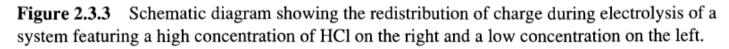
α

Cl

Cl-

β

(a)
$$Pt/H_2/\frac{+}{-} \frac{+}{-} / \frac{+}{-} \frac{+}{-}$$



- (a) The cell initially features a higher activity of hydrochloric acid (+ as H⁺, as Cl⁻) on the right
- (b) hence discharging it spontaneously produces H+ on the left and consumes it on the right. → Assume that five units of H⁺ are reacted.
- (c) For hydrochloric acid, $t_{\scriptscriptstyle +}$ ~ 0.8 and $t_{\scriptscriptstyle -}$ ~ 0.2
 - → Therefore, four units of H⁺ must migrate to the right and one unit of Cl⁻ to the left to maintain electroneutrality.
- (d) The final state of the solution

- Transference numbers are determined by the kinetics of ionic conduction (resistance or conductance)
- The value of conductance L for a segment of solution immersed in an electric field is defined as

$$L = \kappa A/l$$

- \rightarrow directly proportional to the cross-sectional area (A) perpendicular to the field vector
- \rightarrow inversely proportional to the length (I) of the segment along the field.
- \rightarrow The proportionality constant is the conductivity, κ ,
 - : which is an intrinsic property of the solution
- Conductance, L,
- \rightarrow is given in units of siemens (S = Ω^{-1}),
- Conductivity, к
- \rightarrow is expressed in S cm⁻¹ or Ω^{-1} cm⁻¹

 Since the passage of current through the solution is accomplished by the independent movement of different species

 \rightarrow κ : the sum of contributions from all ionic species, i.

• Each component of κ

 \rightarrow is proportional to the concentration of the ion, the magnitude of its charge $|z_i|$, and some index of its migration velocity.

$$\kappa = F \sum_{i} |z_{i}| u_{i} C_{i}$$

- That index is the mobility, u_i
- \rightarrow The limiting velocity of the ion in an electric field of unit strength.
- → Mobility usually carries dimensions of $cm^2 V^{-1} s^{-1}$ (i.e., cm/s per V/cm).

- When a field of strength & is applied to an ion,
- \rightarrow It will accelerate under the force imposed by the field until the frictional drag exactly counterbalances the electric force.
- \rightarrow Then, the ion continues its motion at that terminal velocity.

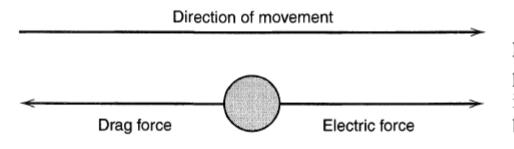


Figure 2.3.4 Forces on a charged particle moving in solution under the influence of an electric field. The forces balance at the terminal velocity.