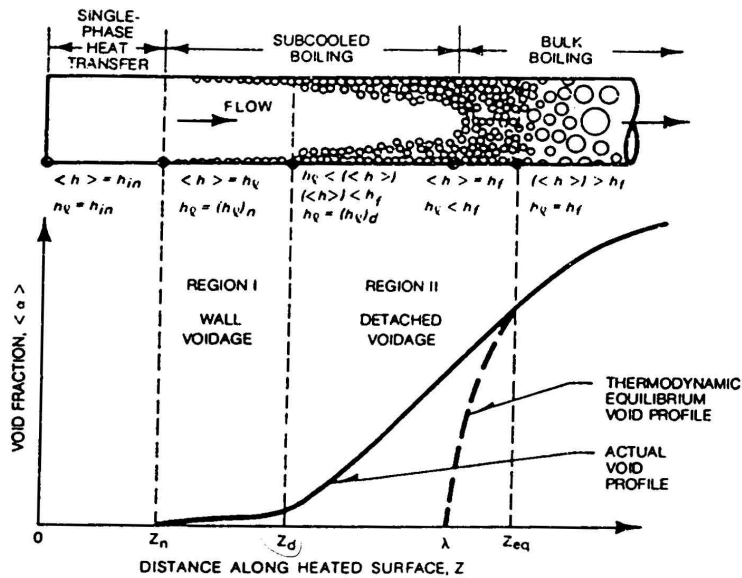
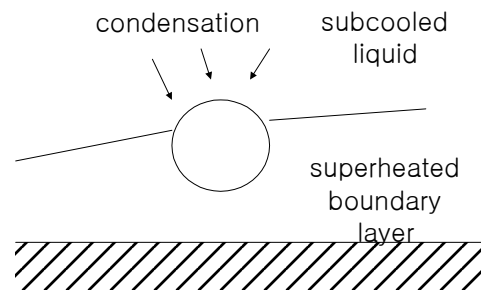


## IV. Subcooled Boiling Model



- ✓ bubble formation
- ✓ bubble condensation
- ➔ complicate phenomena



For calculating the void fraction in subcooled boiling, we have to know

1.  $Z_n, (h_f)_z$
2.  $Z_d, (h_f)_z$
3.  $h_f(z)$  or  $\delta w'$ 
  - thermodynamic nonequilibrium ( $h_f \neq h_c$ )
4. recondensation ratio of the detached bubbles
5. slip ratio

(1) Determination of void departure point,  $Z_d$

- wall voidage region
- detached voidage region
- location of the initial void ejection into the subcooled liquid core
- determined by the void departure criterion of Table 5-1

(2) Heat removal mechanism from the heated surface during subcooled boiling

1- latent heat to form the vapor,  $q''_{evap}$

$$q''_{evap} = V_{if} \rho_v h_{fg} \quad \text{where} \quad V_{if} = n f B_d \quad (1.11)$$

2- by convection caused by bubble agitation or pumping by boundary layer,

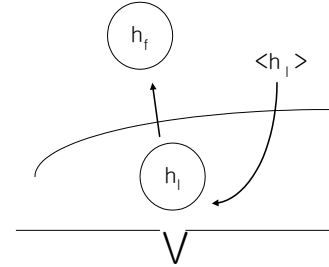
$$q''_{pump}$$

$q''_{pump}$  = energy flux to raise from  $\langle h_f \rangle$  to  $h_f$

+ energy flux for saturation

$$= V_{if} [\rho_f (h_f - \langle h_f \rangle) + \rho_v (h_f - h_g)]$$

$$(1.12)$$



Bowling(1962) defined

$$\begin{aligned} \varepsilon &= \frac{q''_{pump}}{q''_{evap}} = \frac{\rho_f (h_f - \langle h_f \rangle) + \rho_v (h_f - h_g)}{\rho_v h_{fg}} \\ &\approx \frac{\rho_f (h_f - h_g)}{\rho_v h_{fg}} \end{aligned} \quad (1.13)$$

3- by condensation at the top of growing bubble while still attached to the wall

4- single phase convection,  $q''_{1\phi}$

Neglecting the third mechanism,

$$q'' = q''_{1\phi} + q''_{evap} + q''_{pump} \quad (1.14)$$

(3) Models to determine the void fraction profile in subcooled boiling region

- profile fit model
- mechanistic model

1- Profile Fit Model by Levy

Assume  $h = h_c (\langle h \rangle)$

$$\text{i.e.} \quad \frac{h_c - h}{h_c - (h_c)_{fd}} = F \left[ \frac{\langle h \rangle - (h_c)_{fd}}{h_c - (h_c)_{fd}} \right] \quad (1.15)$$

B. C :  $F = 1$  at  $h = (h_c)_{fd}$

$F > 0$  for  $\langle h \rangle \gg h_c$

The function that satisfy these requirements are the form of  $F = \text{EXP}$

$$\therefore \frac{h_c - h}{h_c - (h_c)_{fd}} = \exp \left[ - \frac{\langle h \rangle - (h_c)_{fd}}{h_c - (h_c)_{fd}} \right] = F \quad (1.16)$$

Since

$$\begin{aligned} \langle X(z) \rangle &= \frac{\langle h(z) \rangle - h_c(z)}{h_v - h_c(z)} \\ \therefore \langle x \rangle &= \frac{\langle h \rangle - h_c + [h_c - (h_c)_{id}]F}{h_v + [h_c - (h_c)_{id}]F} \end{aligned} \quad (1.17)$$

Then,

$$\begin{aligned} \langle x \rangle &= \frac{\langle h \rangle - h_c}{h_v} + \frac{h_c - (h_c)_{id}}{h_v} F \\ \therefore \langle x \rangle &= \langle x \rangle + \langle x \rangle_{id} F \end{aligned}$$

Finally,

$$\langle x \rangle = \langle x \rangle + \langle x \rangle_{id} \exp\left(\frac{\langle x \rangle}{\langle x \rangle_{id}} - 1\right) \quad (1.18)$$

Now from the flow quality, we can obtain the void fraction from void quality correlation.

(10) Zuber-Findley-Void Quality Correlation

$$\langle \alpha \rangle = \frac{\langle x \rangle}{C_v \left[ \langle x \rangle + \frac{\rho_v}{\rho_l} (1 - \langle x \rangle) \right] + \frac{\rho_v V_{wz}}{G}}$$

Modified Armand model

$$\langle \alpha \rangle = \frac{(0.833 + 0.167 \langle x \rangle) \langle x \rangle v_v}{(1 - \langle x \rangle) v_l + \langle x \rangle v_p}$$

2) Mechanistic Model

1) Determination of the void departure point

neglect the wall voidage region

solve the energy balance equation to calculate  $\langle h_f(z) \rangle$

find the position which satisfy Zuber-Saha correlation,

$$h_c = (h_f)_{id} = \begin{cases} 0.0022 \frac{q'' D_{eff} C_{eff}}{k_f}, & \text{for } Pe = \frac{GD_{eff} C_{eff}}{k_f} < 70,000 \\ 151 q'' / G, & \text{for } Pe > 70,000 \end{cases} \quad (1.19)$$

2) Void propagation equation

$$\frac{\partial \langle \alpha \rangle}{\partial t} + C_R \frac{\partial \langle \alpha \rangle}{\partial z} = \left( \frac{\rho_v}{\rho_l} - C_v \langle \alpha \rangle \right) \Omega \quad (1.10)$$

where  $C_R = C_v \langle \beta \rangle + V_{wz}$

and the characteristic frequency of the phase change is defined as,

$$\Omega = c_{\alpha} \Gamma$$

The net amount of vapor formed per unit volume for constant pressure is,

$$\Gamma = \frac{p_H q''_s(Z, t)}{A_{v, \infty} h_{v, \infty} [1 + \varepsilon(Z, t)]} - \frac{p_H q''_{cond}(Z, t)}{A_{v, \infty} h_{v, \infty}} \quad (1.11)$$

3) Condensation heat transfer

$$p_H q''_{cond} = \frac{H_v h_{v, \infty} A_{v, \infty} \langle \alpha \rangle}{c_p} = T_{sat} \quad (1.12)$$

where  $H_v$  is a condensation coefficient.

4) Ratio of the heat flux due to microconvection to that causing vapor formation is given by Rouhani as,

$$\varepsilon(Z, t) = \frac{\rho_v (h_v - h_l)}{\rho_v h_{v, \infty}} \quad (1.13)$$

And the boiling heat flux is approximated as,

$$q''_s(Z, t) = q''(Z, t) \left[ 1 - \frac{h_v - h_l(Z, t)}{h_v - h_l(t)} \right] \quad (1.14)$$

Inserting Eqs. (1.12), (1.13) and (1.14) into Eq. (1.11),

$$\Omega(Z, t) = \frac{-\rho p_H q''}{A_{v, \infty} \rho_v (h_v - h_l)} - \frac{h_l - h_l(Z, t)}{\rho_v h_{v, \infty} + \rho_v (h_v - h_l)} - \frac{H_v \langle \alpha \rangle}{c_p} (h_v - h_l) \quad (1.15)$$

5) The energy equation of the two mixture is given as,

$$\frac{-\rho}{\rho_v} (1 - \langle \alpha \rangle) \frac{\partial h_l}{\partial t} + (1 - \langle \alpha \rangle) G (1 - \langle \alpha \rangle) \frac{\partial h_l}{\partial z} = \frac{q'' p_H W_v}{A_{v, \infty}} \quad \Omega(h_v - h_l) \quad (1.16)$$

where the assumptions used are :

- i) The internal heat generation,  $q'''$ , is neglected.
- ii) The kinetic and potential energy term are neglected.
- iii) The state is steady.
- iv) The vapor is saturated.

6) The drift flux parameters

- A** system constant parameters : Dix model, constant values  $\frac{1}{2}$
- B** void dependent model : Okawa Lahey model

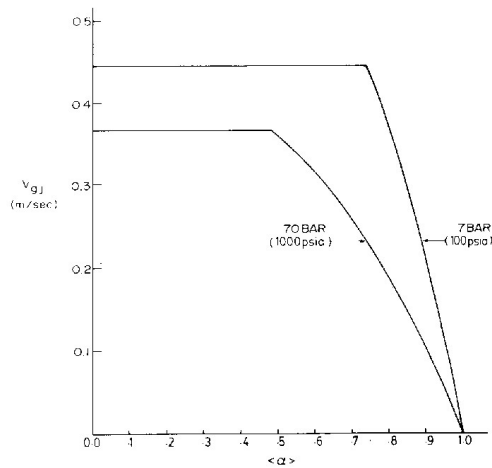


Figure 16

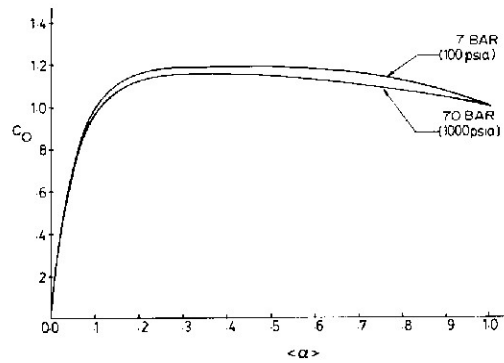


Figure 17

- Finally, we have to solve the each coupled equations, (4.1.10), (4.1.15) and (4.1.16) with void dependent drift flux parameters.

**[Example]**

A 12ft long and rectangular fuel channel has uniform axial heat flux,  $\dot{q}_o''$  ( $= 55,56 \text{ Btu/ft}^2 \text{ sec}$ ), under constant pressure, 1000 psia, the inlet coolant velocity is 12ft/sec. Size and radius of channel and fuel are 0.65 and 0.225 in, respectively.

- (a) Determine the void departure point with inlet liquid enthalpy of 511.9 Btu/lbm.
- (b) Calculate the exit thermal equilibrium quality.
- (c) Extend your calculation to determination of exit flow quality.
- (d) Finally, what is the exit void fraction ?

**[Answer]**

(a) Void departure point,  $Z_0$

$$Pe = \frac{GD_{eff}c_{pl}}{k_f}$$

$c_{pl}$  :  $k_f$  for 500°F water = 1.176 Btu/lb°F ;  $9.76 \times 10^{-3} \text{ Btu/ft}^2 \text{ °F sec}$

$D_{eff} = 1A/P = 0.335 \text{ ft}$  ;  $G = 17.85 \times 12 = 571.2 \text{ lbm/ft}^2 \text{ sec}$

$$\therefore Pe = 2.32 \times 10^6 \approx 70,000$$

From Saha and Zuber's Eq.,

$$h_c = (h_f)_d = 154 \dot{q}''/G \quad \text{for } Pe > 70,000$$

$$= 154 \times 55.56 = 571.2 = 11.9 \text{ Btu/lbm}$$

$$\therefore (h_f)_c = h_c = 11.9 = 527.5 \text{ Btu/lbm}$$

From energy equation : ROC of energy,

$$w(h_f)_c - \dot{q}_0'' P Z_d - w h_f = 0$$

$$\therefore Z_d = 2.5 \text{ ft}$$

(b) thermal equilibrium quality profile

ROC of energy

$$w(h(z)) - \dot{q}_0'' P z = w h_f = 0$$

$$h(z) = (1 - x_c) h_f + x_c h_c$$

$$\therefore x_c = \frac{(\dot{q}_0'' P z - L)(w + h_{fg}) - h_c}{h_{fg}}$$

$$= (71.7 - 511.9 - 512.0) / 619.1 = 6.8 \%$$

(c) exit flow quality

$$\langle x \rangle = \langle x_c \rangle = \langle x_c \rangle_d \exp\left(\frac{\langle x_c \rangle}{\langle x_c \rangle_d} - 1\right)$$

$\langle x_c \rangle_d$

$$\langle x_c \rangle_d = \frac{(\dot{q}_0'' P Z_d)(w + h_{fg}) - h_c}{h_{fg}}$$

$$= (15.6 + 511.9 - 512.0) / 619.1 = 0.023$$

$$\therefore \langle x \rangle = 0.068 = (0.023) \exp\left(\frac{0.068 - 0.023}{0.023} - 1\right)$$

$$= 0.068 + 1.38 \times 10^{-1} = 0.68$$

(d) exit void fraction

Apply Zuber-Findley correlation. Or from Modified Armand model,

$$\langle \alpha \rangle = \frac{(0.833 + 0.167 \langle x \rangle) \langle x \rangle c_v}{(1 - \langle x \rangle) c_l + \langle x \rangle c_v}$$

$$= (0.833 + 0.167 \times 0.68) \times 0.68 \times 0.1156 / (1 - 0.31)$$

$$= 92.5\%$$