

2009 spring

Advanced Physical Metallurgy
“Amorphous Materials”

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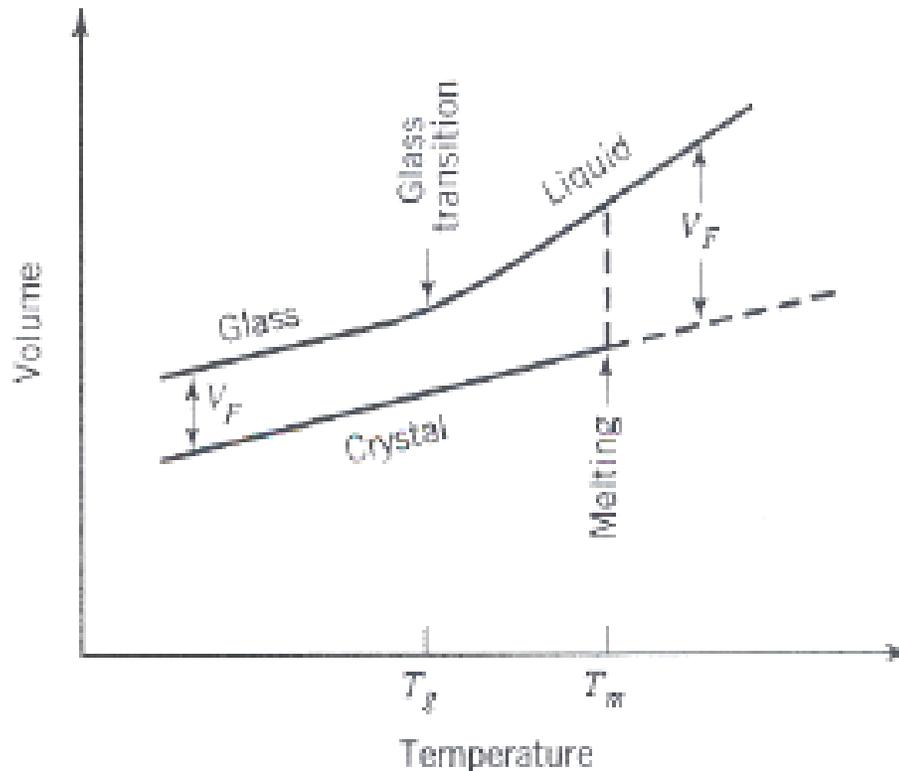
Office hours: by an appointment ¹

Contents for previous class

- **Free volume and the glass transition**
 - **Glass transition**
 - **Classification of phase transition**
 - **Glass: Solid? or liquid?**
 - **Amorphous vs Nanocrystalline**
 - 1) ***Microstructural observation***
 - 2) ***Thermal analysis***
 - ***DSC (Differential Scanning Calorimetry)***
- **local clusters with atomic scale are difficult to identify by conventional observation tools of microstructure.**
: ***Characterization of structure by pair distribution function***

Free volume and the glass transition

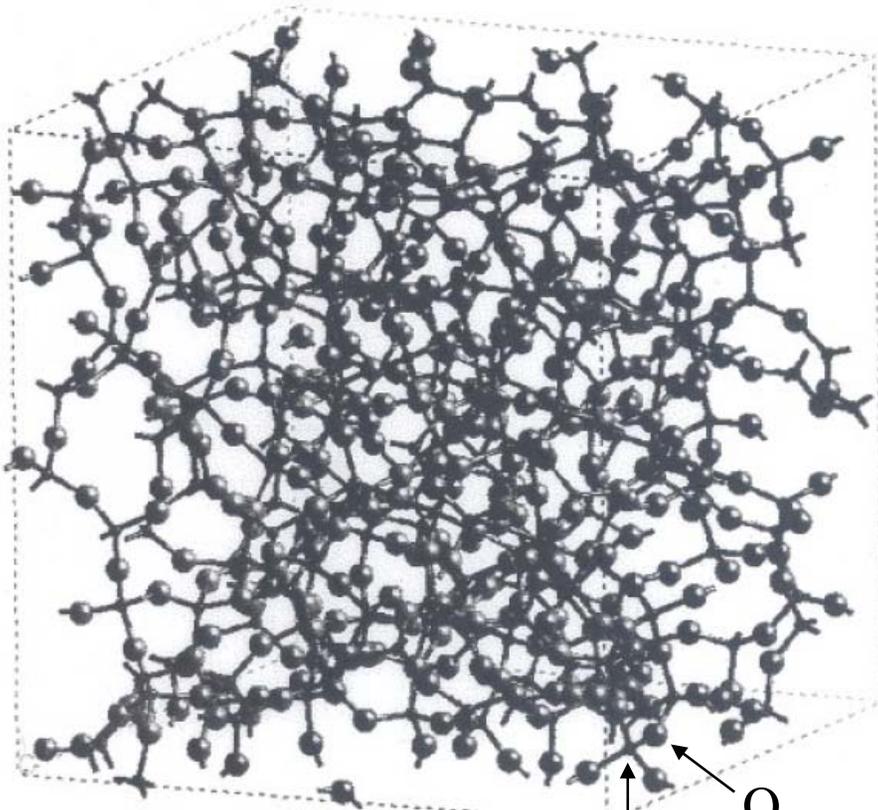
Free volume = specific volume (volume per unit mass) of glass - specific volume of the corresponding crystal



At the glass transition temperature, T_g , the free volume increases leading to atomic mobility and liquid-like behavior. Below the glass transition temperature atoms (ions) are not mobile and the material behaves like solid

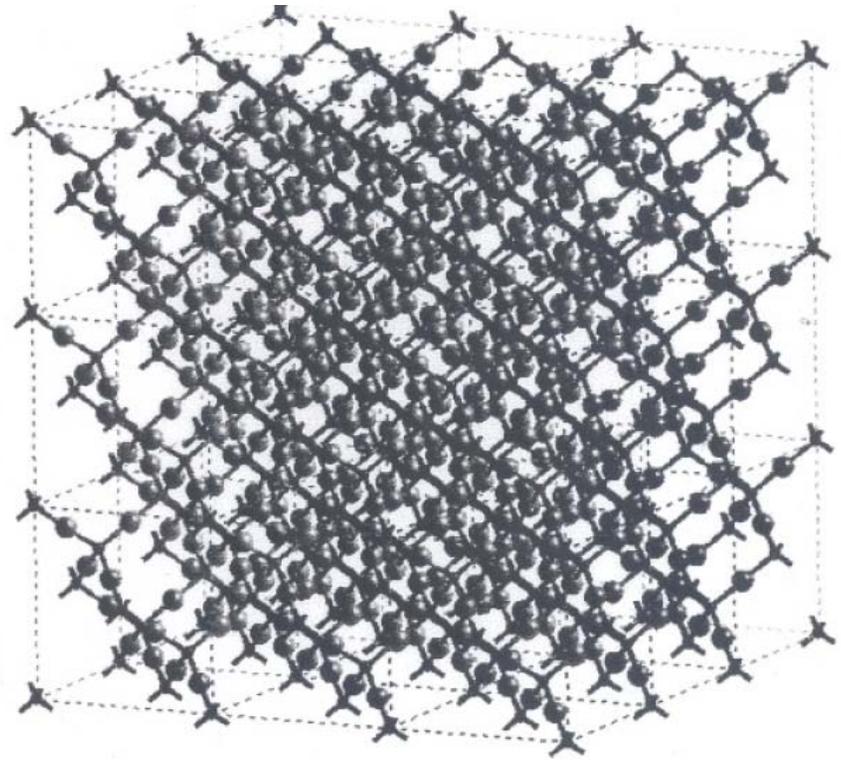
Silica - SiO_2

Amorphous silica

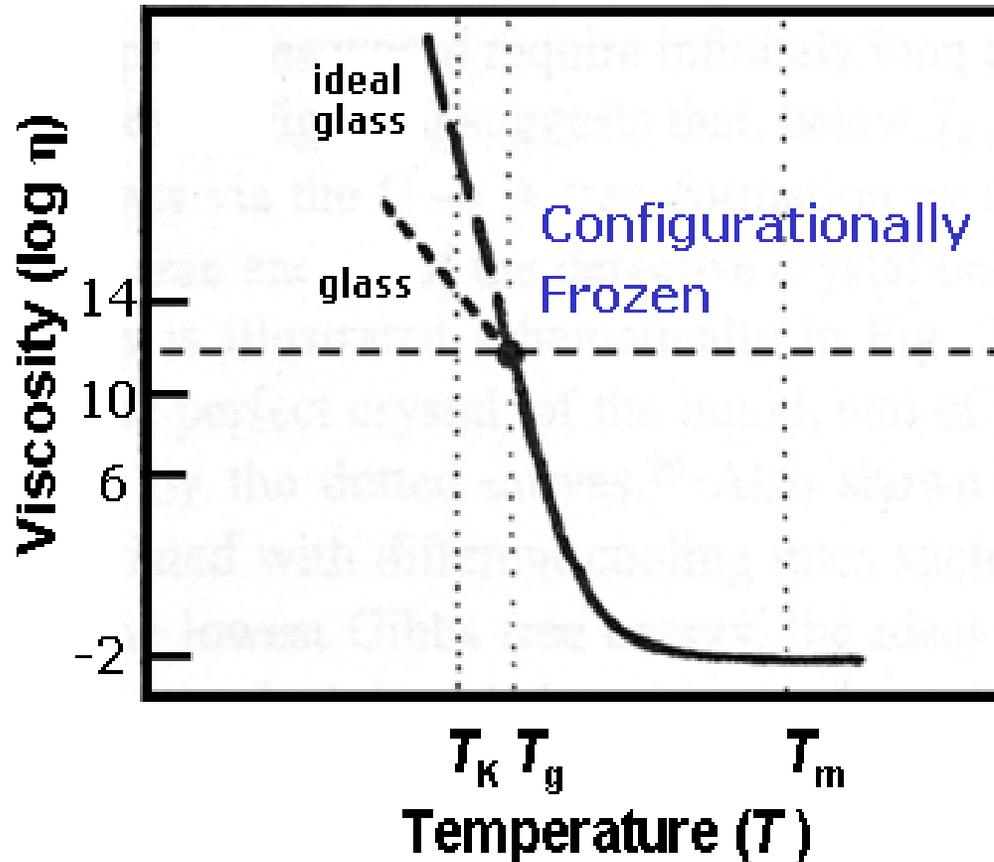


Si
O

Crystalline SiO_2



Glass : undercooled liquid with high viscosity



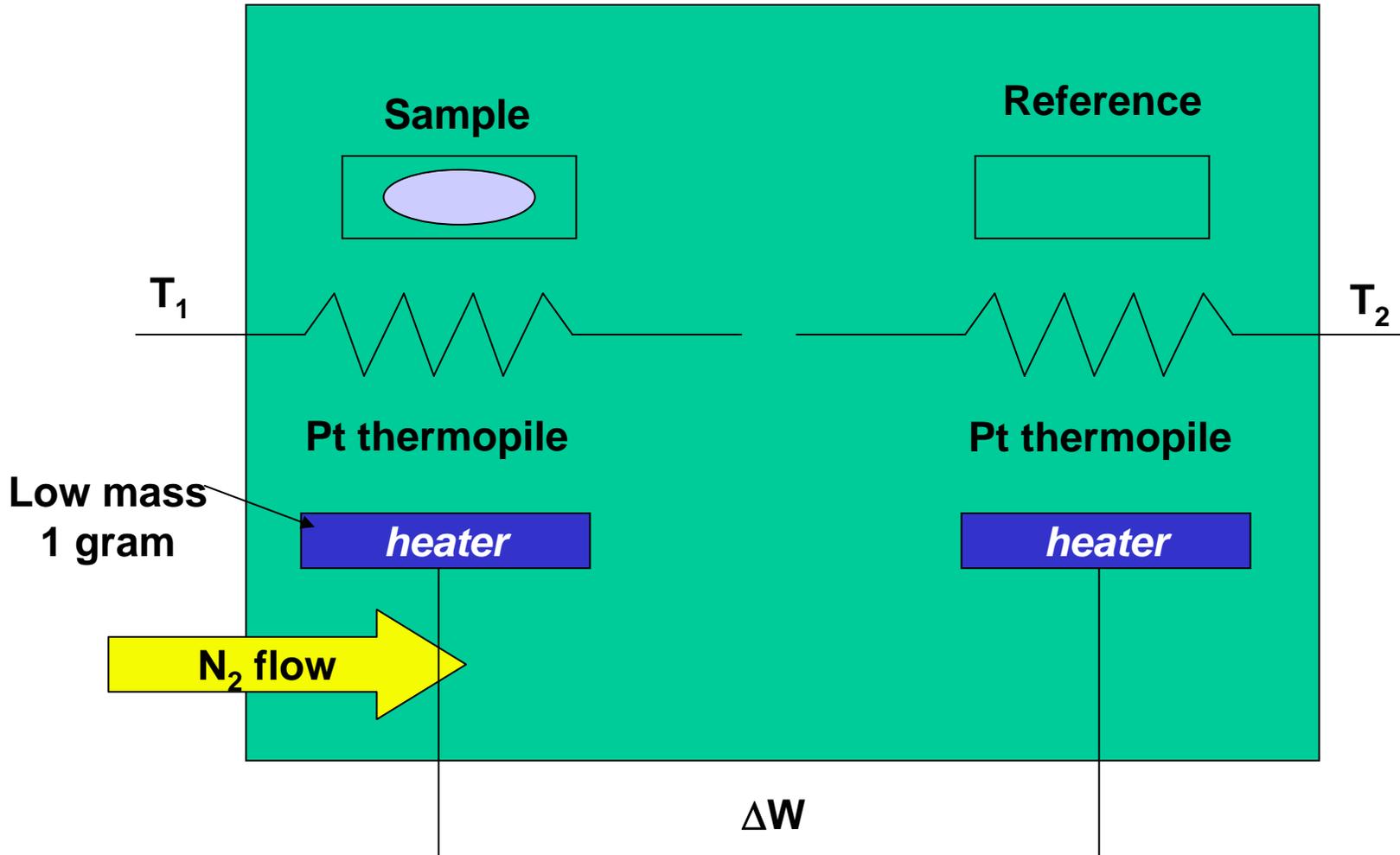
A solid is a materials whose viscosity exceeds $10^{14.6}$ poise

cf) liquid $\sim 10^{-2}$ poise

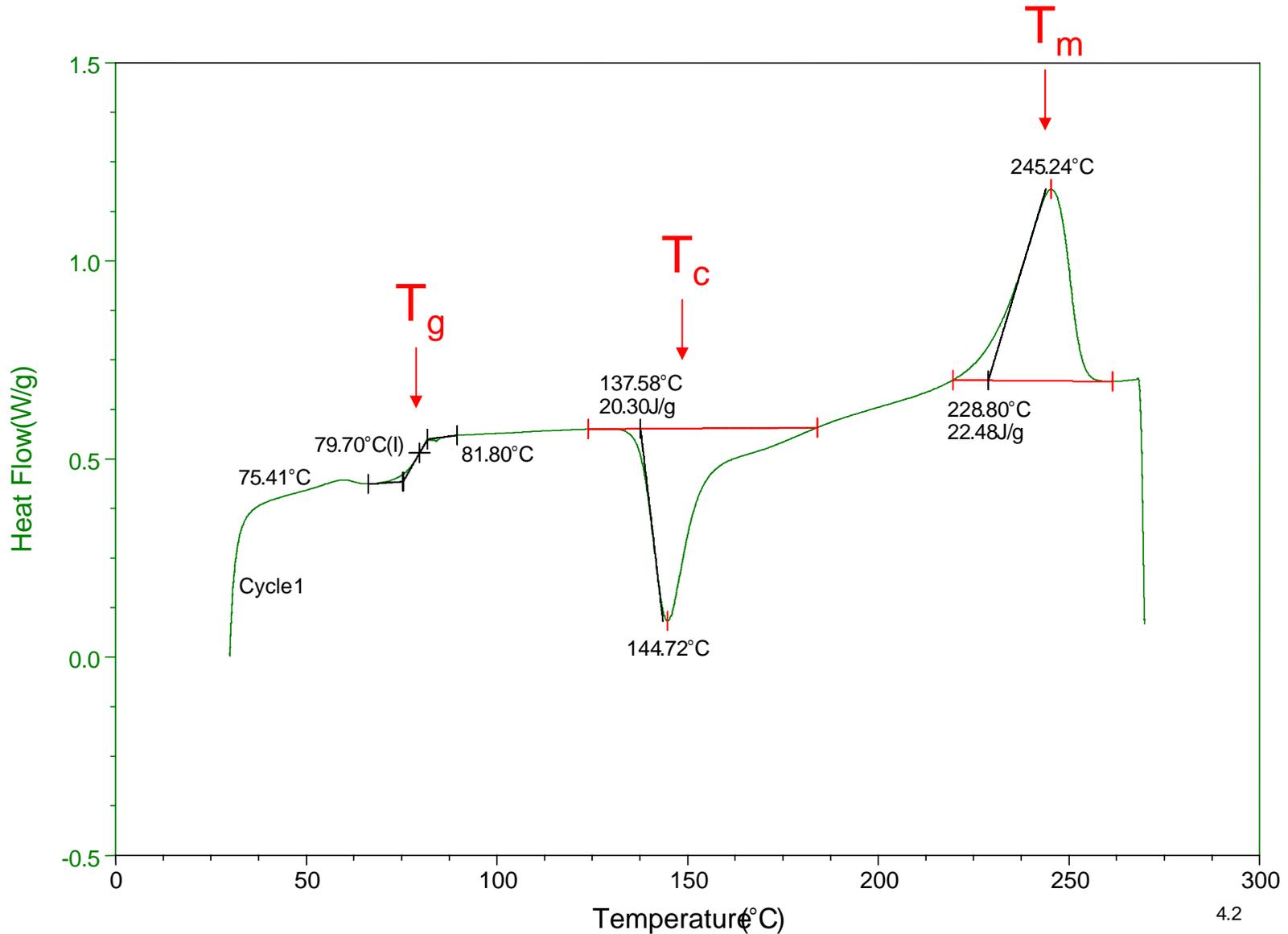
Definitions

- A *calorimeter* measures the heat into or out of a sample.
- A *differential calorimeter* measures the heat of a sample relative to a reference.
- A *differential scanning calorimeter* does all of the above and heats the sample with a linear temperature ramp.
- Differential Scanning Calorimetry (DSC) **measures** the **temperatures** and **heat flows** associated with transitions in materials as a function of time and temperature in a controlled atmosphere.

Schematic of DSC Instrument



Example DSC – PET (polyethylene terephthalate)



What Can You Measure with DSC?

- **Glass transitions**
- **Melting and boiling points**
- **Crystallization time and temperature**
- Percent crystallinity
- **Heats of fusion and reactions**
- Specific heat capacity
- Oxidative/thermal stability
- **Rate and degree of cure**
- Reaction kinetics
- Purity

Contents for today's class

- **Amorphous vs Nanocrystalline**

- 1) *Microstructural observation*

- 2) ***Thermal analysis***

- ***DSC (Differential Scanning Calorimetry)***

- **local clusters with atomic scale are difficult to identify by conventional observation tools of microstructure.**

- : Characterization of structure by pair distribution function***

- 3) ***Intensive Structural Analysis: radial distribution function***

- **Amorphous vs Nanocrystalline**

1) *Microstructural observation*
XRD, (HR)TEM, EXAFS ...

2) **Thermal analysis**

DSC (Differential Scanning Calorimetry)

: Measure heat absorbed or liberated during heating or cooling

cf) - **glass** → **nucleation & growth**
(perfect random)

- **local clustering**: quenched-in nuclei → **only growth**

- **Nanocrystalline** → **growth**

→ local clusters with atomic scale are difficult to identify by conventional observation tools of microstructure.

: *Characterization of structure by pair distribution function*

3) *Intensive Structural Analysis: radial distribution function*

- **Chen & Sapepen (Harvard,1988)**

glass → **nucleation & growth**
(perfect random)

→ Isothermal annealing
: rapid heating + maintain the temp.



- **Glass :**

$$x = 1 - \exp(-bt^n) \quad (n: 2\sim 4, \text{ nucleation mechanism})$$

crystallized volume fraction after time t

→ **Corresponding heat release**

$$-\frac{dH}{dt} = \Delta H (1-x)n \cdot bt^{n-1}$$

(ΔH : total transformation enthalpy)

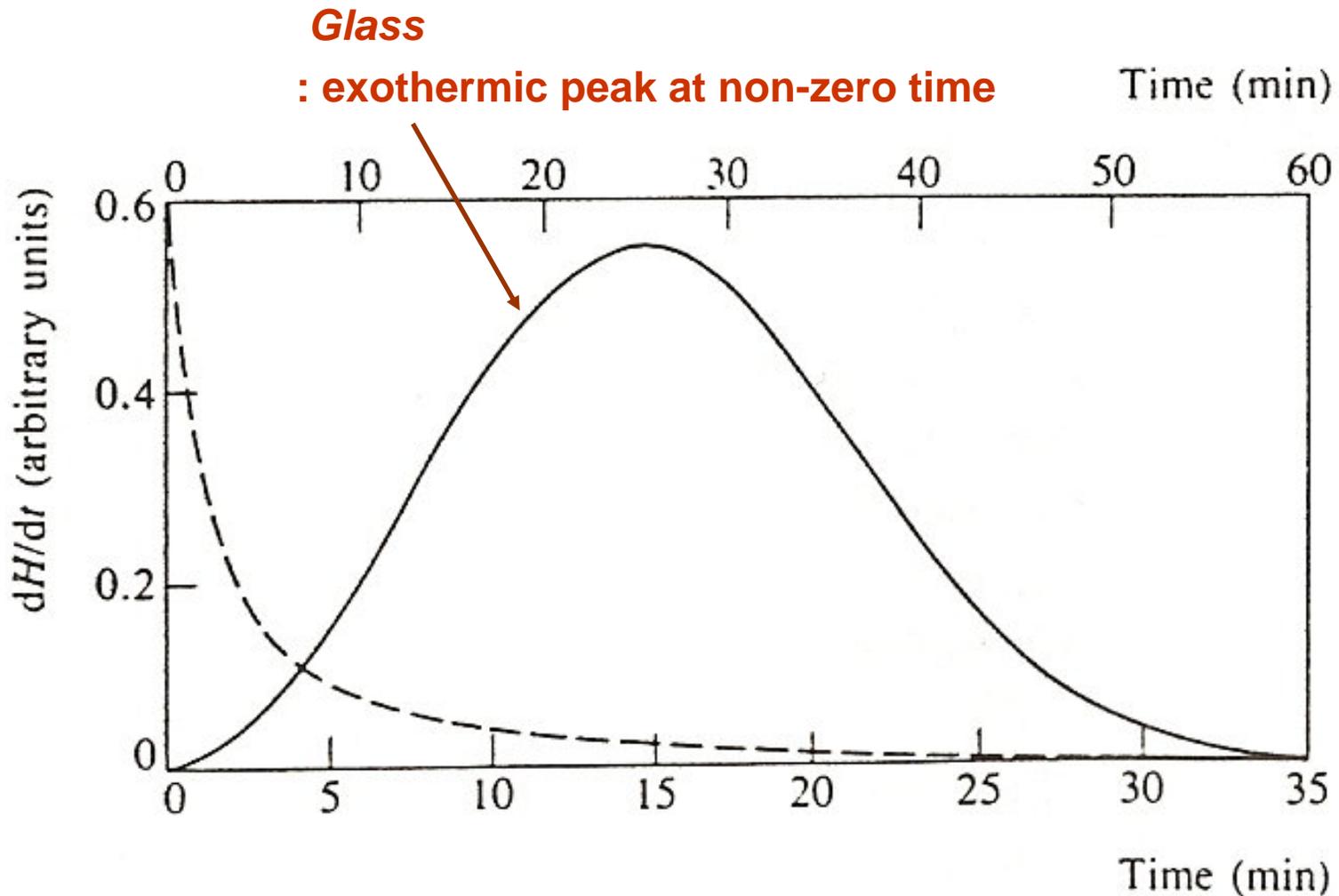


Fig. 1.4 Isothermal enthalpy release rates for crystallite nucleation and growth (solid line) and crystallite grain-coarsening mechanisms (dashed line)

- **Nanocrystalline** → **grain growth**

$$\rightarrow \frac{dr}{dt} = M \cdot \frac{\gamma}{r^m}$$

(*M*: atomic mobility, *γ*: interfacial surface tension)

→ corresponding heat release

$$-\frac{dH}{dt} = H(0) \cdot r(0) \cdot M\gamma / r^{m+2}$$

(*H*(0): zero time enthalpy of a grain size of *r* (0))

→ **Monotonically decreasing curve**

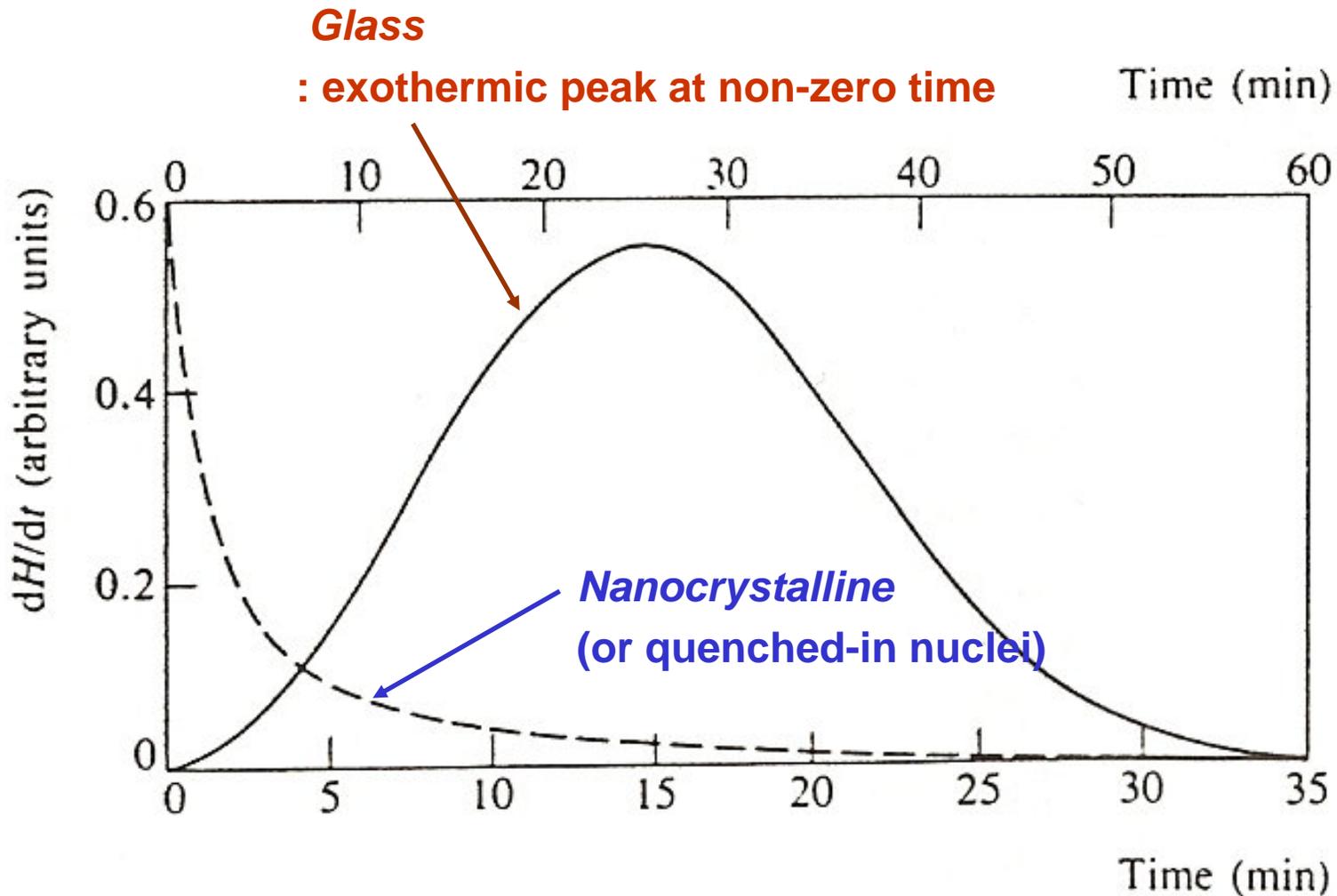


Fig. 1.4 Isothermal enthalpy release rates for crystallite nucleation and growth (solid line) and crystallite grain-coarsening mechanisms (dashed line)

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XRD, (HR)TEM, EXAFS ...

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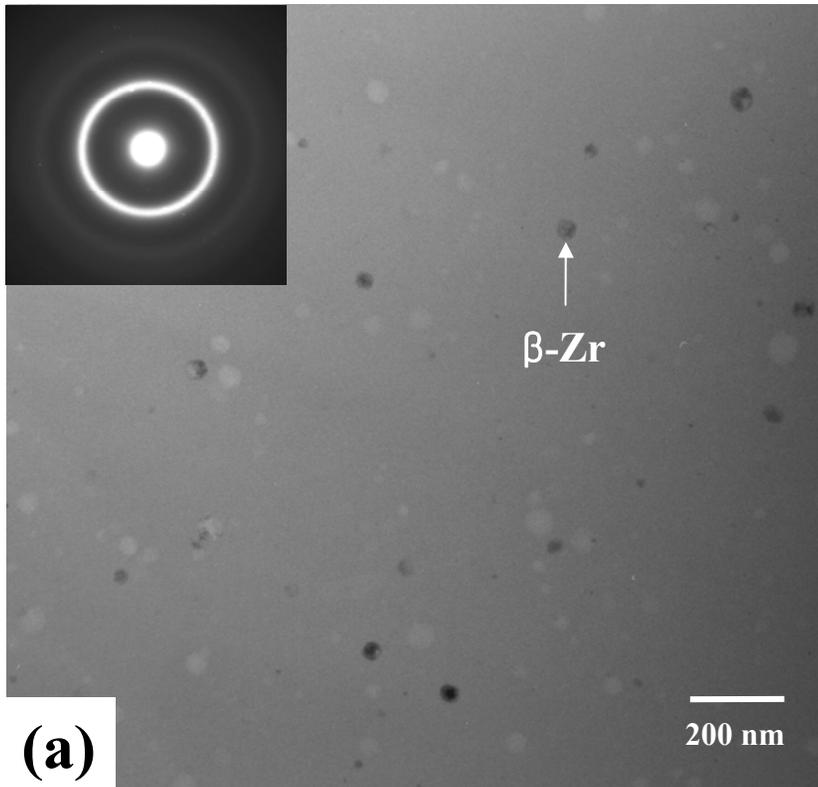
→ ***local clusters with atomic scale are difficult to identify by conventional observation tools of microstructure.***

: Characterization of structure by pair distribution function

3) ***Intensive Structural Analysis: radial distribution function***

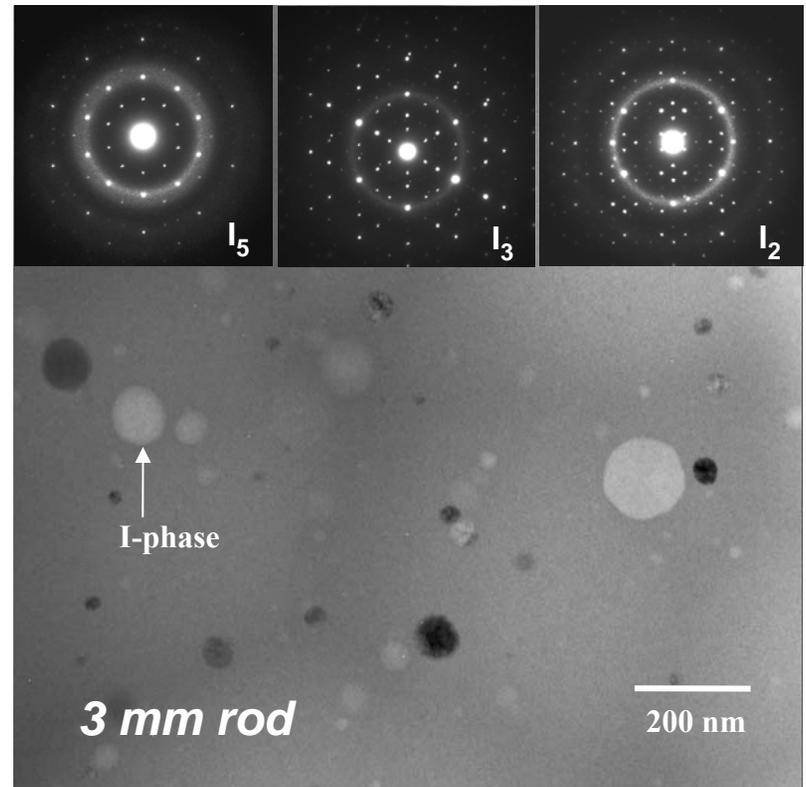
Effect of quenched-in quasicrystal nuclei

2 mm rod



(a)

β -Zr particle (~70 nm) in amorphous matrix



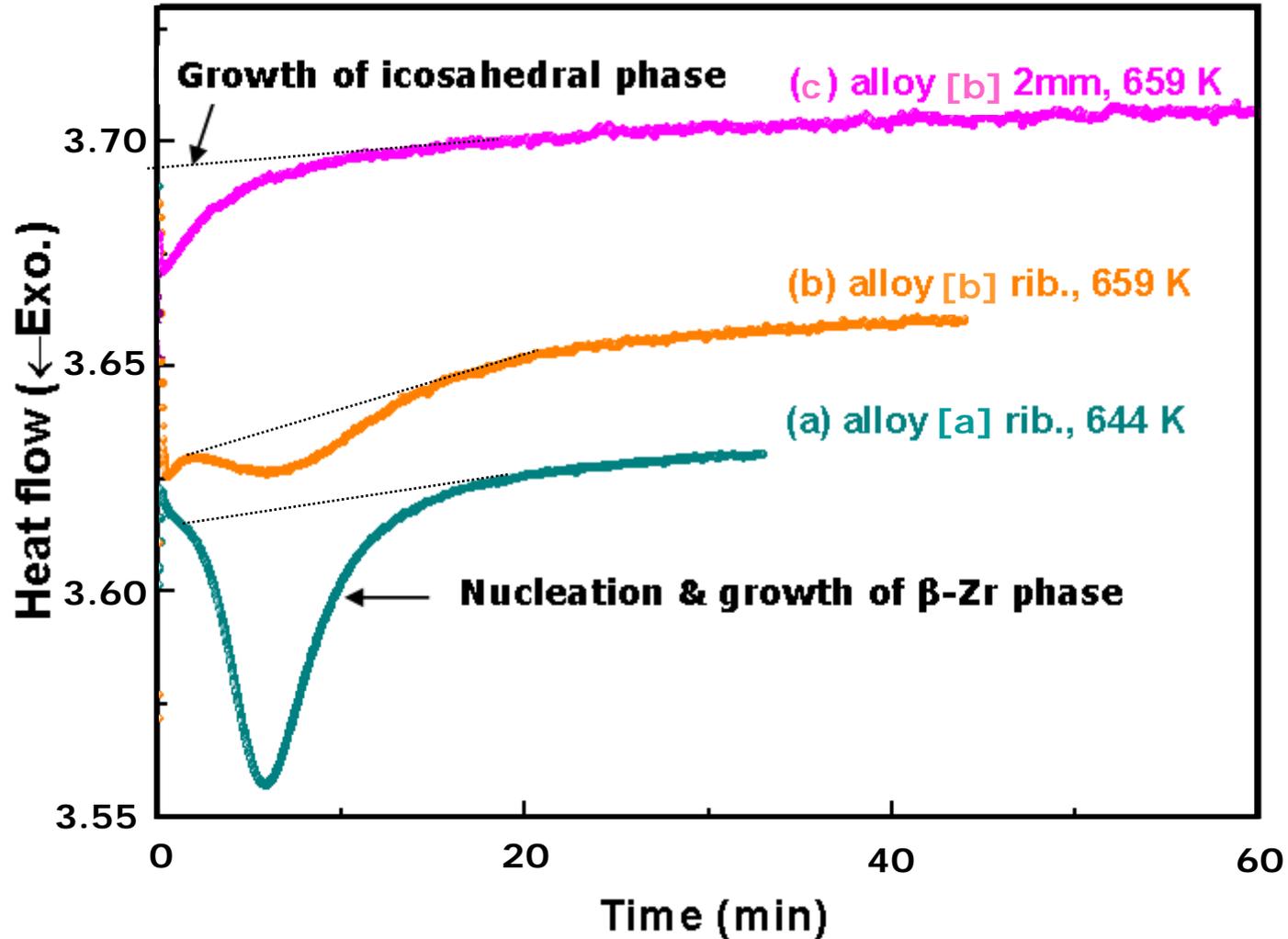
3 mm rod

Fully amorphous structure

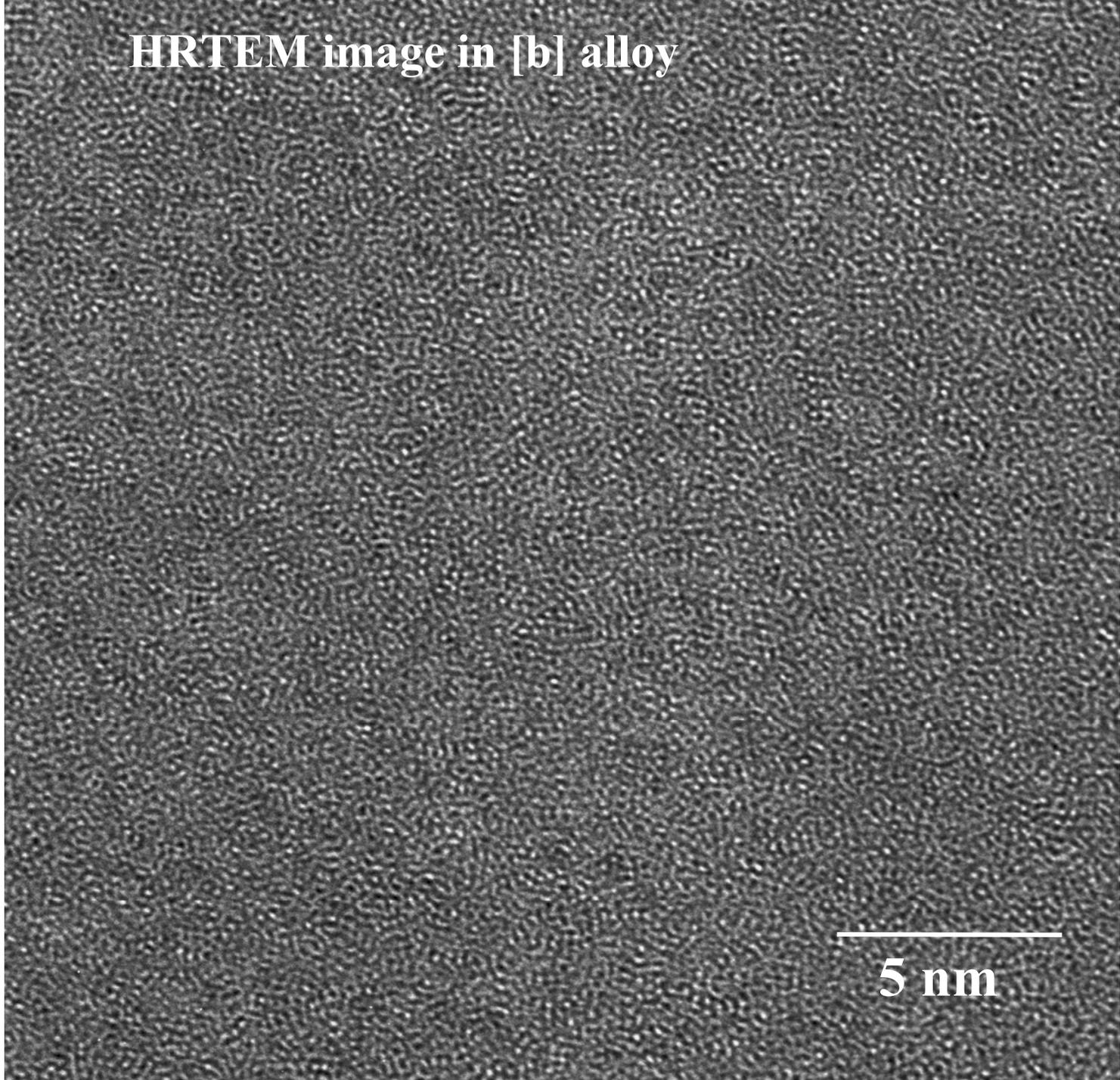
Effect of quenched-in quasicrystal nuclei

■ Isotherm in DSC

Isothermal annealing



HRTEM image in [b] alloy

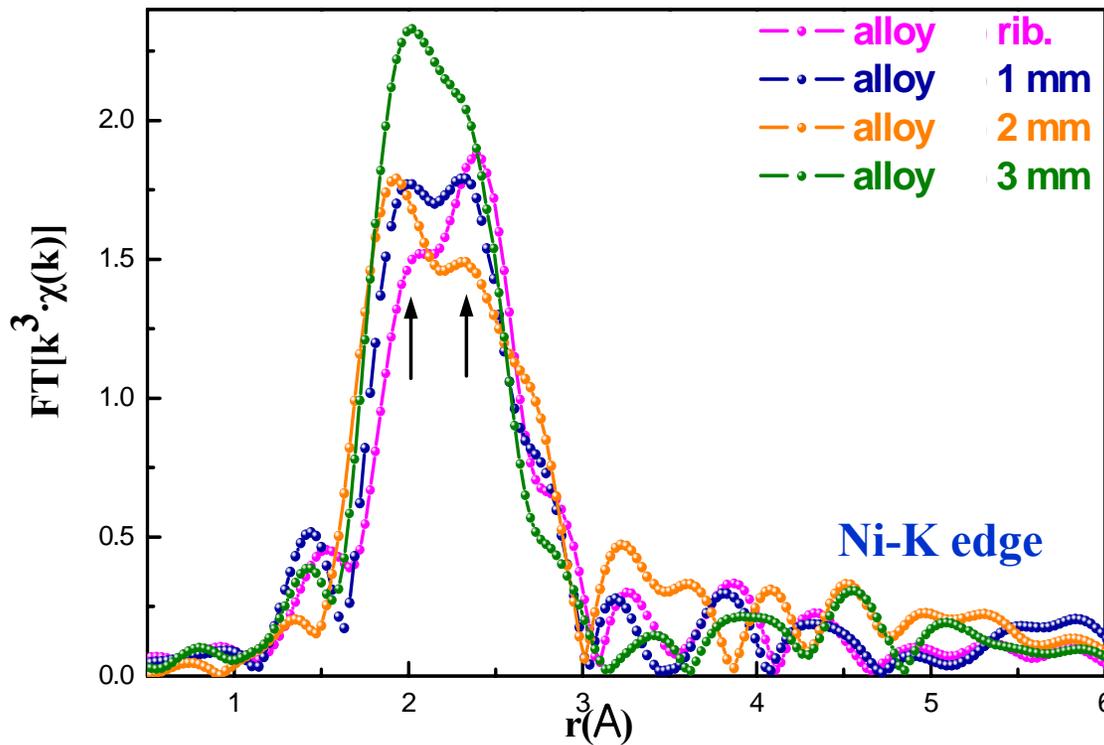


5 nm

Effect of quenched-in quasicrystal nuclei

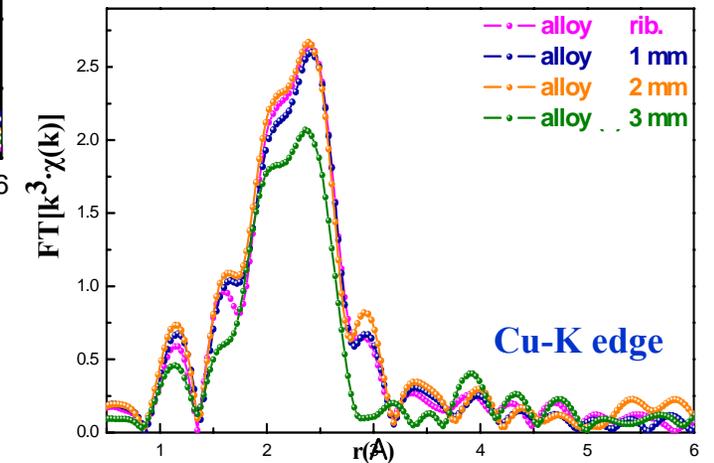
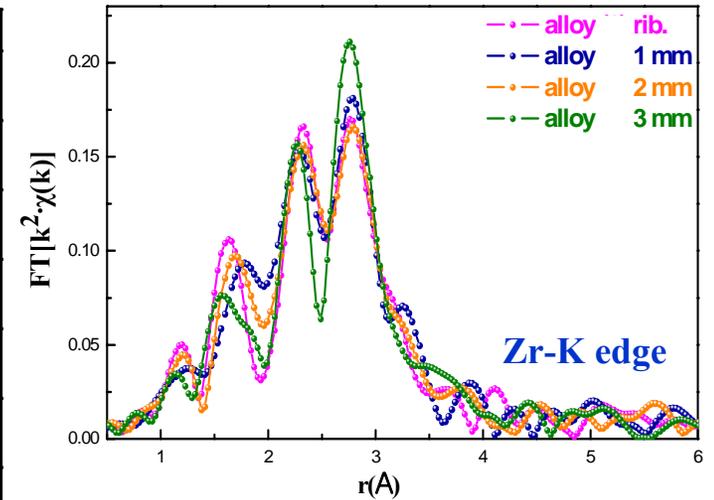
EXAFS analysis

(b) $Zr_{57}Ti_8Nb_{2.5}Cu_{13.9}Ni_{11.1}Al_{7.5}$



Distinctive structural change around Ni atom

Intensity change due to microstructural change



- ***Amorphous vs Nanocrystalline***

- 1) ***Microstructural observation***

- XRD, (HR)TEM, EXAFS ...***

- 2) ***Thermal analysis***

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- : Measure heat absorbed or liberated during heating or cooling***

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- (perfect random)***

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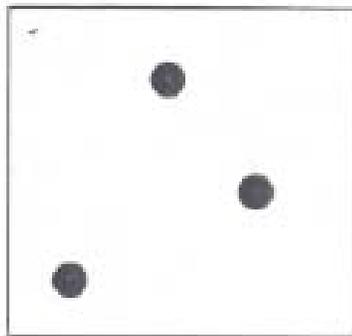
- Nanocrystalline → growth***

- local clusters with atomic scale are difficult to identify by conventional observation tools of microstructure.***

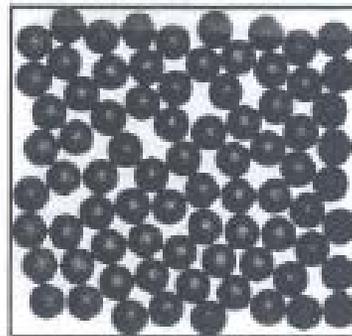
- : Characterization of structure by pair distribution function***

- 3) Intensive Structural Analysis: radial distribution function***

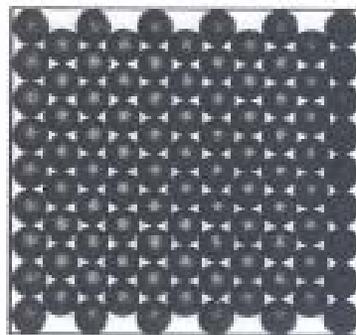
Characterizing the structure - radial distribution function, also called pair distribution function



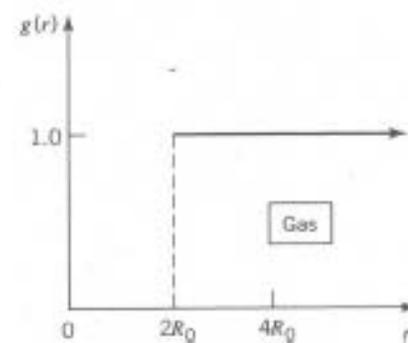
(a)



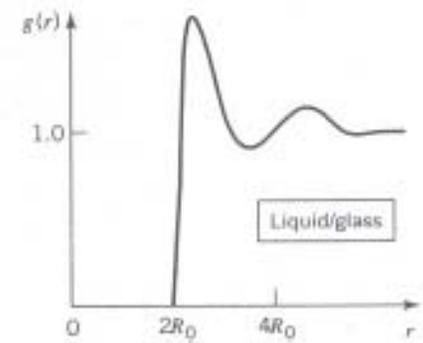
(b)



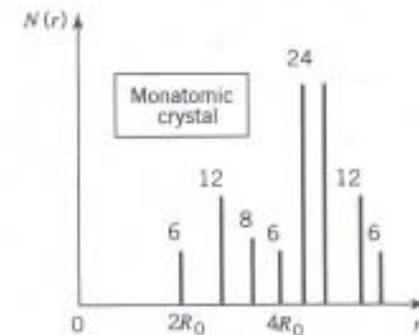
(c)



(a)



(b)



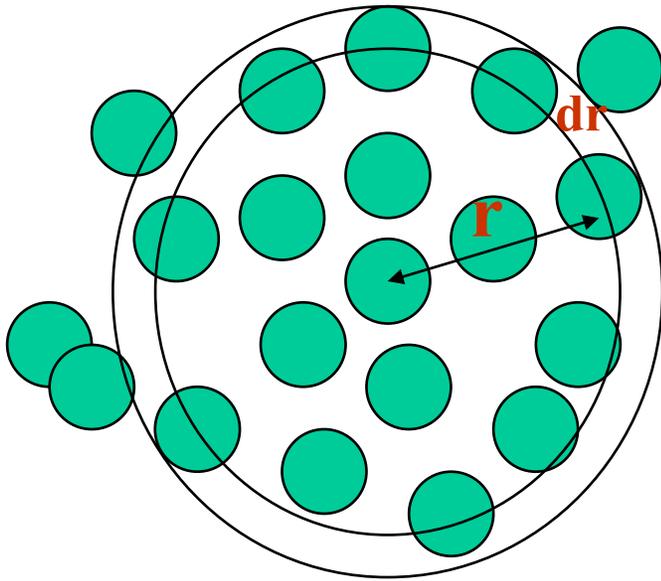
(c)

Figure 2.4 Hard-sphere model of (a) gas, (b) liquid/glass, and (c) crystalline solid.

Figure 2.5 Pair-distribution functions for (a) a gas and (b) liquid or glass. (c) The radial dependence of the number of neighbors $N(r)$ for a primitive cubic crystal with one atom per lattice site.

Gas, amorphous/liquid and crystal structures have very different radial distribution function

Radial distribution function - definition



1. Carve a shell of size r and $r + dr$ around a center of an atom. The volume of the shell is $dv=4\pi r^2 dr$
2. Count number of atoms with centers within the shell (dn)
3. Average over all atoms in the system
4. Divide by the average atomic density $\langle\rho\rangle$

$$g(r) = \frac{1}{\langle\rho\rangle} \frac{dn(r, r + dr)}{dv(r, r + dr)}$$

Count thy neighbours

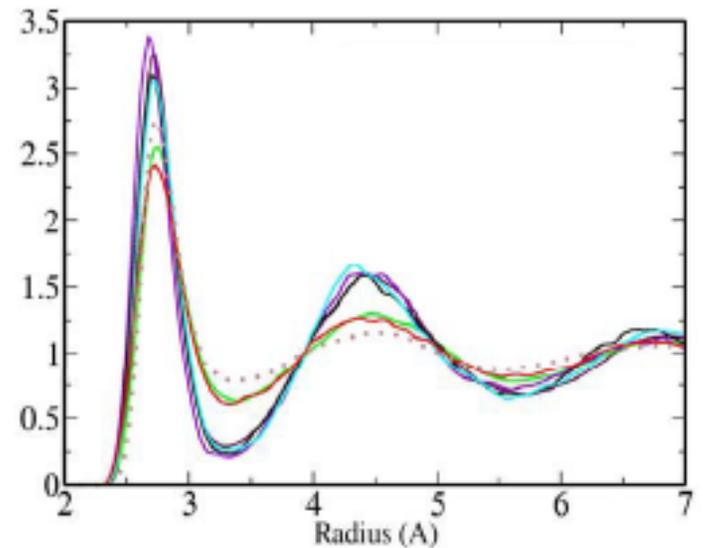
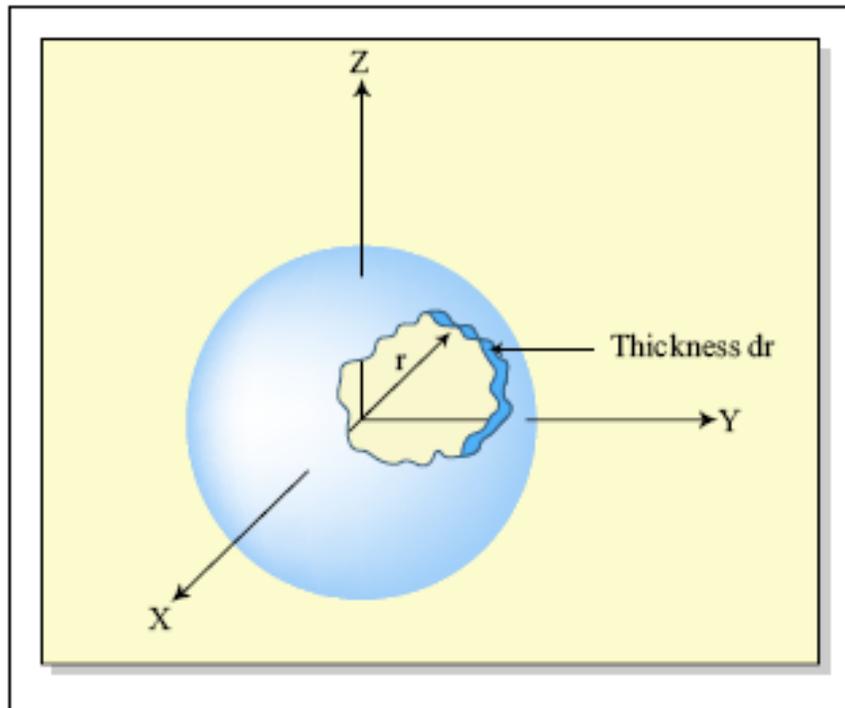


Figure by MIT OCW.

Properties of the radial distribution function

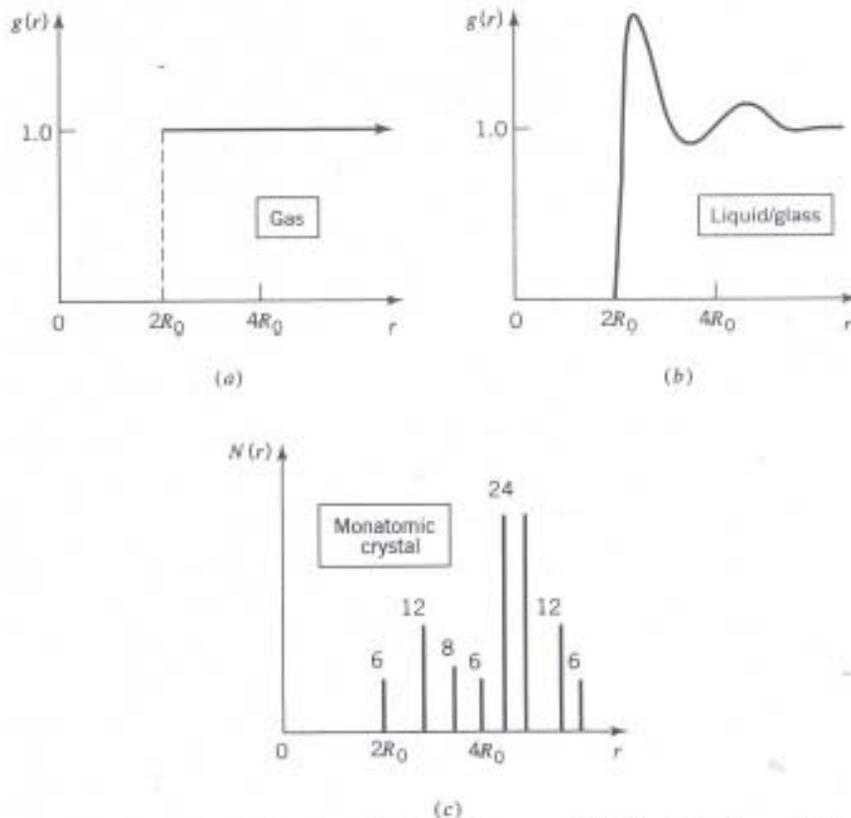


Figure 2.5 Pair-distribution functions for (a) a gas and (b) liquid or glass. (c) The radial dependence of the number of neighbors $N(r)$ for a primitive cubic crystal with one atom per lattice site.

For gases, liquids and amorphous solids $g(r)$ becomes unity for large enough r .

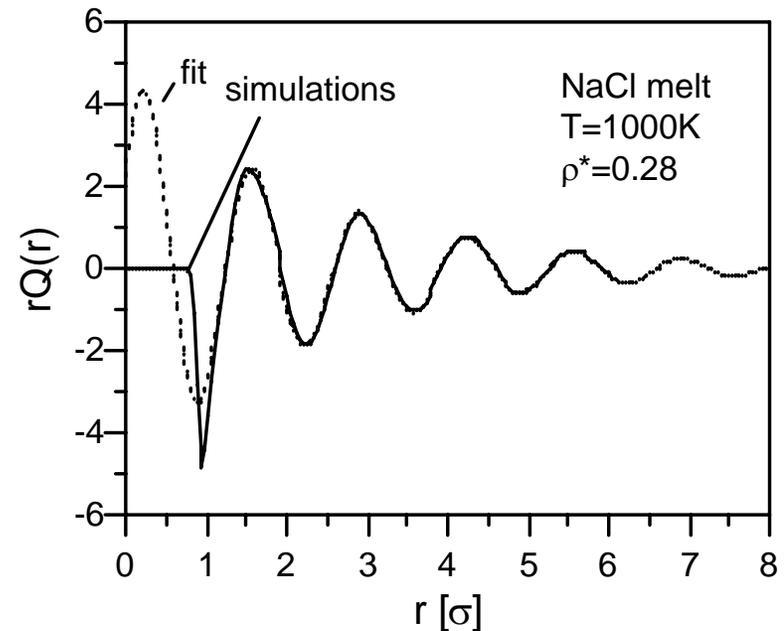
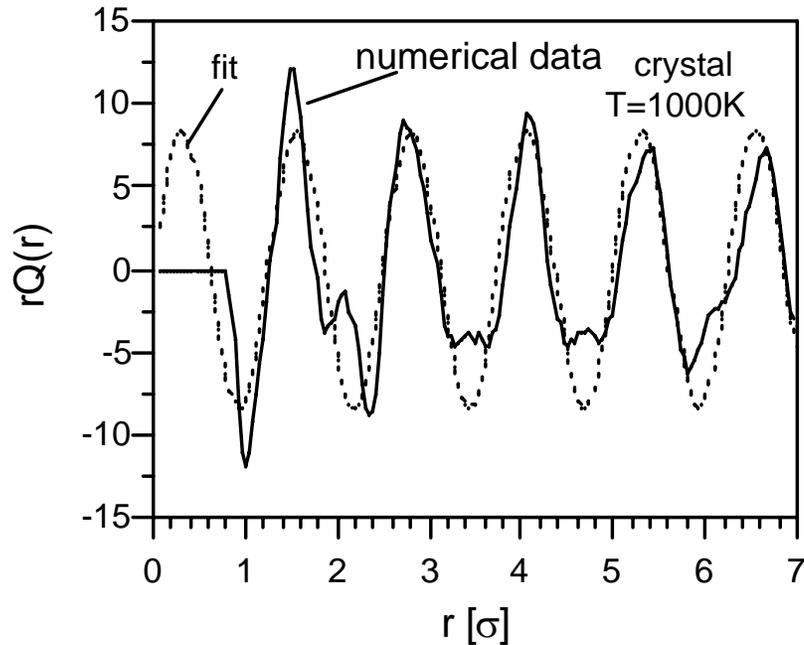
The distance over which $g(r)$ becomes unity is called the correlation distance which is a measure of the extent of so-called **short range order (SRO)**

The first peak corresponds to an average nearest neighbor distance

Features in $g(r)$ for liquids and amorphous solids are due to packing (exclude volume) and possibly bonding characteristics

Radial Distribution Function - Crystal and Liquid

$$Q(r) = g(r) - 1 \sim \frac{1}{r} \sin(r/d + \varphi) \exp(r/\lambda)$$



Liquid/amorphous $g(r)$, for large r exhibit oscillatory exponential decay
Crystal $g(r)$ does not exhibit an exponential decay ($\lambda \rightarrow \infty$)

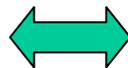
Radial distribution functions and the structure factor

- The structure factor, $S(k)$, which can be measured experimentally (e.g. by X-rays such as EXAFS) is given by the Fourier transform of the radial distribution function and vice versa

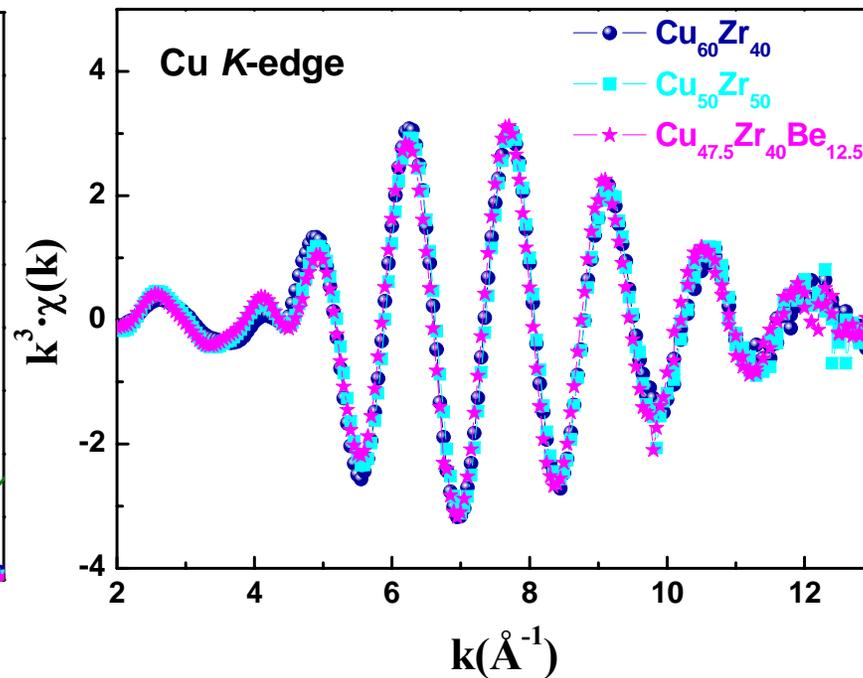
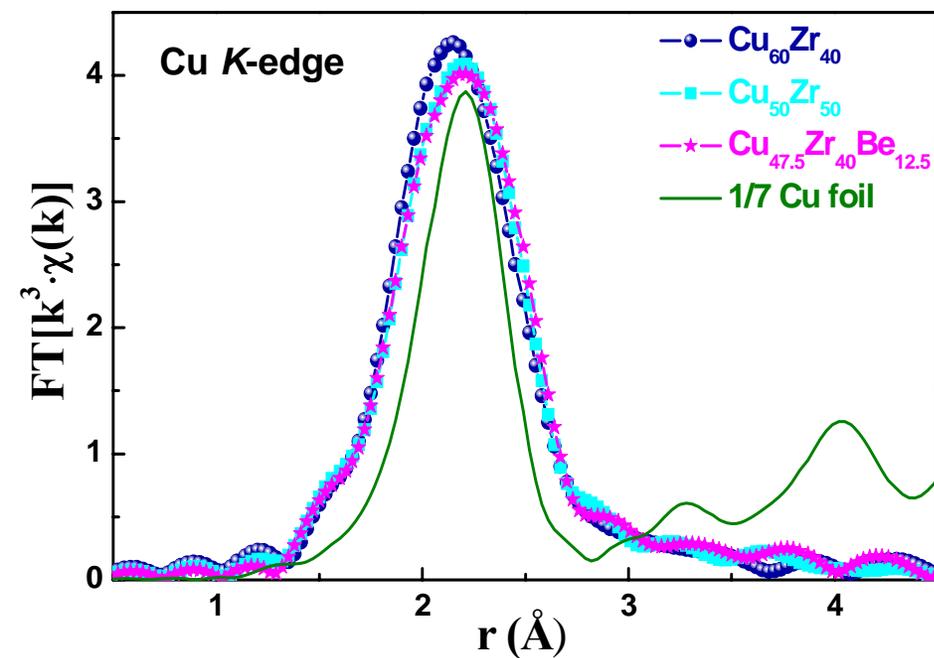
$$S(k) = 1 + \frac{4\pi\langle\rho\rangle}{k} \int_0^{\infty} r[g(r) - 1]\sin(kr)dr$$

Radial distribution functions can be obtained from experiment and compared with that from the structural model

Radial distribution functions



Structure factor



More detailed structural characterization - Voronoi Polyhedra

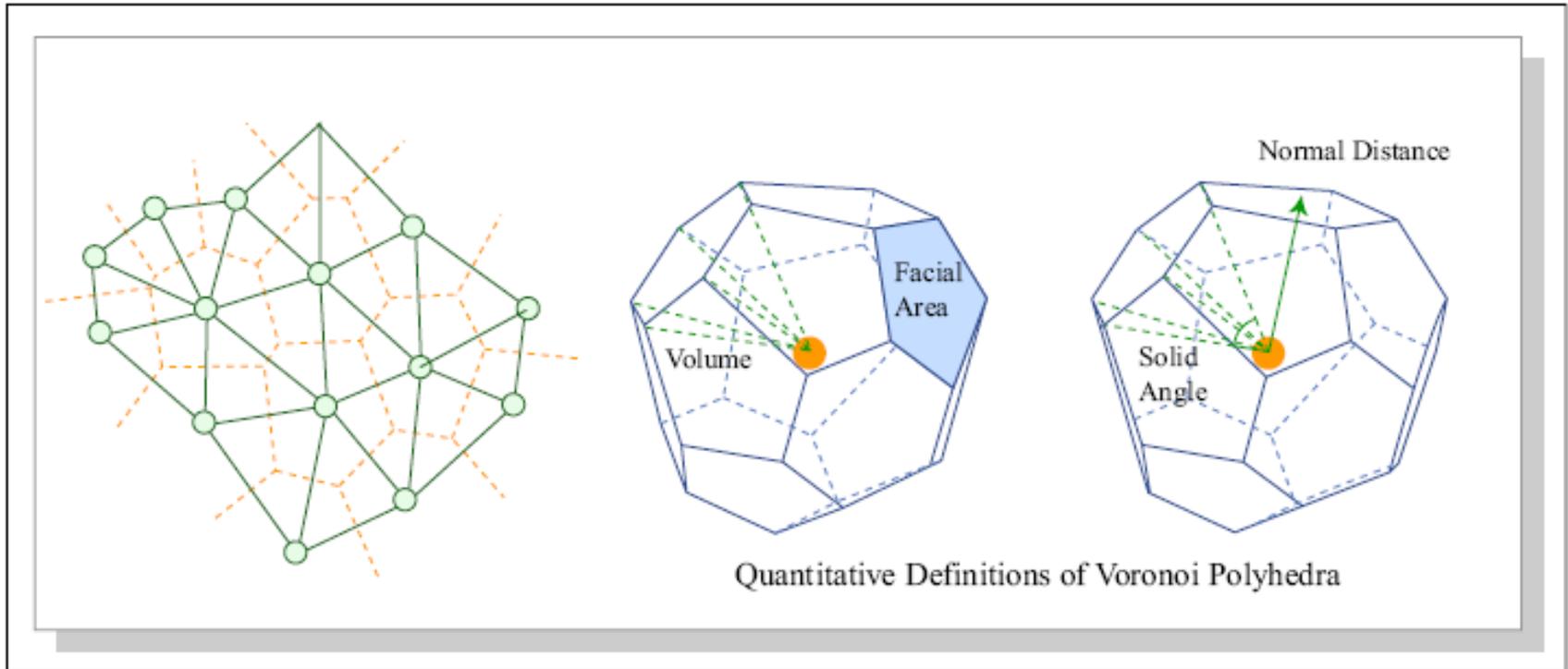
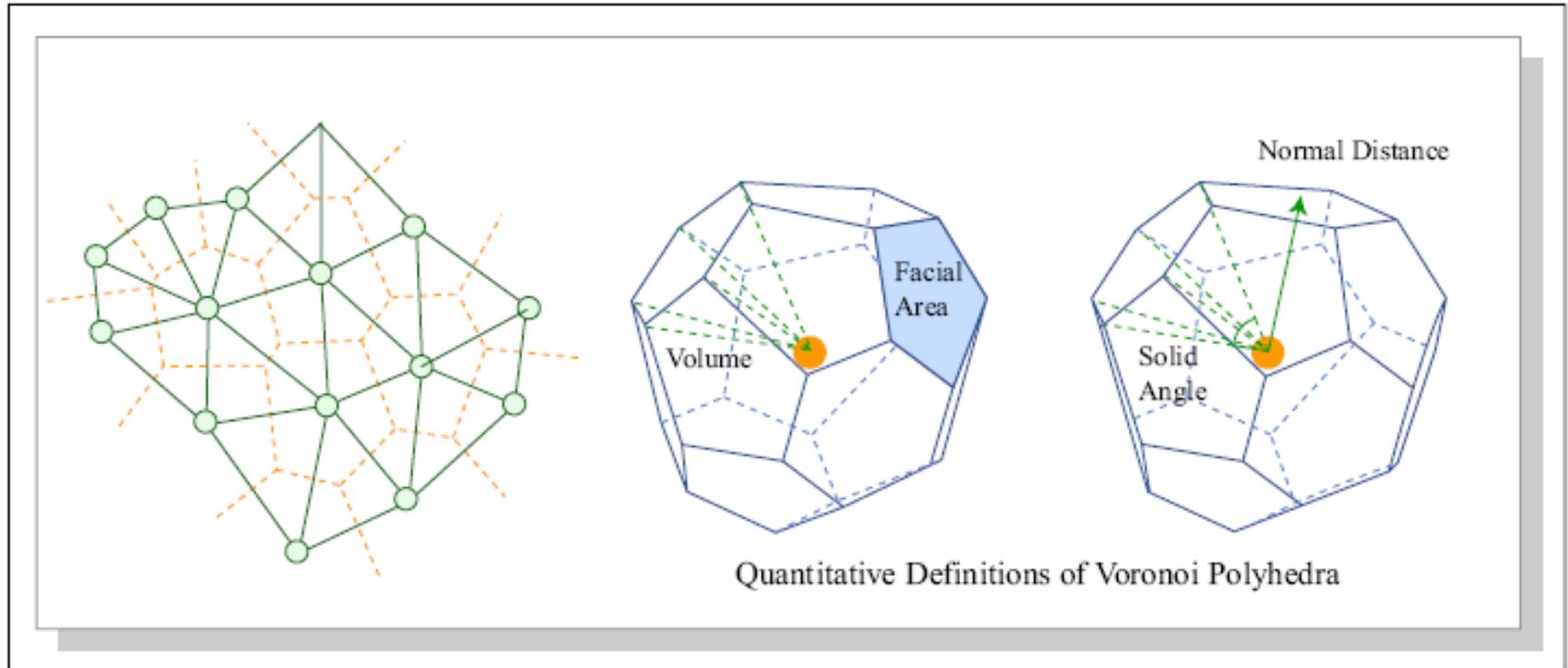


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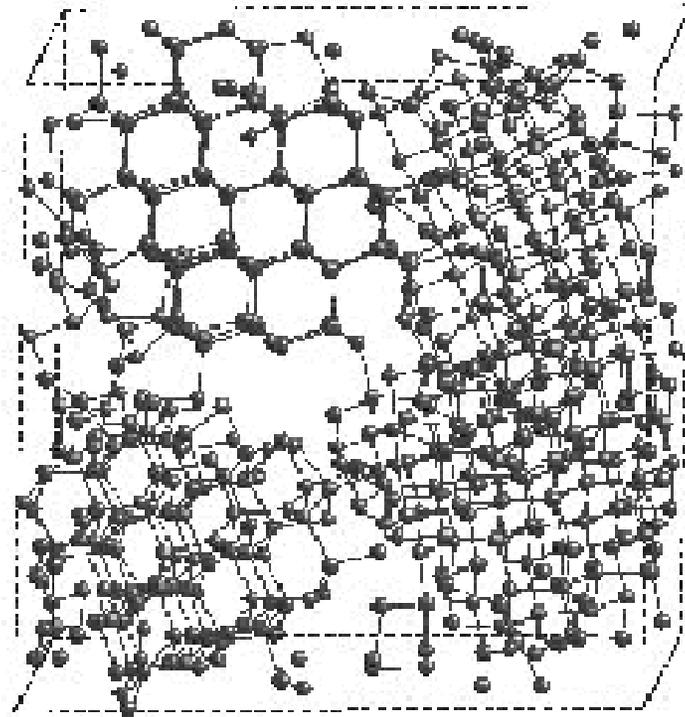
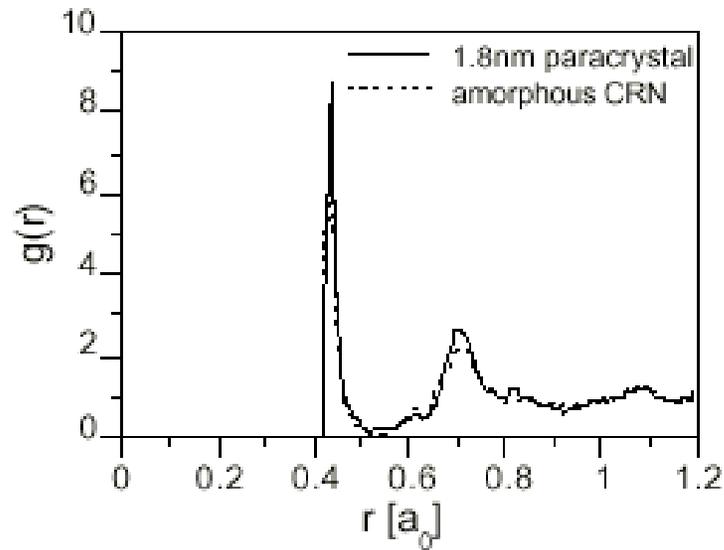
- Draw lines between a center of an atom and nearby atoms.
- Construct planes bisecting the lines perpendicularly
- The sets of planes the closest to the central atom forms a convex polyhedron
- Perform the statistical analysis of such constructed polyhedrons, most notably evaluate an average number of faces

More detailed structural characterization - Voronoi Polyhedra



- **For no-directional bonding promoting packing number of faces is large ~ 13-14 (metallic glasses)**
- **For directional bonding (covalent glasses) number of faces is small**
- **Ionic glasses - intermediate**
- **In all cases the number of faces is closely related to the number of nearest neighbors (the coordination number)**

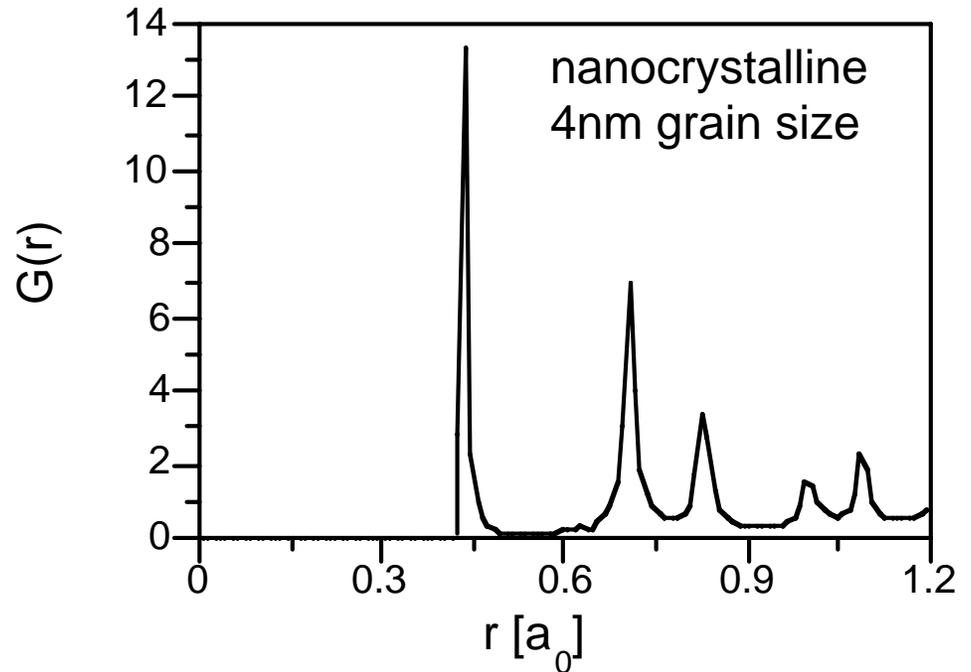
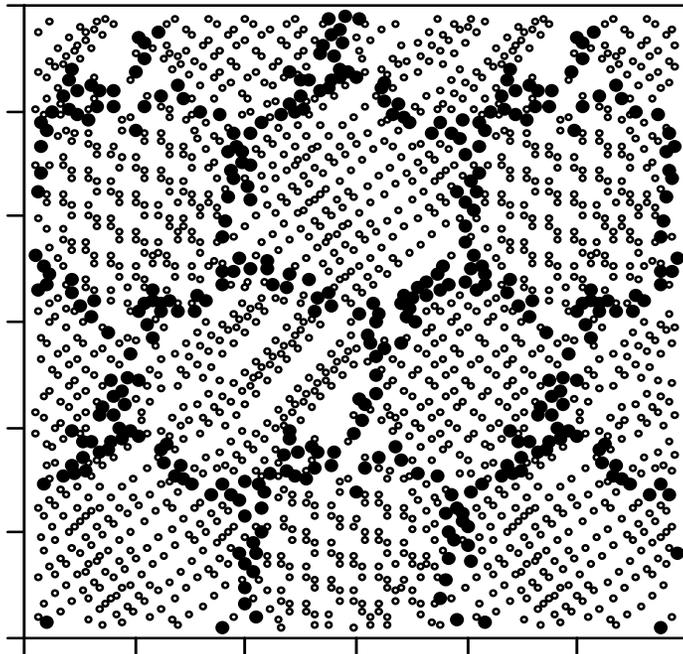
Medium range order and radial distribution function



Radial distribution functions (and also X-ray) of amorphous silicon and model Si with ~ 2 nm crystalline grains are essentially the same - medium range order difficult to see by standard characterization tools. Such structure is called a paracrystal.

Radial Distribution Function

Nanocrystalline material



Nanocrystalline materials shows clear crystalline peaks with some background coming from the grain boundary