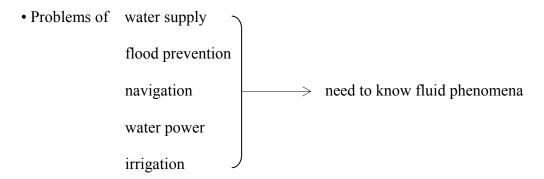
Chapter 1 Fundamentals

- 1.1 Scope of Fluid Mechanics
- **1.2 Historical Perspective**
- 1.3 Physical Characteristics of the Fluid State
- 1.4 Units, Density, Weight Density, Specific Volume, and Specific Gravity
- 1.5 Compressibility, Elasticity
- 1.6 Viscosity
- 1.7 Surface Tension, Capillarity
- 1.8 Vapor Pressure

1.1 Scope of Fluid Mechanics



1.2 Historical Perspective

• d'Alembert (1744)

"The theory of fluids must necessarily be based upon experiment"

• Two schools theoretical group
$$\rightarrow$$
 hydrodynamics practical group \rightarrow hydraulics

- Navier and Stokes
 - \rightarrow general equations for viscous fluid \rightarrow equation of motion

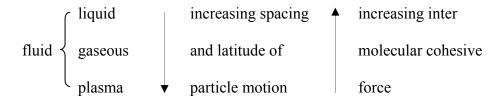
[Re] Navier-Stokes equation

Claude-Louis Navier (1785-1836, French engineer) and George Gabriel Stokes (1819-1903, UK mathematician & physicist)

- model the weather, ocean currents, water flow in a pipe, the air's flow around a wing, and motion of stars inside a galaxy
- design of aircraft and cars, the study of blood flow, the design of power stations, the analysis of pollution,
- exact solution one of the seven most important open problems in mathematics
- New problems in modern times
 - Dispersion of man's wastes in lakes, rivers, and oceans
 - → *Environmental Hydraulics* → www.ehlab.re.kr

1.3 Physical Characteristics of the Fluid State

• state: solid



• fluid – continuum → no voids or holes

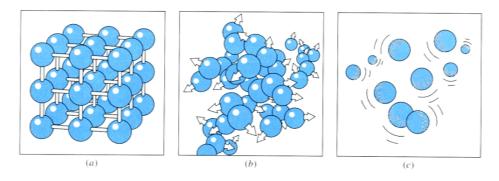


FIGURE 1–5

The arrangement of atoms in different phases: (a) molecules are at relatively fixed positions in a solid, (b) groups of molecules move about each other in the liquid phase, and (c) molecules move about at random in the gas phase.

• Classification of states by stress-strain relationships

	strain			
stress	solid	fluid		
tension		unable to support tension (surface tension)		
compression	elastic deformation → permanent distortion	elastic deformation (compressible fluid)		
shear (tangential forces)	•	permanent distortion or flow (change shape) to infinitesimal shear stress		

^{*} Fluid does not resist any small shearing stress → "Flow occurs"

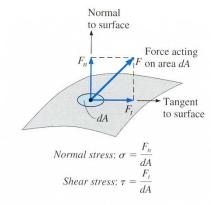


FIGURE 1-3

The normal stress and shear stress at the surface of a fluid element. For fluids at rest, the shear stress is zero and pressure is the only normal stress.

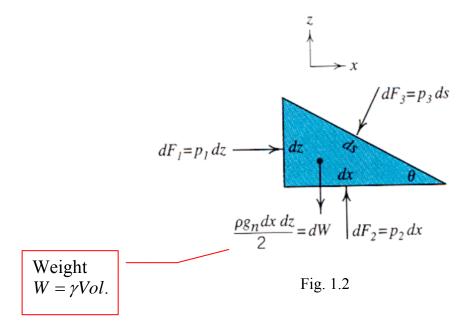
• Comparison between real fluid and ideal fluid

atmaga	real fluid (viscous fluid)		ideal fluid (non- viscous fluid)
stress	in motion	at rest	at rest / in motion
compression (pressure)	0	0	0
shear	0	×	×

• Comparison between compressible fluid and incompressible fluid

incompressible fluid	compressible fluid	
① Compressibility is of small important.	① Compressibility is predominant.	
② Liquids and gases may be treated similarly.	② Behavior of liquids and gases is quite dissimilar.	
3 Fluid problems may be solved with the principles of mechanics.	3 Thermodynamics and heat transfer concepts must be used as well as principles of mechanics.	

- Properties of pressure (compression)
- ① Pressure must be transmitted to solid boundaries normal to those boundaries. \rightarrow Fig. 1.1
- ② At a point, pressure has the same magnitude in all directions. \rightarrow Fig. 1.2
- 3 Pressure is a scalar quantity.



[Pf] $\sum F = 0$

Apply Newton's law for static equilibrium

$$\sum F_x = p_1 dz - p_3 ds \sin \theta = 0 \tag{a}$$

$$\sum F_z = p_2 dx - \rho g dx dz / 2 - p_3 ds \cos \theta = 0$$
 (b)

Substitute following relations into Eq. (a) & (b)

$$dz = ds \sin \theta$$

$$dx = ds \cos \theta$$

$$\therefore (a): p_1 ds \sin \theta - p_3 ds \sin \theta = 0 \rightarrow p_1 = p_3$$

(b):
$$p_2 ds \cos \theta - \rho g \frac{dz}{2} ds \cos \theta - p_3 ds \cos \theta = 0$$

$$\therefore p_2 = p_3 + \frac{1}{2} \rho g dz$$

As
$$dz \to 0$$
 then $p_2 \approx p_3$

$$\therefore p_1 = p_2 = p_3 \text{ at a point } (dx = dz = 0)$$

1.4 Units, Density, Weight Density, Specific Volume, and Specific Gravity

- SI units SI system metric system
- Basic dimensions and units

U.S.	customary
system	

Dimension	SI unit	English system (FSS)	
Length (L)	metre (m)	feet (ft)	
Mass (M)	kilogram (kg)	slug (-)	
Time (t)	second (s)	second (s)	
Temp. (T)	kelvin (K)	degree Rankine (°R)	

- Frequency (f): hertz $(HZ = s^{-1})$
- Force, F
- → introduce Newton's 2nd law of motion

$$F = ma$$

Force = $mass \times acceleration$

$$a = v / t = L / t^2 \qquad \left[L t^{-2} \right] \qquad (\text{m/s}^2)$$

$$v = L/t \qquad \qquad \left\lceil Lt^{-1} \right\rceil \qquad \qquad (\text{m/s})$$

$$\therefore F \to 1 \text{kg} \cdot \text{m/s}^2 = 1 \text{N}(Newton)$$

• Energy, E (work)

$$E = FL \rightarrow \text{kg} \cdot \text{m}^2/\text{s}^2 = J(Joule)$$

• Power, P

$$P = E / t \rightarrow J / s = \text{kg} \cdot \text{m}^2/\text{s}^3$$

• Pressure, p; Stress, σ , τ

$$p = F / A \rightarrow N/m^2 = Pa (pascal) = kg/m \cdot s^2$$

- Temperature, T: degree Celsius (°C)
- Density, ρ
- = mass per unit volume
- ~ depends on the number of molecules per unit of volume
- ~ decreases with increasing temperature

$$\rho = \frac{M}{V} \to \text{kg/m}^3$$



- Specific weight (weight density), γ
- = weight (force) per unit volume

$$\gamma = \frac{W}{V} \to N/m^3 = kg/m^2 \cdot s^2$$

[Re]

$$W = Mg$$
 (Newton's 2nd law of motion)

g = acceleration due to gravity

$$\therefore \gamma = \rho g \tag{1.1}$$

- Specific volume=volume per unit mass= $1/\rho$
- Specific gravity, s.g. , \sim r. d. (relative density)
 - = ratio of density of a substance to the density of water at a specified temperature and pressure

$$s.g. = \frac{\rho_f}{\rho_w} = \frac{\gamma_f}{\gamma_w}$$

[Re] s.g. of sea water =
$$1.03$$

s.g. of soil =
$$2.65$$

s.g. of mercury =
$$13.6$$

• For water at 5 °C (p. 694, App. 2)

	SI	English system
ρ	$1,000 \text{ kg/m}^3$	1.94 slugs/ft ³
γ	9,806 N/m ³	62.4 lb/ft ³
g	9.81 m/s ²	32.2 ft/s^2

- Advantage of SI system and English FSS system
- ① It distinguishes between force (F) and mass (M).
- ② It has no ambiguous definitions.

• Greek Alphabet α Alpha angle β Beta [beitə] angle γ,Γ Gamma specific weight, circulation δ,Δ thickness of boundary layer Delta eddy viscosity, height of surface roughness \mathcal{E} Epsilon ζ Zeta Eta η θ,Θ Theta Iota [aioutə] Kappa [kæpə] K λ, Λ Lambda Mu [mju:] dynamic viscosity μ Nu kinematic viscosity ν ξ Xi [gzai, ksai] vorticity Omicron 0 Pi [pai] π Rho mass density ρ σ, Σ Sigma Sigma Xi, Scientific Research Society, 1886 honor society for scientists & engineers Tau shear τ υ,Υ Upsilon

Phi Beta Kappa

 φ,Φ

Phi [fai]

 χ Chi [kai]

 ψ, Ψ Psi [psai, sai] stream function

 ω,Ω Omega angular velocity

• Prefixes

E exa 10^{18}

P peta 10¹⁵

T tera 10^{12}

G giga 10^9

M mega 10^6

k kilo 10³

h hecto 10^2

da deca 10^1

d deci 10⁻¹

c centi 10^{-2}

m milli 10^{-3}

 μ micro 10^{-6}

n nano 10⁻⁹

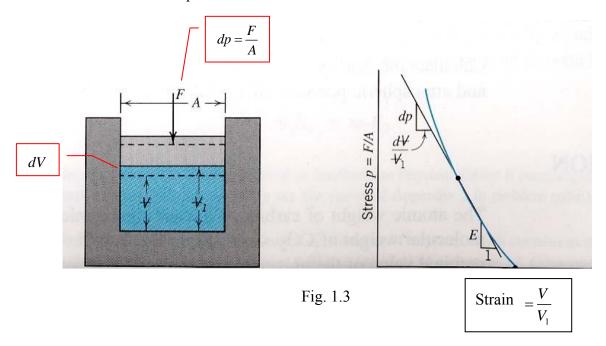
p pico 10⁻¹²

f femto 10^{-15}

a atto 10^{-18}

1.5 Compressibility, Elasticity

• Elastic behavior to compression



• Compressibility ≡ change in volume due to change in pressure

solid - modulus of elasticity, E (N/m²)

fluid - bulk modulus

Minus means that increase in pressure causes decrease in volume

• Stress strain curve ($E\uparrow$, difficult to compress) \rightarrow Fig. 1.3 (see Table 1-1)

$$dp \propto \frac{dV}{V_1} \rightarrow dp = -E \frac{dV}{V_1}$$

$$E = -\frac{dp}{\frac{dV}{V_1}} = -V_1 \frac{dp}{dV} \neq const = fn(p,T) \rightarrow p \uparrow \rightarrow E \uparrow$$

$$C = \frac{1}{E} = -\frac{dV}{V_1} \frac{1}{dp}$$

= modulus of compressibility (m^2/N)

[Re] large E/small $C \rightarrow$ less compressible

- incompressible fluid (inelastic): $E = \infty, C \ll 1$
 - \rightarrow constant density ρ =const.
 - ~ water
- compressible fluid
- → changes in density → variable density
- $\sim gas$

[Table 1.1] Bulk modulus of water, $E (10^6 \text{ N/m}^2)$

Pressure	Temperature, °C				
$10^6 \mathrm{N/m^2}$	0°	20°	50°	100°	150°
0.1	1950	2130	2210	2050	
10.0	2000	2200	2280	2130	1650
30.0	2110	2320	2410	2250	1800
100.0	2530	2730	<u>2840</u>	2700	2330

- E increases as pressure increases.
- E is maximum at about 50 °C.
- → The water has minimum compressibility at about 50 °C.

[Table A2-1]

Compressibility		Modulus of Elasticity, E (kPa)		
steel	1/80 of water	water	2,170,500	
mercury	1/12.5 of water	sea water	2,300,000	
nitric acid	6 of water	mercury	26,201,000	

• For the case of a fixed mass of liquid at constant temperature

$$E = -V_1 \frac{dp}{dV}$$

$$\frac{\Delta V}{V_1} \approx -\frac{\Delta p}{E}$$

$$\frac{V_2 - V_1}{V_1} \approx -\frac{p_2 - p_1}{E}$$

[Ex] For water; $E = 2,200 \times 10^6 \,\text{Pa}$ @ 20°C

$$p_2 = p_1 + 7 \times 10^6 \,\mathrm{Pa}$$

$$\therefore \frac{V_2 - V_1}{V_1} \approx -\frac{p_2 - p_1}{E} = -0.0032$$

$$V_2 = (1 - 0.0032) V_1$$

$$\Delta V \approx 0.3\%$$
 decrease

→ water is incompressible

1.6 Viscosity

- Two types of fluid motion (real fluid)
 - 1) laminar flow:
 - viscosity plays a dominant role
 - fluid elements or particles slide over each other in layers (laminar)
 - molecular diffusion

[Ex] flow in a very small tube, a very thin flow over the pavement, flow in the laminar flow table

2) turbulent flow:

- random or chaotic motion, eddies of various sizes are seen
- common in nature (streams, rivers, pipes)
- large scale mixing between the layers

[Ex] flows in the water supply pipe, flows in the storm sewer pipe, flows in the and canals and streams

· Reynolds number

$$Re = \frac{Vd}{v}$$
 Diameter of pipe, Depth of stream

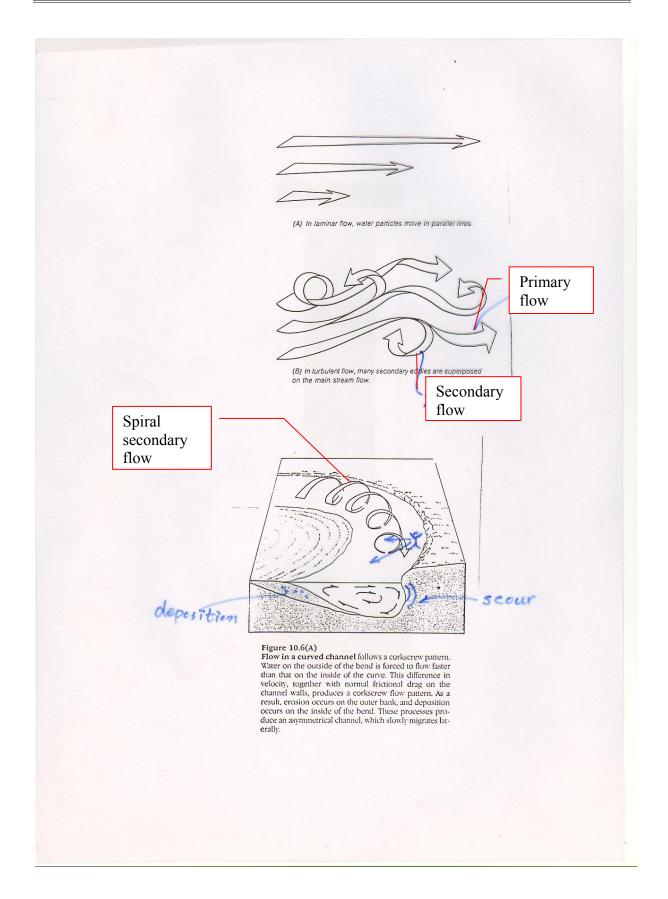
where V = flow velocity; d = characteristic length; v = kinematic viscosity

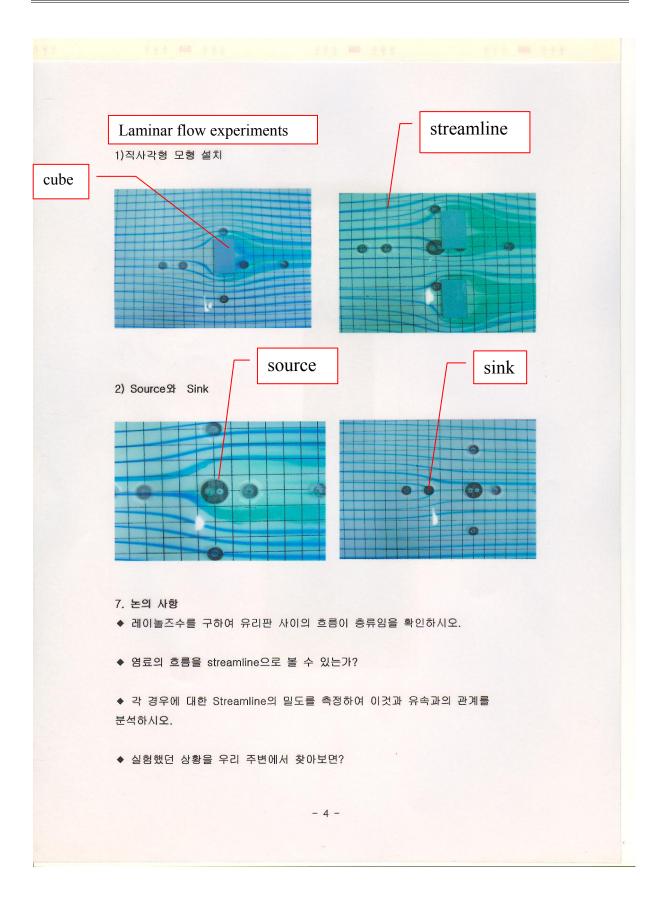
• Reynolds experiments

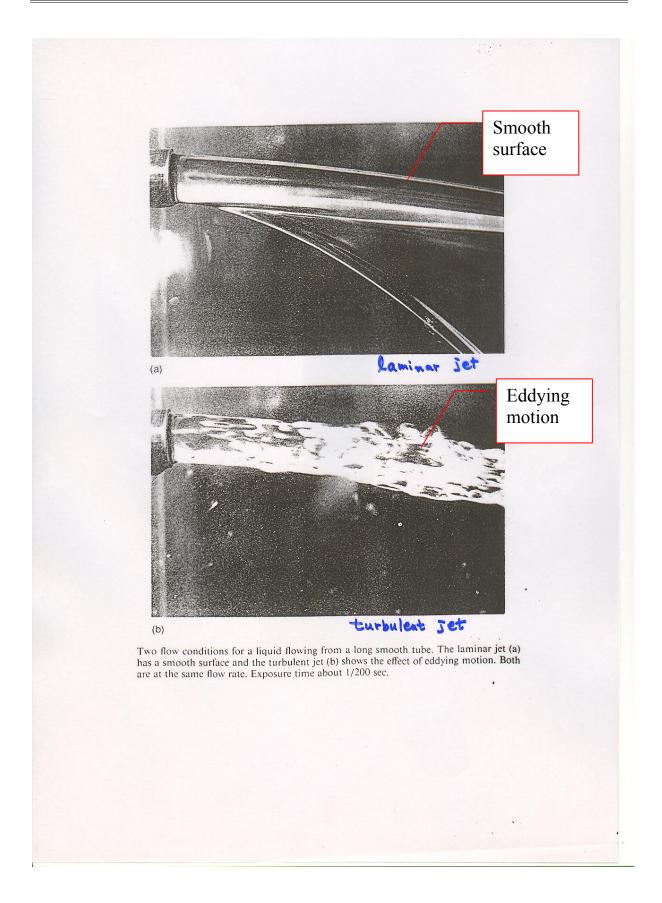
laminar flow: Re < 2,100

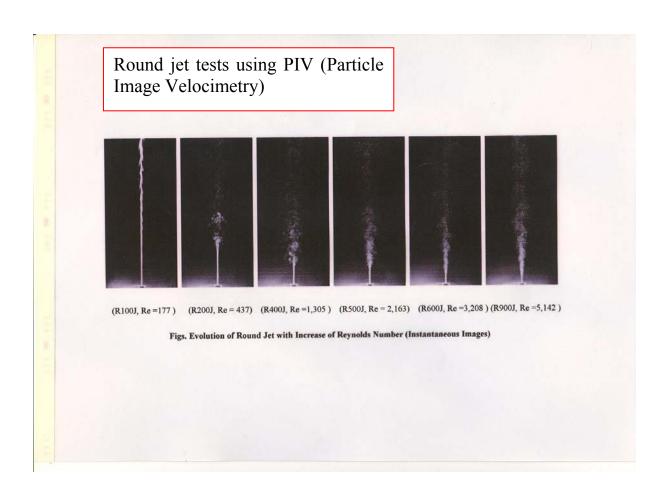
transition: 2,100<Re < 4,000

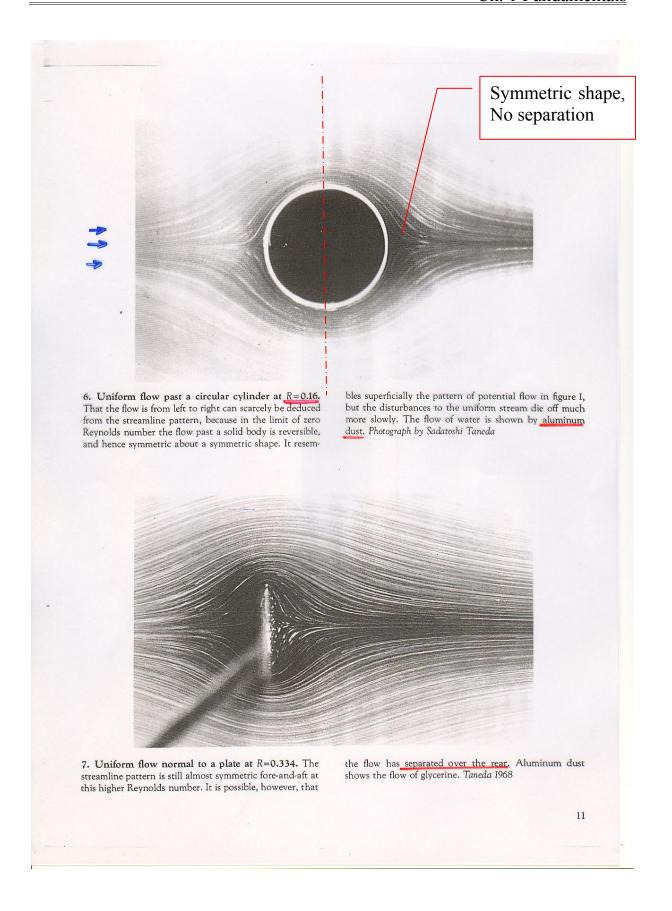
turbulent flow: Re > 4,000

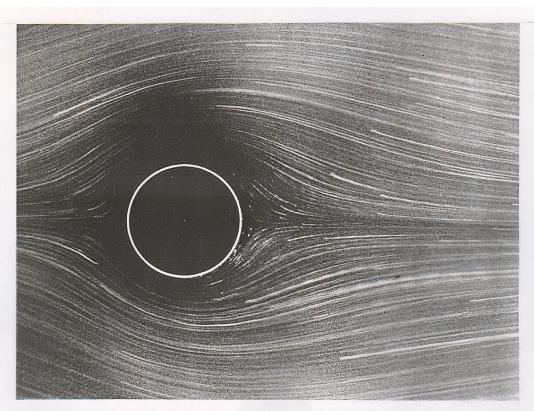








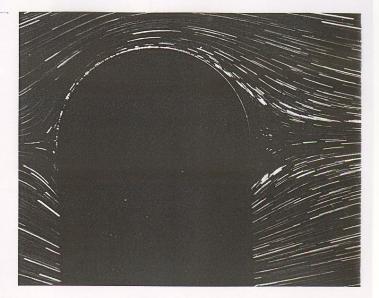




24. Circular cylinder at R=1.54. At this Reynolds number the streamline pattern has clearly lost the foreand-aft symmetry of figure 6. However, the flow has not yet separated at the rear. That begins at about R=5,

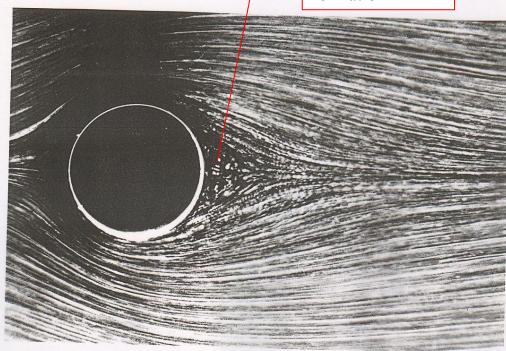
though the value is not known accurately. Streamlines are made visible by aluminum powder in water. Photograph by Sadatoshi Taneda

25. Sphere at R=9.8. Here too, with wall effects negligible, the streamline pattern is distinctly asymmetric, in contrast to the creeping flow of figure 8. The fluid is evidently moving very slowly at the rear, making it difficult to estimate the onset of separation. The flow is presumably attached here, because separation is believed to begin above R=20. Streamlines are shown by magnesium cuttings illuminated in water. *Photograph by Madeleine Coutanceau and Michele Payard*



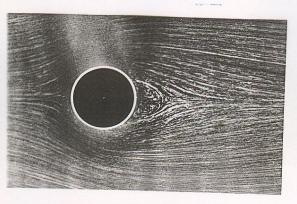
20

Separation, eddy formation

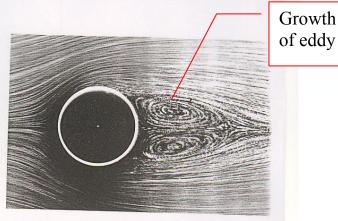


40. Circular cylinder at R=9.6. Here, in contrast to figure 24, the flow has clearly separated to form a pair of recirculating eddies. The cylinder is moving through a tank of water containing aluminum powder, and is illuminated

by a sheet of light below the free surface. Extrapolation of such experiments to unbounded flow suggests separation at R=4 or 5, whereas most numerical computations give R=5 to 7. Photograph by Sadatoshi Taneda

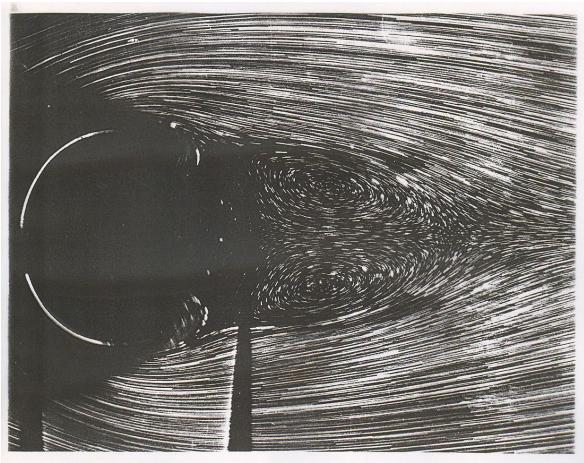


41. Circular cylinder at R=13.1. The standing eddies become elongated in the flow direction as the speed increases. Their length is found to increase linearly with Reynolds number until the flow becomes unstable above R=40. *Taneda* 1956a



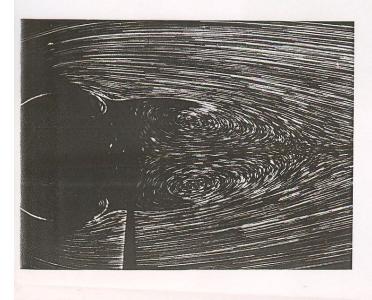
42. Circular cylinder at *R*=**26.** The downstream distance to the cores of the eddies also increases linearly with Reynolds number. However, the lateral distance between the cores appears to grow more nearly as the square root. *Photograph by Sadatoshi Taneda*

28



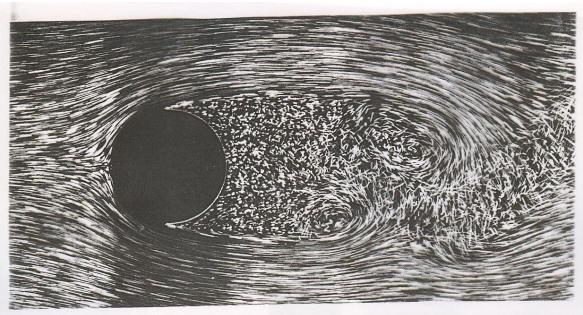
43. Circular cylinder at R=24.3. A different view of the flow is obtained by moving a cylinder through oil. Tiny magnesium cuttings are illuminated by a sheet of light from an arc projector. The two dark wedges below the cir-

cle are an optical effect. The lengths of the particle trajectories have been measured to find the velocity field to within two per cent. Coutanceau & Bouard 1977



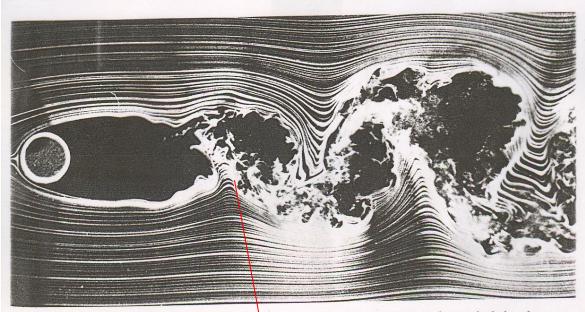
44. Circular cylinder at R=30.2. The flow is here still completely steady with the recirculating wake more than one diameter long. The walls of the tank, 8 diameters away, have little effect at these speeds. Photograph by Madeleine Coutanceau and Roger Bouard

29



47. Circular cylinder at R=2000. At this Reynolds number one may properly speak of a boundary layer. It is laminar over the front, separates, and breaks up into a turbulent wake. The separation points, moving forward as

the Reynolds number is increased, have now attained their upstream limit, ahead of maximum thickness. Visualization is by air bubbles in water. ONERA photograph, Werlé & Gallon 1972

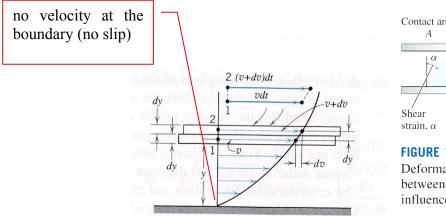


48. Circular cylinder at *R*=10,000. At five times the speed of the photograph at the top of the page, the flow pattern is scarcely changed. The drag coefficient consequently remains almost constant in the range of Reynolds

number spanned by these two photographs. It drops later when, as in figure 57, the boundary layer becomes turbulent at separation. Photograph by Thomas Corke and Hassan Nagib

Karman vortex street – periodic shedding of vortices in sinuous form

• laminar flow



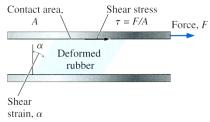


FIGURE 1-2

Deformation of a rubber eraser placed between two parallel plates under the influence of a shear force.

Fig 1.4

• strain = relative displacement

$$= \frac{d_2 - d_1}{dy} = \frac{dvdt}{dy} = \frac{dv}{dy}dt$$

[Cf] solid mechanics

$$\tau_{yx} = G \frac{d\zeta}{dy}$$

total angular displacement

[Re]
$$d_2 = v_2 dt; d_1 = v_1 dt$$
$$d_2 - d_1 = (v_2 - v_1) dt$$

• Experiment has shown that, in many fluids, shearing (frictional) stress per unit of contact area, τ is proportional to the time rate of relative strain.

$$\therefore \tau \propto \frac{dv}{dy} dt / dt = \frac{dv}{dy} \text{ (velocity gradient)}$$

$$\tau = \mu \frac{dv}{dy} \rightarrow \text{Newton's equation of viscosity}$$

$$\text{Large } \mu \rightarrow \text{sticky, difficult to flow}$$
where $\mu = \text{coefficient of viscosity}$

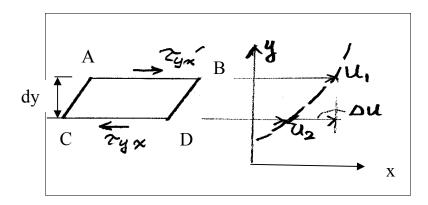
= dynamic (absolute) viscosity

- viscosity = measure of fluid's resistance to shear or angular deformation
- = internal resistance of a fluid to motion (fluidity)

[Re] Friction forces result from

- cohesion for liquid
- momentum interchange between molecules for gas

[Re] angular deformation due to tangential stress



- •rate of angular deformation
- (i) displacement of AB relative to CD

$$= \left(u + \frac{du}{dy}\Delta y\right)\Delta t - u\Delta t = \frac{du}{dy}\Delta y\Delta t$$

(ii) angular displacement of AC

$$= \frac{du}{dy} \Delta y \Delta t / \Delta y = \frac{du}{dy} \Delta t$$

(iii) time rate of angular deformation

$$= \frac{du}{dy} \Delta t / \Delta t = \frac{du}{dy}$$
ic viscosity, μ

$$\tau = \mu \frac{dv}{dy}$$

• dynamic viscosity, μ

$$\tau = F / A$$

$$[\tau] = \lceil MLT^{-2} / L^2 \rceil \lceil ML^{-1}T^{-2} \rceil = \text{kg/(m} \cdot \text{s}^2) = \text{Pa}$$

$$\left[\frac{dv}{dy}\right] = \left[\frac{LT^{-1}}{L}\right] = \left[T^{-1}\right]$$

$$\left[\mu \right] = \left[\tau / \frac{dv}{dy} \right] = \left[\frac{ML^{-1}T^{-2}}{T^{-1}} \right] = \left[ML^{-1}T^{-1} \right] = kg/m \cdot s = N \cdot s / m^2 = Pa \cdot s$$

 \Rightarrow 1 poises (Poiseuille) = $10^1 \text{ Pa} \cdot \text{s}$

• kinematic viscosity, ν

$$\left[v\right] = \left[\frac{ML^{-1}T^{-1}}{ML^{-3}}\right] = \left[L^2T^{-1}\right] = m^2/s$$

 $1 \text{ m}^2/\text{s} = 10^4 \text{ stokes} = 10^6 \text{ centistokes}$

- Remarks on Eq. (1.12)
 - ① τ, μ are independent of pressure. [Cf] friction between two moving solids
 - ② Shear stress τ (even smallest τ) will cause flow (velocity gradient).
 - 3 Shearing stress in viscous fluids at rest will be zero.

$$\frac{dv}{dy} = 0 \rightarrow \tau = 0$$
 regardless of μ

① At solid boundary,
$$\frac{dv}{dy} \neq \infty \ (\rightarrow \tau \neq \infty \ (\text{no infinite shear}))$$

- → Infinite shearing stress between fluid and solid is not possible.
- ⑤ Eq. 1.12 is limited to laminar (non-turbulent) fluid motion in which viscous action is predominant.

[Cf] turbulent flow

$$\tau = \varepsilon \frac{dv}{dy}$$

$$\varepsilon \gg \mu$$

where $\varepsilon = eddy$ viscosity

- 6 Velocity at a solid boundary is zero.
 - → No slip condition (continuum assumption)
- Newtonian and non-Newtonian fluids
 - i) Newtonian fluid ~ water
 - ii) Non-Newtonian fluid ~ plastic, blood, suspensions, paints, polymer solutions →
 rheology

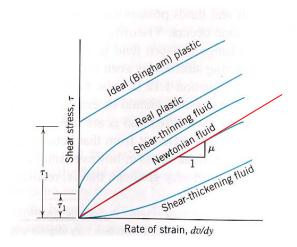


Fig. 1.5

• Non-Newtonian fluid

1)
$$\tau - \tau_1 = \mu \frac{dv}{dy}$$
 plastic, $\tau_1 = \text{threshold}$

2)
$$\tau = K \left(\frac{dv}{dy}\right)^n$$
 $n > 1$ Shear-thickening fluid

n < 1 Shear-thinning fluid

 Couette flow: laminar flow in which the shear stress is constant thin fluid film between two large flat plates
 thin fluid film between the surfaces of coaxial cylinders

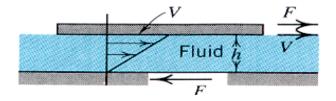


Fig. 1.7

$$\frac{dv}{dy} = \frac{V}{h} \quad \sim \text{linear velocity gradient}$$

$$\therefore \quad \tau = \mu \frac{V}{h} \sim \text{constant}$$

• Turbulent flow

$$\tau = (\mu + \varepsilon) \frac{dv}{dy}$$

 ε = eddy viscosity = viscosity due to turbulent factor

• Mechanism of viscosity for liquid and gas

	gas	liquid
main cause of viscosity	exchange of molecule's momentum → interchange of molecules between the fluid layers of different velocities	intermolecular cohesion
effect of temperature variation	temp↑ → molecular activity↑ → viscosity↑ → shearing stress↑	temp↑ → cohesion↓ → viscosity↓ → shear stress↓

[Re] Exchange of momentum

fast-speed layer (FSL)



molecules from FSL speed up molecules in LSL molecules from LSL slow down molecules in FSL

Two layers tend to stick together as if there is some viscosity between two.

low-speed layer (LSL)

- 1) exchange of momentum: exchange momentum in either direction from high to low or
 from low to high momentum due to random motion of
 molecules
- 2) transport of momentum: transport of momentum from layers of high momentum (high velocity, mv) to layers of low momentum

1.7 Surface Tension, Capillarity

- surface tension
 - occur when the liquid surfaces are in contact with another fluid (air) or solid
 - f_n (relative sizes of intermolecular cohesive and adhesive forces to another body)
 - as temp \uparrow \to cohesion \downarrow \to σ \downarrow $\ \ \,$ Table A2.4b, p. 694
- some important engineering problems related to surface tension
 - capillary rise of liquids in narrow spaces
 - mechanics of bubble formation
 - formation of liquid drops
 - small models of larger prototype \rightarrow dam, river model
- surface tension, σ (F/L, N/m)
 - force per unit length
 - force attracting molecules away from liquid

Consider static equilibrium

$$\sum F = 0$$
 (forces normal to the element a, b, c, d)

$$(p_i - p_0)dxdy = 2\sigma dy \sin \alpha + 2\sigma dx \sin \beta$$

where p_i = pressure inside the curvature; p_o = pressure inside the curvature

$$\sin \alpha = \frac{dx}{2R_1}, \quad \sin \beta = \frac{dy}{2R_2} \left[dx = 2(R_1 \sin \alpha) \right]$$

$$\therefore p_i - p_0 = \sigma \left(\frac{1}{R_1} + \frac{1}{R_2} \right) \tag{1.15}$$

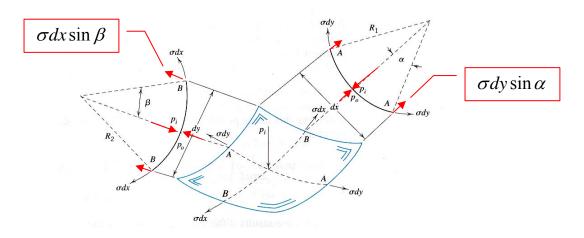


Fig. 1.9

- Cylindrical capillary tube
 - due to both cohesion and adhesion

cohesion \leq adhesion \rightarrow rise (water)

cohesion > adhesion \rightarrow depression (mercury)

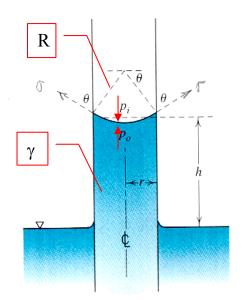


Fig. 1.10

For a small tube, given conditions are as follows

$$R_1 = R_2 = R$$
 (liquid surface \approx section of sphere) \leftarrow Ch. 2

$$p_0 = -\gamma h$$
 (hydrostatic pressure)

$$p_i = 0$$
 (atmospheric)

Substitute above conditions into Eq. 1.15:
$$p_i - p_0 = \sigma \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$
 (1.15)

$$\therefore \gamma h = \sigma \frac{2}{R}$$

By the way, $r = R \cos \theta$

$$\therefore \gamma h = \sigma \frac{2}{r/\cos\theta} = \frac{2\sigma\cos\theta}{r}$$

$$h = \frac{2\sigma\cos\theta}{\gamma r} \tag{1.16}$$

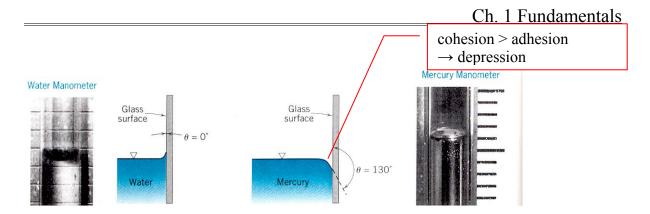
in which $h = \text{capillary rise} \rightarrow r \uparrow \rightarrow h \downarrow$

 θ = angle of contact

 $r = \text{radius of tube} \leq 2.5 \text{ mm for spherical form}$

[Ex] water and mercury \rightarrow Fig. 1.11

If $r > 12 \,\mathrm{mm}$, h is negligible for water.



- Pressure measurement using tubes in hydraulic experiments → Ch.2 manometer
- ~ capillarity problems can be avoided entirely by providing tubes large enough to render the capillarity correction negligible.
- Fomation of curved surface, droplet
 - At free liquid surface contacting the air, cohesive forces at the outer layer are not balanced by a layer above.
 - →The surface molecules are pulled tightly to the lower layer.
 - →Free surface is curved.

[Ex] Surface tension force supports small loads (water strider).

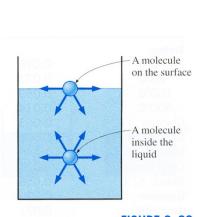


FIGURE 2–20
Attractive forces acting on a liquid molecule at the surface and deep inside the liquid.



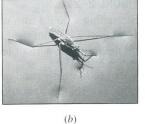


FIGURE 2–19
Some consequences of surface tension.

[IP 1.10] For a droplet of water (20 °C), find diameter of droplet

Given:
$$p_i - p_0 = 1.0 \text{ kPa}$$

At 20°C,
$$\sigma = 0.0728$$
 N/m \leftarrow App. 2

[Sol]

$$p_i - p_0 = \sigma \left(\frac{1}{R_1} + \frac{1}{R_2}\right) = \frac{2\sigma}{R}$$
 (1.15)

$$1 \times 10^3 \text{ N/m}^2 = 2(0.0728) \cdot \frac{1}{R}$$

$$\therefore$$
 $R = 0.000146 \text{m} = 0.146 \text{mm} \rightarrow d = 0.292 \text{mm}$

[IP 1.11] Find height of capillary rise in a clean glass tube of 1 mm diameter if the water temperature is 10°C or 90°C.

[Sol]

From App. 2 Table A 2.4b;

@ 10°C
$$\sigma = 0.0742 \text{ N/m}, \ \gamma = 9.804 \text{ kN/m}^3$$

@ 90°C
$$\sigma = 0.0608 \text{ N/m}, \ \gamma = 9.466 \text{ kN/m}^3$$

Use Eq. 1.16
$$h = \frac{2\sigma\cos\theta}{\gamma r}$$
(1.16)

$$h_{10} = \frac{2(0.0742)(1)}{9804(0.0005)} = 0.030 \text{m} = 30 \text{mm}$$

$$h_{90} = \frac{2(0.0608)(1)}{9466(0.0005)} = 0.026$$
m=26mm

1.8 Vapor Pressure

- vapor pressure = partial pressure exerted by ejected molecules of liquid
 - \rightarrow Table A2.1 and A2.4b
- liquids ~ tend to vaporize or evaporate due to molecular thermal vibrations (molecular activity)
 - → change from liquid to gaseous phase

 $temperature \uparrow \rightarrow molecular \ activity \uparrow \rightarrow vaporization \uparrow \rightarrow vapor \ pressure \uparrow$

- volatile liquids:
 - \sim easy to vaporize \rightarrow high vapor pressure

gasoline: $p_v = 55.2 \text{ kPa}$ at 20 °C

water: $p_v = 2.34 \text{ kPa}$ at 20 °C

mercury: $p_v = 0.00017 \text{ kPa}$ at 15.6 °C

- mercury : low vapor pressure and high density = difficult to vaporize
 - → suitable for pressure-measuring devices
- Cavitation: App. **7** (p. 672)

In the interior and/or boundaries of a liquid system

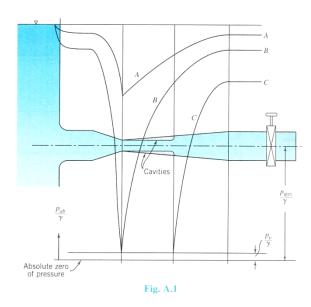
In a flow fluid wherever the <u>local pressure falls to the vapor pressure</u> of the liquid,

local vaporization occurs.

High velocity region

- \rightarrow <u>Cavities</u> are formed in the low pressure regions.
- → The cavity contains a swirling mass of droplets and vapor.
- → Cavities are swept downstream into a region of high pressure.

- → Then, cavities are collapses suddenly.
- → surrounding liquid rush into the void together
- → it causes <u>erosion</u> (pitting) of solid boundary surfaces in machines, and vibration
- → boundary wall receives a blow as from a tiny hammer

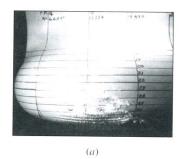


• Prevention of cavitation

- ~ cavitation is of great importance in the design of high-speed hydraulic machinery such as turbines, pumps, in the overflow and underflow structures of high dams, and in high-speed motion of underwater bodies (submarines, hydrofoils).
 - → design improved forms of boundary surfaces

 \rightarrow predict and control the exact nature of cavitation \rightarrow set limits

Body cavitation



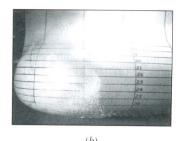


FIGURE 2-28

• Boiling:

- = rapid rate of vaporization caused by an increase in temperature
- = formation of vapor bubbles throughout the fluid mass
- \sim occur (whatever the temperature) when the external absolute pressure imposed on the liquid is equal to or less than the vapor pressure of the liquid
- \sim boiling point = f (imposed pressure, temp.)

$$p_{atm} \le p_v \rightarrow \text{boiling occurs}$$

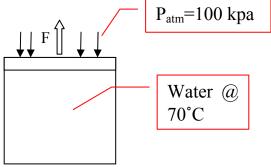
Table A2.4b Table A2.5b

[Ex] boiling point of water

altitude (El. m)	Temp. (°C)	p_{v} (kPa), absolute	p_{atm} (kPa), absolute	boiling point (°C)	remark
m.s.l.	100	101.3	101.3	100	
12,000	60	19.9	19.4	60	undercooked

• Evaporation: When the space surrounding the liquid is too large, the liquid continues to vaporize until the liquid is gone and only vapor remains at a pressure less than or equal p_{v} .

[IP 1.12] For a vertical cylinder of diameter 300 mm, find min. force that will cause the water boil.



[Sol] From Table A2.4b; p_v =31.16 kPa at 70 °C

For water to boil; $p' \le p_v = 31.16$,

$$p' = 100 - \frac{F}{A} = 31.16$$

$$\therefore F = (100 - 31.16) \frac{\pi (0.3)^2}{4} = 4.87 \text{ kN}$$

Homework Assignment #1

Due: 1 week from today

- Prob. 1.2
- Prob. 1.10
- Prob. 1.27
- Prob. 1.46
- Prob. 1.49
- Prob. 1.58
- Prob. 1.69
- Prob. 1.72
- Prob. 1.82