

# Electro-optic effect

Dr Yoonchan Jeong

School of Electrical Engineering, Seoul National University

Tel: +82 (0)2 880 1623, Fax: +82 (0)2 873 9953

Email: [yoonchan@snu.ac.kr](mailto:yoonchan@snu.ac.kr)

# Nonlinear polarisation

## □ Constitutive relations

$$\mathbf{D} = \epsilon \mathbf{E} = \epsilon_0 \mathbf{E} + \mathbf{P},$$

$$\mathbf{P} = \epsilon_0 \chi \mathbf{E}$$

## □ Origin of nonlinear response

Related to anharmonic motion of bound electrons under the influence of an applied field.

$$\mathbf{P} = \epsilon_0 \chi \mathbf{E} = \epsilon_0 \left( \chi^{(1)} \mathbf{E} + \chi^{(2)} \mathbf{E} \mathbf{E} + \chi^{(3)} \mathbf{E} \mathbf{E} \mathbf{E} + \dots \right)$$

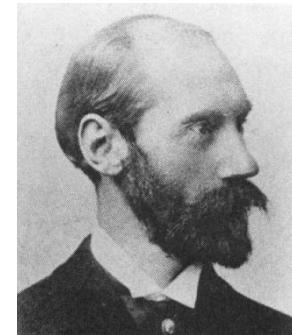
Note:  $\chi^{(2)}$  is non-zero only for media that lack an inversion symmetry (centrosymmetry).

# Linear electro-optic effect

Also called **Pockels** effect: Refractive index change linearly proportional to the external electric field, i.e.  $\Delta n \propto E_{ext}$ .

Recall  $\mathbf{P} = \epsilon_0 \chi \mathbf{E} = \epsilon_0 (\chi^{(1)} \mathbf{E} + \cancel{\chi^{(2)} \mathbf{E} \mathbf{E}} + \cancel{\chi^{(3)} \mathbf{E} \mathbf{E} \mathbf{E}} + \dots)$

For  $\Delta n = C_L E_{ext}$ ,  $C_L \sim 10^{-12} \text{ m/V}$



Friedrich Carl Alwin Pockels (1865 - 1913)

# Quadratic electro-optic effect

Also called **Kerr** effect: Refractive index change quadratically proportional to the external electric field, i.e.  $\Delta n \propto E_{ext}^2$ .

Recall  $P = \epsilon_0 \chi E = \epsilon_0 (\chi^{(1)} E + \chi^{(2)} \cancel{EE} + \chi^{(3)} \cancel{EEE} + \dots)$

For  $\Delta n = C_Q E_{ext}^2$ ,  $C_Q \sim 10^{-18} \text{ m}^2/\text{V}^2$

Kerr constant:  $\Delta n = K \lambda E^2$

e.g.  $K = 5.1 \times 10^{-14} \text{ m/V}^2$  for water



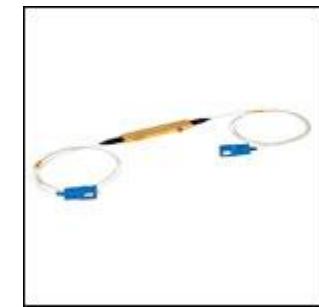
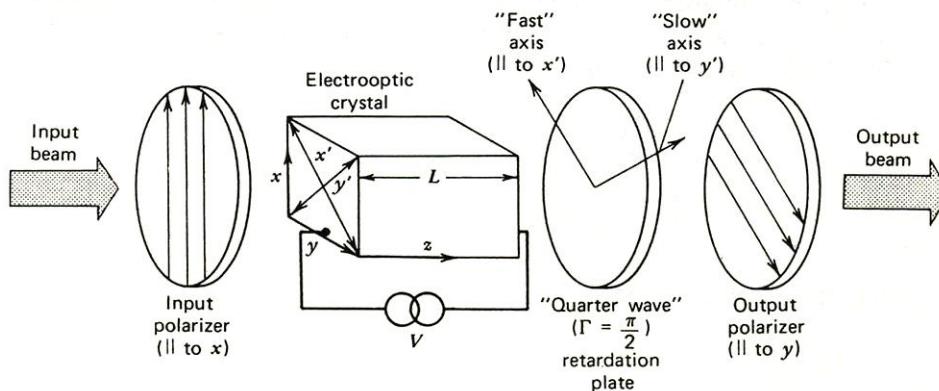
John Kerr  
(1824-1907)

Intensity dependent refractive index:  $\Delta n = n_2 I$ , where  $I = \frac{1}{2} \epsilon_0 c n |E|^2$

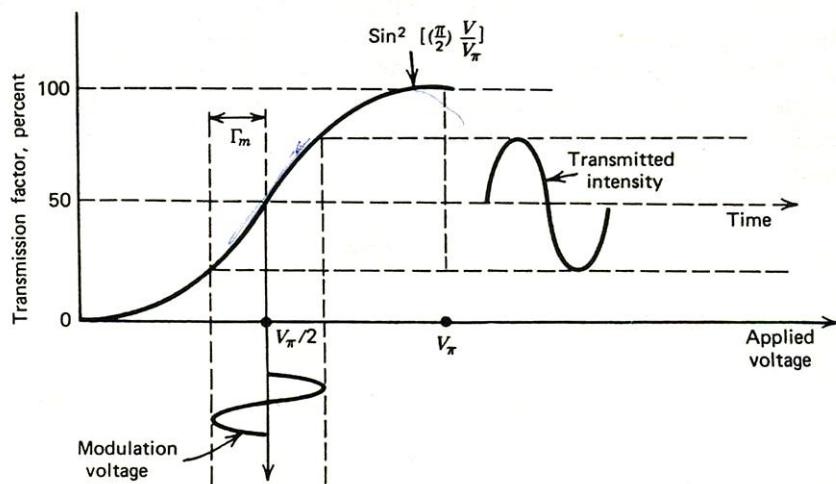
e.g.  $n_2 \sim 3 \times 10^{-20} \text{ m}^2/\text{W}$  for silica glass

# Electro-optic amplitude modulator

Thorlabs



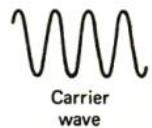
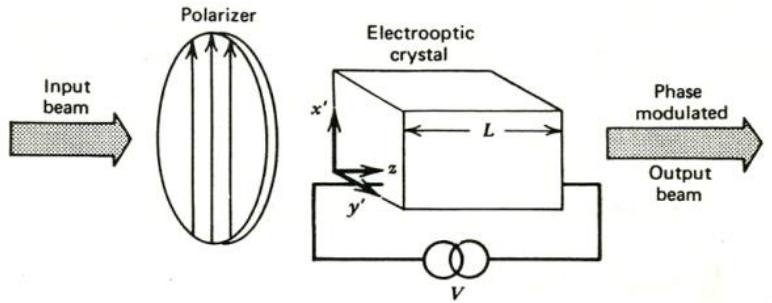
Source: Thorlabs



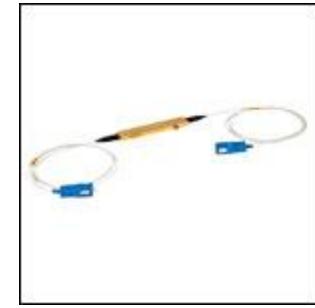
$$\Gamma = \frac{\pi}{2} + \Gamma_m \sin \omega_m t$$

Source: *Optical Waves in Crystals*, A. Yariv and P. Yeh

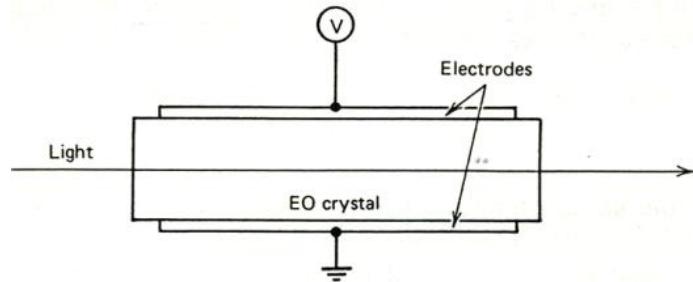
# Electro-optic phase modulator



$$E_{out} = A \cos \left[ \omega t - \frac{\omega}{c} (n_o + C_L E_m \sin \omega_{mt} t) L \right]$$

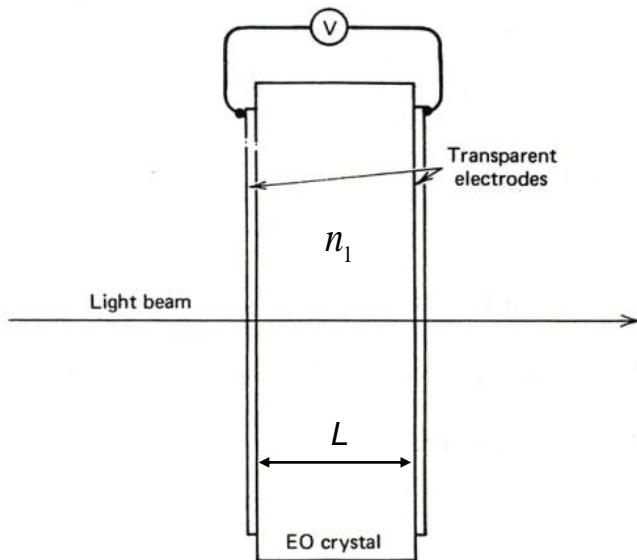


Source: Thorlabs



Source: *Optical Waves in Crystals*, A. Yariv and P. Yeh

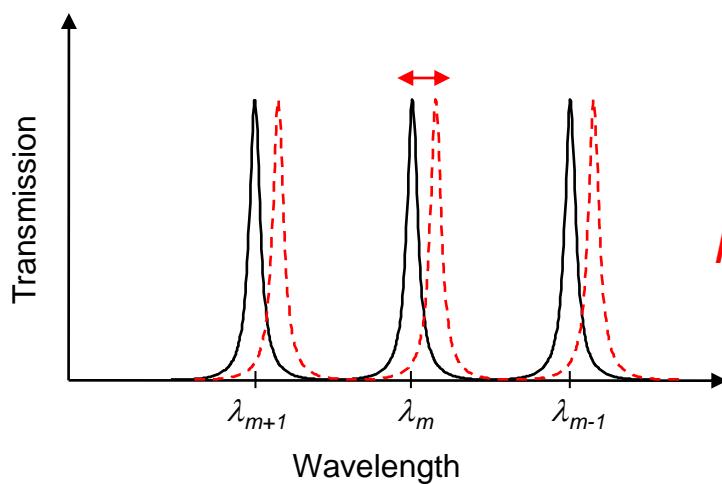
# Electro-optic modulator (Fabry-Perot filter)



Source: *Optical Waves in Crystals*, A. Yariv and P. Yeh



Charles Fabry  
(1867-1945 )      Alfred Perot  
(1863-1925)



*For the maximum transmission:*

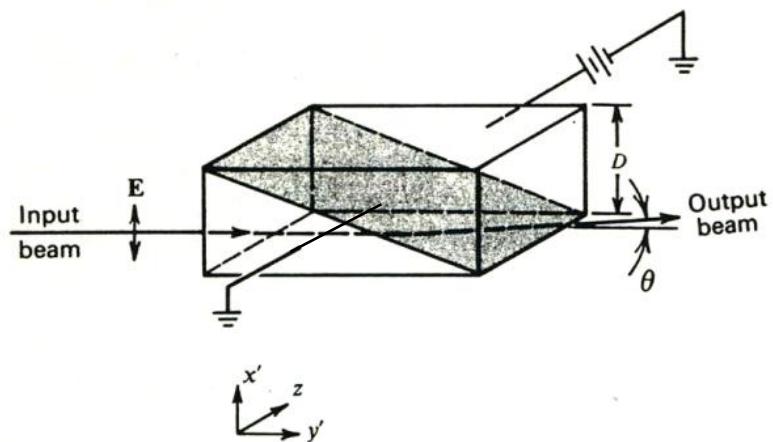
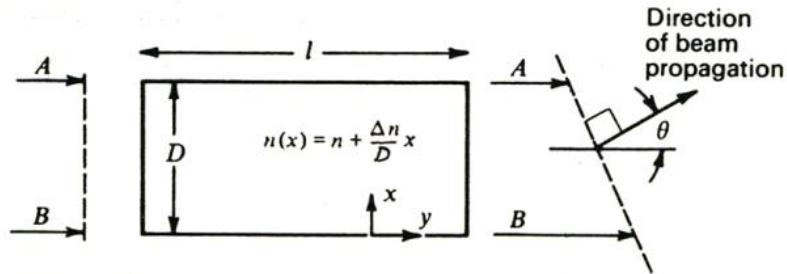
$$2kL = 2\frac{2\pi L}{\lambda} n_1 = 2m\pi, \quad m=1, 2, 3, \dots$$

$$\lambda_m = \frac{2L}{m} n_1$$

*If voltage applied:*

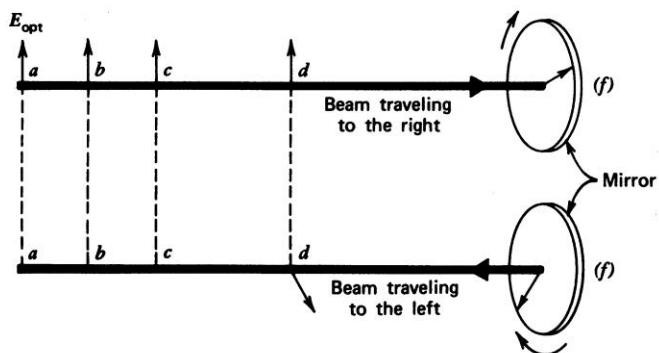
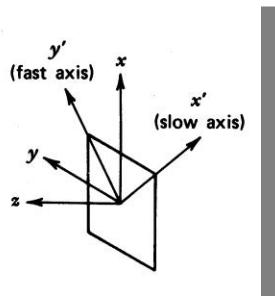
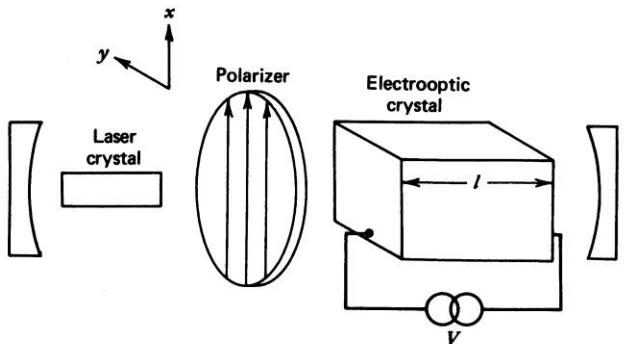
$$\lambda_m = \frac{2L}{m} (n_1 + C_L E_{ext})$$

# Electro-optic beam deflector



Source: *Optical Waves in Crystals*, A. Yariv and P. Yeh

# Electro-optic Q-switch



For beam traveling to right:

At point *d*,

$$\left. \begin{aligned} E_x' &= \frac{E}{\sqrt{2}} \cos \omega t \\ E_y' &= \frac{E}{\sqrt{2}} \cos \omega t \end{aligned} \right\} \text{The optical field is linearly polarized with its electric field vector parallel to } x$$

At point *f*,

$$\left. \begin{aligned} E_x' &= \frac{E}{\sqrt{2}} \cos (\omega t - kl - \frac{\pi}{2}) \\ E_y' &= \frac{E}{\sqrt{2}} \cos (\omega t - kl) \end{aligned} \right\} \text{Circularly polarized}$$

For beam traveling to left:

At point *f*,

$$\left. \begin{aligned} E_x' &= -\frac{E}{\sqrt{2}} \cos (\omega t - kl - \frac{\pi}{2}) \\ E_y' &= -\frac{E}{\sqrt{2}} \cos (\omega t - kl) \end{aligned} \right\} \text{Circularly polarized}$$

At point *d*,

$$\left. \begin{aligned} E_x' &= -\frac{E}{\sqrt{2}} \cos (\omega t - 2kl - \pi) \\ E_y' &= -\frac{E}{\sqrt{2}} \cos (\omega t - 2kl) \end{aligned} \right\} \text{Linearly polarized along } y$$

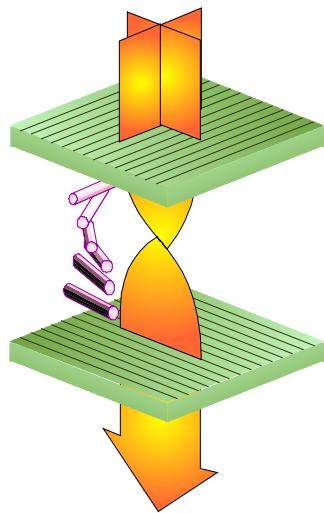
Source: *Optical Waves in Crystals*, A. Yariv and P. Yeh

# Electro-optic property of liquid crystal

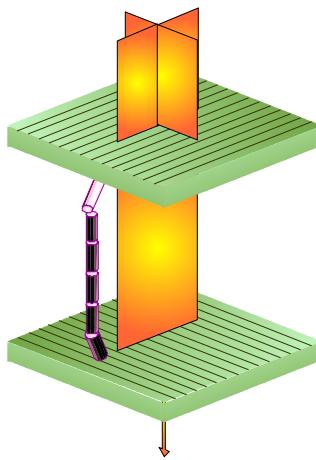
## □ Liquid crystals

- Liquid crystal phases: smectic, nematic, and cholesteric
- Nematic LC: uniaxial dipole moment  
⇒ dynamic director alignment along the applied electric field
- Switching time: ~msec

## □ Twisted nematic LC in liquid crystal displays (LCD's)



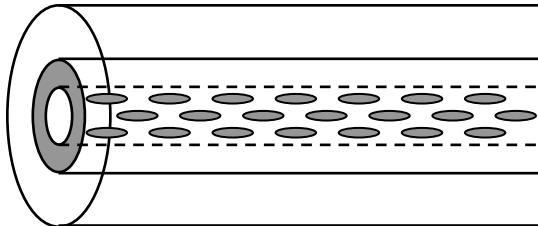
$V_{LC} = 0V$  (off)



$V_{LC} = 5V$  (on)

Applicable to  
fiber-optic devices?

# LC-filled hollow fiber

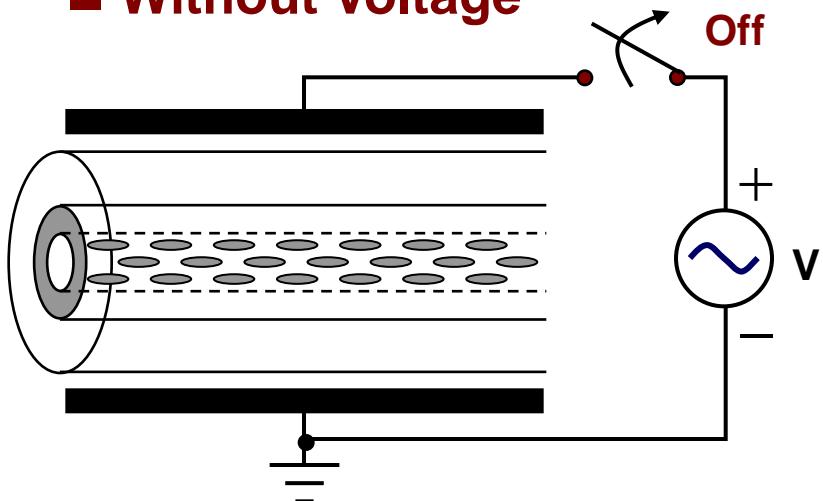


## ■ Initial Alignment of nematic LC

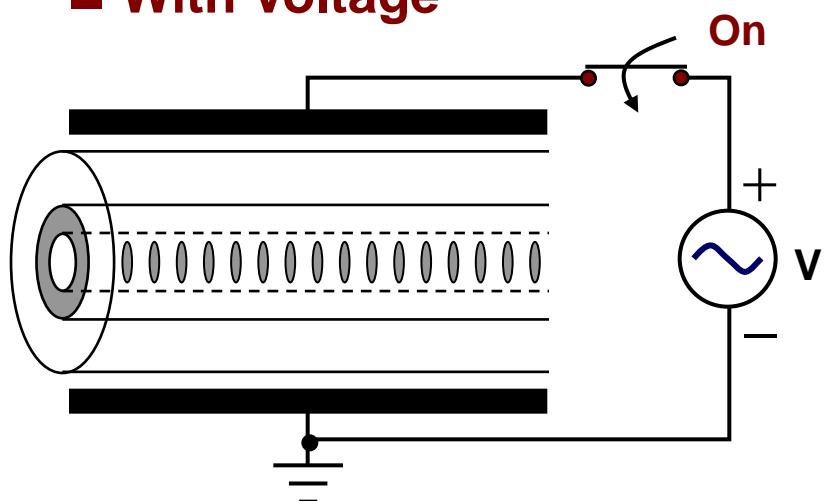
### □ Director alignment of nematic LC

- Highly dependent on the liquid crystals-capillary interface interaction
- Silica: longitudinal direction, borosilicate capillaries: radial direction

## ■ Without Voltage



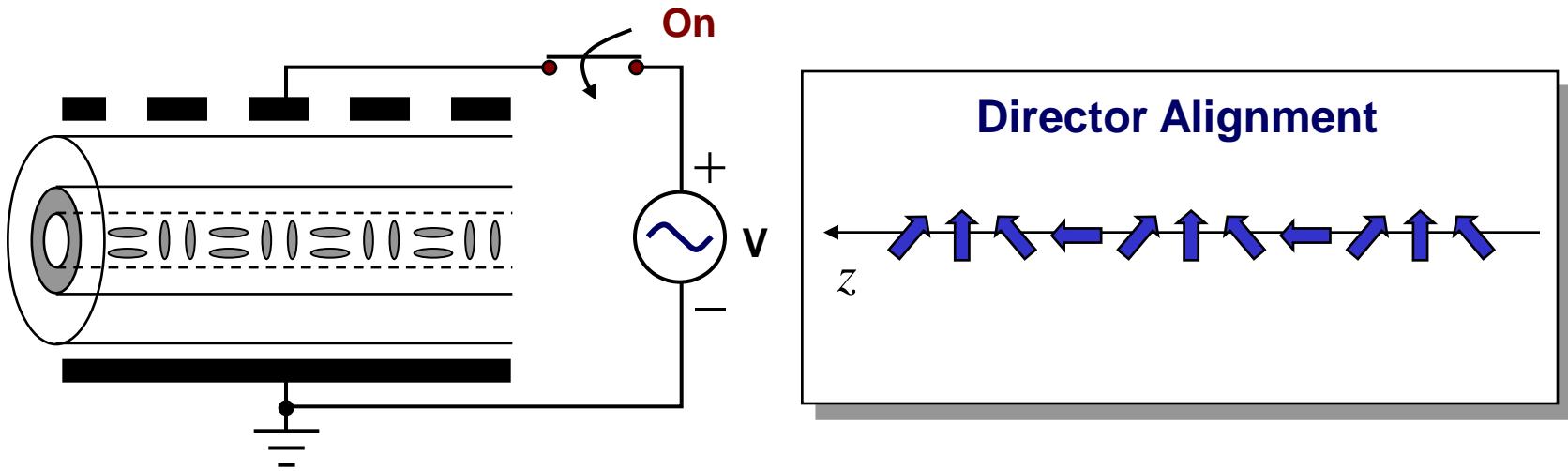
## ■ With Voltage



# LC fiber grating with a comb electrode

## □ Comb electrode

- Periodically patterned electrode with openings

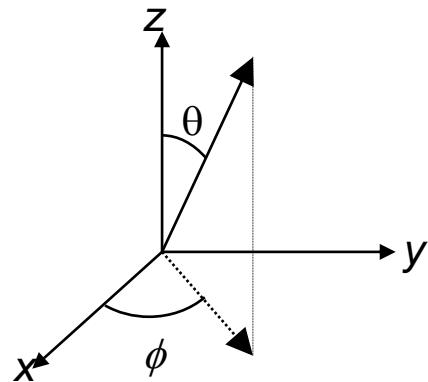


## □ Electrically controllable director alignment

- Periodical modulation of director alignment
- Controllable long-period gratings

# Anisotropic mode couplings in the LC core

## □ Permittivity tensor according to director alignment



$$\varepsilon_{xyz}(\theta) = \varepsilon_o \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta & -\sin\theta \\ 0 & \sin\theta & \cos\theta \end{pmatrix} \cdot \begin{pmatrix} n_o^2 & 0 & 0 \\ 0 & n_o^2 & 0 \\ 0 & 0 & n_e^2 \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta & \sin\theta \\ 0 & -\sin\theta & \cos\theta \end{pmatrix}$$

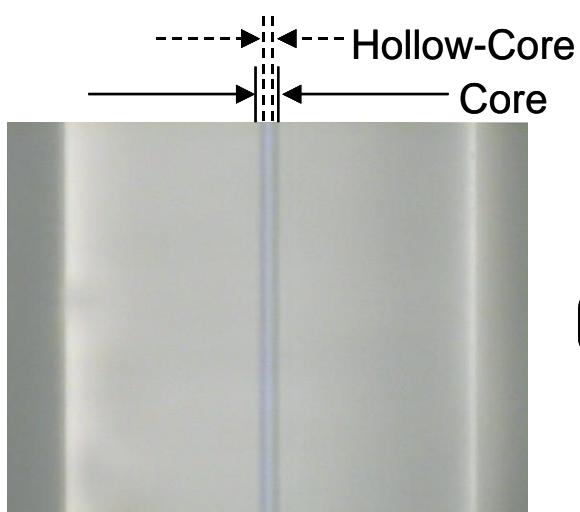
$$\varepsilon_{r\phi z}(\theta, \phi) = \varepsilon_o \begin{pmatrix} \cos\phi & \sin\phi & 0 \\ -\sin\phi & \cos\phi & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot \varepsilon_{xyz}(\theta) \cdot \begin{pmatrix} \cos\phi & -\sin\phi & 0 \\ \sin\phi & \cos\phi & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Permittivity perturbation  $\Rightarrow \Delta\varepsilon_{r\phi z}(\theta, \phi) = \varepsilon_{r\phi z}(\theta, \phi) - \varepsilon_{r\phi z}(0, 0)$

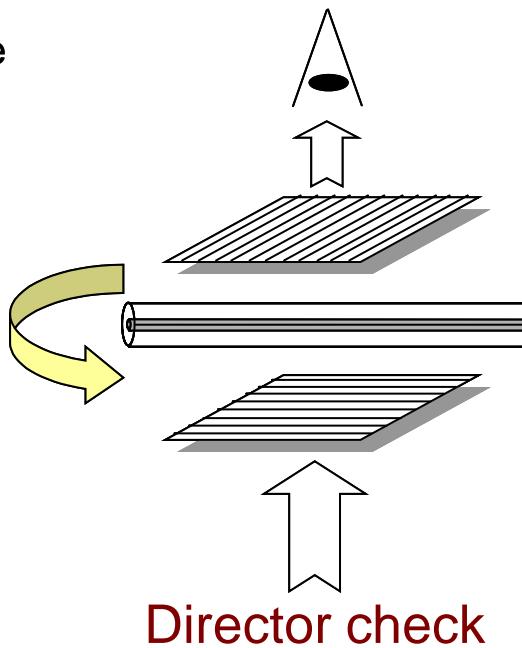
## □ Mode couplings

- Long-period regime: a fundamental  $HE_{11}$  core mode  $\Leftrightarrow$  cladding modes
- Cladding modes to be coupled:  $TM_{0m}^{cl}, TE_{0m}^{cl}, HE_{1m}^{cl}, HE_{2m}^{cl}, HE_{3m}^{cl}$   
 $\Leftrightarrow$  Non-symmetric azimuthal  $\phi$ -variation in  $\Delta\varepsilon_{r\phi z}(\theta, \phi)$

# LC-filled hollow fiber

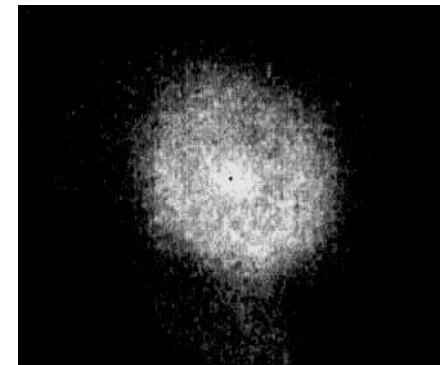


Fiber image



Director check

LC-filling: **MLC-6295**



Far-field image

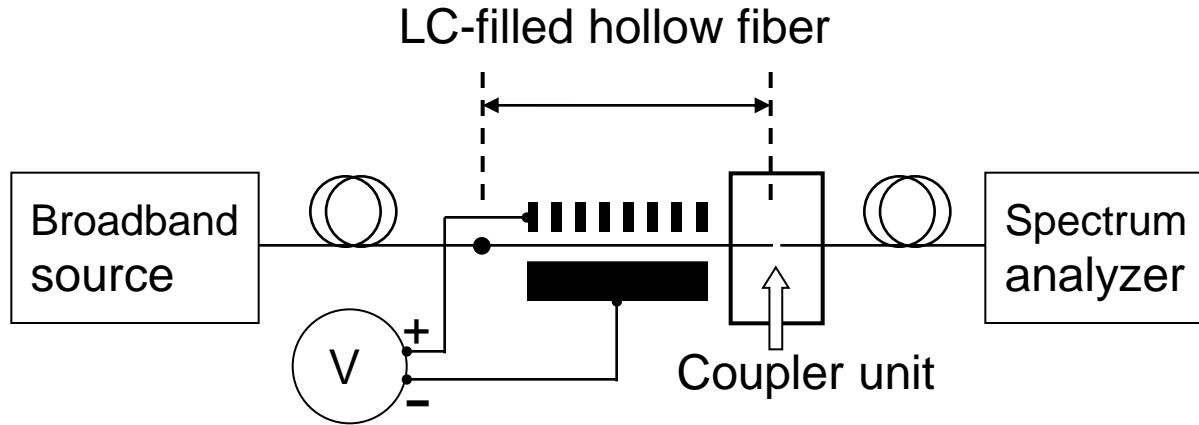
## Properties of MLC-6295

- Smectic/Nematic turning point:  $-30\text{ }^{\circ}\text{C}$ , clearing point  $+101\text{ }^{\circ}\text{C}$
- $n_o: 1.4772$ ,  $n_e: 1.5472$  @  $20\text{ }^{\circ}\text{C}$ , 589 nm

## Director alignment check

- Visibility detection under a microscope between crossed polarizers
- Uniform director alignment to the direction of fiber axis

# Experimental layout



## □ Experimental apparatus

- Broadband source: EDFA ASE

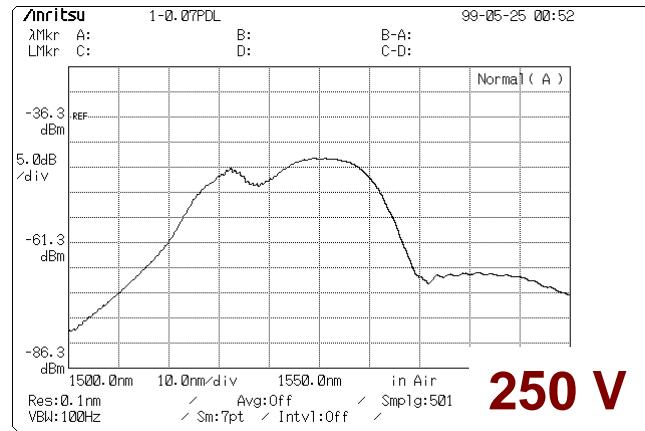
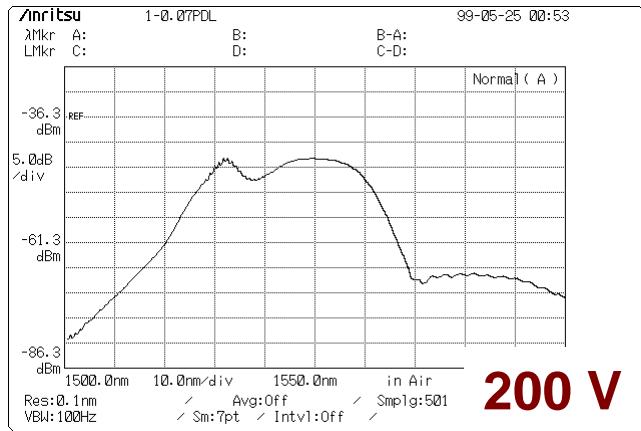
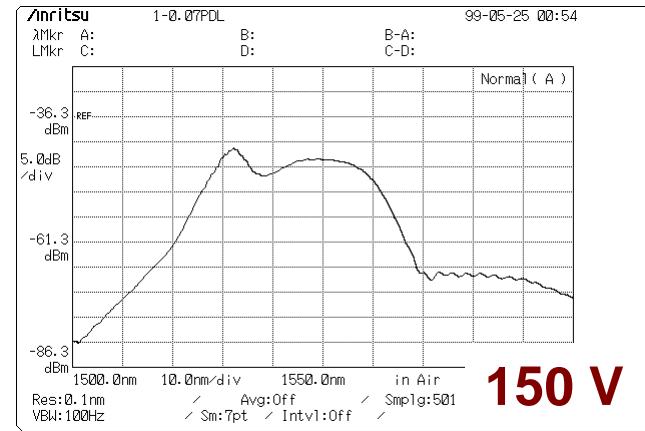
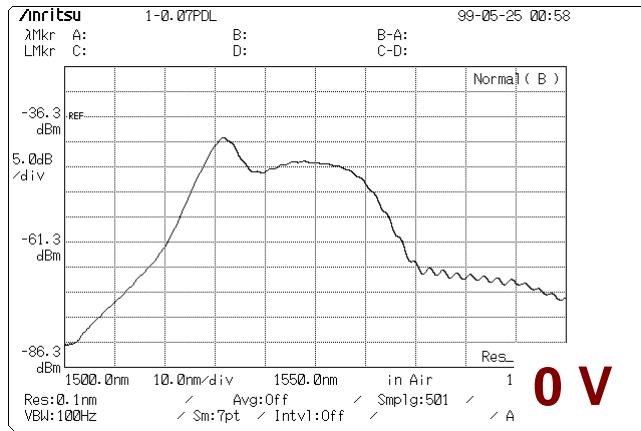
- Comb electrode

Period of openings:  $483 \mu\text{m}$ , effective grating length: 15.5 mm

- Applied voltage: 0 ~ 250 V

# Long-period LC fiber grating

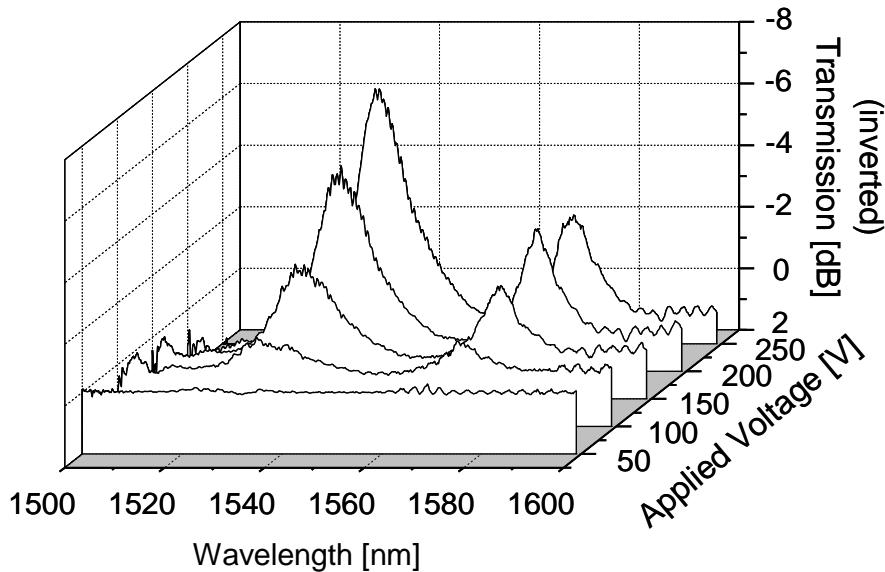
## □ Spectral responses according to applied voltages



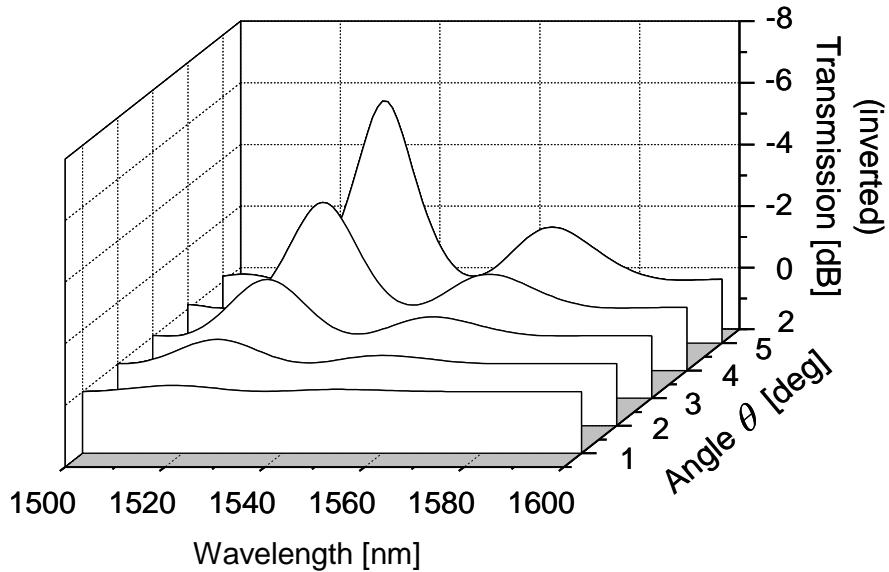
# Long-period LC fiber grating

## □ Normalized spectral responses

Experiments



Simulations



## □ Simulations

- Based on the discretized coupled-mode theory in anisotropic media
- Resonant couplings to the 3rd and 4th TM cladding modes

# Nonlinear response of fiber gratings

## ■ Nonlinear Coupled-Mode Theory

$$\nabla \cdot (E' \times H_p^* + E_p^* \times H') = -i\omega E_p^* \cdot (\Delta\epsilon_L + \Delta\epsilon_{NL}) E', \quad (p=1,2,\dots)$$

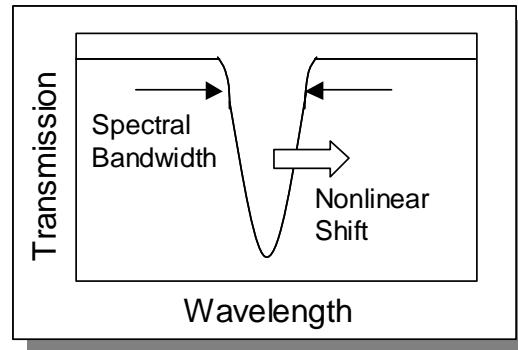
$$\Delta\epsilon_{NL(q)} = \epsilon_o \frac{3}{4} \chi^{(3)}(r, \phi, z) \cdot \sum_s \alpha_{(q,s)} |E_s(t, z)|^2 |\hat{e}_s|^2, \quad \alpha_{(q,s)} = \begin{cases} 1 & (q=s), \\ 2 & (q \neq s). \end{cases}$$

## ■ Efficiency of All-Optical Switching in Fiber Gratings

- Conditions for high efficiency:

- Large nonlinear spectral shift &  
Rapid spectral modulation band

- Nonlinear spectral shift:  $\frac{\Delta\lambda_s}{\lambda} \approx \frac{n_{2,eff} I_{eff}}{\Delta n_g}$



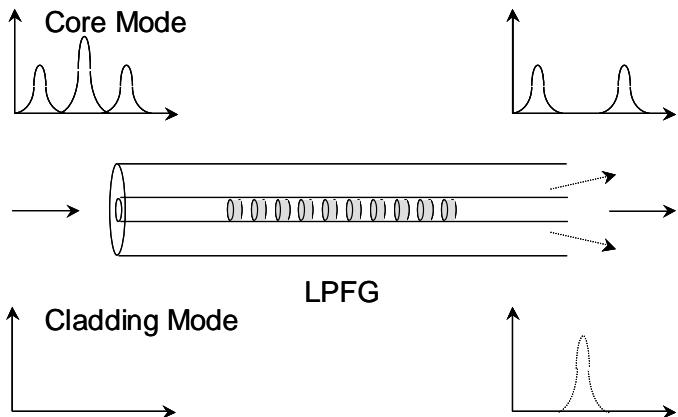
FBG: Steep spectral modulation slope but small spectral shift

LPFG: Large spectral shift but slow spectral modulation slope

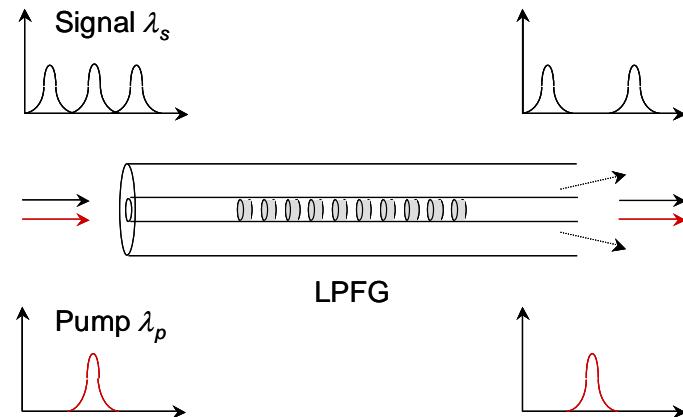
⇒ Cascaded LPFG's

# Nonlinear response of LPFGs

## ■ SPM Regime

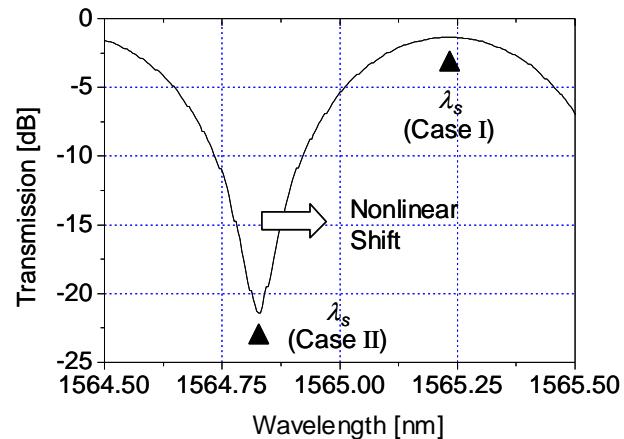


## ■ XPM Regime



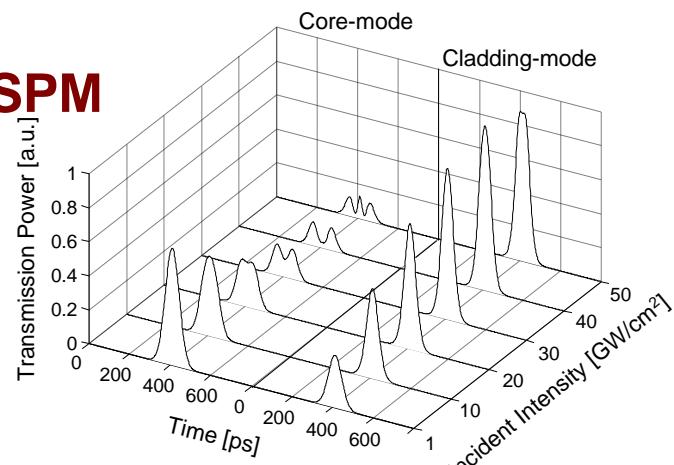
## ■ All-Optical Gating Mode

- Normally white mode (Case I)
- Normally black mode (Case II)

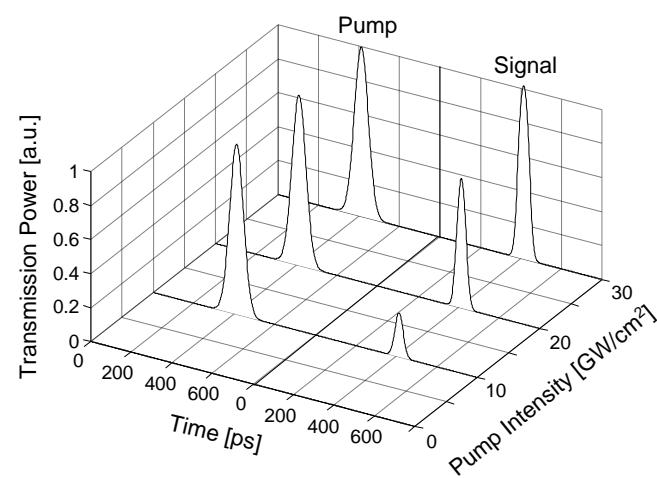
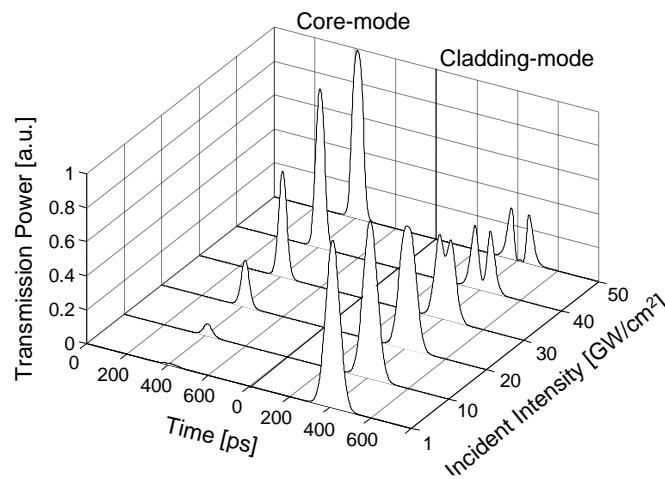
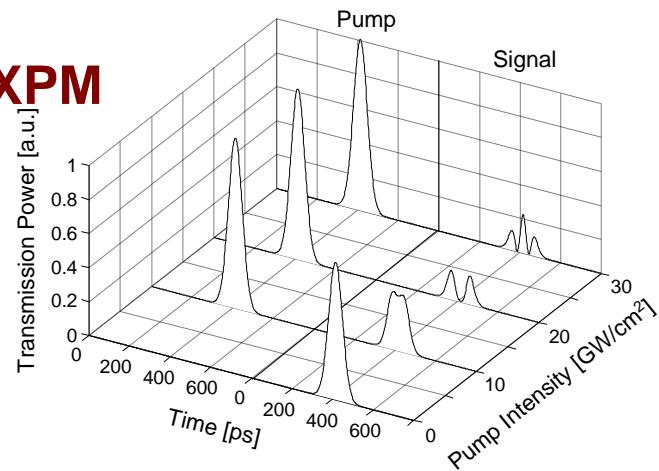


# Nonlinear transmission of wave packets

■ SPM



■ XPM



Y. Jeong and B. Lee, *IEEE J. Quantum Electron.*, 35(9), 1284 (1999).

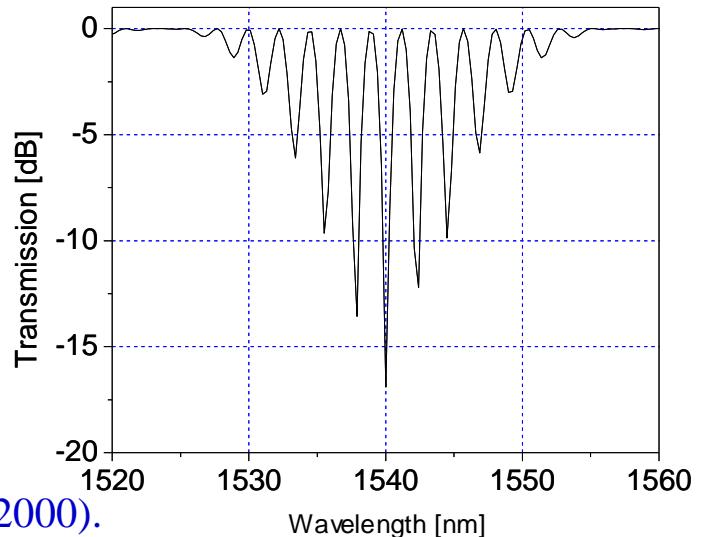
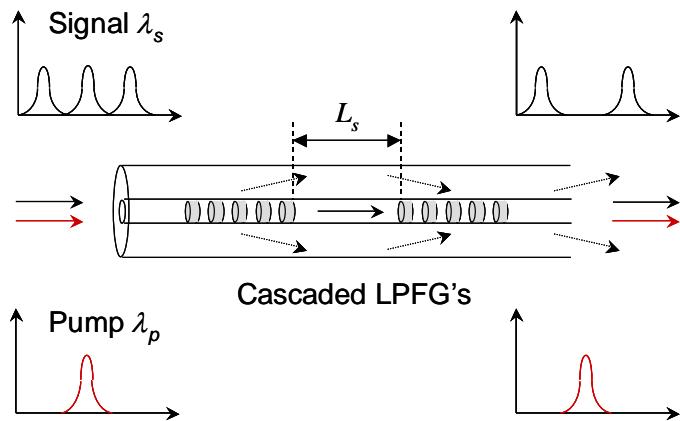
# Cascaded LPFGs

## ■ Spectral Response of Cascaded LPFG's

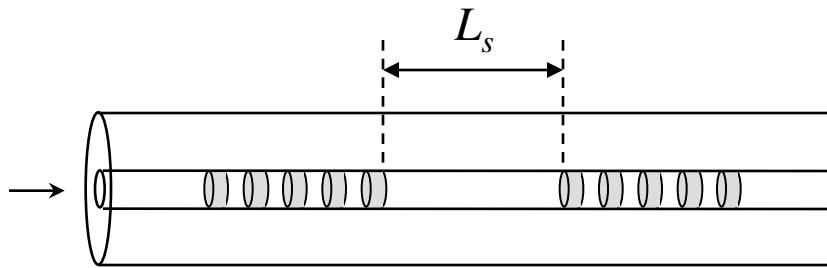
- Transmission of cladding mode:  $|t_{cl}|^2 \propto f_{cl} \left\{ 1 + \cos\left(\frac{2\pi}{\lambda} \Delta n_g L_s + 2\phi_{co}\right) \right\}$
- Spectral fringe spacing:  $\Delta\lambda_{fringe} \approx \frac{\lambda^2}{\Delta n_g L_s}$
- Nonlinear spectral shift:  $\frac{\Delta\lambda_s}{\lambda} \approx \frac{n_{2,eff} I_{eff}}{\Delta n_g}$

*cf. E. M. Dianov et al., ECOC, Gent, Belgium, 1997, pp. 65-68.*

## ■ XPM Regime



# Linear spectra of cascaded LPFGs



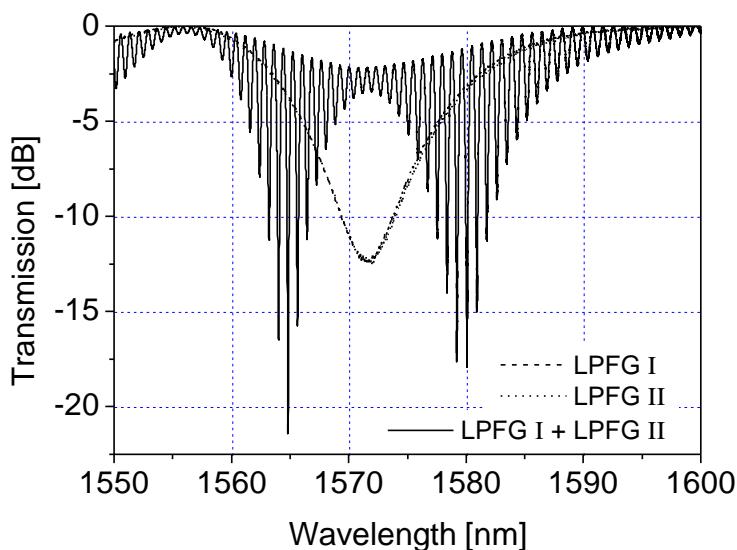
Cascaded LPFGs

## ■ Grating Lengths and Separation

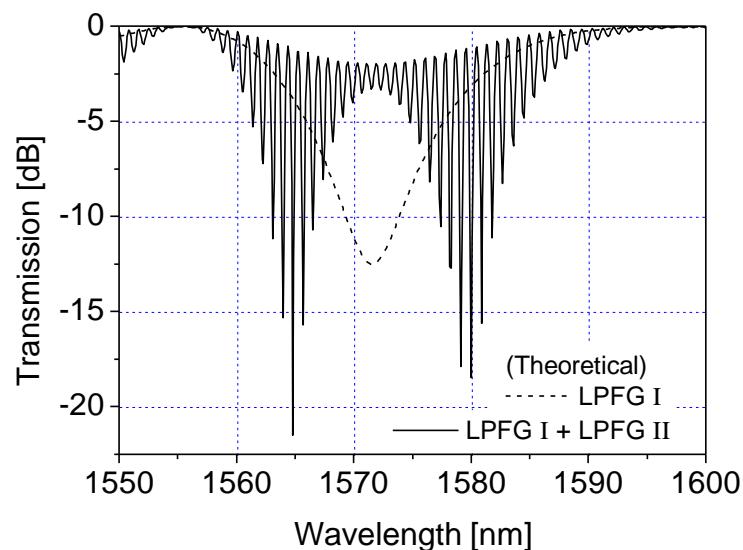
$$\Lambda = 500 \mu\text{m}$$

$$L_I = 3 \text{ cm}, L_{II} = 3 \text{ cm}, L_s = 60 \text{ cm}$$

## ■ Experimental

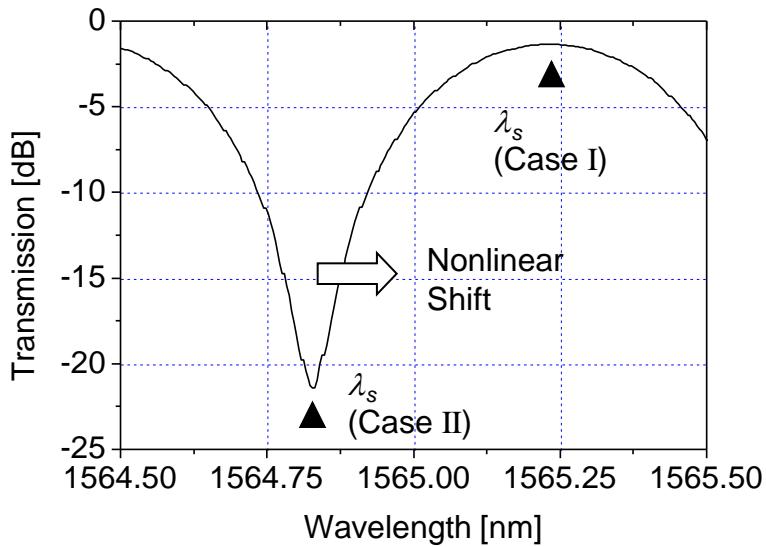


## ■ Theoretical

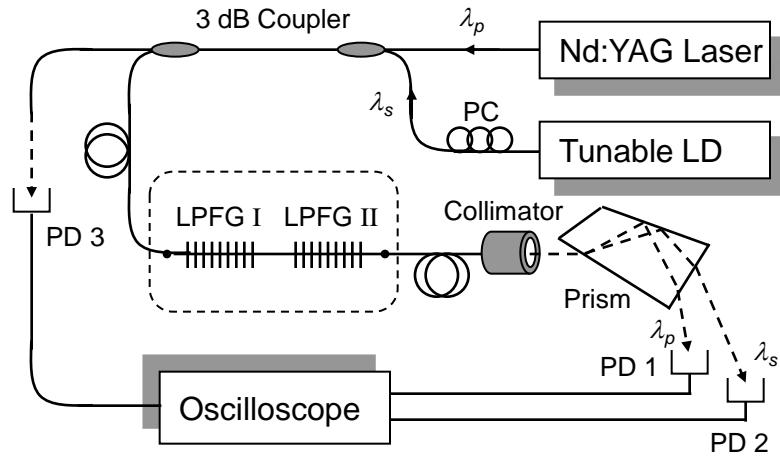


# Experimental arrangement

## ■ Transmission Dip



## ■ Arrangement

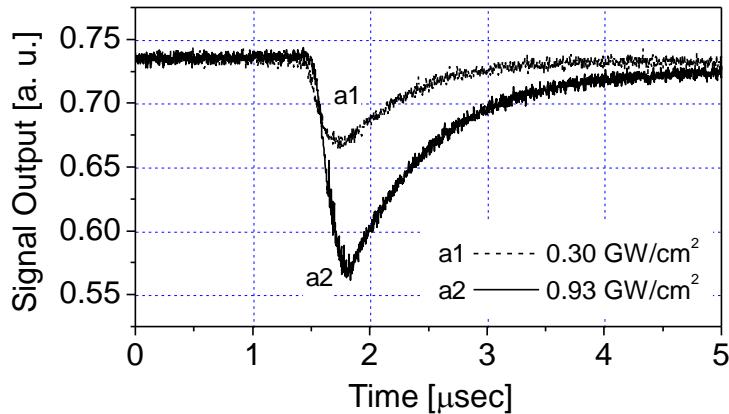


## ■ Experiments

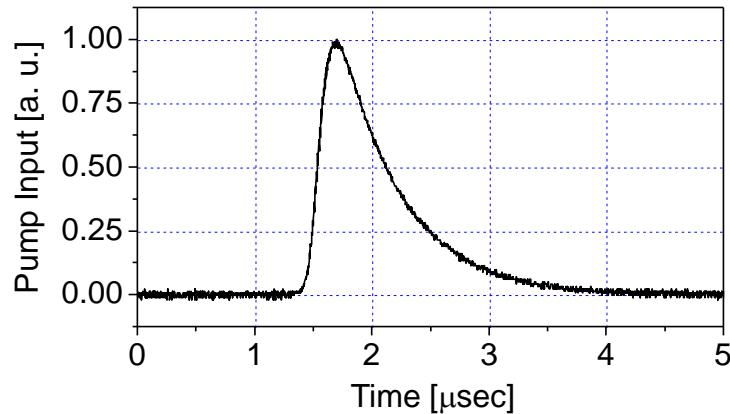
- Signal wave: Tunable LD @1565.2 nm (Case I), @1564.8 nm (Case II)
- Pump wave: Q-switched Nd:YAG laser (1 kHz)

# Experimental results

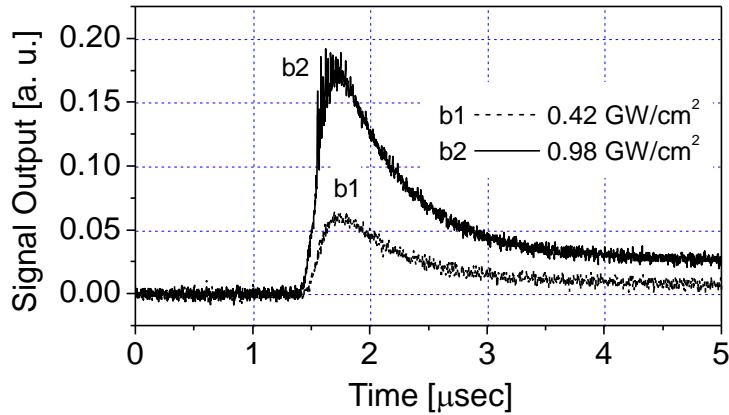
■ Case I



■ Pump



■ Case II



$$\Delta\lambda_s \sim 0.12 \text{ nm}/(\text{GW/cm}^2)$$

