

**2014 Spring**

**“Advanced Physical Metallurgy”  
- Bulk Metallic Glasses -**

**06.10.2014**

**Eun Soo Park**

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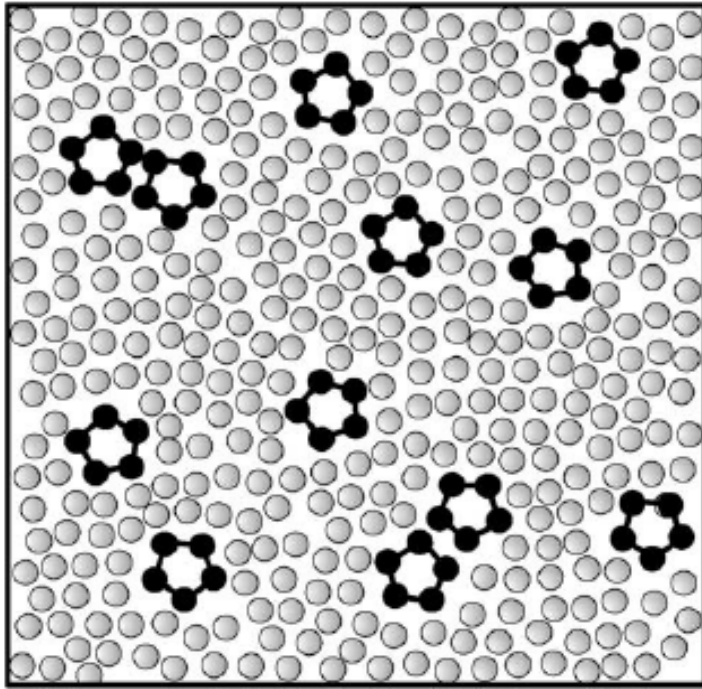
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**Office hours: by appointment**

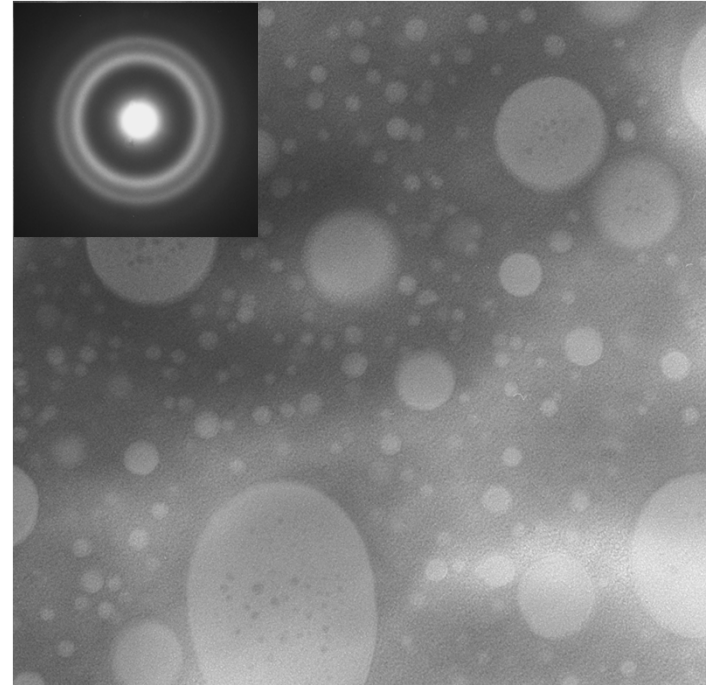
# Effect of element with positive enthalpy of mixing among constituent elements

atomic scale heterogeneity



Enhancement of plasticity in BMGs

Phase separating metallic glasses

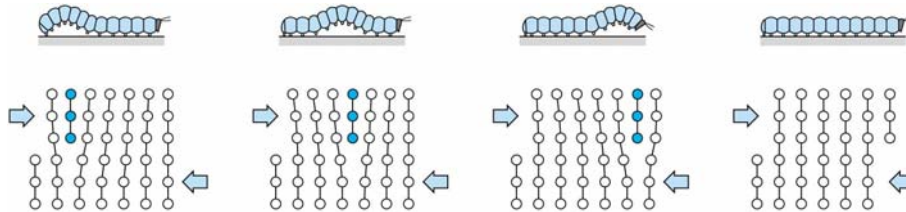
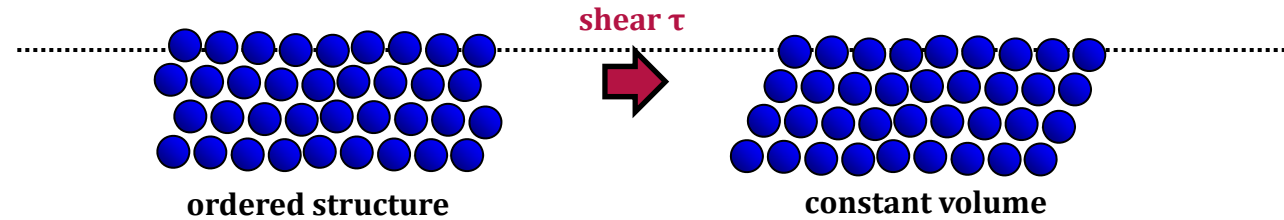


Unique properties

# 8 Mechanical Behavior

## Deformation behavior: crystalline VS. amorphous

**Crystalline**



Dislocation motion in crystalline metal



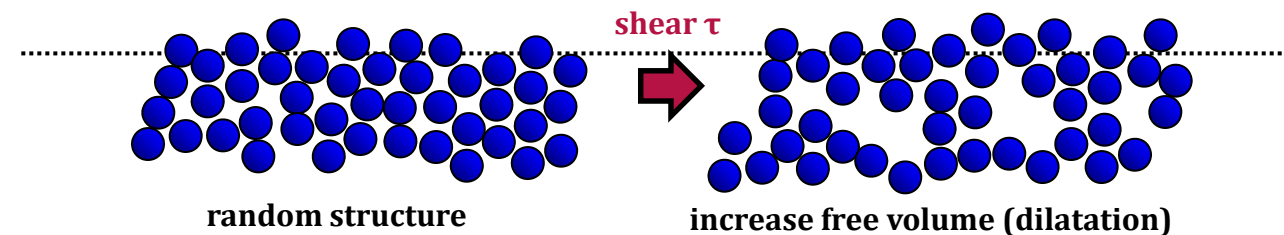
Dislocations

- “Incrementally breaking bonds”
- Has relatively low strength, performs work hardening
- Slip plane + Slip direction = Slip system (preferred crystallographic planes and directions)

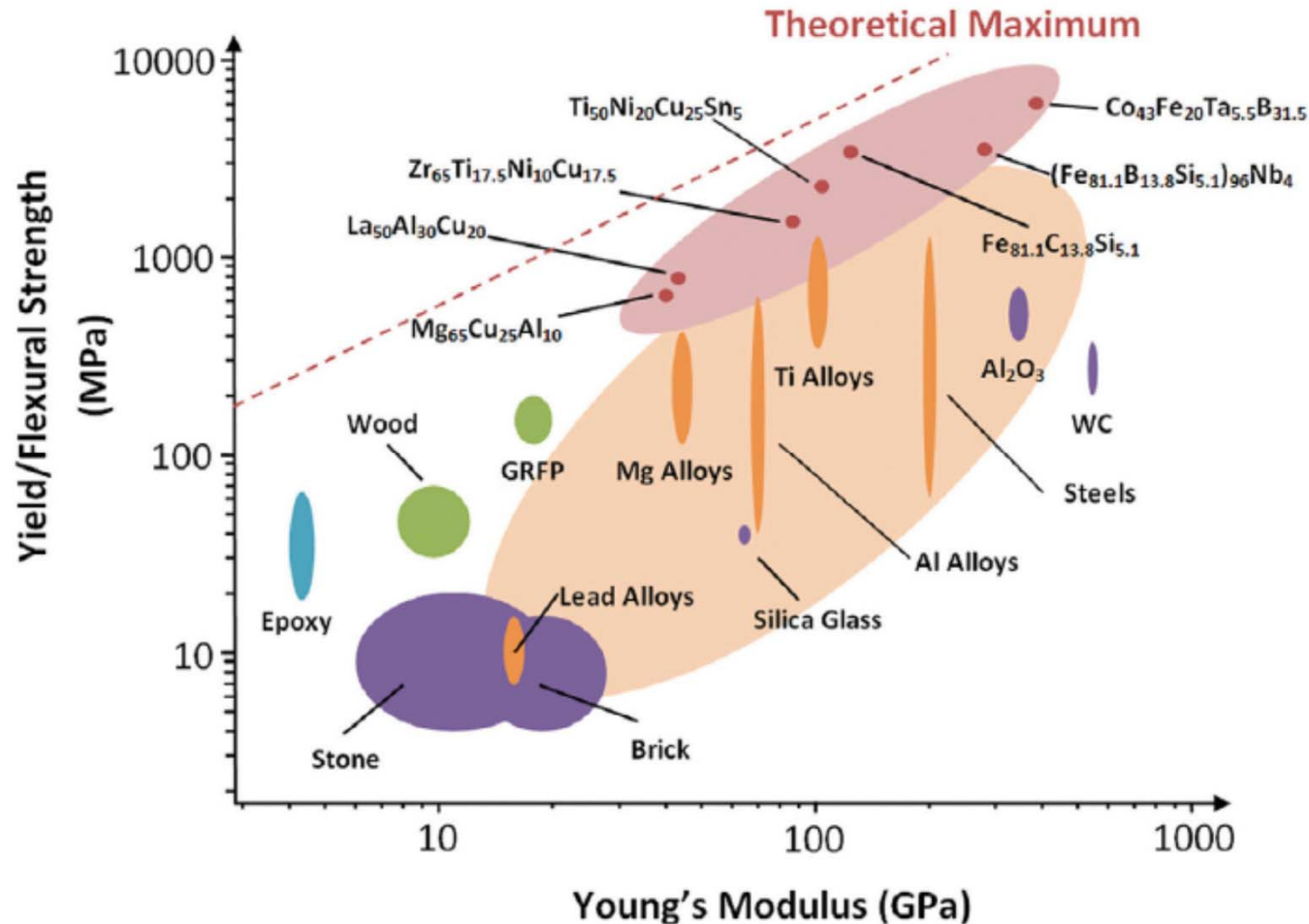
**Amorphous metal do not have slip system.**

**How to deform ?**

**Amorphous**



# a) High strength of Bulk Metallic Glasses



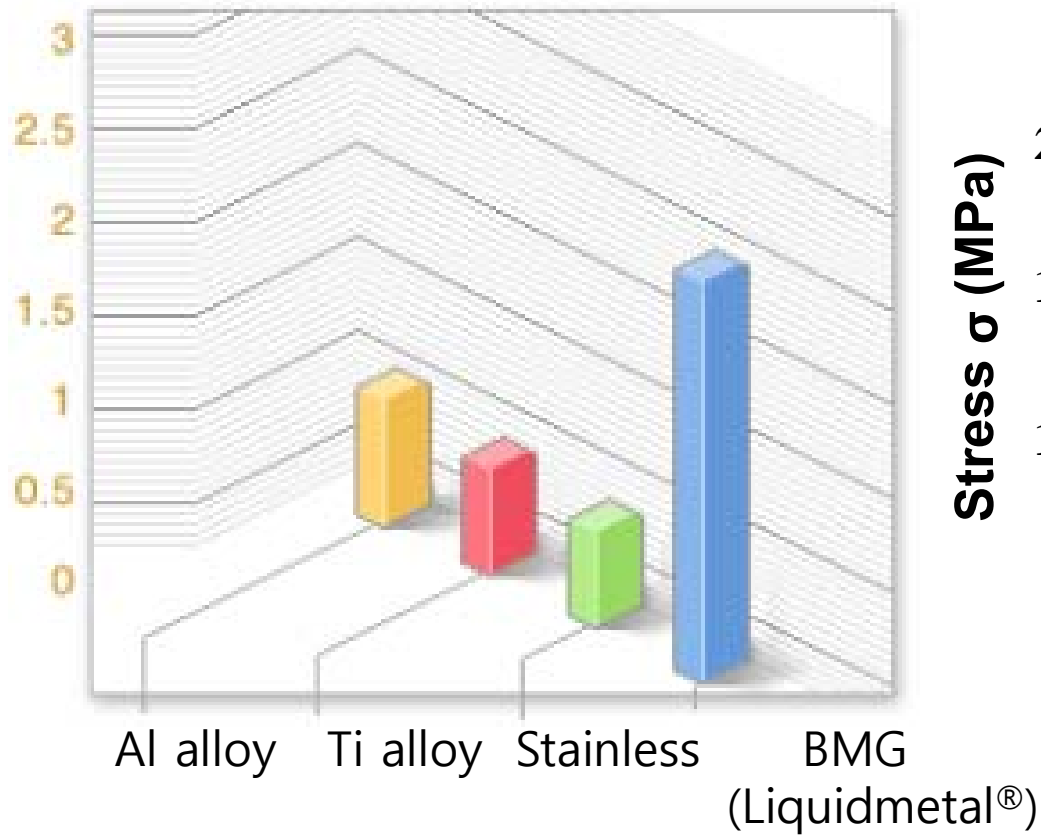
**High fracture strength over 5 GPa in Fe-based BMGs**

*A.L. Greer, E. Ma, MRS Bulletin, 2007; 32: 612.*

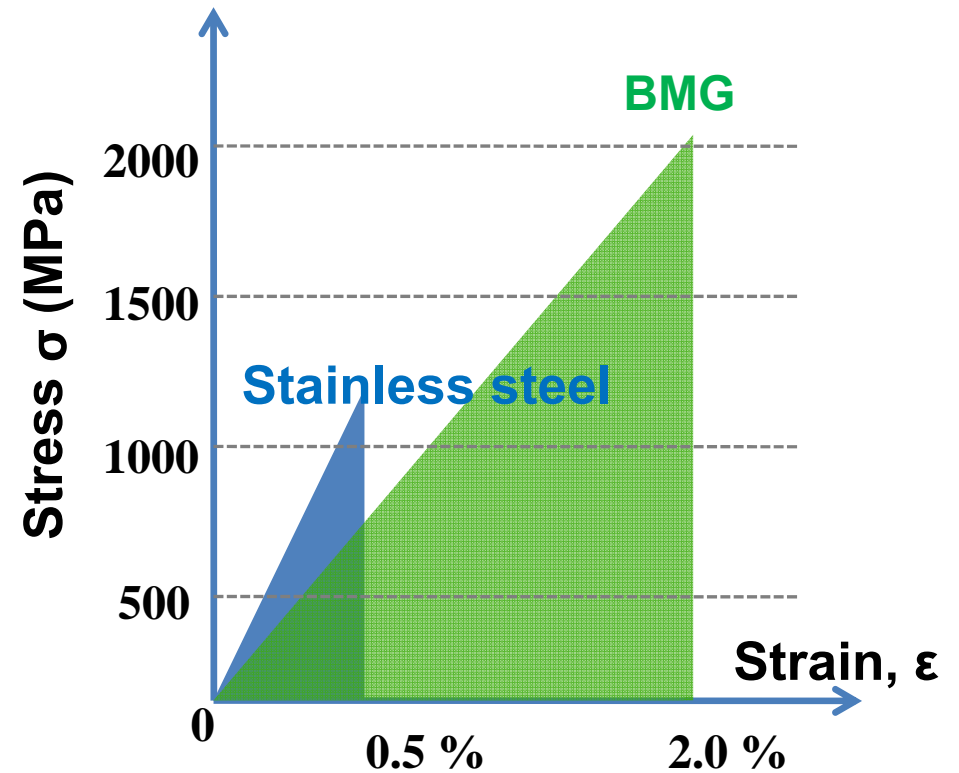
## 2) Large elastic strain limit of BMGs

### Elastic Strain Limit

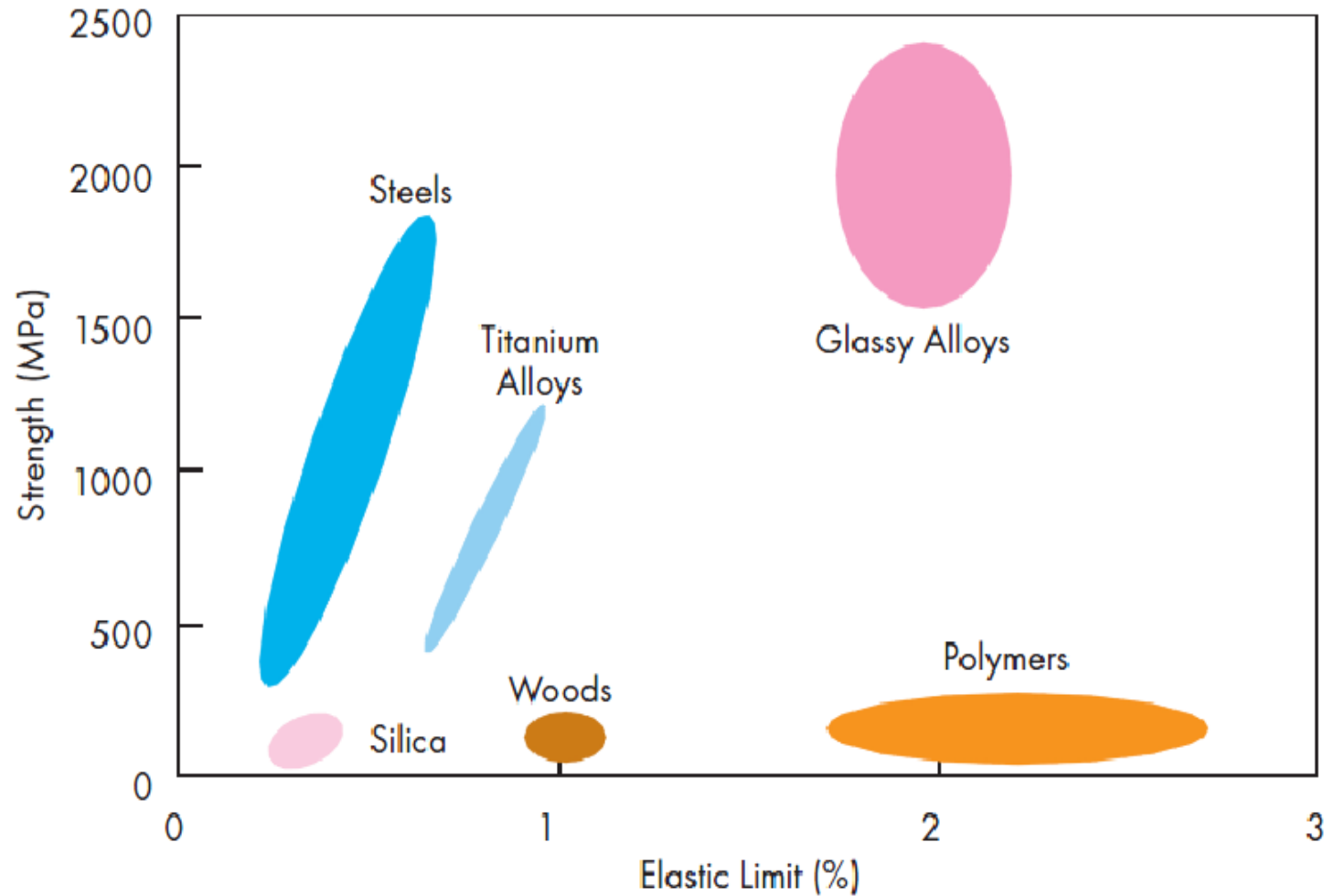
[ as % of Original Shape ]



### Stress-Strain Curve



**\* BMGs with high strength & high elastic limit**



**: Metallic Glasses Offer a Unique Combination of High Strength and High Elastic Limit**

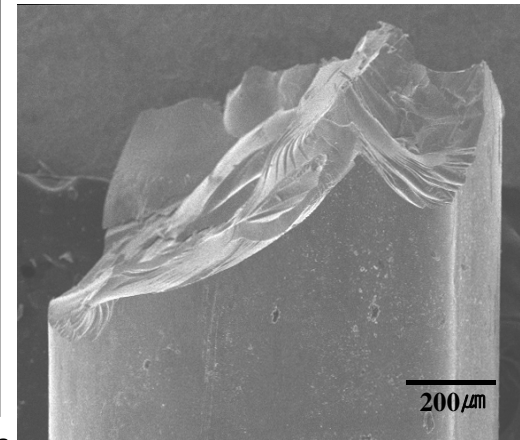
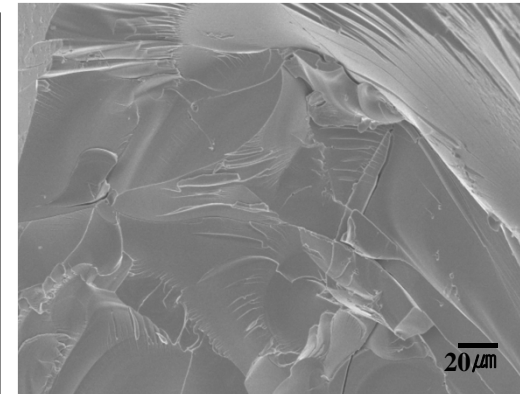
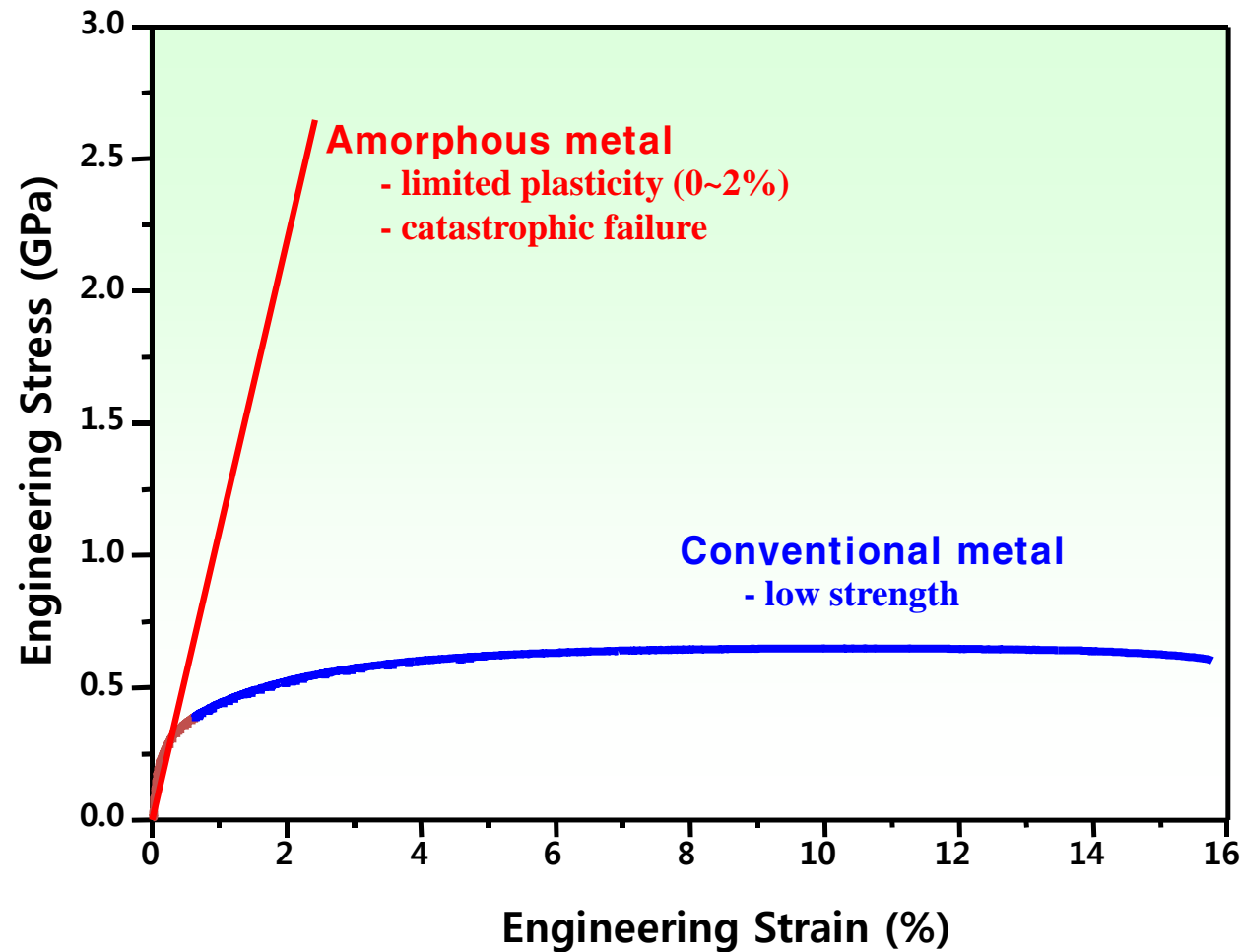
# Drawback of BMGs as a Structural Materials

pc.

# Limited plasticity by shear softening and shear band

- ▶ Microscopically brittle fracture

➔ Death of a material for structural applications





## 8.2 Deformation Behavior

### Deformation behavior of Metallic glass

8.2.2

#### Homogeneous Deformation

- high temp. ( $>0.7T_g$ ) and in the SCLR/  
high strain rate
- Viscous flow  $\rightarrow$  significant plasticity  
: achieve net-shape forming capability
- Newtonian (high temp. & low stress) VS non-  
Newtonian (high temp. & applied stress) :  
associated with the precipitation of nanocrystals

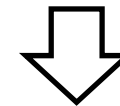


**Homogeneous deformation**

8.2.1

#### Inhomogeneous Deformation

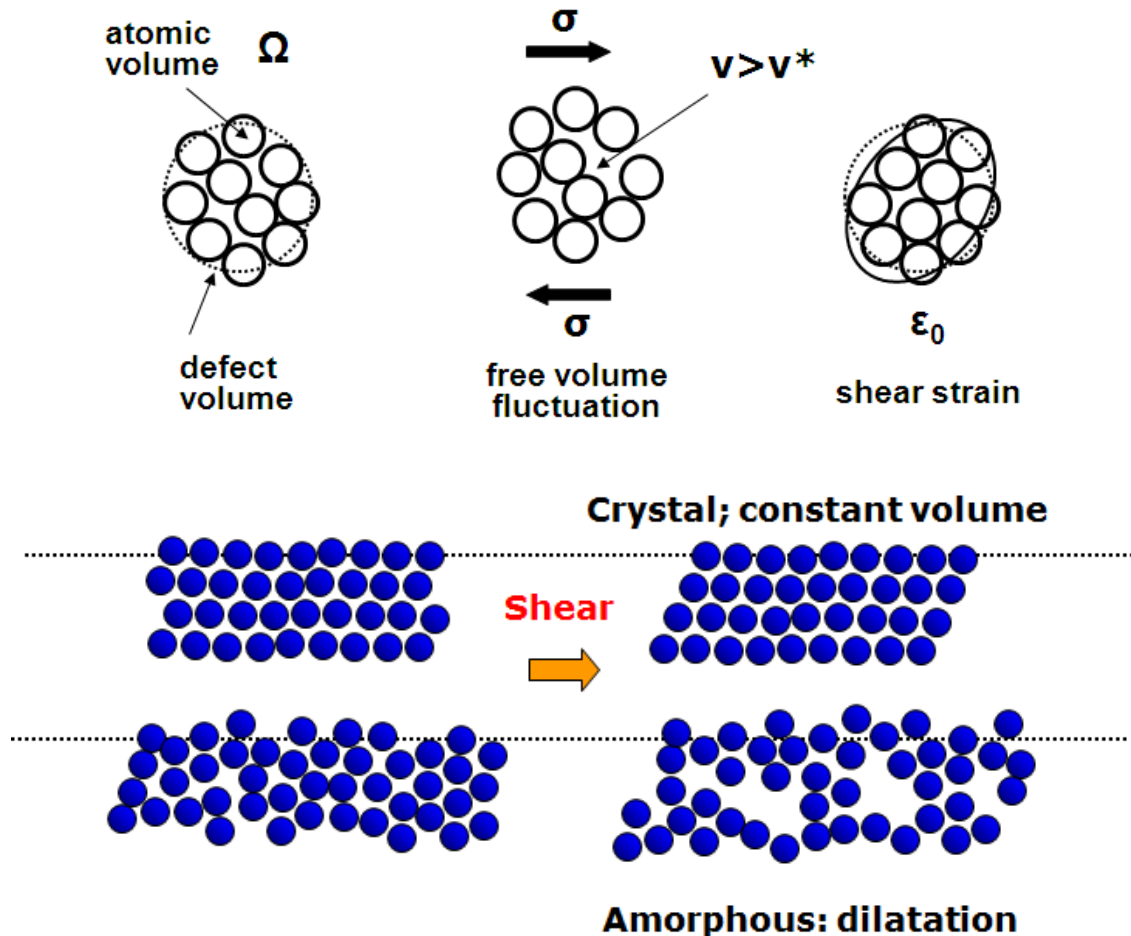
- Low temp. ( $<0.5T_g$ )/ high stress
- Localized shear band/  $45^\circ$  to the  
loading axis
- Strain softening: deformed at lower  
stress and higher rate



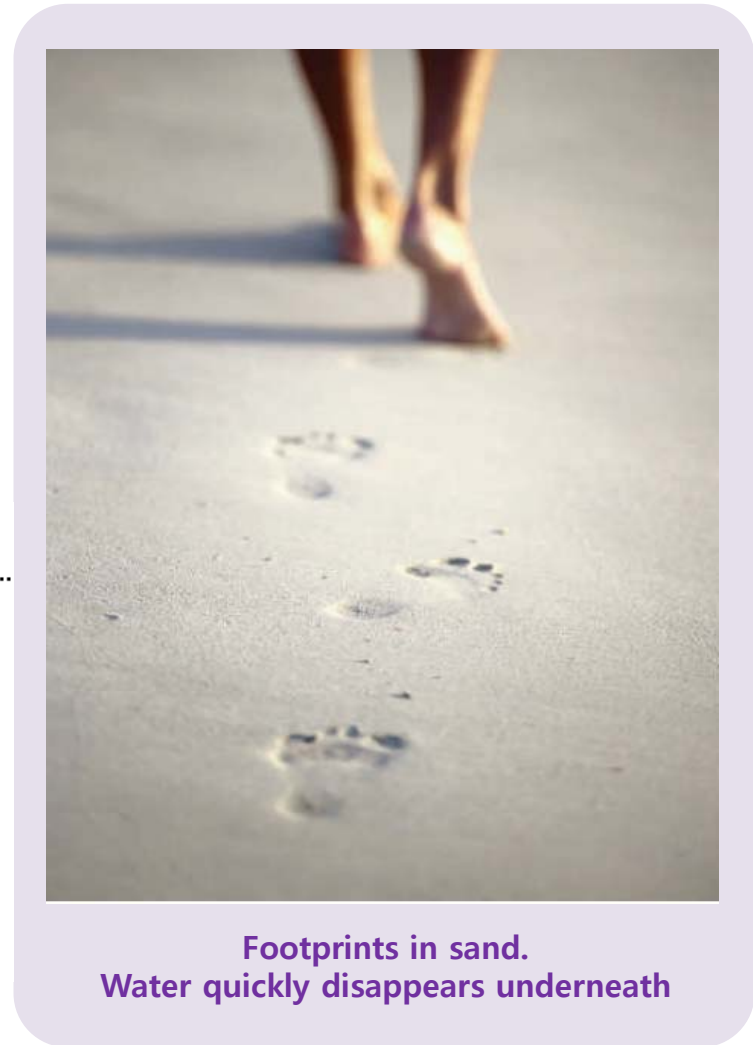
**Catastrophically Failure**

## 8.2.1 Inhomogeneous Deformation

# Elementary flow events in metallic glasses



➡ Shear bands form by accumulation of defects during deformation.

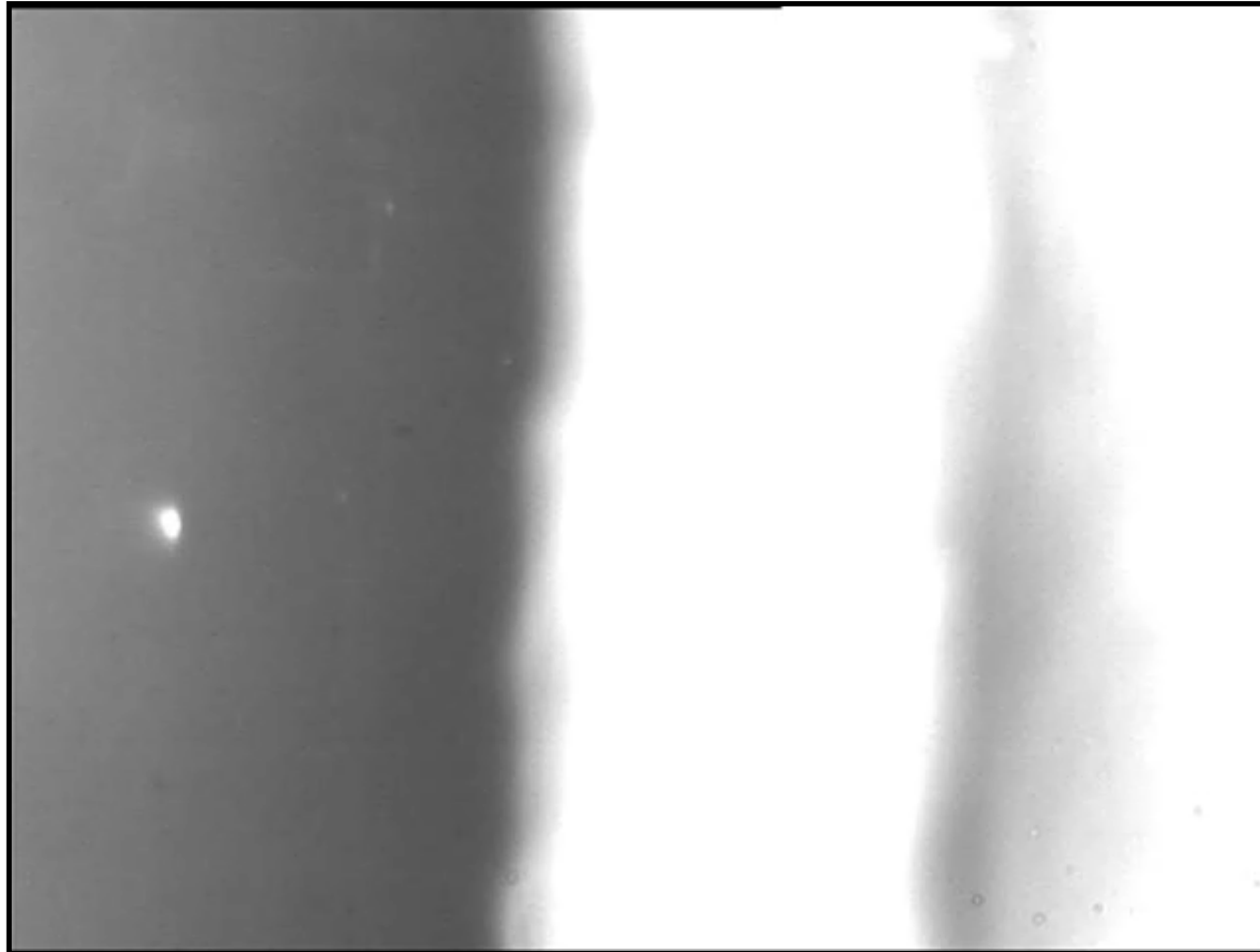


Footprints in sand.  
Water quickly disappears underneath

# Effect of local favored structure on SB nucleation

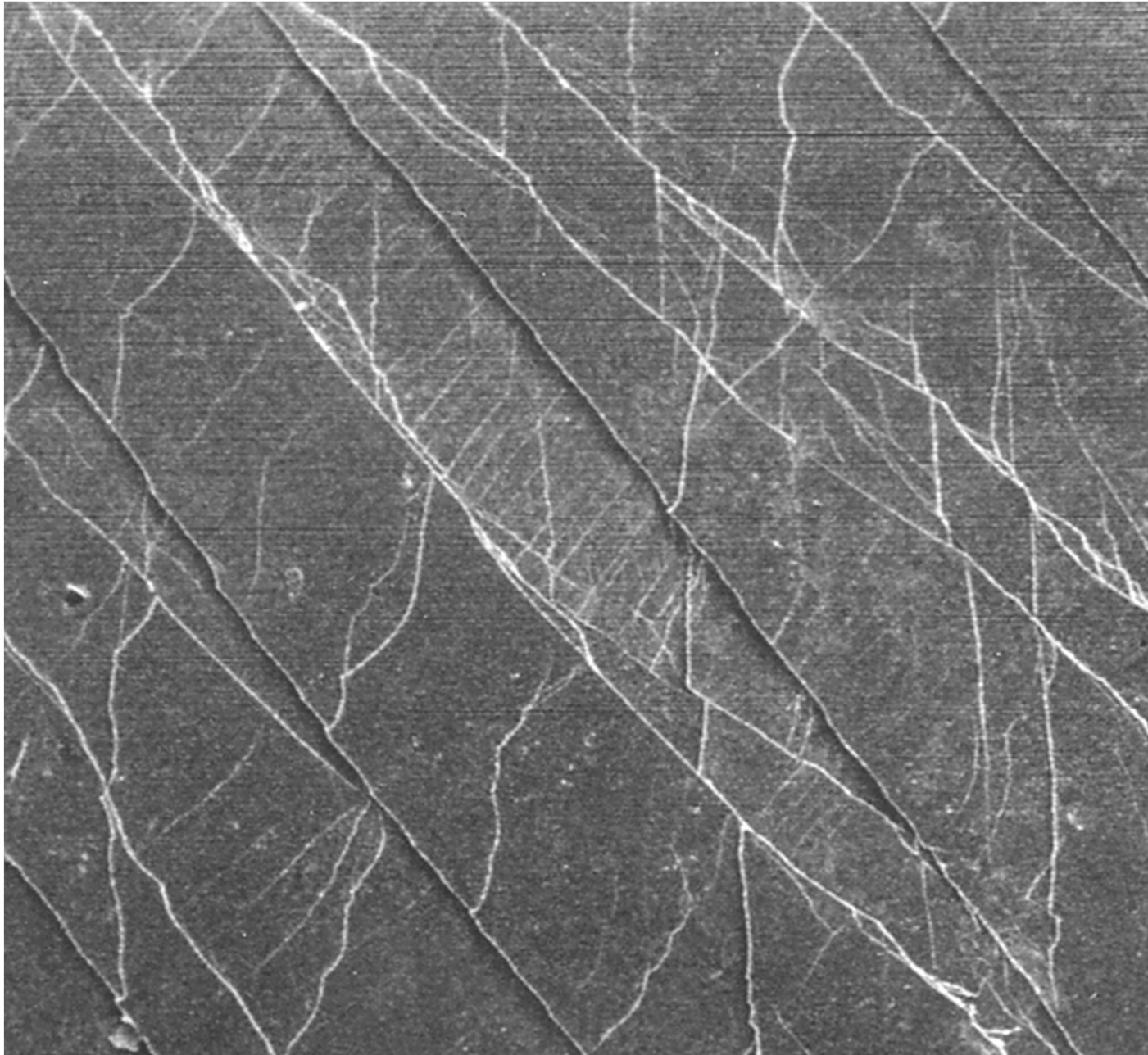
▶  $\text{Ni}_{60}\text{Nb}_{40}$ : fully amorphous phase

$S=0.016$  mm/sec

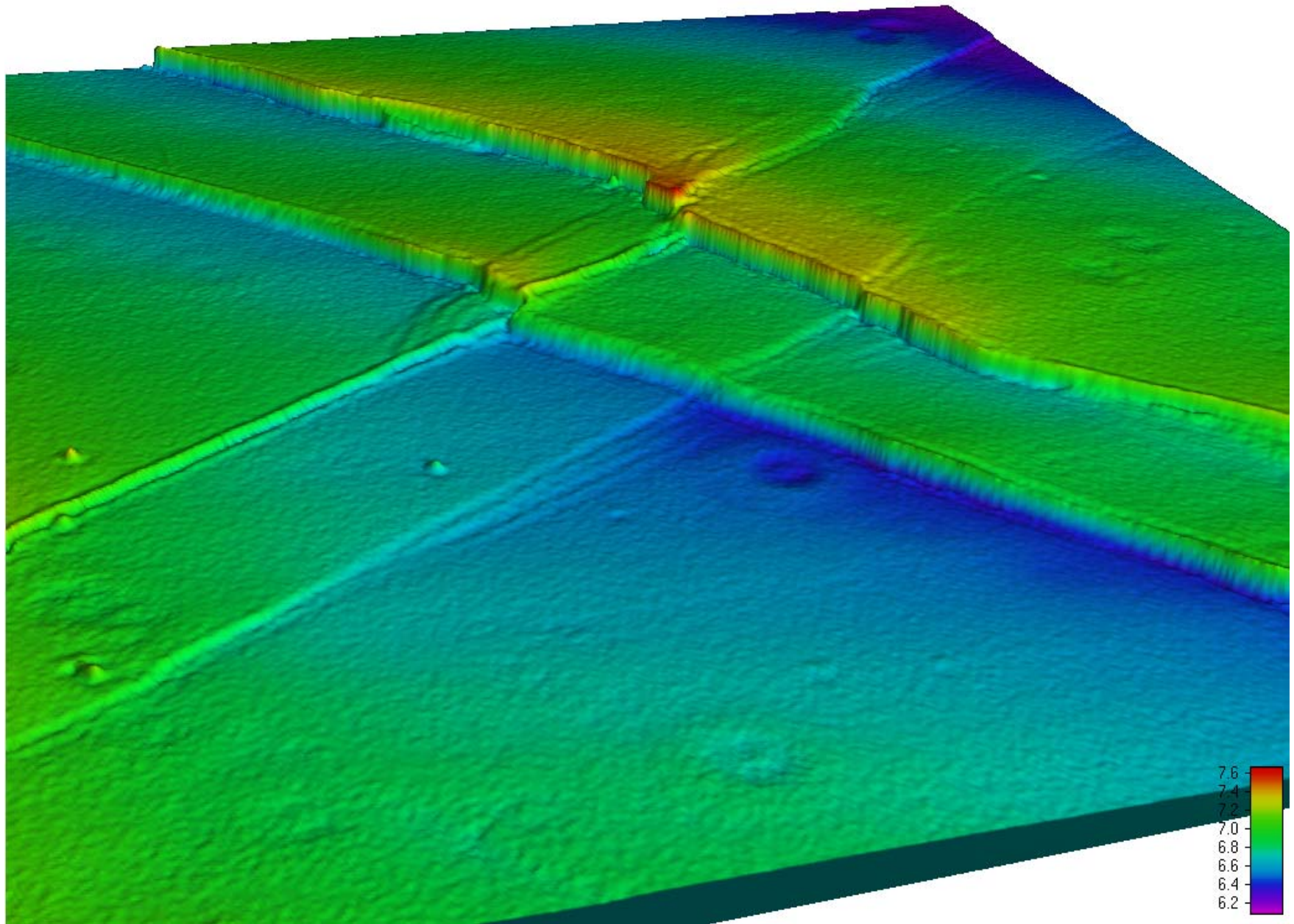


100  $\mu\text{m}$

# Formation of multiple shear bands during deformation

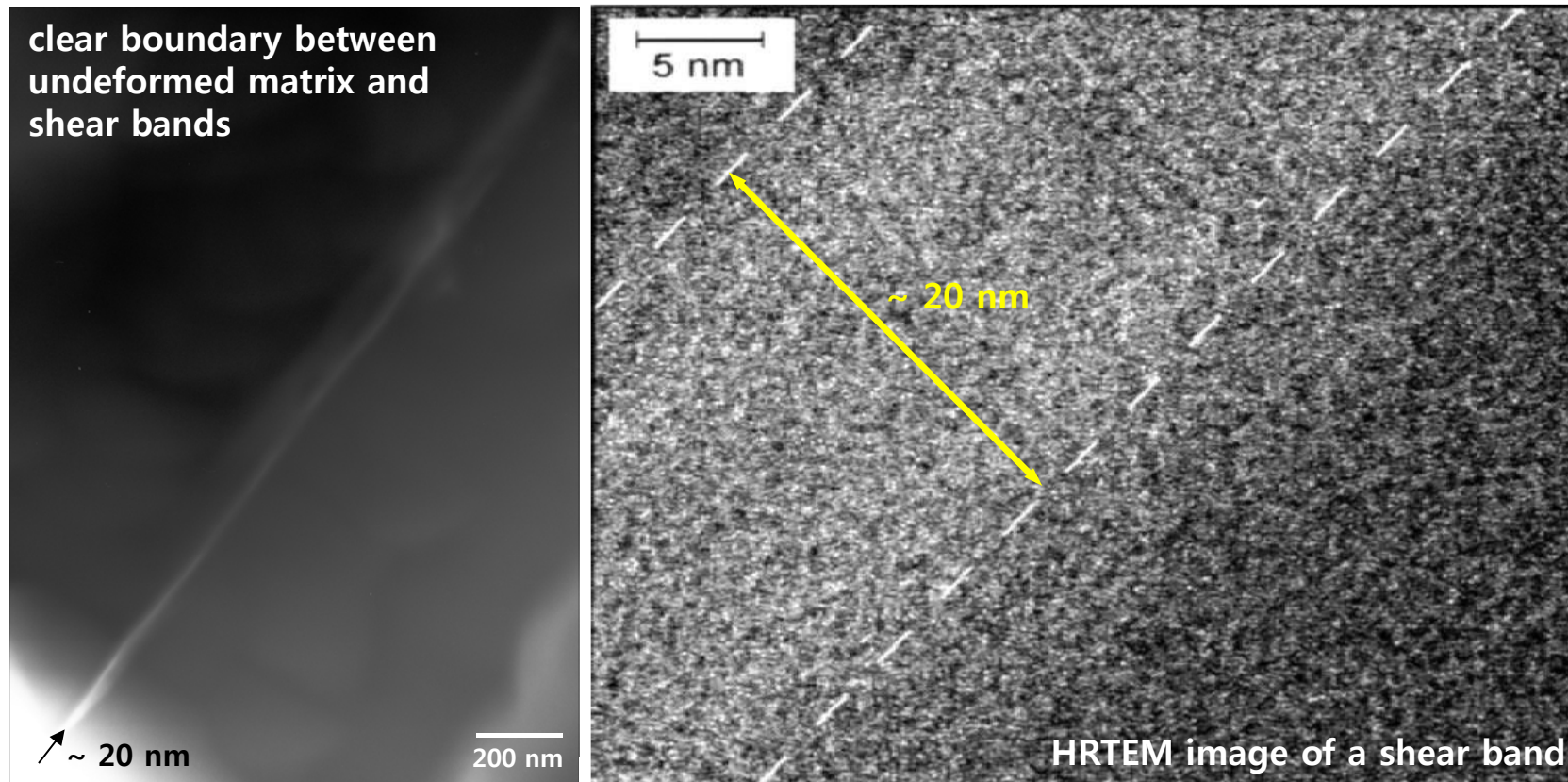






# Formation of shear bands : variation of free volume

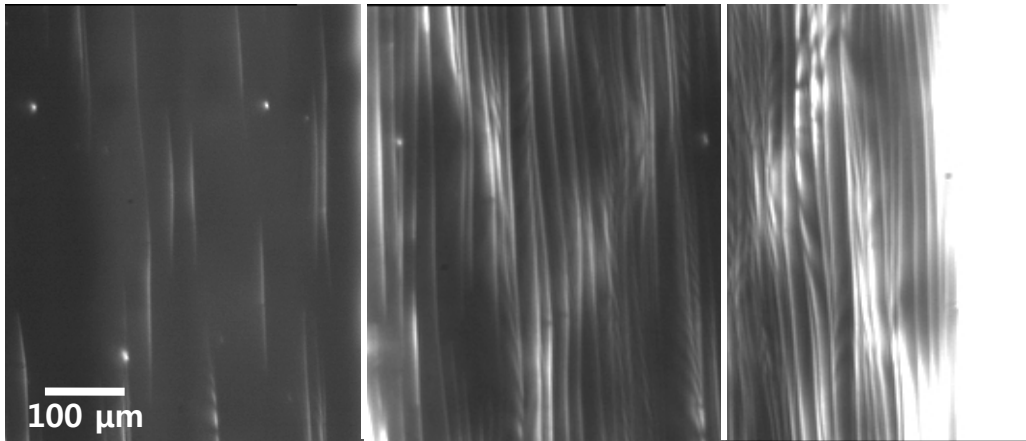
**Shear bands** form by **accumulation of defects** during deformation.



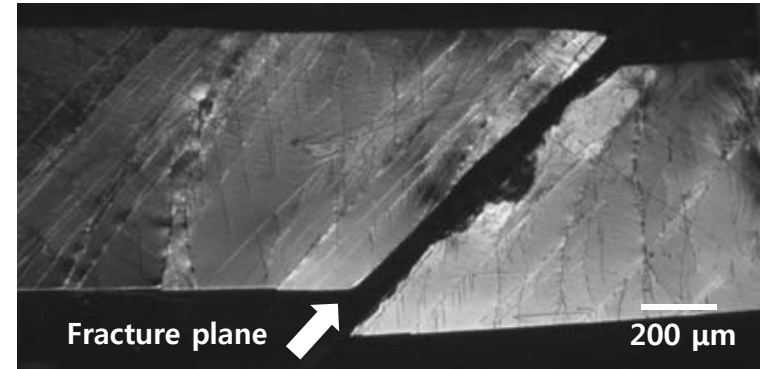
Shear deformed areas with the **same composition** & **different density of free volume**



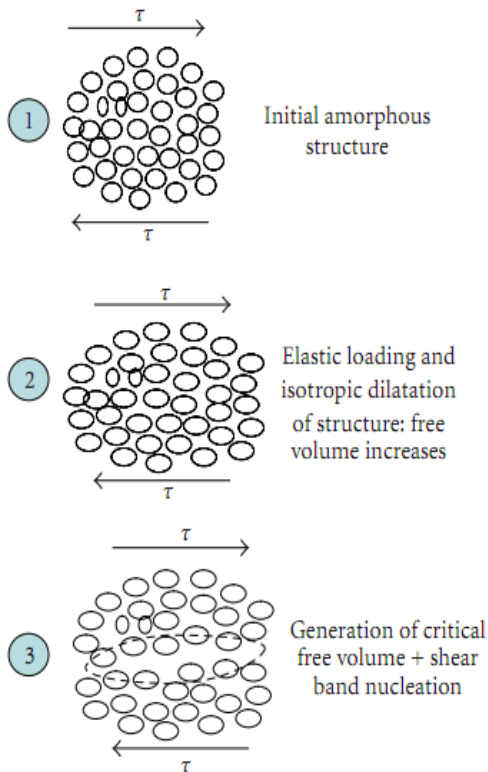
# Shear band nucleation and propagation: strain softening



Shear band formation and propagation in the ribbon bending test



Formation of multiple shear bands in an  $\text{Ni}_{50}\text{Pd}_{30}\text{P}_{20}$  BMG specimen subjected to compression testing. K. Wang et al. / *Acta Mater.* **56** (2008) 2834.



## Plastic deformation of metallic glass

controlled by shear band behavior **Nucleation & Propagation**

Excess volume → Connect to form a shear band

Plastic strain localized into these shear bands

**Catastrophic failure**

Elastic energy rises local temperature

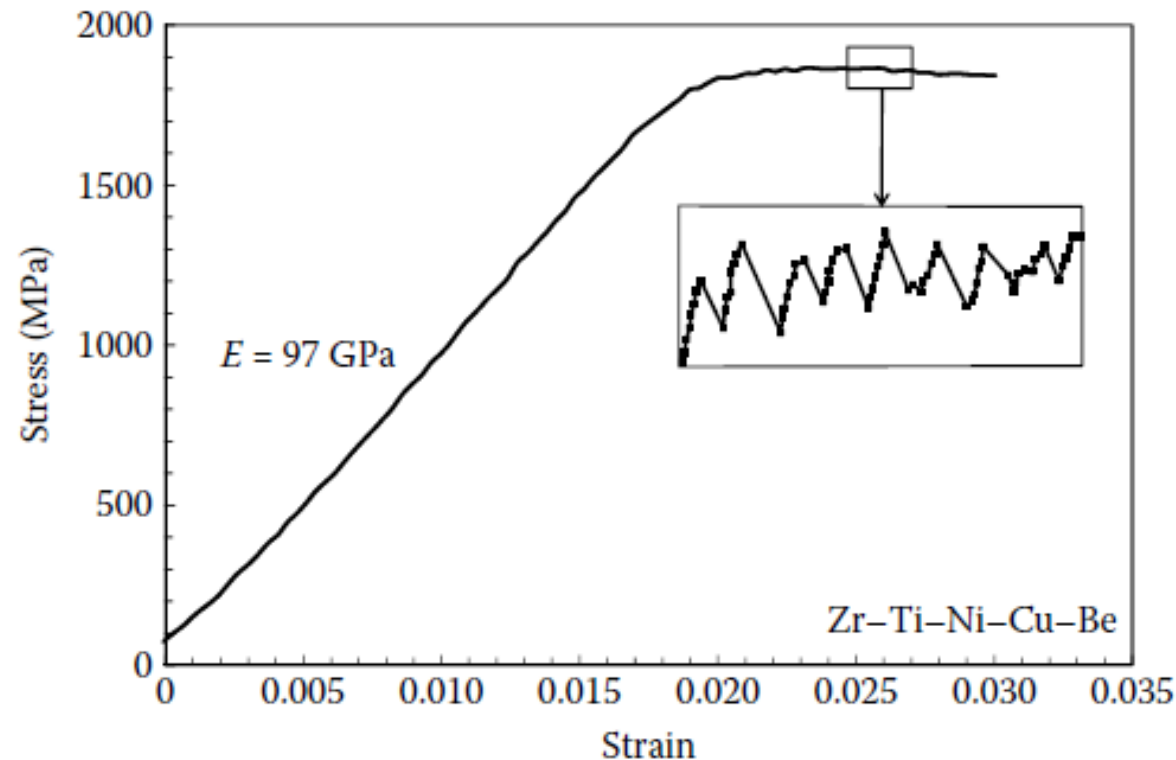
Decrease in the viscosity

Shear softening

Enhancement of ductility

Increase of the shear band density

**SB nucleation and propagation : Multiple serrations, observed only at slow strain rates → temperature rise**



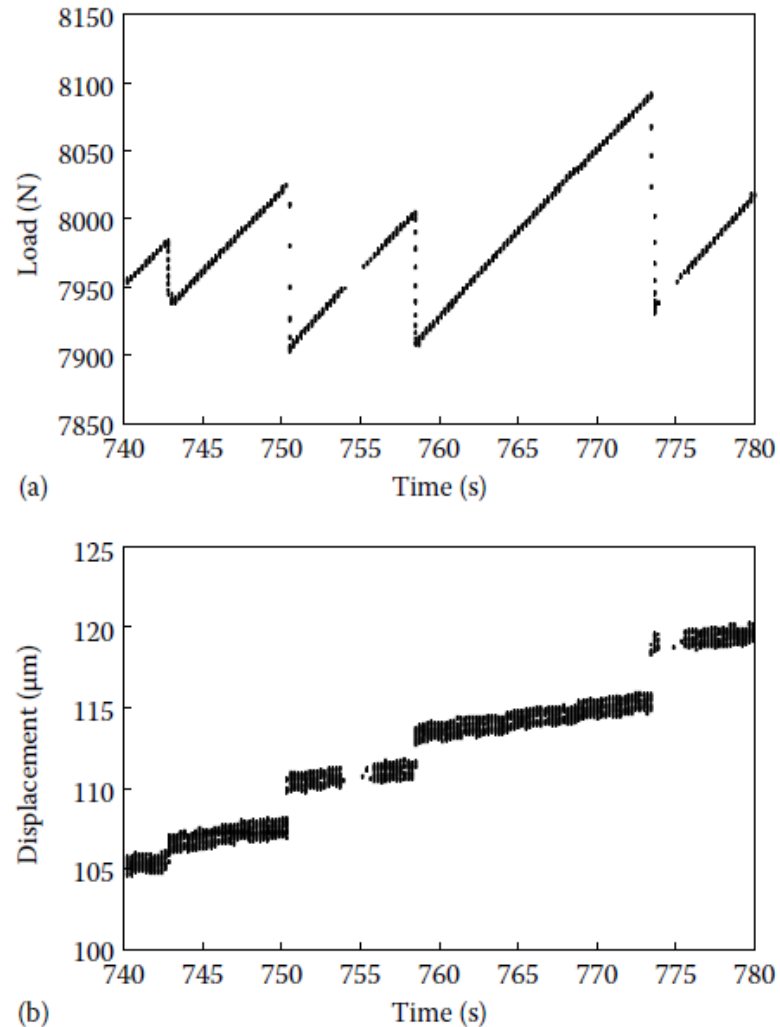
**FIGURE 8.1**

Compressive stress-strain curve for  $\text{Zr}_{40}\text{Ti}_{14}\text{Ni}_{10}\text{Cu}_{12}\text{Be}_{24}$  BMG alloy tested at a strain rate of  $1 \times 10^{-4} \text{ s}^{-1}$ . (Reprinted from Wright, W.J. et al., *Mater. Trans.*, 42, 642, 2001. With permission.)



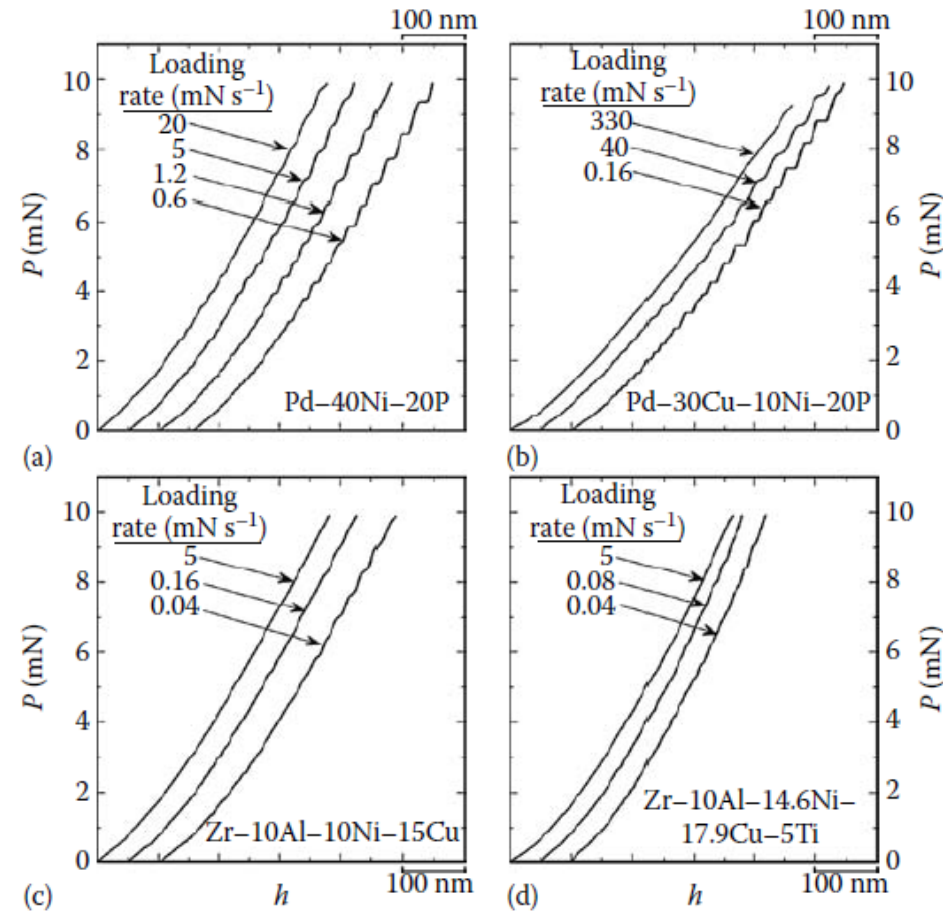
# SB nucleation and propagation : Multiple serrations

→ temperature rise



**FIGURE 8.2** (a) Load as a function of time and (b) total displacement as a function of time in the serrated flow region of the  $\text{Zr}_{40}\text{Ti}_{14}\text{Ni}_{10}\text{Cu}_{12}\text{Be}_{24}$  BMG alloy tested in uniaxial compression. (Reprinted from Wright, W.J. et al., *Mater. Trans.*, 42, 642, 2001. With permission.)

**Serrated flow is also observed during nanoindentation, but only at “slow loading rates”. Activation of each individual shear band is associated with the occurrence of a discrete “pop-in” event (sudden rise in load). High loading rate → multiple shear bands → smooth load-displacement curve**



**FIGURE 8.3**

Typical load–displacement ( $P$ – $h$ ) curves measured on the loading portion of nanoindentation experiments, for four different BMGs investigated. (a)  $\text{Pd}_{40}\text{Ni}_{40}\text{P}_{20}$ , (b)  $\text{Pd}_{40}\text{Cu}_{30}\text{Ni}_{10}\text{P}_{20}$ , (c)  $\text{Zr}_{65}\text{Al}_{10}\text{Ni}_{10}\text{Cu}_{15}$ , and (d)  $\text{Zr}_{52.5}\text{Al}_{10}\text{Ni}_{14.6}\text{Cu}_{17.9}\text{Ti}_5$ . Curves are offset from the origin for clear viewing, and the rate of indentation loading is specified in each graph. (Reprinted from Schuh, C.A. and Nieh, T.G., *Acta Mater.*, 51, 87, 2003. With permission.)

## 8.4 Temperature rise at shear bands

Most of the plastic strain is localized in narrow shear bands, which form approximately on the planes of maximum resolved shear stress. The inhomogeneous flow in metallic glasses appears to be related to a local decrease in the viscosity in shear bands. One of the reasons suggested for this was the local adiabatic heating that could lead to a substantial increase in the temperature.

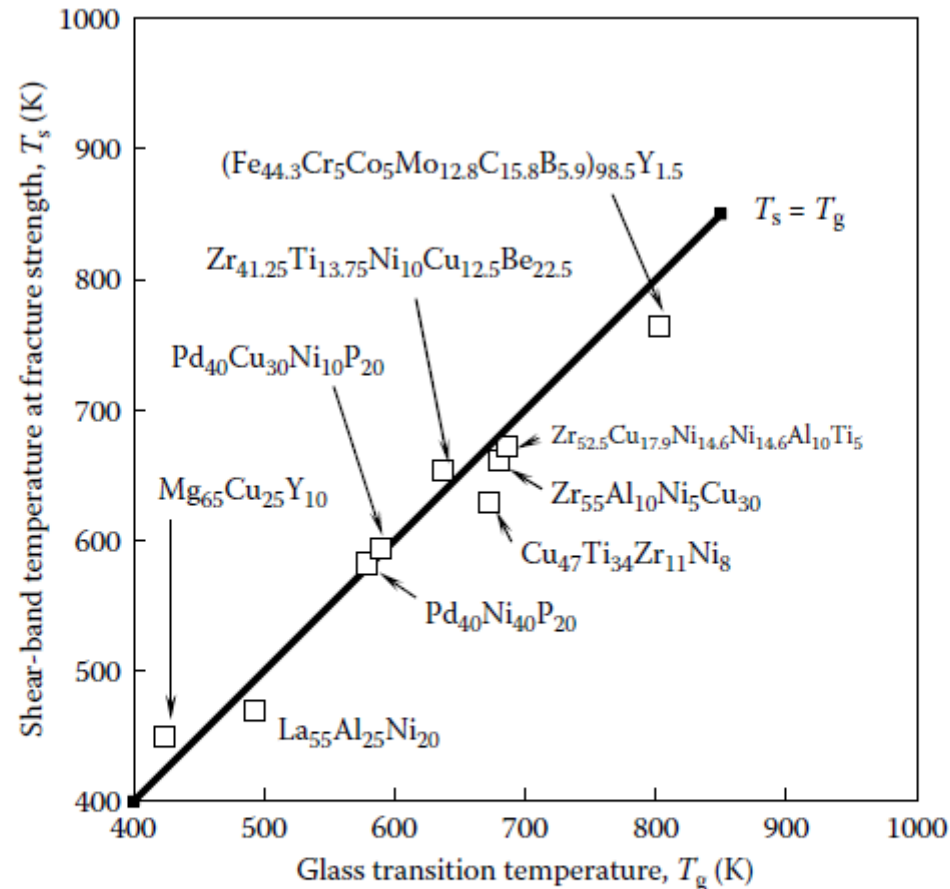
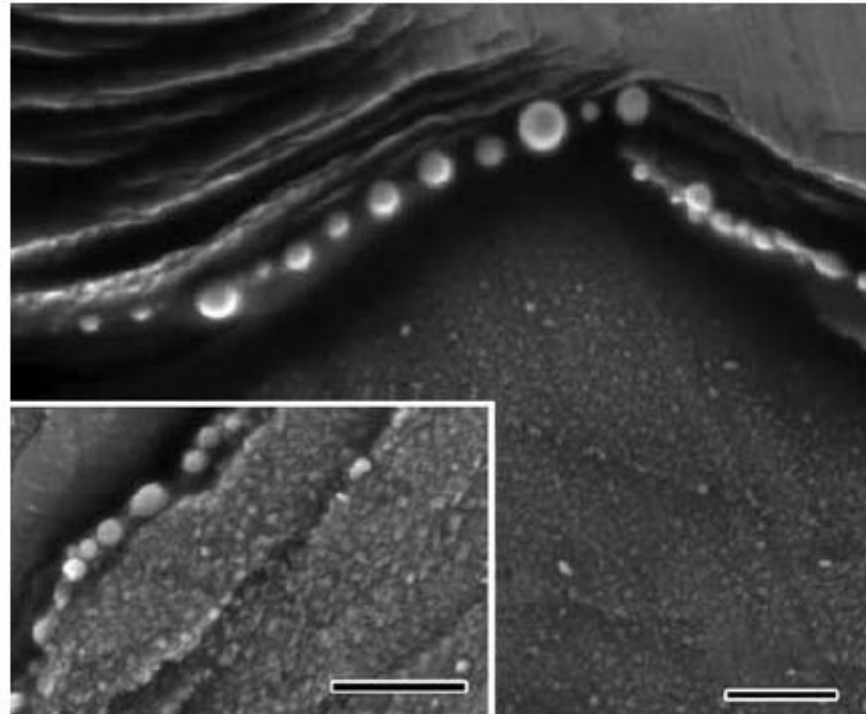


FIGURE 8.8

Temperature rise,  $\Delta T$  in the shear bands at the time of fracture for different BMG alloys plotted against the glass transition temperature,  $T_g$ . (Reprinted from Yang, B. et al., *J. Mater. Res.*, 21, 915, 2006. With permission.)

## 8.4 Temperature rise at shear bands

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**FIGURE 8.9**

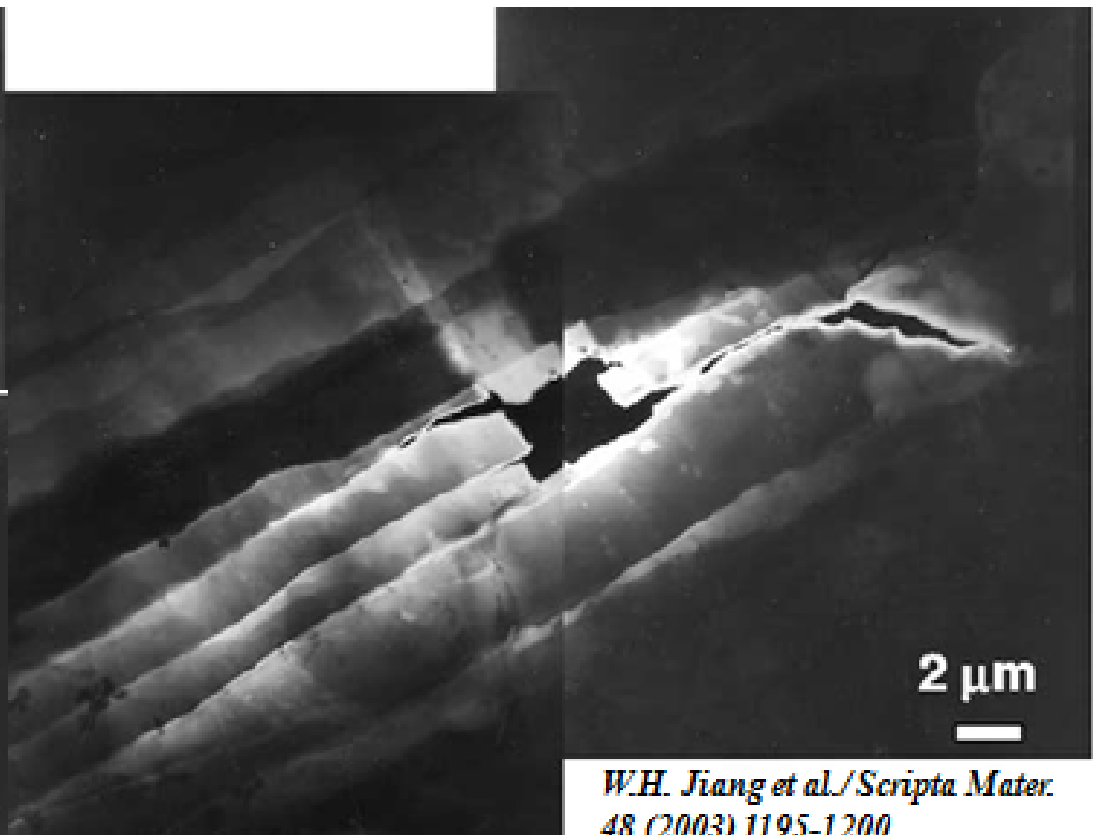
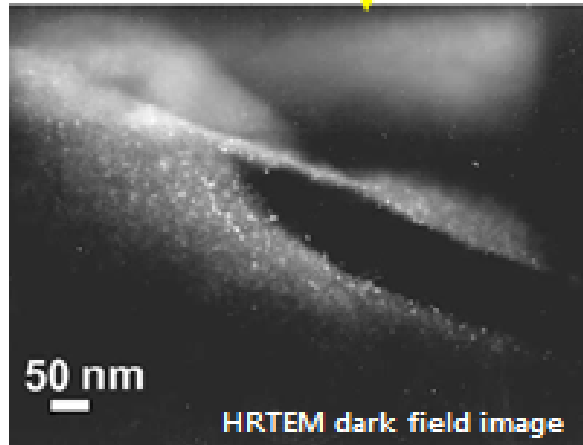
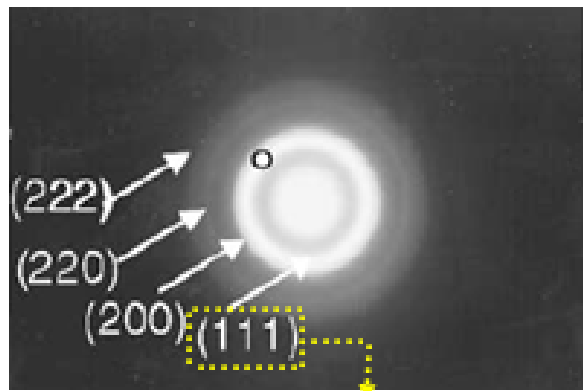
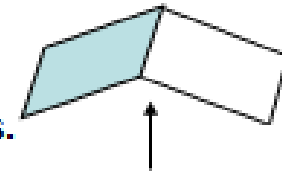
Scanning electron micrograph of the surface of  $Zr_{41.2}Ti_{13.8}Cu_{12.5}Ni_{10}Be_{22.5}$  BMG, which was originally coated with a tin coating. During deformation, the “fusible coating” had melted near the shear bands. The round shape of the tin beads clearly suggests that the coating had melted due to the temperature rise as a result of deformation and had resolidified. The bar in the micrographs corresponds to  $1\mu m$ . (Reprinted from Lewandowski, J.J. and Greer, A.L., *Nat. Mater.*, 5, 15, 2006. With permission.)

## 8.4.1 Nanocrystallization near Shear Bands

### TEM analysis after bend test in Al-based ribbon

\* **Compressive region of amorphous  $\text{Al}_{90}\text{Fe}_5\text{Gd}_5$  (at -40°C)**

: A high density of nanocrystals is observed within shear bands.



*W.H. Jiang et al./Scripta Mater.  
48 (2003) 1195-1200*

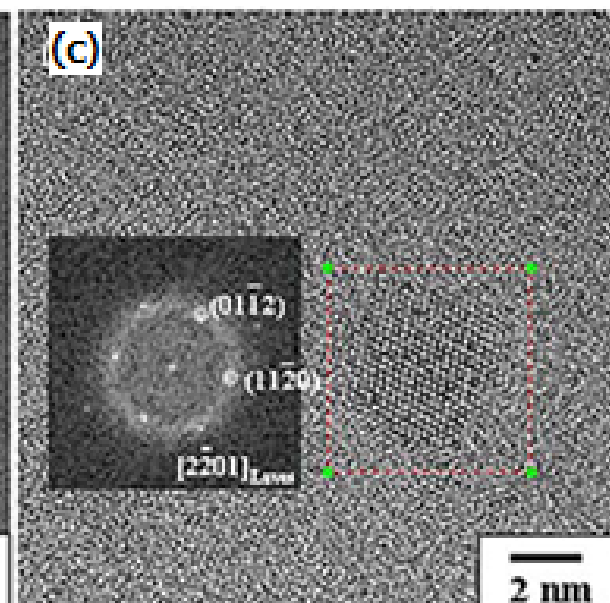
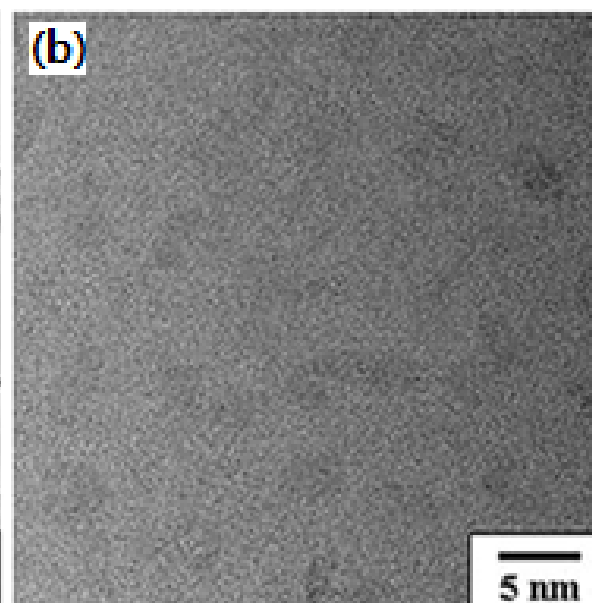
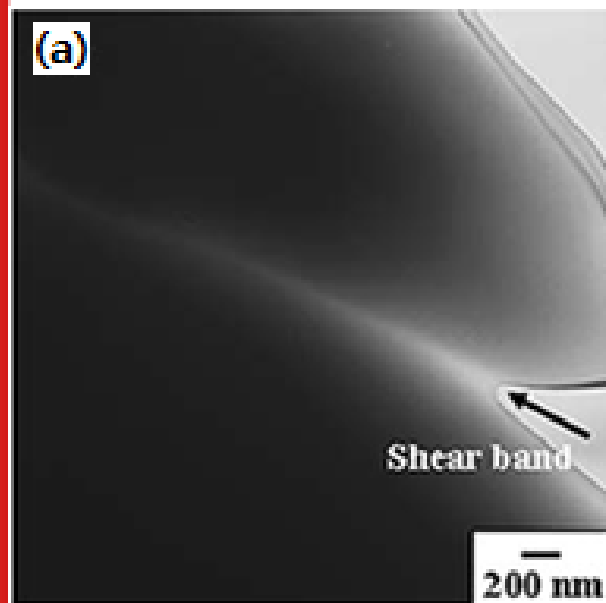
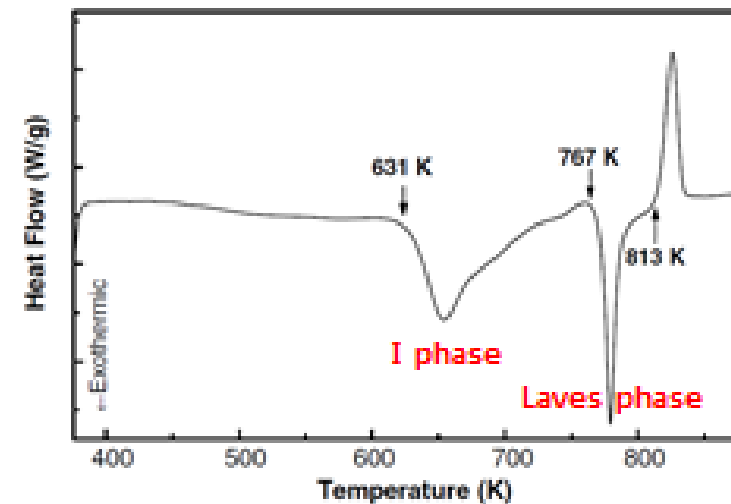
**Low GFA (unstable Amor. Matrix) → Severe plastic deformation → Precipitation of nanocrystals within shear bands**

# TEM analysis after severe compressive loading

\* Quasi-forming  $\text{Ti}_{40}\text{Zr}_{29}\text{Cu}_9\text{Ni}_8\text{Be}_{14}$  BMG exhibits large plastic strain.

: nanocrystals is observed within shear bands.

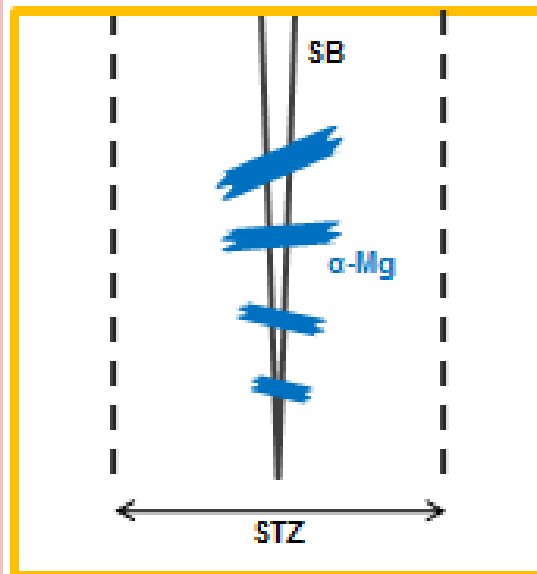
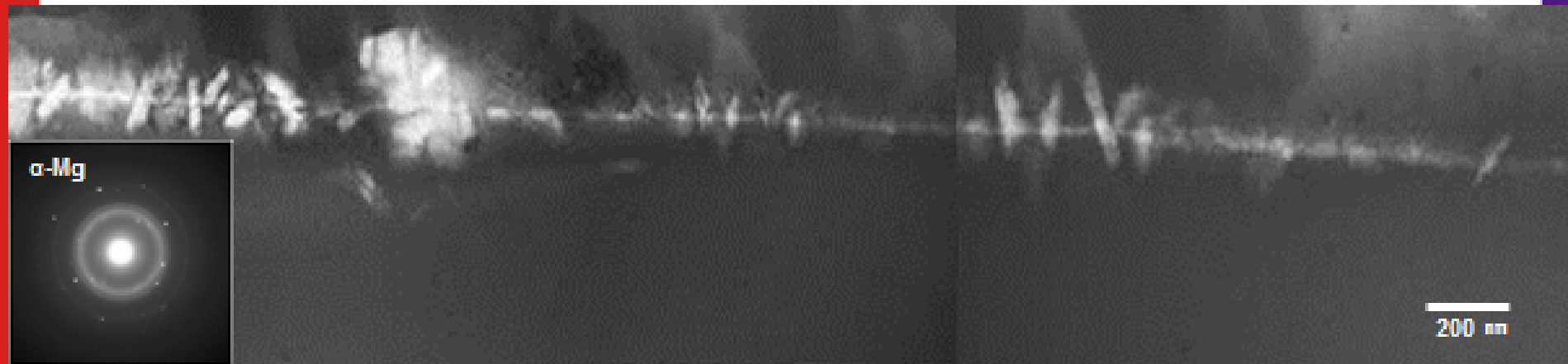
*H.J. Chang et al./ Scripta Mater. 55 (2006) 509-512*



Unstable Amor. Matrix → Severe plastic deformation → Precipitation of nanocrystals within shear bands

# TEM analysis after severe compressive loading

\* Mg-rich  $\text{Mg}_{80}\text{Cu}_{15}\text{Gd}_5$  BMGC ~ large plastic strain



Precipitation of several hundreds nm scale  $\alpha$ -Mg in SB & STZ region occurs during the severe compressive deformation, which is related to relatively low  $T_g$  (or  $T_x$ ) value as well as unstable amorphous matrix in Mg-rich BMGC.

*J.I. Lee will present the detail at July 8 (11: 45, room E7)*

Unstable Amor. Matrix  $\rightarrow$  Severe plastic deformation  $\rightarrow$  Precipitation of nanocrystals in SB and STZ region & relatively low  $T_g$  (or  $T_x$ )

# Atomistic models for plastic deformation in metallic glasses

## Free volume theory



## STZ model

F. Spaepen

A. S. Argon

### Free volume theory

### Shear transformation zone (STZ)

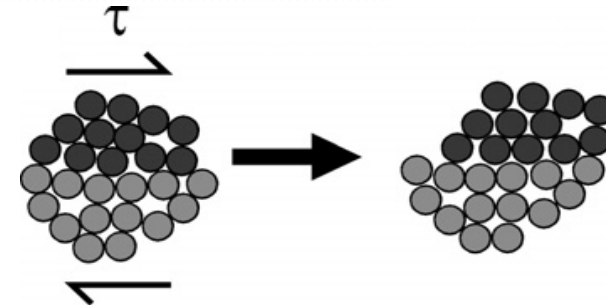
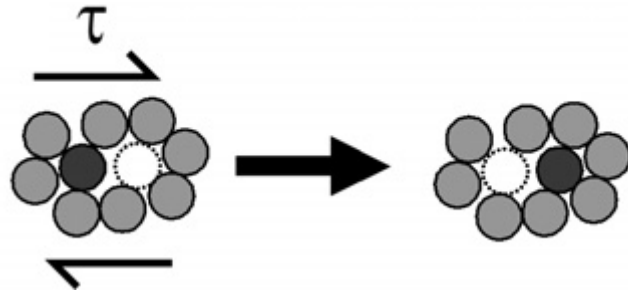
Homogeneous flow @ steady state

Homogeneous plastic flow

Steady / Non-steady

Inhomogeneous flow @ steady state

Inhomogeneous plastic flow



Single-atom/ Diffusion-like model/  
Internal volume creation

Spontaneous & cooperative reorganization of a  
small cluster of randomly close-packed atoms

**Steady state inhomogeneous flow :**  
**dynamic equilibrium between shear-induced**  
**disordering (creation of free volume) &**  
**diffusional annihilation of structural disorder**

STZ motion = local shear transformation  
STZ pushes apart the atoms around free volume  
site along activation path

Forward – backward process  
Thermally activated, similar energy scales  
Dilatational mechanism

**Plastic flow in metallic glass in which strain is**  
**produced by local shear transformations**  
**nucleated under the applied stress & the**  
**assistance of thermal fluctuations in regions**  
**around free volume sites (adiabatic heating)**



# Atomic bond topology

## Free volume theory



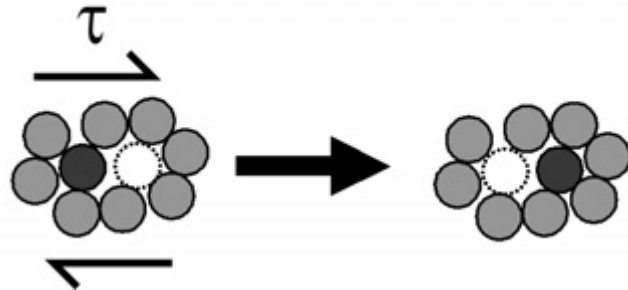
## STZ model

F. Spaepen

Free volume theory

Homogeneous flow @ steady state

Inhomogeneous flow @ steady state



T. Egami

Atomic bond topology

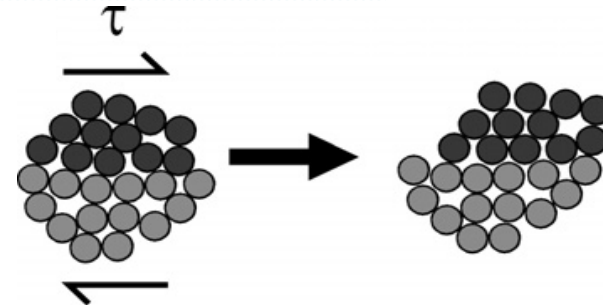
A. S. Argon

Shear transformation zone (STZ)

Homogeneous plastic flow

Steady / Non-steady

Inhomogeneous plastic flow



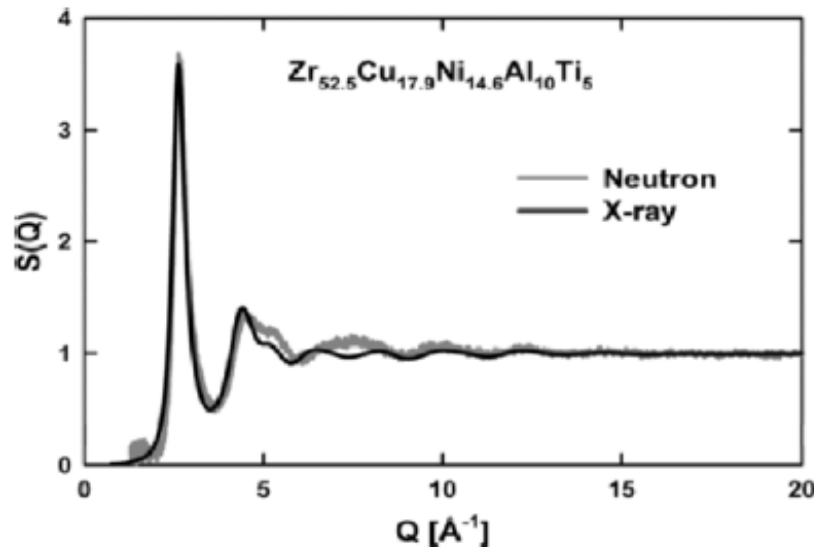
STZ: basic shear unit

(a few to perhaps up to 100 atoms)

- Free volume approach
  - (1) dense random packing of hard spheres
  - (2) free volume cannot be described by the volume alone, and we have to consider the shape
- Network of atomic connectivity / topology of the atomic structure

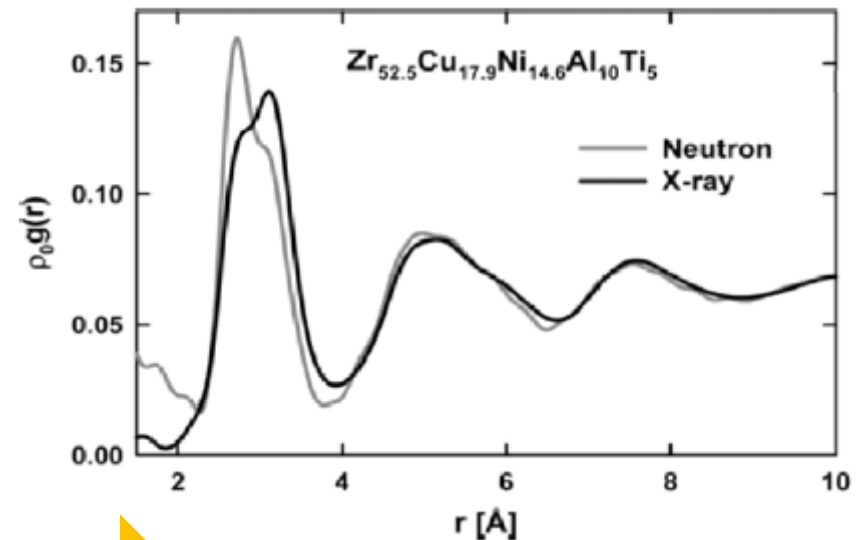
# Atomistic theory of metallic liquids and glasses – T. Egami

- Structure of liquids and glasses is usually described in terms of the atomic pair-density correlation function (PDF;  $\rho_0 g(r)$ ) or the radial distribution function (RDF;  $4\pi r^2 \rho_0 g(r)$ )
- PDF : distribution of the distances between pairs of atoms, averaged over the volume and angle.



Structure function  $S(Q)$  of BMG  $Zr_{52.5}Cu_{17.9}Ni_{14.6}Al_{10}Ti_5$

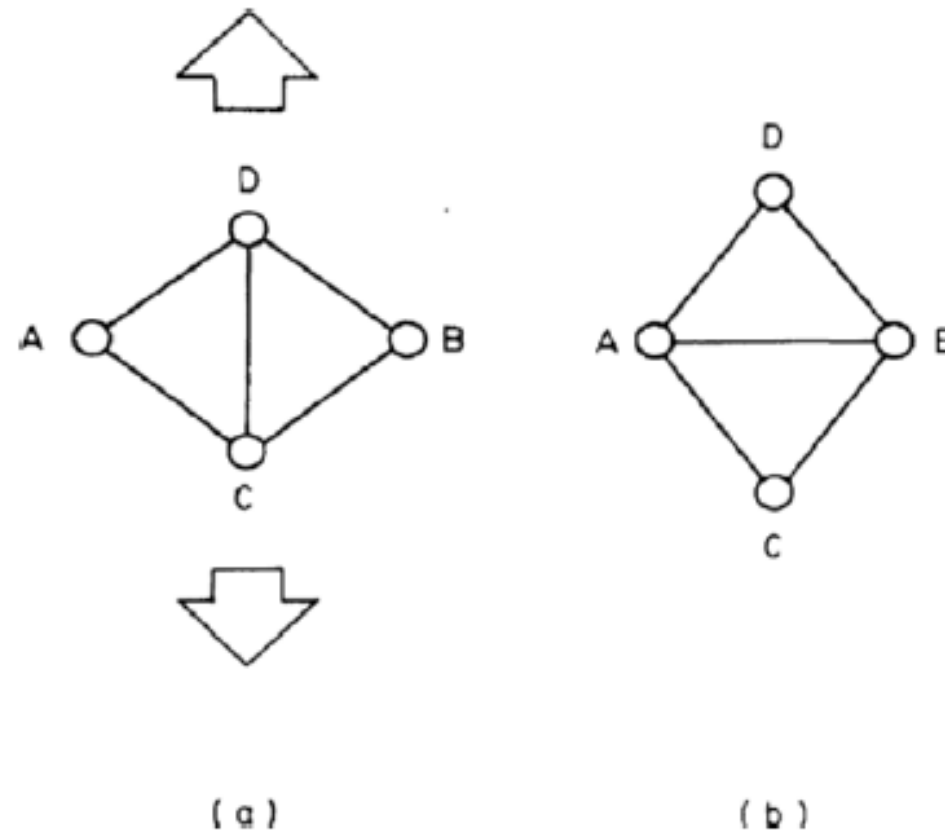
fourier  
transformation



PDF of BMG  $Zr_{52.5}Cu_{17.9}Ni_{14.6}Al_{10}Ti_5$

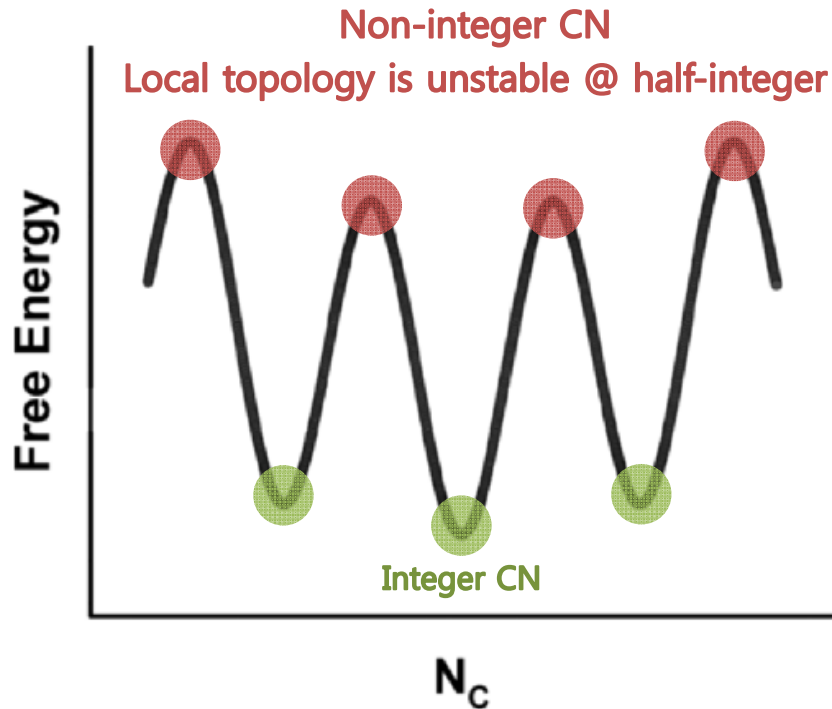
- The idea most frequently used in discussing atomic transport and deformation is free volume.
- Free volume is a space between atoms, and it is intuitively reasonable to assume that atoms need some space for moving around.

# Bond-exchange mechanism of shear deformation



**Fig. 2.17.** The bond-exchange mechanism of shear deformation.<sup>44</sup> When a vertical tensile stress is applied the bond C–D is cut, and the new bond A–B is formed. The total number of bonds remains unchanged, but the distribution of orientation becomes anisotropic. Bond orientational anisotropy (BOA) is formed as a result of such a bond-exchange process (reprinted from reference [44] with permission from the American Physical Society)

# T. Egami: Local topological instability



The energy landscape of an atom as a function of  $x=r_A/r_B$

**Total volume expands more than 6 %: unstable structure**

**Local volume strain is larger than 11 %: the site is topologically unstable; local CN may change**

**This leads to the definition of the free-volume in terms of the critical local volume strain.**

$$\Delta x = \frac{1/2}{\partial N_C(x) / \partial x},$$

$$\frac{\partial N_C(x)}{\partial x} = 8\pi \left(1 - \frac{\sqrt{3}}{2}\right) \left[1 + x + \sqrt{x(x+2)} + \frac{1}{2\sqrt{x(x+2)}}\right]$$

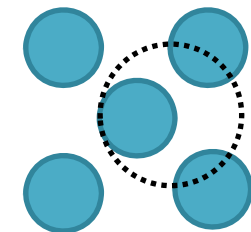
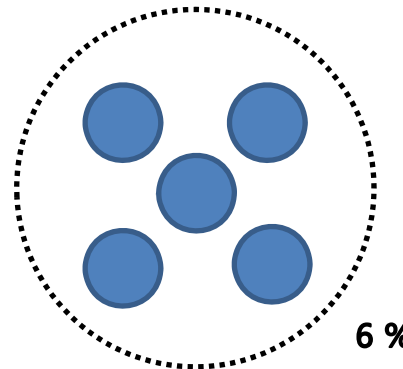
$\Delta x$  caused by : local volume strain / uniform expansion

Homogeneous volume strain  $\langle \varepsilon_v \rangle = (3/2)\Delta x/x,$

$$x=1, \quad \varepsilon_v^{\text{crit}}(H) = \frac{3}{2} \Delta x \Big|_{x=1} = \frac{6\sqrt{3}-9}{8\pi} = 0.0554.$$

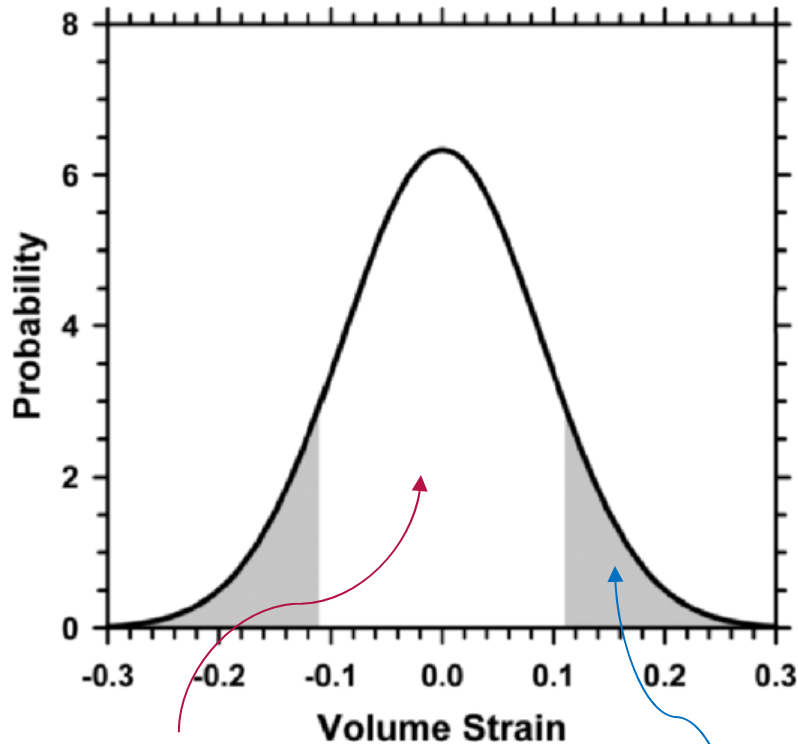
Local volume strain  $\varepsilon_v = 3\Delta x/x,$

$$x=1, \quad \varepsilon_v^{\text{crit}}(L) = 3 \Delta x \Big|_{x=1} = \frac{6\sqrt{3}-9}{4\pi} = 0.111.$$



11 %

# T. Egami: Local topological fluctuation



Free volume site (n-type defect)

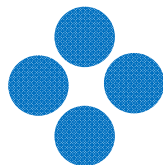
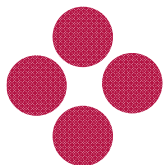
Negative (**dilatational**) volume strain > 11 %

$$\epsilon_v < -\epsilon_v^{\text{crit}}(L)$$

Antifree volume site / p-type defect

Positive (**compressive**) volume strain > 11 %

$$\epsilon_v^{\text{crit}}(L) < \epsilon_v$$



- Defect sites are *liquid-like* / topologically unstable  
*Solid-like* / topologically stable sites ( $\epsilon_v < 11\%$ )

여기에서 제안된 critical local volume strain은 free-volume theory에서 정의된  $v^*$ 와 같은 order of magnitude를 가진다. 즉, free-volume은 원자 크기만큼의 부피가 아니라, 11% 정도의 local dilatation이 원자 topology를 불안정하게 하여 CN을 1 정도 바꿈

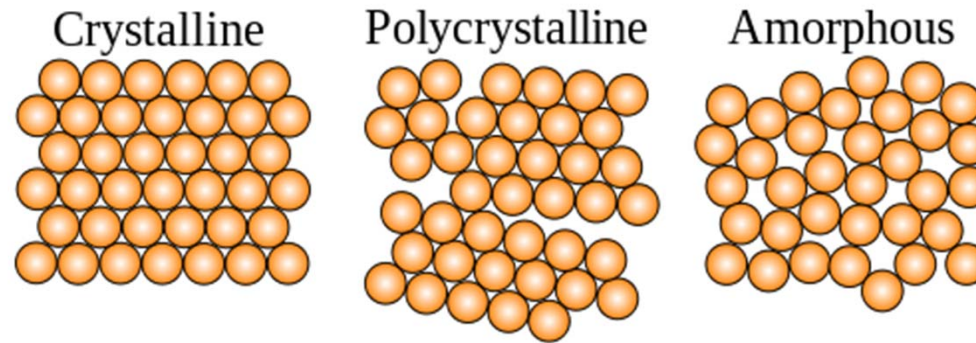
- Deformation of metallic glasses

본 조건에서 정의된 defect는 negative와 positive 양 방향의 strain이 가능하기 때문에, 기존의 hard sphere model에서처럼 소성변형에 반드시 free volume이 필요한 것은 아니다. Free volume은 주로 소성변형의 결과로 생겨나는 것이지 꼭 pre-existing할 필요는 없다.

Microscopic bases for the mode-coupling theory

$$m = \left. \frac{\partial \log \eta(T)}{\partial (T_g / T)} \right|_{T=T_g} = \frac{13}{1 - (T_g / T_s)} = 13K_\alpha = \frac{39(1-\nu)}{2(1-2\nu)}$$

# Atomic processes and deformation mechanisms



- Plastic flow is a *kinetic process*.
- At absolute zero, **polycrystalline solid** as having a well defined **yield strength**, below which it does not flow and above which flow is rapid.
- Variables that solid strength depends on : **strain, strain-rate, and temperature**. (atomistic processes : glide-motion of dislocation lines, their coupled glide and climb, the diffusive flow of individual atoms, the relative displacement of grains by grain boundary sliding, mechanical twinning etc.)
- **Deformation mechanisms** were considered to describe polycrystal plasticity (or flow); they divided into five groups.

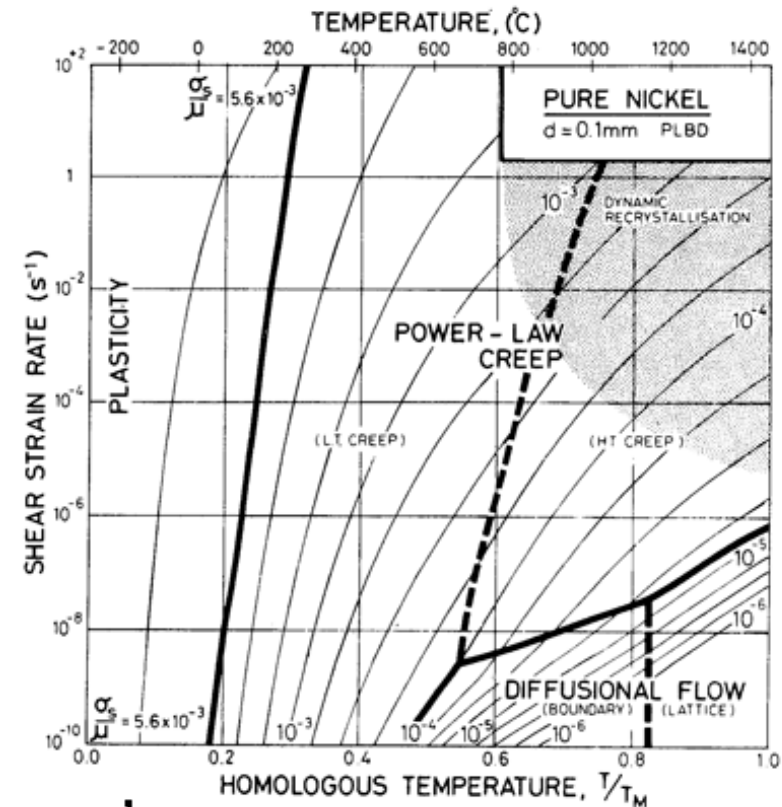
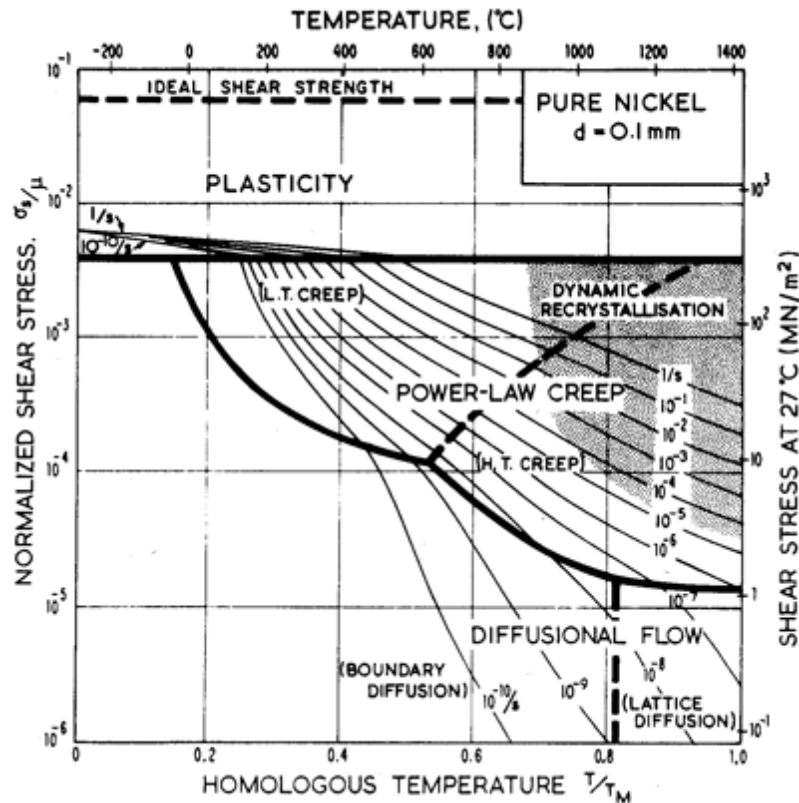
1. Collapse at the ideal strength
2. Low-temperature plasticity by dislocation glide
3. Low-temperature plasticity by twinning
4. Power-law creep by dislocation glide, or glide-plus-climb
5. Diffusional flow

- 위의 메커니즘들은 복잡하게 superimpose될 수 있다. (superplastic flow 등)



# Ashby deformation maps for crystalline materials

*Delineating the different modes and mechanism of plastic deformation of a material as a function of stress, temperature, and structure*



- Rate equations  $\dot{\gamma} = \left( \frac{2}{3} ((\dot{\epsilon}_1 - \dot{\epsilon}_2)^2 + (\dot{\epsilon}_2 - \dot{\epsilon}_3)^2 + (\dot{\epsilon}_3 - \dot{\epsilon}_1)^2) \right)^{\frac{1}{2}} \rightarrow \dot{\gamma} = f(\tau, T, \text{structure})$   
steady-state constitutive flow law
- 각 소성 메커니즘들이 어떻게 결합되어 나타나는지를 요약하여 보여주는 것이 바로 deformation-mechanism map이다.
- normalized stress  $\sigma_s/\mu$   
homologous temperature,  $T/T_M$  (where  $\mu$  is the shear modulus and  $T_M$  the melting temperature)  
shear strain  $\gamma'$

# Empirical deformation mechanism maps for metallic glasses

*Developed by Spaepen using the results for melt-spun metallic glasses,  
Explained by using the concept of free volume model*

## Flow Mechanisms

### ❖ Basic Modes of Deformation

- Homogeneous Flow
  - Each volume element undergoes the same strain.
- Inhomogeneous Flow
  - Strain is concentrated in a few thin shear bands.

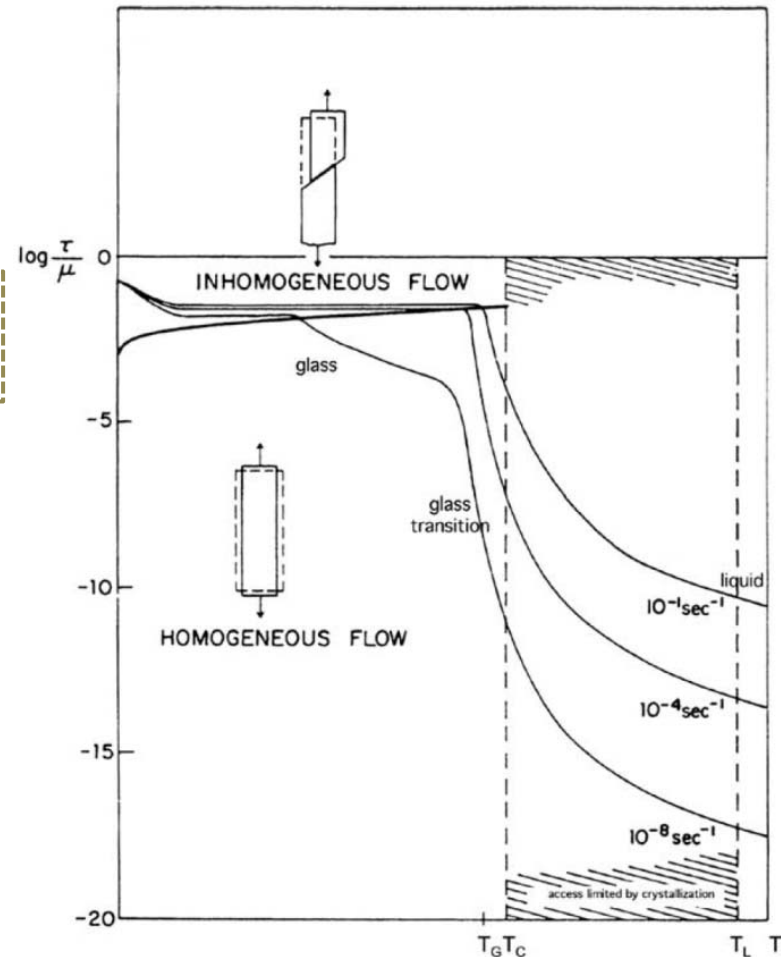
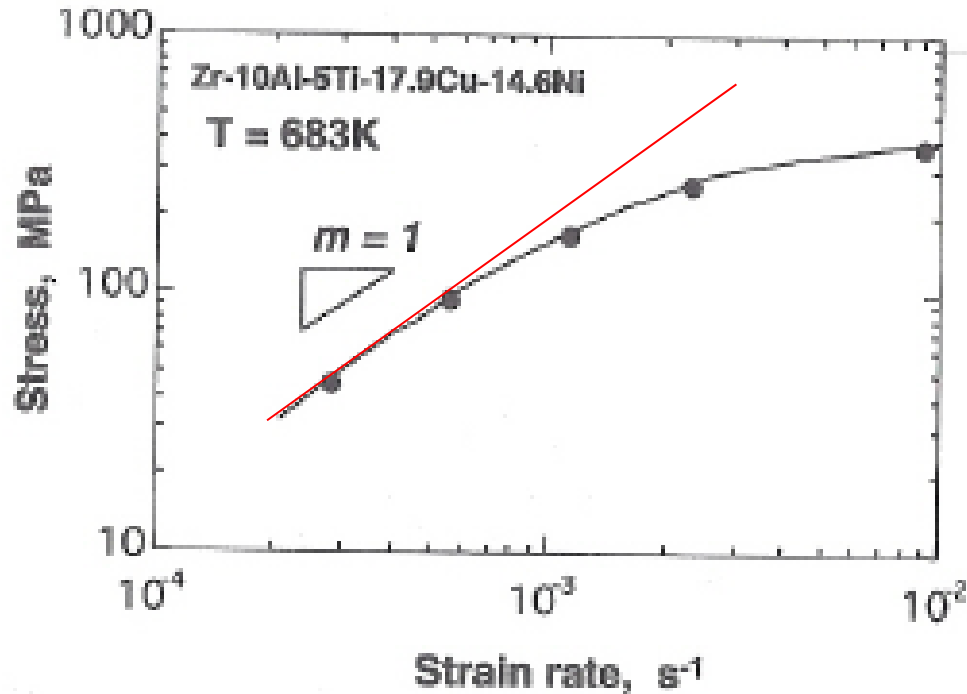


Fig. 1. Deformation mechanism map for a metallic glass.



# Homogeneous Deformation



- Under low strain rate  
→ Homogeneous deformation  
(= Newtonian fluid)

- Under high strain rate  
→ Inhomogeneous deformation  
(= non-Newtonian fluid)

- Newtonian to non-Newtonian transition is dependent on the test temperature.

# Liquid Flow

## ❖ Liquid Region (above and near $T_g$ )

- Homogeneous Flow
- Low stress in liquid region
- Strain rate is proportional to the stress
- Viscosity is not dependent on stress, but temperature.

$$\sinh\left[\frac{\varepsilon_0 v_0 \sigma}{2kT}\right] \approx \frac{\varepsilon_0 v_0 \sigma}{2kT} \text{ @ low stress}$$

- Newtonian Viscous Flow

$$\tau = \eta \cdot \dot{\gamma}$$

Shear stress      Viscosity      Strain rate

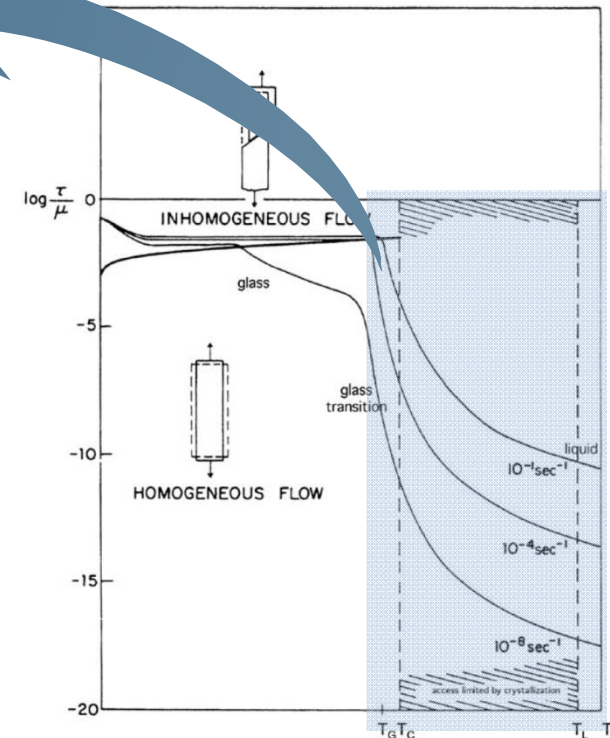


Fig. 1. Deformation mechanism map for a metallic glass.

# Deformation-induced Softening

- Softening : Lowering of viscosity in the shear bands
- Structural Change : Creation of free volume due to high stress level

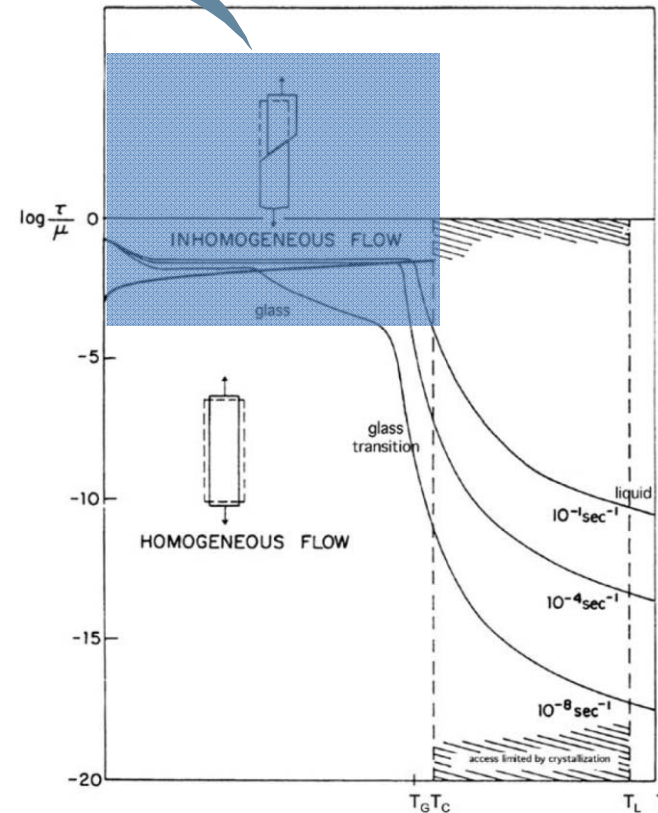
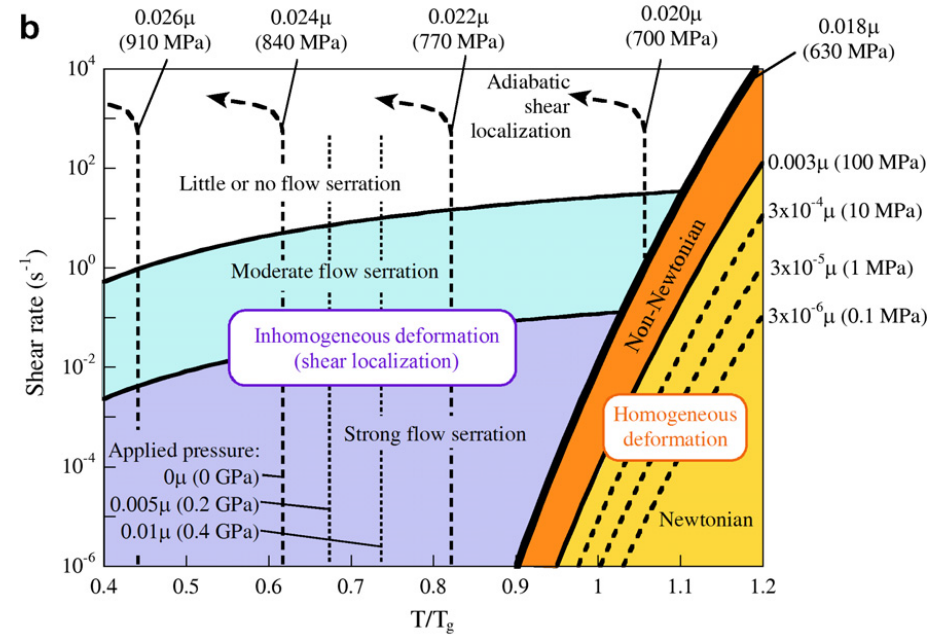
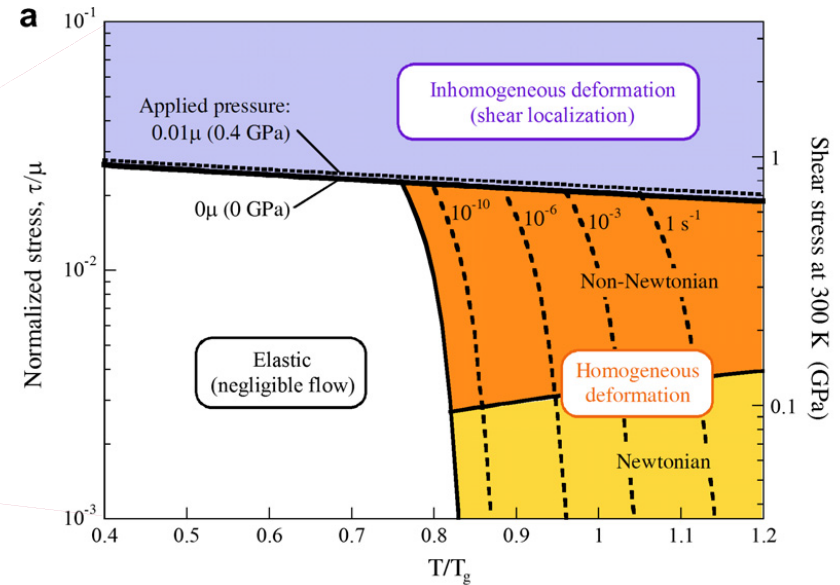
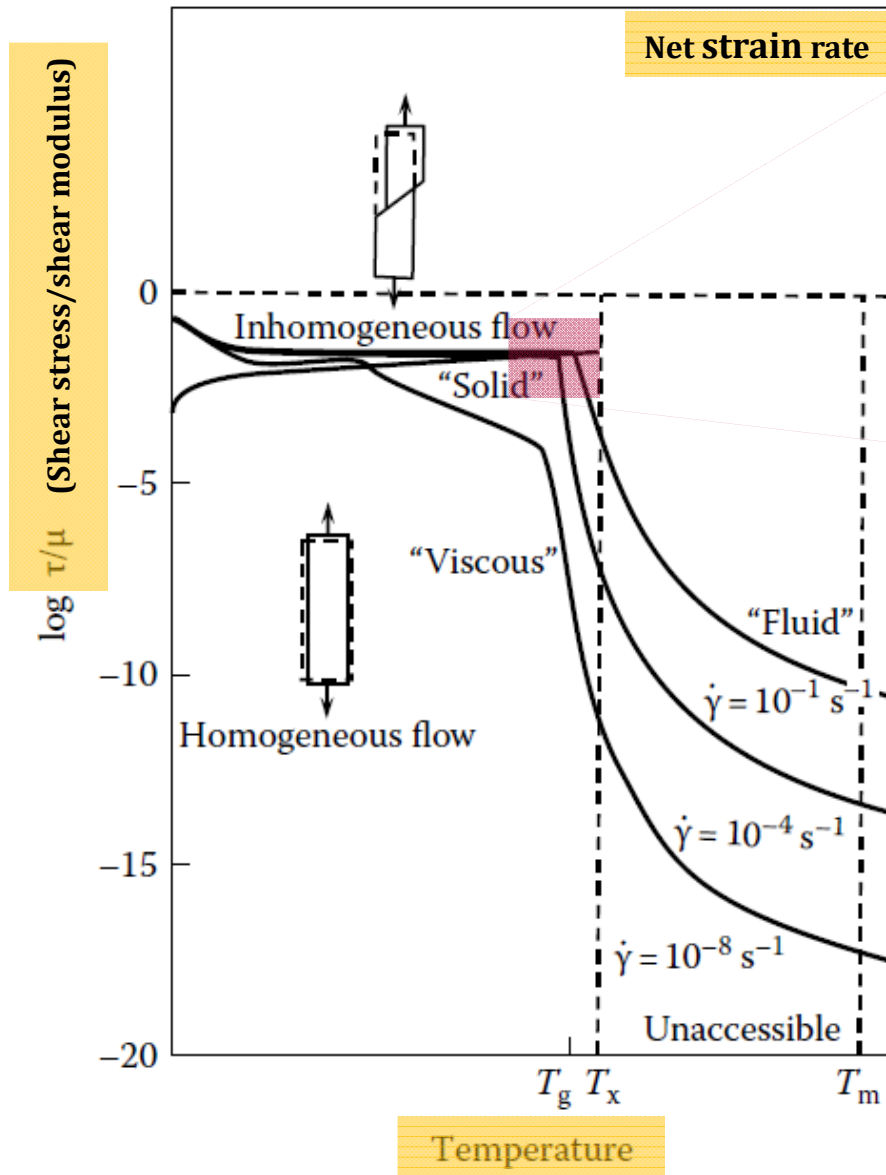


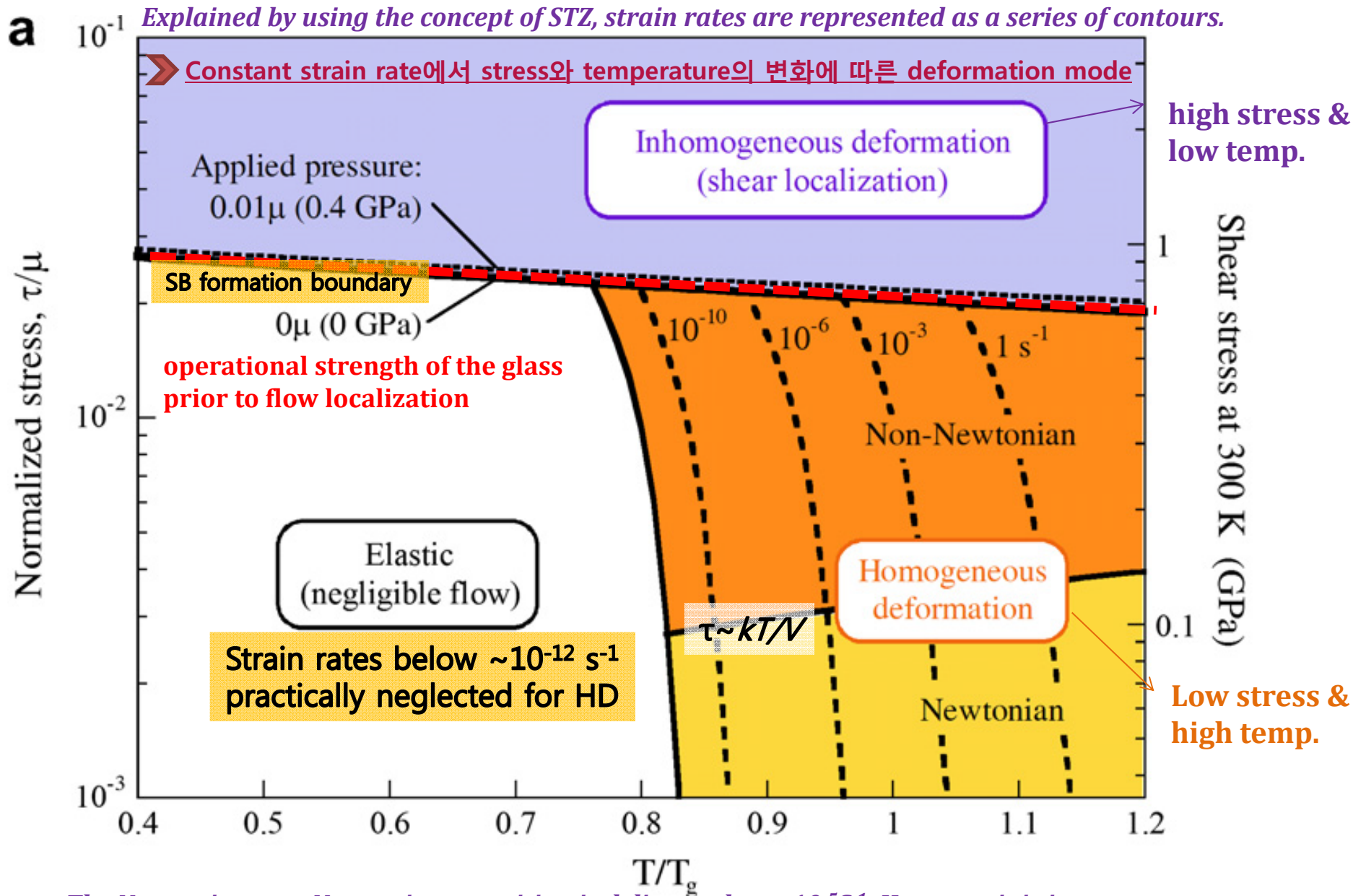
Fig. 1. Deformation mechanism map for a metallic glass.

# Empirical deformation mechanism maps for metallic glasses

*Developed by Spaepen using the results for melt-spun metallic glasses,  
Explained by using the concept of free volume model*



# Deformation map drawn by C.A. Schuh

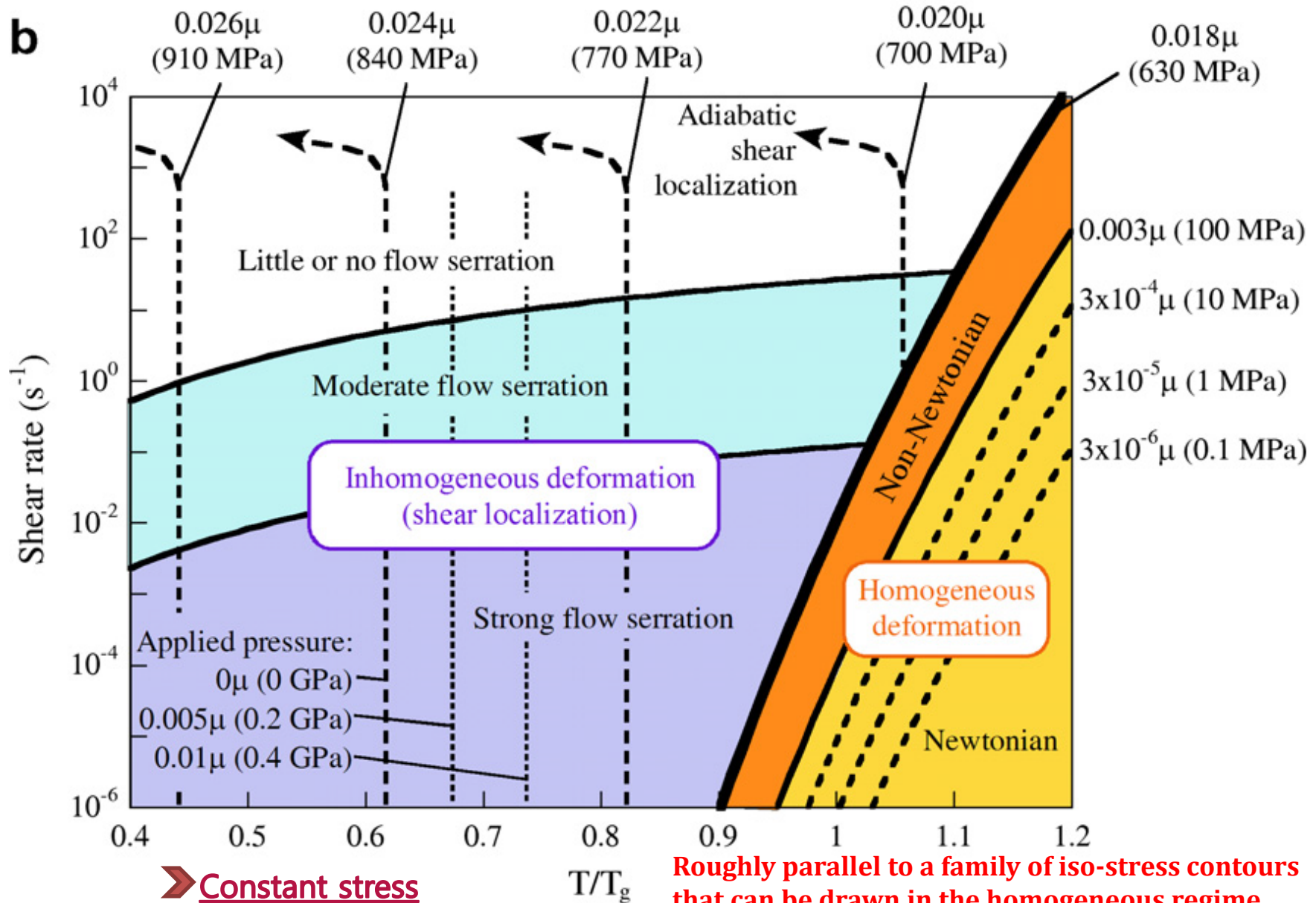


*The Newtonian-non-Newtonian transition is delineated at  $\sim 10^{-5} \text{ s}^{-1}$ . However, it is important to note that at high enough shear rates, non-Newtonian flow as well as shear localization can occur at high temperature - even in the supercooled liquid region.*



# Deformation map drawn by C.A. Schuh

*Explained by using the concept of STZ, stress is represented as a series of contours.*



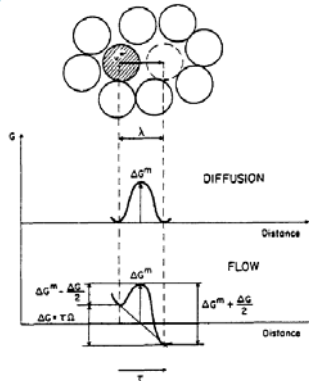
# Deformation modes

## Plastic deformation

( $\gamma$ ,  $\tau$ , T)

### F. Spaepen : Free volume theory

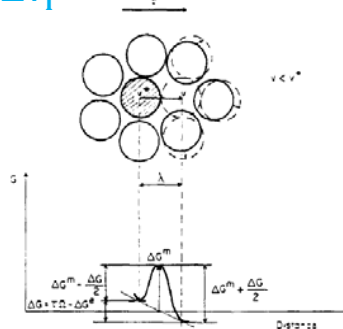
#### Homogeneous flow @ steady state



#### Inhomogeneous flow @ steady state

Competition of shear-induced disordering and a diffusion controlled reordering;  
creation of FV vs. relaxation

$$\Delta v_f^+ = \Delta v_f^-$$



### A. S. Argon / C. A. Schuh: STZ model

#### Homogeneous plastic flow

Viscous flow of a SCL

#### Steady-state flow

Structural disordering과 ordering,  
즉 free volume creation과 annihilation 사이의 균형.

$$\Delta v_f^+ = \Delta v_f^-$$

Local diffusive jump 또는 STZ operation이 stress를 분산시키고, dilatation을 통해 free volume을 만들지만 동시에 relaxation이 진행되어 free volume을 없앤다.

Structural maintenance

#### Non-steady-state flow

Structural transience가 일어남.

균형이 이루어지지 않아 net gain / loss of free volume이 일어날 수 있다.

“overshoot” “undershoot”

#### Inhomogeneous plastic flow

Localization → Shear band formation

local production of FV (dilatation)

local evolution of structural order due to STZ operation

redistribution of internal stresses

# Summary

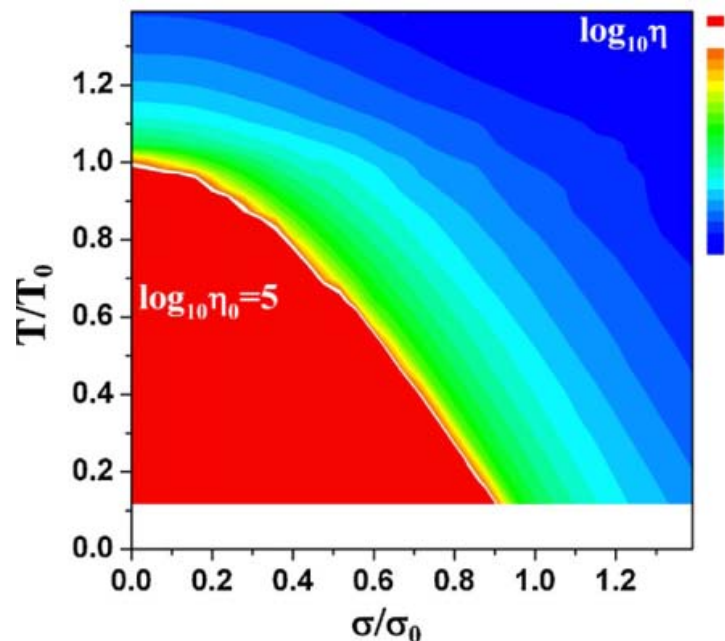
➤ Plastic deformation in metallic glasses controlled by shear band nucleation and propagation.

➤ Atomistic views of deformation of metallic glasses

F. Spaepen: Free volume theory

A.S. Argon: Shear transformation zone theory

T. Egami: Atomic bond topology



- Free volume theory: liquid 상에서의 free volume 개념이 모호, MD simulation 결과와는 맞지 않음

- Free volume theory는 현상을 설명하기에 매우 적합하지만 그 자체로 microscopic theory가 될 수는 없다. (free volume이 없어도 변형 가능)

- Local topological fluctuation은 원자 수준의 stress를 온도에 따라 재배열함에 따라 thermal property를 설명할 수 있다.

➤ Deformation map predicts the deformation modes of metallic glasses

normalized stress  $\sigma_s/\mu$ , homologous temperature  $T/T_M$ , shear strain  $\gamma'$