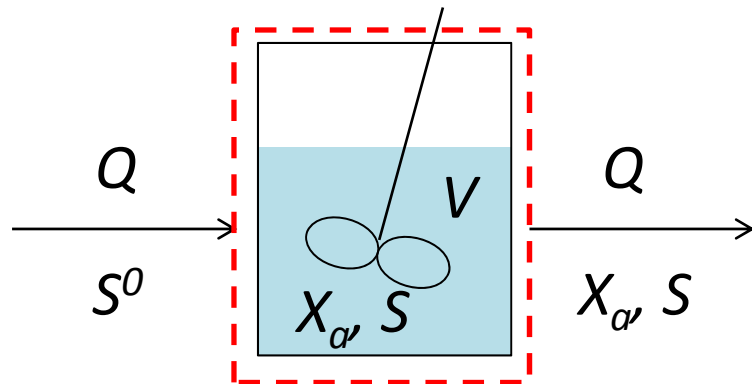


Microbial kinetics in reactors I

Today's lecture

- Master equations and key trends
- Including inert biomass
- Observed yield
- Soluble microbial products

CSTR, Monod: Master equations



Assumption:

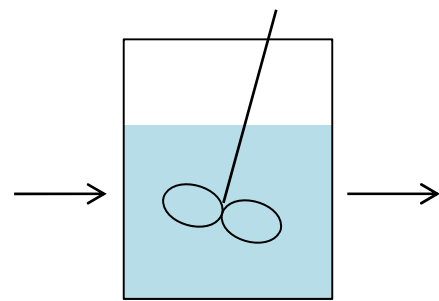
- Steady state
- $X_a = 0$ in the influent
(negligible influent biomass)

$$S = K \frac{1 + b\theta}{Y\hat{q}\theta - (1 + b\theta)}$$

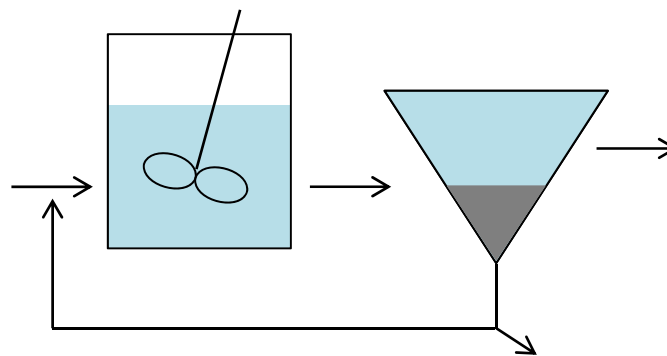
$$X_a = Y \frac{S^0 - S}{1 + b\theta}$$

HRT vs. SRT

- HRT: **H**ydraulic **R**etention **T**ime; the average time the water stays in the system
- SRT: **S**olids **R**etention **T**ime (or mean cell residence time, MCRT); the average time the biomass stays in the system

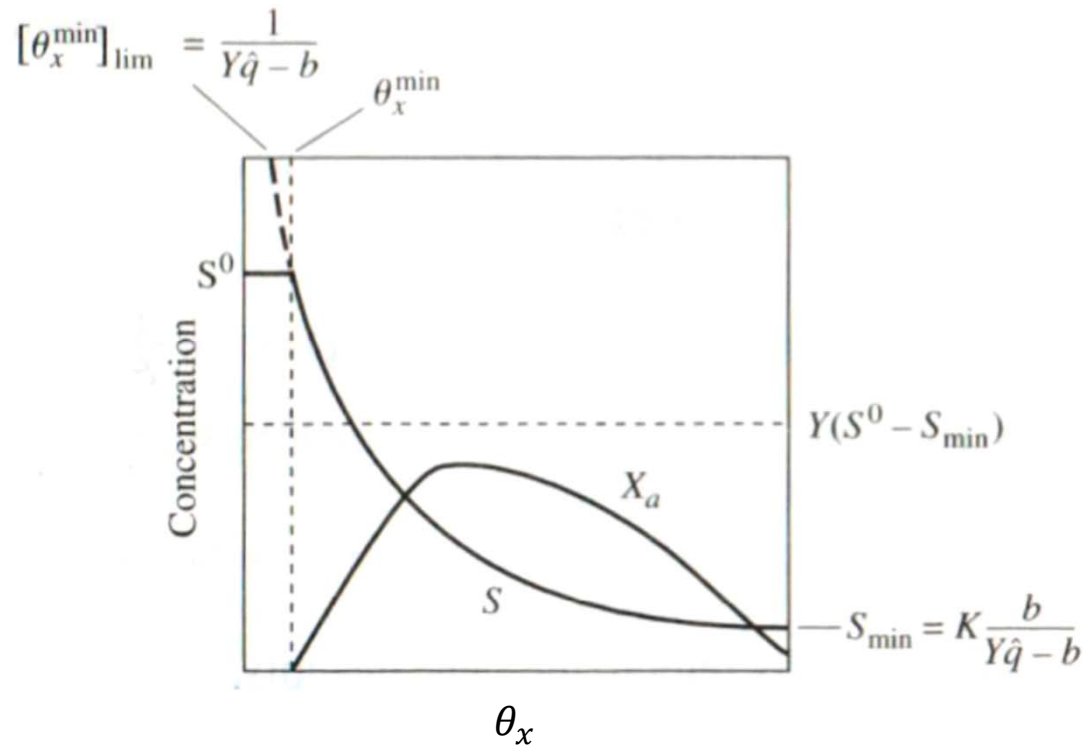


A chemostat: $HRT = SRT$



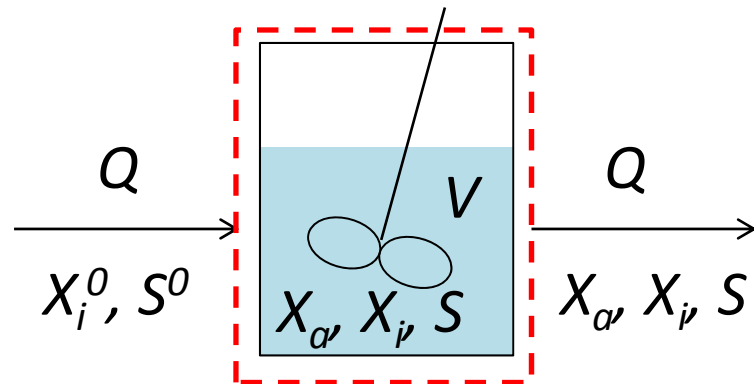
An activated sludge process with sludge return: $HRT < SRT$

θ_x vs. S : key trends



- 1) $\theta_x \leq \theta_x^{min}$:
washout
- 2) $\theta_x \rightarrow \infty$:
 $S = S_{min}$
- 3) For $\theta_x^{min} < \theta_x$, S
decreases with
increase in θ_x ,
but X_a peaks at
some point

Including inert biomass

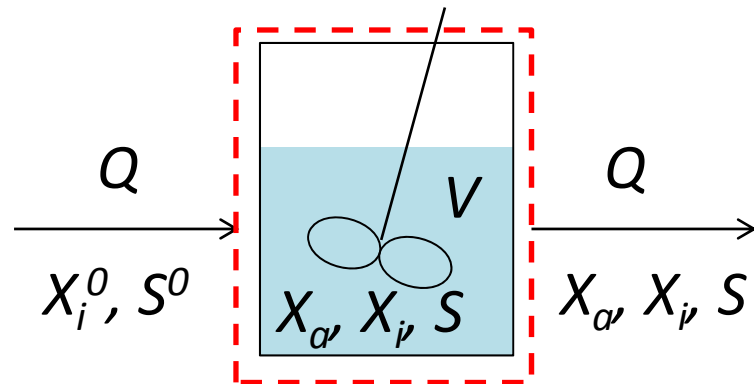


Influent contains some non-biodegradable, particulate organics: this is included when you measure VSS

Recall:

$$\left(\frac{1}{X_a} \frac{dX_a}{dt} \right)_{inert} = - \frac{1}{X_a} \frac{dX_i}{dt} = -(1 - f_d)b$$

Including inert biomass



Solution for inert biomass: $X_i = X_i^0 + X_a(1 - f_d)b\theta_x$

Solution for total VSS:

$$X_v = X_i + X_a = X_i^0 + Y(S^0 - S) \frac{1 + (1 - f_d)b\theta_x}{1 + b\theta_x}$$

Observed yield

The VSS in a CSTR is calculated as:

$$X_v = X_i + X_a = X_i^0 + \underbrace{Y(S^0 - S)}_{\text{substrate utilized at the reactor}} \underbrace{\frac{1 + (1 - f_d)b\theta_x}{1 + b\theta_x}}_{\text{VSS gained at the reactor}}$$

Influent inert biomass
substrate utilized at the reactor
VSS gained at the reactor

The net yield in the CSTR is: $Y \frac{1 + (1 - f_d)b\theta_x}{1 + b\theta_x}$

This value is more often called as **Observed Yield (Y_{obs})**.

Soluble microbial products (SMP)

- Cell components that released during cell lysis, diffuse through the cell membrane, are lost during synthesis, or are excreted for some purpose
- Does not include intermediates of degradation pathway
- MW = 100s – 1000s
- Biodegradable

Significance of SMP

- Appear in all cases
- Constitute the majority of the effluent COD & BOD in many cases
- Can complex metals, foul membranes, & cause color or foaming

Two types of SMP

- UAP (substrate-**U**tilization-**A**ssociated **P**roducts):
produced directly during substrate metabolism

$$r_{UAP} = -k_1 r_{ut}$$

r_{UAP} = rate of UAP-formation [$M_p L^{-3} T^{-1}$]
 k_1 = UAP-formation coefficient [$M_p M_s^{-1}$]

- BAP (**B**iomass-**A**ssociated **P**roducts):
formed directly from biomass as part of
maintenance and decay

$$r_{BAP} = k_2 X_a$$

r_{BAP} = rate of BAP-formation [$M_p L^{-3} T^{-1}$]
 k_2 = BAP-formation coefficient [$M_p M_x^{-1} T^{-1}$]

SMP biodegradation

- Assume both UAP and BAP follow Monod kinetics with different parameters:

$$r_{deg-UAP} = -\frac{\hat{q}_{UAP}UAP}{K_{UAP} + UAP}X_a$$

$$r_{deg-BAP} = -\frac{\hat{q}_{BAP}BAP}{K_{BAP} + BAP}X_a$$

SMP in a CSTR (a Chemostat)

- Steady-state mass balance for UAP & BAP:

$$0 = -k_1 r_{ut} V - \frac{\hat{q}_{UAP} UAP}{K_{UAP} + UAP} X_a V - Q \cdot UAP$$

$$0 = k_2 X_a V - \frac{\hat{q}_{BAP} BAP}{K_{BAP} + BAP} X_a V - Q \cdot BAP$$

Solution for UAP & BAP in Eqs. [3.38] & [3.39]