

# Guided waves and optical fibres

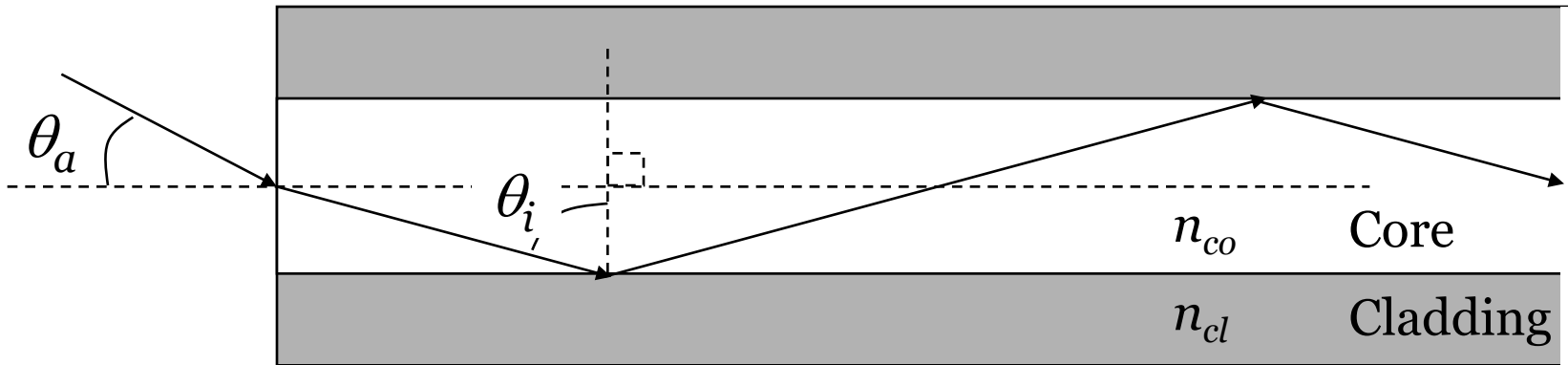
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# Optical Waveguides



## □ Total Internal Reflection

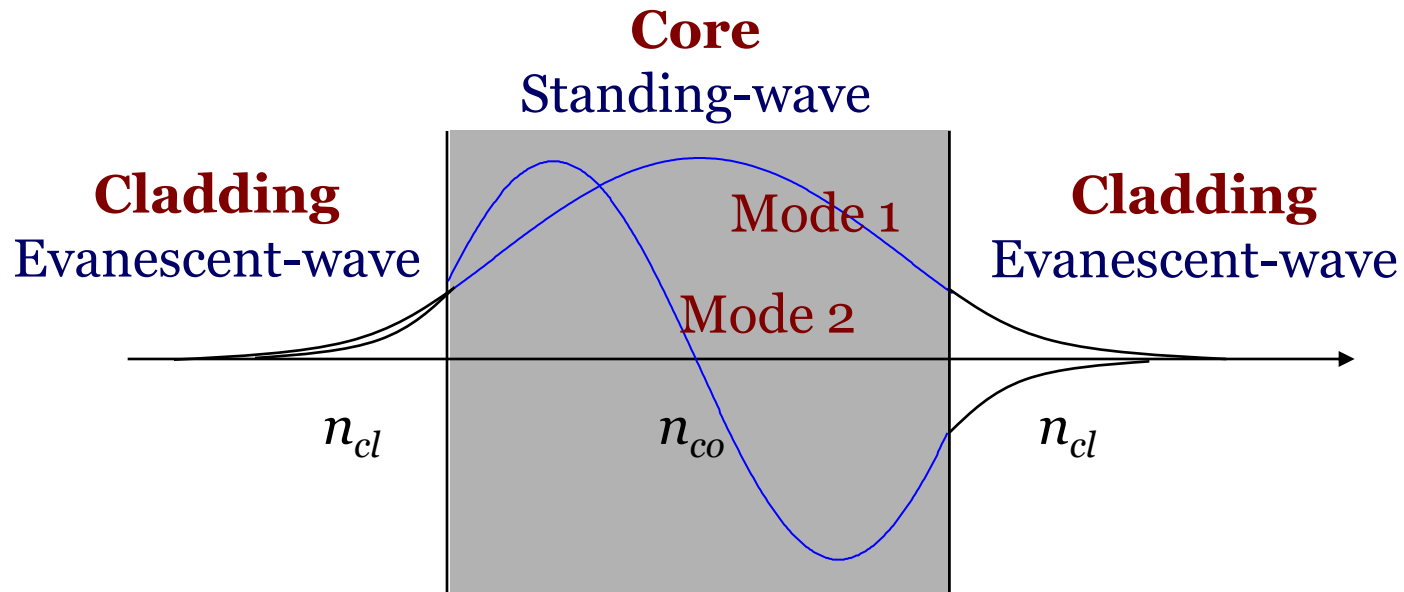
$$\theta_i > \theta_c = \sin^{-1}\left(\frac{n_{cl}}{n_{co}}\right) \quad \text{If the incident angle is greater than } \theta_c$$

## □ Numerical Aperture

$$NA = n_o \sin \theta_a \approx \theta_a = \sqrt{n_{co}^2 - n_{cl}^2}$$

# Optical Waveguides

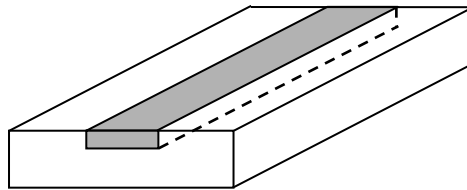
## Quantized Mode State



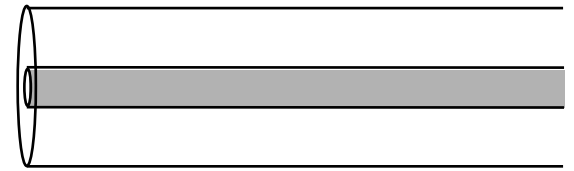
### ■ Planar W/G



### ■ Channel W/G



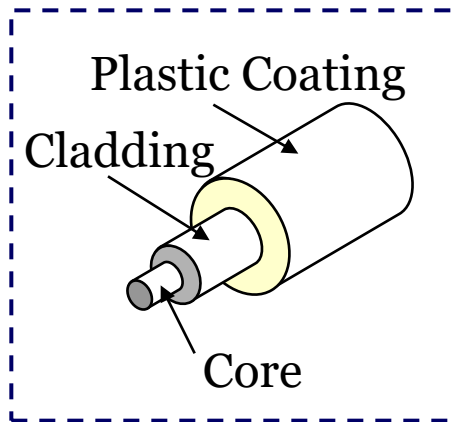
### ■ Circular W/G



# Optical Fibers

■ A flexible optically transparent fiber, as of glass or plastic, through which light can be transmitted by successive internal reflection

## ■ Structure of Optical Fiber



# Optical Fiber Fabrication

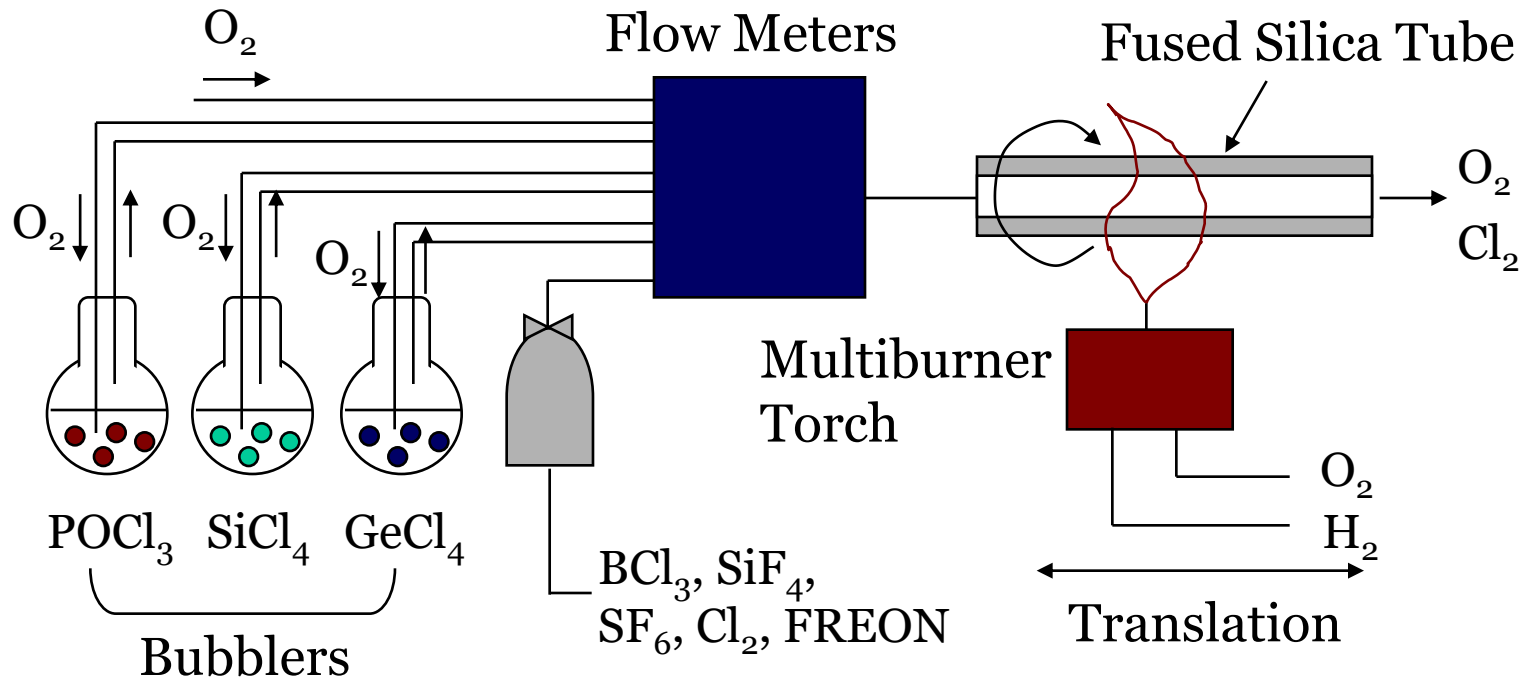
- **Double Crucible**    Directly drawing
- **Rod in Tube**    Preform and drawing

## Preform Fabrication

### □ **Deposition Techniques**

- Modified chemical vapor deposition (MCVD)
- Plasma-enhanced modified chemical vapor deposition (PMCVd)
- Outside vapor deposition (OVD)
- Axial vapor deposition (AVD)

# Preform Fabrication by MCVD



## ■ Dopants:

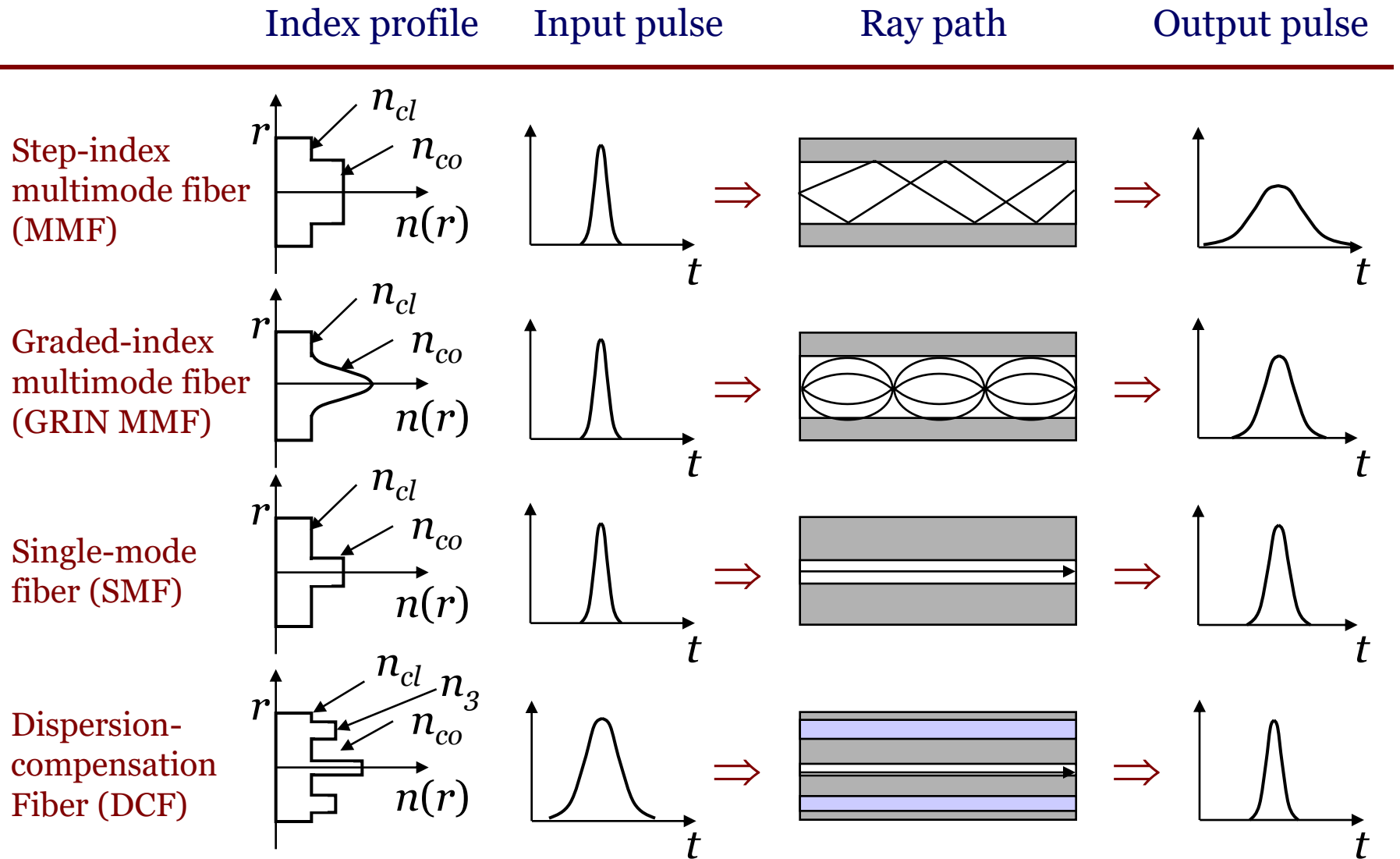
$\text{GeO}_2$ ,  $\text{P}_2\text{O}_5$ ,  $\text{ErCl}_3$ ,  $\text{Nd}_2\text{O}_3$

## Drawing and Spooling

## □ Procedure

- Drawn from the Preform
- Quality checked
- Coated for protection
- Stored on a spool

# Optical Fibers

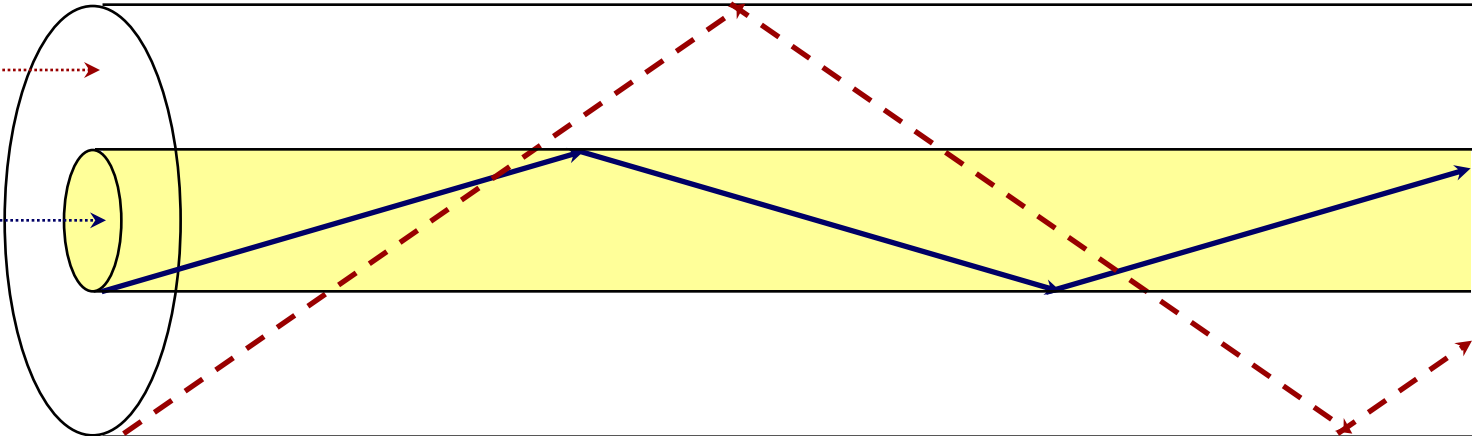


# Single-Mode Fiber

Air or Jacket →

Cladding →

Core →



————— : Core mode

- - - - - : Cladding mode



# Core Mode

## □ Mode Expansion

*Core ( $r \leq r_{co}$ )*

$$E_z = a_{co} J_\nu(h_{co} r)$$

$$H_z = b_{co} J_\nu(h_{co} r)$$

$$\rightarrow E_r, E_\phi, H_r, H_\phi$$

$$\text{where } h_{co} = \sqrt{k_o^2 n_{co}^2 - \beta^2}$$

*Cladding ( $r \geq r_{co}$ )*

$$E_z = a_{cl} K_\nu(h_{cl} r)$$

$$H_z = b_{cl} K_\nu(h_{cl} r)$$

$$\rightarrow E_r, E_\phi, H_r, H_\phi$$

$$\text{where } h_{cl} = \sqrt{\beta^2 - k_o^2 n_{cl}^2}$$

*note* :  $\exp[i(\omega t - \beta z + \nu\phi)]$  : omitted

■ Continuity condition of tangential fields at  $r = r_{co}$

$\Rightarrow$  **Core-bounded mode**

# Exact Core Mode

## □ Mode Expansion

*Core* ( $r \leq r_{co}$ )

$$E_z = a_{co} J_\nu(h_{co}r)$$

$$H_z = b_{co} J_\nu(h_{co}r)$$

$$\rightarrow E_r, E_\phi, H_r, H_\phi$$

$$\text{where } h_{co} = \sqrt{k_o^2 n_{co}^2 - \beta^2}$$

*Cladding* ( $r_{co} < r \leq r_{cl}$ )

$$E_z = a_{cl} K_\nu(h_{cl}r) + c_{cl} I_\nu(h_{cl}r)$$

$$H_z = b_{cl} K_\nu(h_{cl}r) + d_{cl} I_\nu(h_{cl}r)$$

$$\rightarrow E_r, E_\phi, H_r, H_\phi$$

$$\text{where } h_{cl} = \sqrt{k_o^2 n_{cl}^2 - \beta^2}$$

*Air* ( $r > r_{cl}$ )

$$E_z = a_{ai} K_\nu(h_{ai}r)$$

$$H_z = b_{ai} K_\nu(h_{ai}r)$$

$$\rightarrow E_r, E_\phi, H_r, H_\phi$$

$$\text{where } h_{ai} = \sqrt{\beta^2 - k_o^2 n_{ai}^2}$$

*note* :  $\exp[i(\omega t - \beta z + \nu\phi)]$  : omitted

- Continuity condition of tangential fields at  $r = r_{co}$ ,  $r = r_{cl}$   
 $\Rightarrow$  **Core-bounded mode**

# Cladding Mode

## □ Mode Expansion

*Core* ( $r \leq r_{co}$ )

$$E_z = a_{co} J_\nu(h_{co}r)$$

$$H_z = b_{co} J_\nu(h_{co}r)$$

$$\rightarrow E_r, E_\phi, H_r, H_\phi$$

$$\text{where } h_{co} = \sqrt{k_o^2 n_{co}^2 - \beta^2}$$

*Cladding* ( $r_{co} < r \leq r_{cl}$ )

$$E_z = a_{cl} J_\nu(h_{cl}r) + c_{cl} Y_\nu(h_{cl}r)$$

$$H_z = b_{cl} J_\nu(h_{cl}r) + d_{cl} Y_\nu(h_{cl}r)$$

$$\rightarrow E_r, E_\phi, H_r, H_\phi$$

$$\text{where } h_{cl} = \sqrt{k_o^2 n_{cl}^2 - \beta^2}$$

*Air* ( $r > r_{cl}$ )

$$E_z = a_{ai} K_\nu(h_{ai}r)$$

$$H_z = b_{ai} K_\nu(h_{ai}r)$$

$$\rightarrow E_r, E_\phi, H_r, H_\phi$$

$$\text{where } h_{ai} = \sqrt{\beta^2 - k_o^2 n_{ai}^2}$$

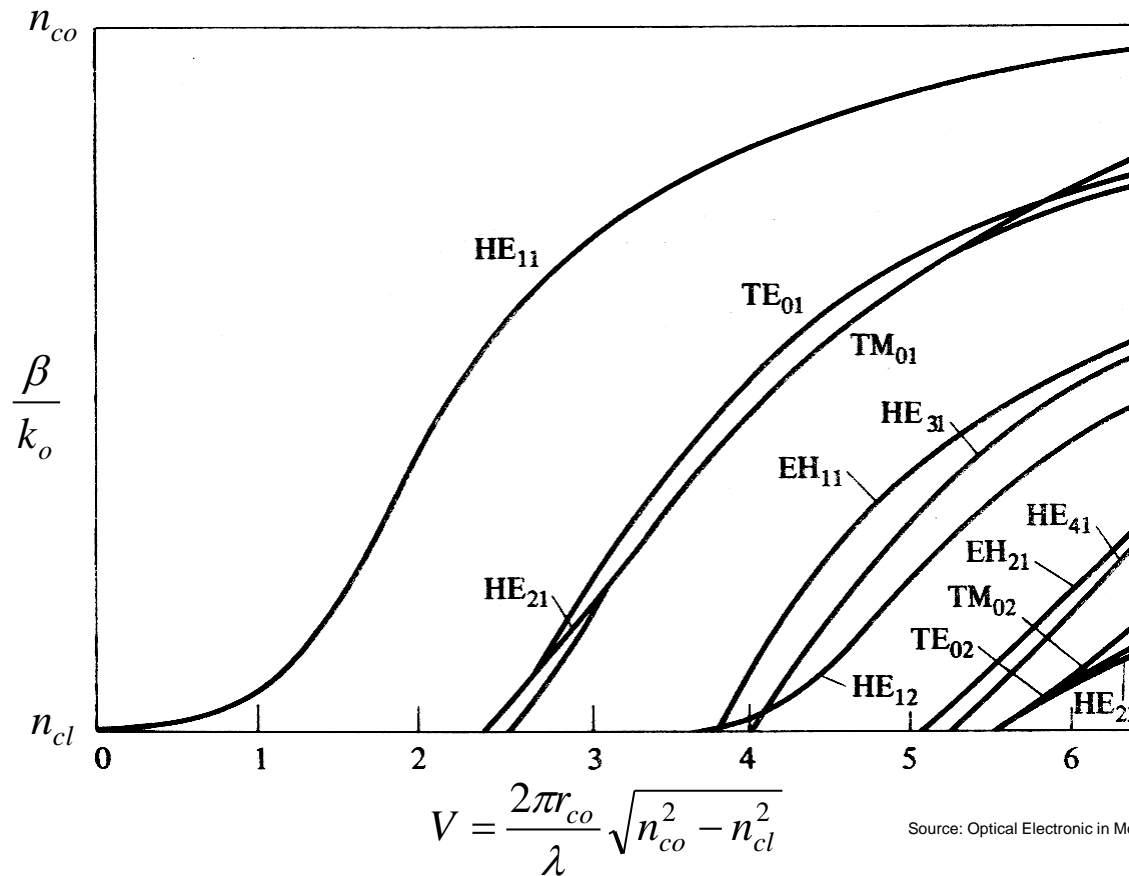
*note* :  $\exp[i(\omega t - \beta z + \nu\phi)]$  : omitted

■ Continuity condition of tangential fields at  $r = r_{co}$ ,  $r = r_{cl}$

$\Rightarrow$  **Cladding-bounded mode**

# Effective Index of Core Mode

□ As a function of  $V$  parameter

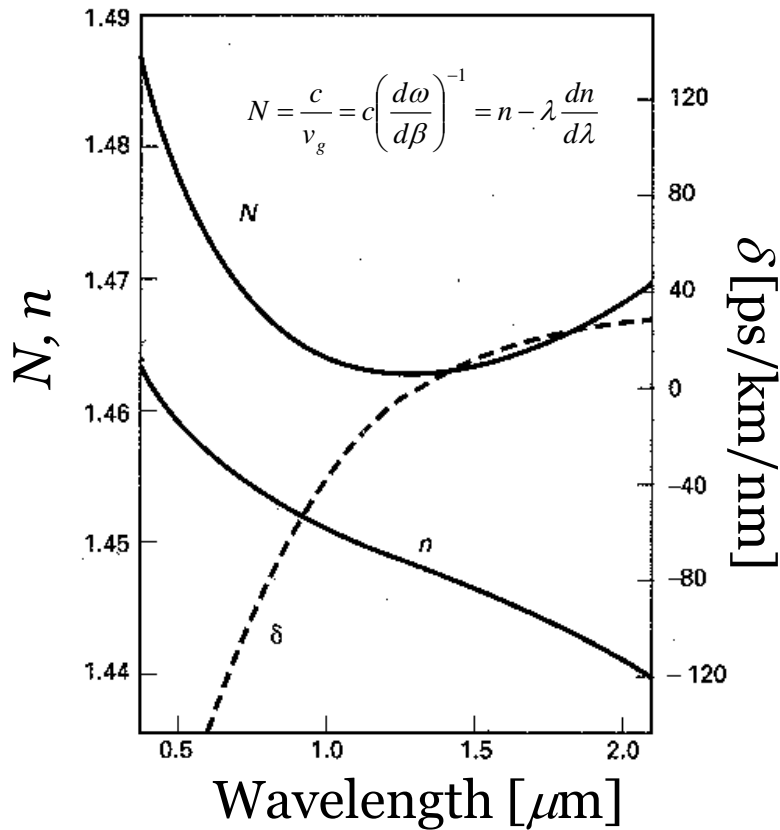


Source: Optical Electronic in Modern Communications, A. Yariv

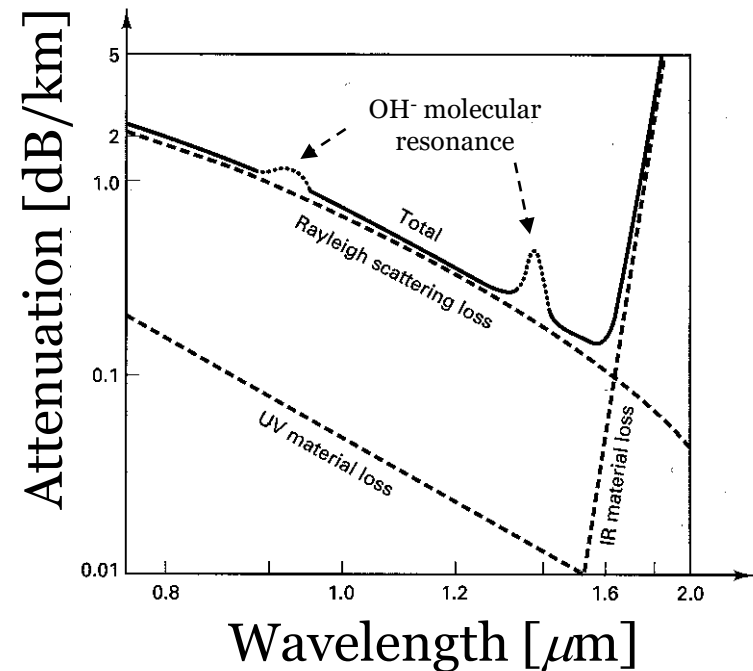
■  $V < 2.405 \Rightarrow$  Single-mode operation

# Dispersion and Attenuation in SMF

## □ Dispersion and Attenuation vs. Wavelength



- 1.3  $\mu\text{m}$ : Zero dispersion
- 1.5  $\mu\text{m}$ : Minimum loss



Source: Nonlinear Fiber Optics, G. P. Agrawal

# Attenuation in SMF

## □ Causes of Attenuation

### - Absorption

Intrinsic absorption: ultraviolet and infrared

Absorption by impurities: OH<sup>-</sup> and transition metal

Absorption by atomic defects

### - Scattering

Rayleigh scattering prohibits the use of wavelength below 0.8  $\mu\text{m}$ , which is proportional to  $1/\lambda^4$ .

### - Geometrical effects

Bending loss

**Typically, the attenuation in SMF is 0.2 dB/km.**

# Dispersion in SMF

## □ Types of Dispersion

- Intermodal dispersion

  - Pulse spreading in multimode fiber

- Intramodal dispersion

  - Material dispersion

  - Waveguide dispersion: usually *smaller* than material dispersion

    - Short wavelength: The effective index is close to  $n_{core}$ .

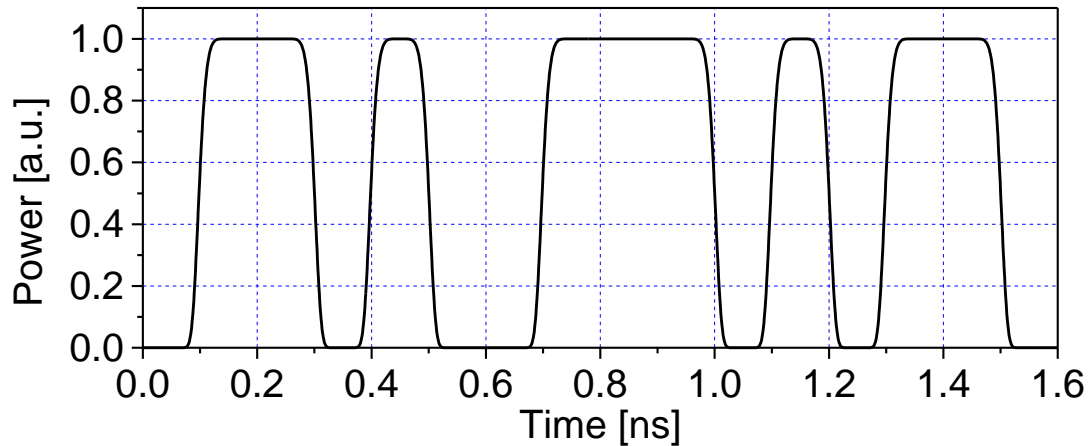
    - Long wavelength: The effective index is close to  $n_{cladding}$ .

    - Recall V parameter!**

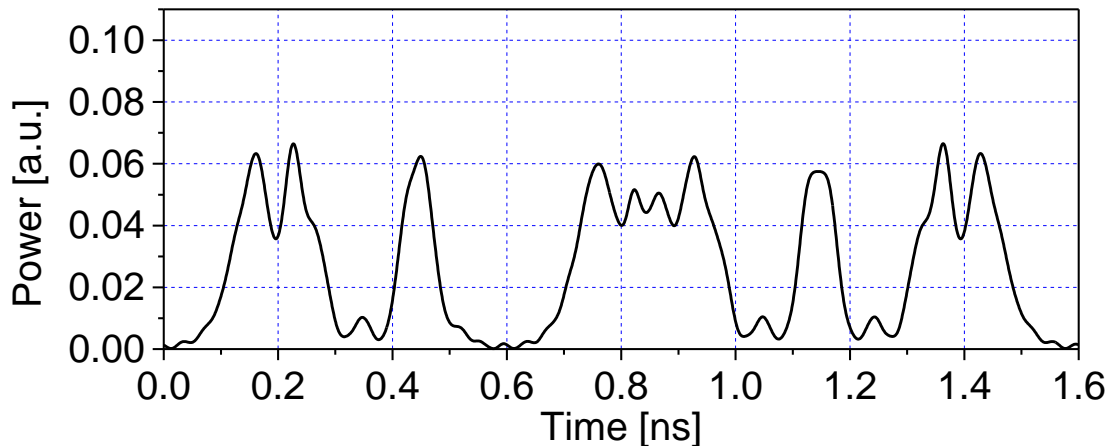
**Dispersion is a problem in fiber communications: It eventually limits the *bandwidth* of the fiber.**

# Data Transmission in SMF

## ■ Initial Optical Pulses (10 Gbps, 0 dBm)



## ■ After 50-km Transmission



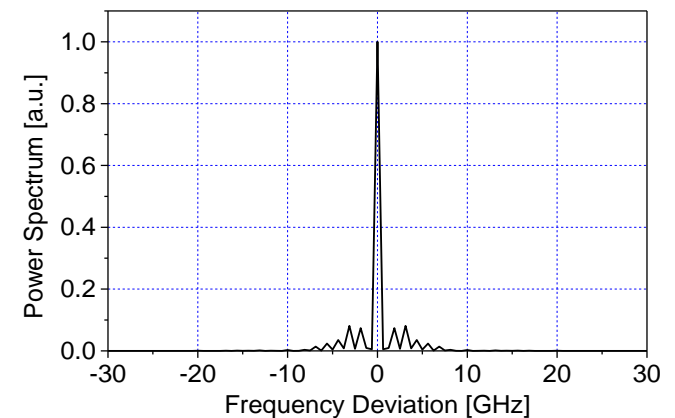
■ Group velocity dispersion (GVD)

⇒ Frequency chirp

■ Nonlinear effect

⇒ Four-wave mixing (FWM)

## ■ Power Spectrum





# Nonlinearities in Fibers

## □ Stimulated Raman Scattering (SRS)

A stimulated effect in which the energy from a photon incident on a molecule delivers parts of its energy to mechanical vibration of the molecule and part into reradiated light (*Stokes light*) of longer wavelength than the incident light

## □ Stimulated Brillouin Scattering (SBS)

A stimulated effect (highly directional) due to interaction between the traveling light wave, composed of photons, and *a traveling sound wave* that it induces, which can be considered as composed of quantum sound particles, *phonons*

## □ Four-Wave Mixing (FWM)

Third-order cross-product of electric field.

$f_i - f_j - f_k \Rightarrow$  frequency mixing, interfering effect in WDM