

Fig. 7.13 Flow past a circular cylinder: (a) laminar separation; (b) turbulent separation; (c) theoretical and actual surface pressure distributions.

Circular cylinder

$$\frac{D}{\frac{1}{2} e v^2 A} = C_0$$

1.0 ~ 1.2

$C_D \approx \text{const}$
 $D \sim V^2$

$$D \sim v^2$$

0.5

smooth surface

$$C_D \approx \text{const}$$

Laminar sep.

~~dimple~~

roughness



drag crisis

$C_2 \downarrow$

furbo.

turbulent
sep.

trans critical region

Red



turb.
sep.

Laminar sep.

~~dimple~~

roughness



drag crisis


$C_2 \downarrow$

furbo.

turbulent
sep.

trans critical region

Red



turb.
sep.

Subcritical regime

 10^5

106

critical regime

super critical
regime

mechanism

$$Re_d = \frac{Ud}{\nu} = \frac{U \times 0.1}{1.5 \times 10^{-4}} \Rightarrow U = 150 \text{ m/s}$$

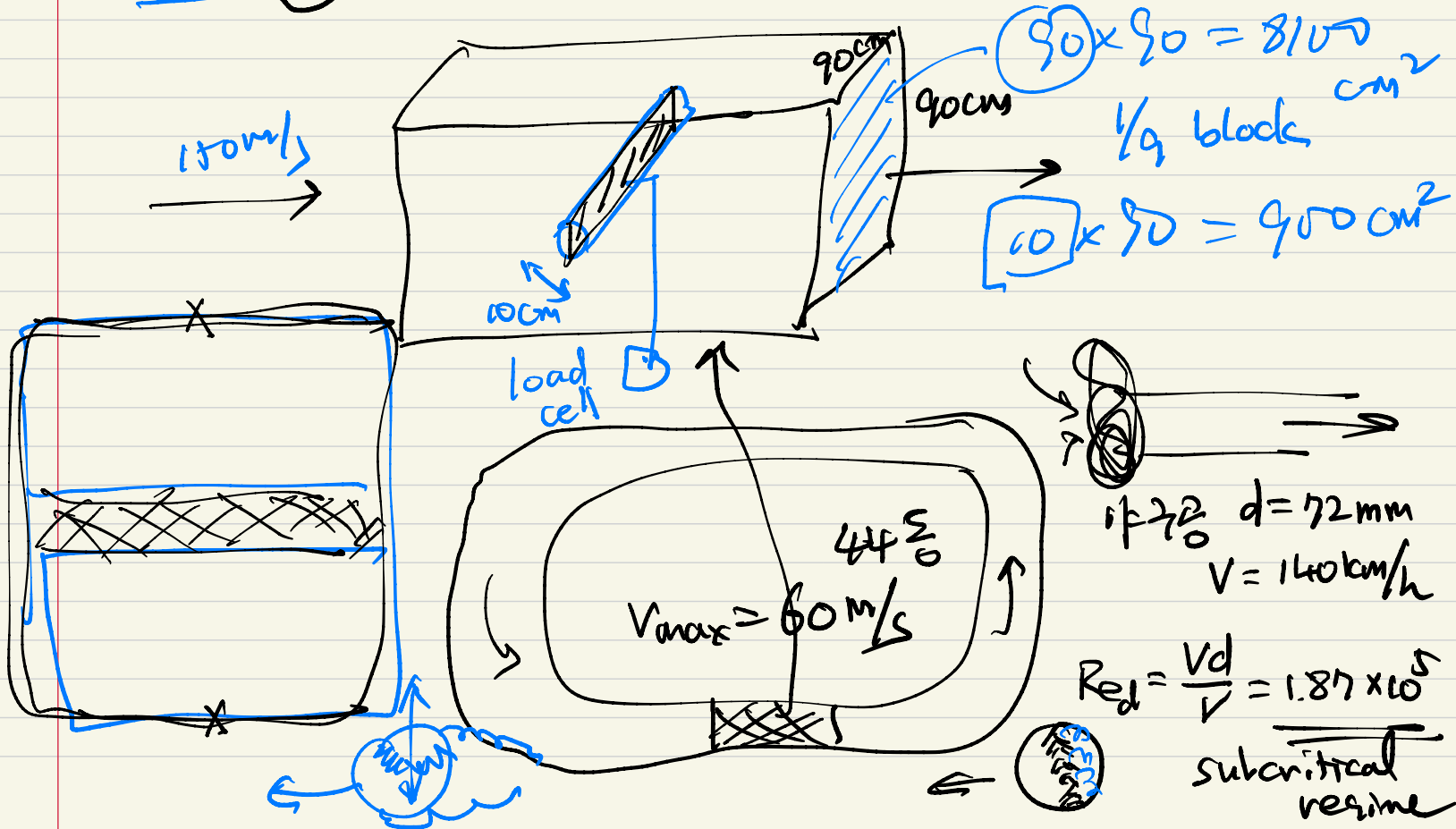
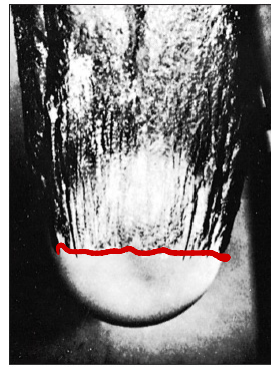
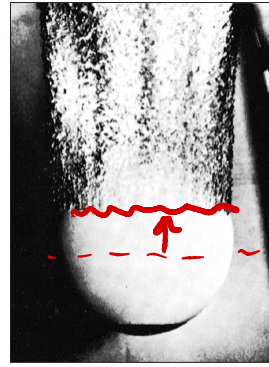


Fig. 7.14 Strong differences in laminar and turbulent separation on an 8.5-in bowling ball entering water at 25 ft/s: (a) smooth ball, laminar boundary layer, (b) same entry, turbulent flow induced by patch of nose-sand roughness. (NAVAIR Weapons Division Historical Archives.)



(a) Smooth ball

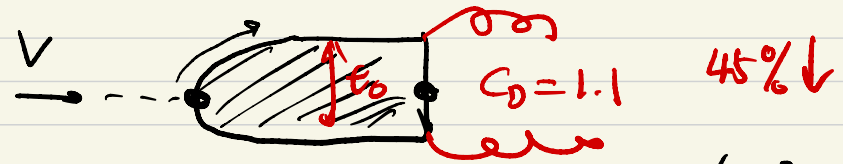
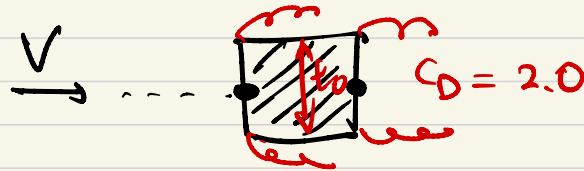


(b) roughness

flow visualization

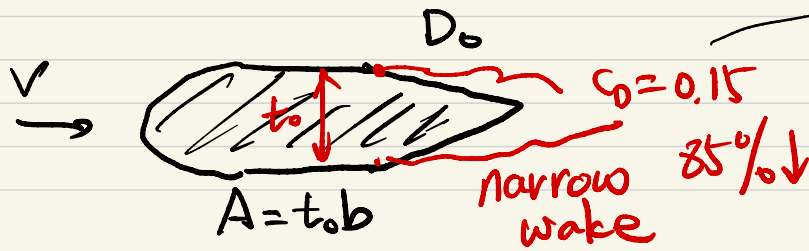
- ① discovery
- ② mechanism

Importance of streamlining

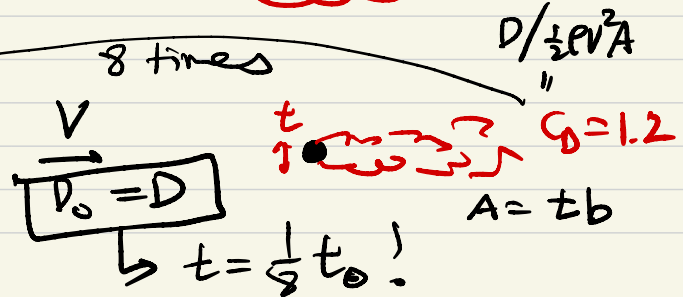


broad wake

45% ↓



narrow wake



8 times

$$D = \frac{1}{2} \rho V^2 A$$

$$A = t b$$

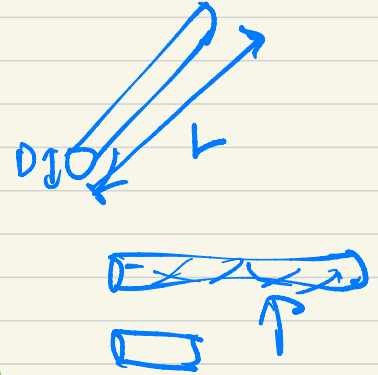
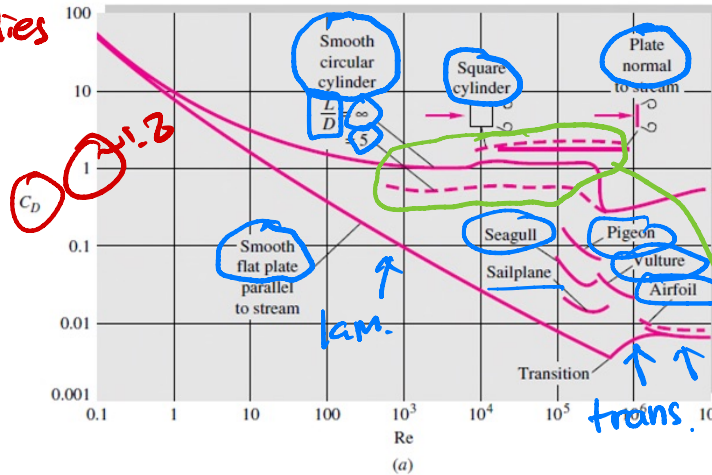
$$t = \frac{1}{8} t_0 !$$

For high-performance vehicles and other moving vehicles,
the name of game is drag reduction

$$C_D = \frac{D}{\frac{1}{2} \rho V^2 A}$$

planform area
except for
normal plate

2D bodies



3D bodies

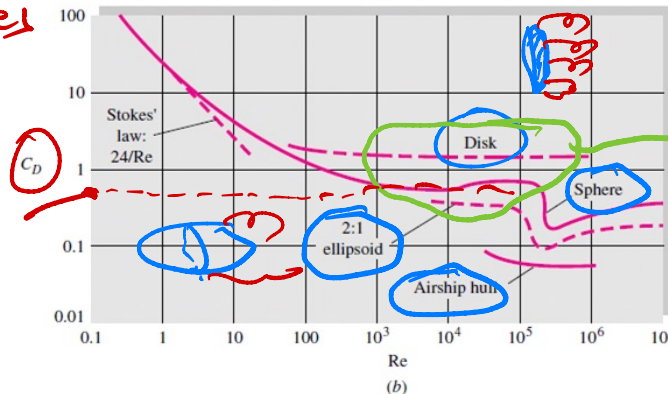


Fig. 7.16 Drag coefficients of smooth bodies at low Mach numbers: (a) two-dimensional bodies; (b) three-dimensional bodies. Note the Reynolds number independence of blunt bodies at high Re .

$C_D \approx \text{const}$
independent
of Re

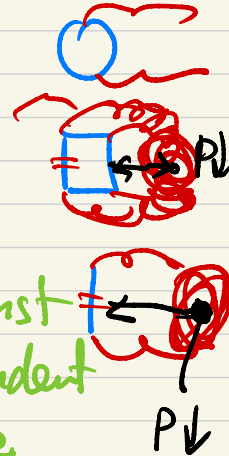












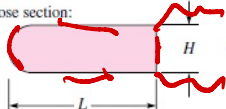


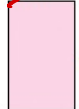
Table 7.2 Drag of Two-Dimensional Bodies at $Re \geq 10^4$





2D bodies
at $Re \geq 10^4$
($C_D \approx \text{const}$)

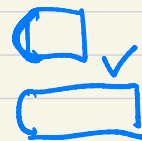
$$C_D = \frac{D}{\frac{1}{2} \rho V^2 A_{\text{frontal area}}}$$

Shape	C_D based on frontal area	Shape	C_D based on frontal area	Shape	C_D based on frontal area
Square cylinder: → 	2.1	Half cylinder: → 	1.2	Plate: → 	2.0
→ 	1.6	→ 	1.7	Thin plate normal to a wall: → 	1.4
Half tube: → 	1.2	Equilateral triangle: → 	1.6	Hexagon: → 	1.0
→ 	2.3	→ 	2.0	→ 	0.7

Shape	C_D based on frontal area					
Rounded nose section: → 	L/H	0.5	1.0	2.0	4.0	6.0
	C_D	1.16	0.90	0.70	0.68	0.64

Flat nose section: → 	L/H	0.1	0.4	0.7	1.2	2.0	2.5	3.0	6.0
	C_D	1.9	2.3	2.7	2.1	1.8	1.4	1.3	0.9

Elliptical cylinder:		Laminar	Turbulent
1:1 → 	1.2	0.3	
2:1 → 	0.6	0.2	
4:1 → 	0.35	0.15	
8:1 → 	0.25	0.1	



skin friction ↑

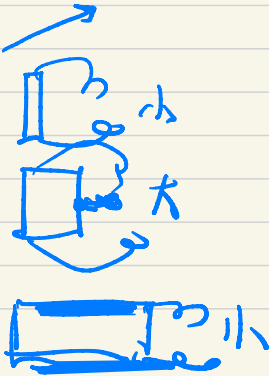


Table 7.3 Drag of Three-Dimensional Bodies at $Re \approx 10^4$ 3β $C_D \approx \text{const}$

Body	C_D based on frontal area	Body	C_D based on frontal area																					
Cube:	1.07	Cone:	<table border="1"> <thead> <tr> <th>θ:</th> <th>10°</th> <th>20°</th> <th>30°</th> <th>40°</th> <th>60°</th> <th>75°</th> <th>90°</th> </tr> </thead> <tbody> <tr> <td>C_D:</td> <td>0.30</td> <td>0.40</td> <td>0.55</td> <td>0.65</td> <td>0.80</td> <td>1.05</td> <td>1.15</td> </tr> </tbody> </table>	θ :	10°	20°	30°	40°	60°	75°	90°	C_D :	0.30	0.40	0.55	0.65	0.80	1.05	1.15					
θ :	10°	20°	30°	40°	60°	75°	90°																	
C_D :	0.30	0.40	0.55	0.65	0.80	1.05	1.15																	
→	0.81	Short cylinder, laminar flow:	<table border="1"> <thead> <tr> <th>L/D:</th> <th>1</th> <th>2</th> <th>3</th> <th>5</th> <th>10</th> <th>20</th> <th>40</th> <th>∞</th> </tr> </thead> <tbody> <tr> <td>C_D:</td> <td>0.64</td> <td>0.68</td> <td>0.72</td> <td>0.74</td> <td>0.82</td> <td>0.91</td> <td>0.98</td> <td>1.20</td> </tr> </tbody> </table>	L/D :	1	2	3	5	10	20	40	∞	C_D :	0.64	0.68	0.72	0.74	0.82	0.91	0.98	1.20			
L/D :	1	2	3	5	10	20	40	∞																
C_D :	0.64	0.68	0.72	0.74	0.82	0.91	0.98	1.20																
Cup:	1.4	→																						
→	0.4	Porous parabolic dish [23]:	<table border="1"> <thead> <tr> <th>Porosity:</th> <th>0</th> <th>0.1</th> <th>0.2</th> <th>0.3</th> <th>0.4</th> <th>0.5</th> </tr> </thead> <tbody> <tr> <td>C_D:</td> <td>1.42</td> <td>1.33</td> <td>1.20</td> <td>1.05</td> <td>0.95</td> <td>0.82</td> </tr> <tr> <td>C_D:</td> <td>0.95</td> <td>0.92</td> <td>0.90</td> <td>0.86</td> <td>0.83</td> <td>0.80</td> </tr> </tbody> </table>	Porosity:	0	0.1	0.2	0.3	0.4	0.5	C_D :	1.42	1.33	1.20	1.05	0.95	0.82	C_D :	0.95	0.92	0.90	0.86	0.83	0.80
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Disk:	1.17	Average person:	<table border="1"> <tbody> <tr> <td>$C_D A$:</td> <td>9 ft²</td> <td>$C_D A = 1.2 \text{ ft}^2$</td> </tr> </tbody> </table>	$C_D A$:	9 ft ²	$C_D A = 1.2 \text{ ft}^2$																		
$C_D A$:	9 ft ²	$C_D A = 1.2 \text{ ft}^2$																						
Parachute (Low porosity):	1.2	→																						
→	8.5 m ²	Pine and spruce trees [24]:	<table border="1"> <thead> <tr> <th>U, m/s:</th> <th>10</th> <th>20</th> <th>30</th> <th>40</th> </tr> </thead> <tbody> <tr> <td>C_D:</td> <td>1.2 ± 0.2</td> <td>1.0 ± 0.2</td> <td>0.7 ± 0.2</td> <td>0.5 ± 0.2</td> </tr> </tbody> </table>	U , m/s:	10	20	30	40	C_D :	1.2 ± 0.2	1.0 ± 0.2	0.7 ± 0.2	0.5 ± 0.2											
U , m/s:	10	20	30	40																				
C_D :	1.2 ± 0.2	1.0 ± 0.2	0.7 ± 0.2	0.5 ± 0.2																				
Streamlined train (approximately 5 cars):		→																						
→		Tractor-trailer truck:	Without deflector: 0.96; with deflector: 0.76																					
Bicycle:		→																						
→		Upright: $C_D A = 0.51 \text{ m}^2$; Racing: $C_D A = 0.30 \text{ m}^2$																						

$$C_D = \frac{D}{\frac{1}{2} \rho U^2 A}$$

$$C_D A = \frac{D}{\frac{1}{2} \rho U^2}$$

$$C_D A = 9 \text{ ft}^2$$

$$= 9 \times 0.3048^2 \text{ m}^2$$

$$= 0.81 \text{ m}^2$$

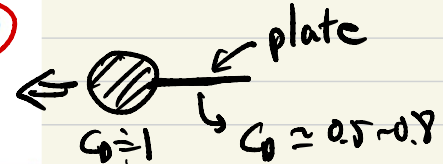
$$C_D A = 105$$

$$U = \frac{100}{10} = 10 \text{ m/s}$$

$$D = C_D A \cdot \frac{1}{2} \rho U^2$$

$$= 0.81 \times \frac{1}{2} \times 1.2 \times 10^2$$

$$\approx 50 \text{ N}$$



Body	Ratio	C_D based on frontal area	Body	Ratio	C_D based on frontal area																		
Rectangular plate:	b/h	<table> <tr><td>5</td><td>1.18</td></tr> <tr><td>10</td><td>1.2</td></tr> <tr><td>20</td><td>1.3</td></tr> <tr><td>∞</td><td>2.0</td></tr> </table>	5	1.18	10	1.2	20	1.3	∞	2.0	Flat-faced cylinder:	L/d	<table> <tr><td>0.5</td><td>1.15</td></tr> <tr><td>1</td><td>0.90</td></tr> <tr><td>2</td><td>0.85</td></tr> <tr><td>4</td><td>0.87</td></tr> <tr><td>8</td><td>0.99</td></tr> </table>	0.5	1.15	1	0.90	2	0.85	4	0.87	8	0.99
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Ellipsoid:	L/d	<table> <tr> <th></th> <th>Laminar</th> <th>Turbulent</th> </tr> <tr><td>0.5</td><td>0.5</td><td>0.2</td></tr> <tr><td>1</td><td>0.47</td><td>0.2</td></tr> <tr><td>2</td><td>0.27</td><td>0.13</td></tr> <tr><td>4</td><td>0.25</td><td>0.1</td></tr> <tr><td>8</td><td>0.2</td><td>0.08</td></tr> </table>		Laminar	Turbulent	0.5	0.5	0.2	1	0.47	0.2	2	0.27	0.13	4	0.25	0.1	8	0.2	0.08	Buoyant rising sphere [50].	C_D	0.95
	Laminar	Turbulent																					
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1	0.47	0.2																					
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8	0.2	0.08																					
			$135 < Re_d < 1E5$	$C_D \approx 0.5$																			

