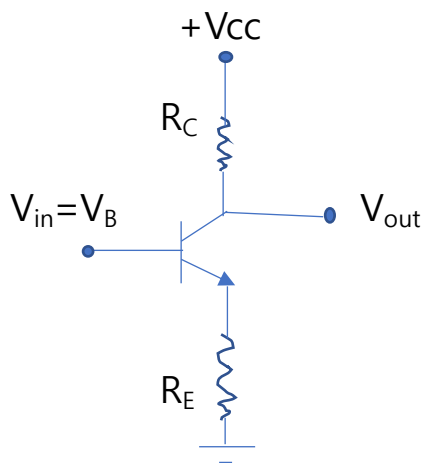


## Lecture 11; Transistor2

### 6. Common-Emitter Follower

: Current is amplified, and Voltage is also amplified.



$$V_{out} = V_{cc} - R_C I_C \text{ and } I_C = I_E = V_E / R_E = (V_{in} - 0.6) / R_E$$

$$\text{Thus } V_{out} = V_{cc} - R_C (V_{in} - 0.6) / R_E \therefore \Delta V_{out} = -\Delta V_{in} R_C / R_E$$

Therefore  $\Delta V_{out}$  is amplified from  $\Delta V_{in}$  with Gain =  $-R_C / R_E$

Current ( $I_C$ ) is also amplified by  $\beta$  times ( $=\beta I_B$ )

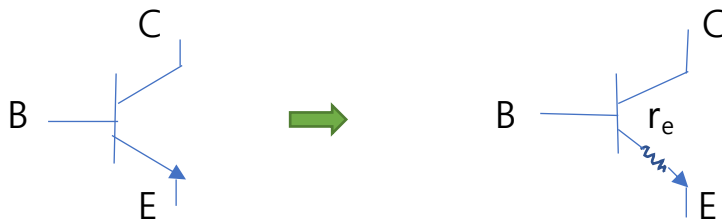
To check the impedance of  $Z_{in}$  and  $Z_{out}$

$$Z_{in} = \Delta V_B / \Delta I_B = \Delta V_E / (\Delta I_E / \beta) = \beta R_E$$

$$\Delta V_{out} = -R_C \Delta I_C \text{ thus } Z_{out} = Z_C = |\Delta V_C / \Delta I_C| = |\Delta V_{out} / \Delta I_C| = R_C$$

$\therefore Z_{out} \ll Z_{in}$  if  $R_E$  and  $R_C$  are appropriately chosen, thus the common emitter amplifier can be a good device to drive or to be driven

Let's introduce the Ebers-Moll model of Transistor for precise design



(1)  $I_C = I_S \{ \exp(V_{BE}/V_T) - 1 \}$  : Ebers-Moll eqn

It indicates current  $I_C$  is a function of  $V_{BE}(=V_B-V_E)$

where  $V_T = kT/q$  and  $k = \text{Boltzmann const.} = 1.38 \times 10^{-23} \text{ [J/}^\circ\text{K]}$

$T = \text{Kelvin Temp.}$  and  $q = \text{one electron charge} = 1.60 \times 10^{-19} \text{ C}$

Thus  $V_T = 25.3 \text{ mV}$  at  $20^\circ\text{C}$  room temp.

$I_S = \text{Saturation current of TR, or reverse leakage current}$

(2) Intrinsic Emitter Resistance,  $r_e$ , between B and E

As  $V_{BE}/V_T \approx 0.6/0.0253 (\gg 1)$ , E-M eqn can be simplified as

$$I_C = I_S \{ \exp(V_{BE}/V_T) - 1 \} \approx I_S \exp(V_{BE}/V_T)$$

$$\partial I_C / \partial V_{BE} = I_S \exp(V_{BE}/V_T) / V_T = I_C / V_T$$

$$\text{thus } r_e = \partial V_{BE} / \partial I_C = 1 / (\partial I_C / \partial V_{BE}) = V_T / I_C = 25.3 / I_C \text{ in [mV/mA] or } [\Omega]$$

$$1/r_e = r_m = \text{Trans-conductance}$$

(3) Temperature dependence of  $V_{BE}$

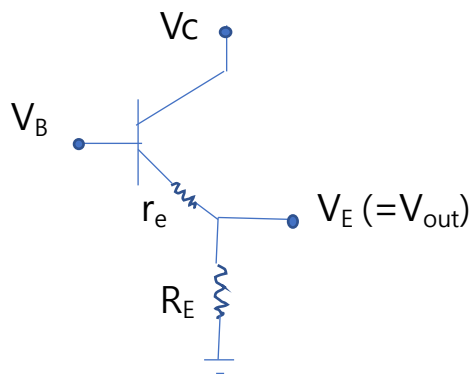
$$\Delta V_{BE}/\Delta T = -2.1 \text{ mV}/^\circ\text{C}$$

(4) Early effect

$V_{BE}$  slightly varies with  $V_{CE}$

Thus  $\Delta V_{BE} = -\alpha \Delta V_{CE}$  and  $\alpha \approx 0.01\%$

### Emitter-Follower (revisited)



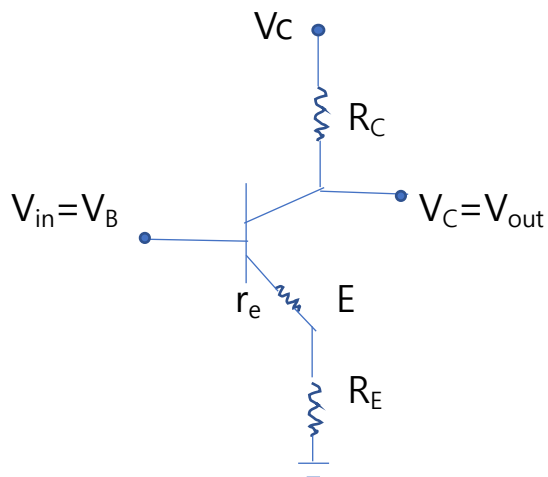
In previous model,  $\Delta V_E = \Delta V_B$  and Gain = 1

$$Z_{in} = \beta R_E \quad \text{and} \quad Z_{out} = R_E$$

In E-M model,  $\Delta V_E = \Delta V_B R_E / (r_e + R_E)$  and Gain =  $R_E / (r_e + R_E) < 1$

$$Z_{in} = \beta(r_e + R_E) \quad \text{and} \quad Z_{out} = R_E$$

## Common Emitter Follower (revisited)



In previous model

$$\Delta V_{out} = -\Delta V_{in} R_C / R_E \text{ and Gain} = -R_C / R_E = -\infty \text{ if } R_E = 0$$

$$Z_{in} = \beta R_E \text{ and } Z_{out} = |-R_C| = R_C$$

In E-M model

$$\Delta V_{out} = -\Delta V_{in} R_C / (r_e + R_E) \text{ and Gain} = -R_C / (r_e + R_E)$$

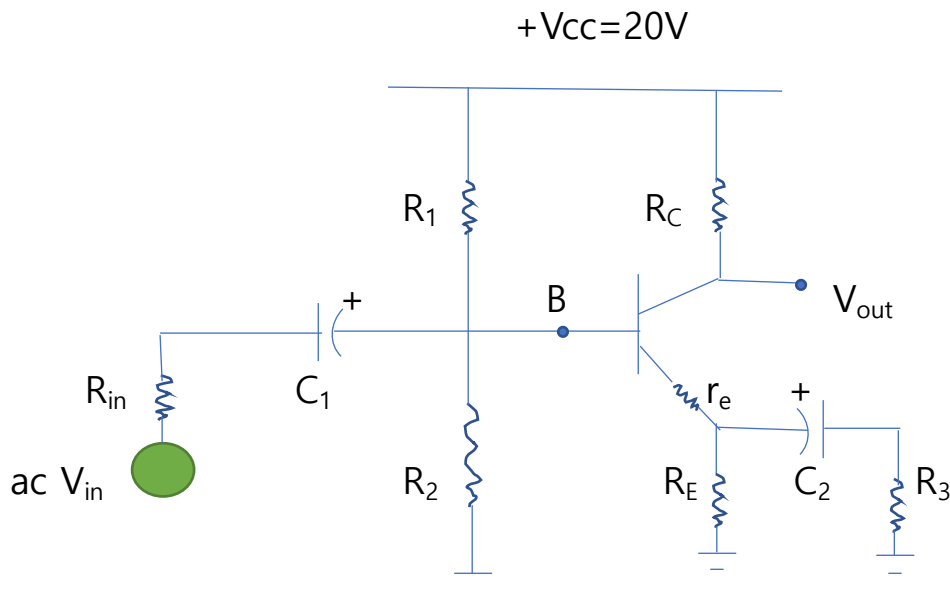
$$Z_{in} = \beta (r_e + R_E) \text{ and } Z_{out} = |-R_C| = R_C$$

Note that the Gain  $= -R_C / (r_e + R_E) = -R_C / r_e$  when  $R_E = 0$ , and it is called 'Grounded Common Emitter Follower'

Ex) Design a AC coupled common emitter follower

$V_{CC}=20V$ ,  $f_{3dB}=100Hz$ , Gain=-100 for ac,  $I_{quiescence}=0.5mA$

(Source: Student Manual for The Art of Electronics, Thomas C. Hayes, Paul Horowitz, Cambridge University Press, 1989)



(1) For DC component

Centering  $V_{out}$  in quiescence, and  $V_{out}=10V=V_{CC}-I_C R_C$  and  $I_C=0.5mA$

Thus  $R_C=(V_{CC}-V_{out})/I_C=(20-10)V/0.5mA=20K\Omega$

Choosing  $R_E$ , so as to give  $V_E$  as 1V (for temperature stability),

$R_E=V_E/I_E=1V/0.5mA=2K\Omega$

$r_e=25.3mV/0.5mA\approx 50\Omega$

$V_B/V_{CC}=R_2/(R_1+R_2)=(1+0.6)/20$  eq(1)

$R_1 \parallel R_2$  drives  $Z_B$ ; and  $Z_B=\beta(r_e+R_E)\approx\beta R_E=200(K\Omega)$

Thus  $R_1 \parallel R_2=R_1 R_2/(R_1+R_2)=Z_B/10=20 (K\Omega)$  eq(2)

From eq(1) (2);  $R_1=220K\Omega$  and  $R_2=20K\Omega$

(2) For AC component

$$\text{Gain} = -R_C / \{r_e + R_E \parallel R_3\} = -100$$

$$\text{Thus } r_e + R_E \parallel R_3 = 200\Omega \text{ and } R_E \parallel R_3 = 150 = (2000)R_3 / (2000 + R_3)$$

$$\therefore R_3 = 162\Omega \approx 150\Omega \text{ from commercial choice}$$

$C_2$  is the DC blocking capacitor, and its location does not matter in general (in frequency domain), although it is better to locate close to the receiver or driver (in time domain), where the AC current flows back and forth.

$$\text{The relevant } R_{eq} \text{ for } C_2 \text{ is } R_3 + r_e \parallel R_E \approx R_3 + r_e = 150 + 50 = 200(\Omega)$$

This is also a cascaded HPF, thus excessive attenuation can be avoided by choosing  $\omega_{2_{3dB}} = \omega_{3dB} / 2 = (2\pi)(100) / 2 = 314 \text{ (rad/s)} = 1 / (R_3 + r_e) C_2$

$$\text{Thus } C_2 = 1 / \{(314)(200)\} = 16\mu\text{F}$$

For  $C_1$  of the biasing circuit; the relevant  $R_{eq}$  for back and forth,  $R_{eq} = (R_1 \parallel R_2) \parallel \beta(r_e + R_E \parallel R_3) + R_{in}(\text{if any})$ , and  $R_1 \parallel R_2 = 20K\Omega$ ,

$$r_e + R_E \parallel R_3 \approx r_e + R_3 = 200\Omega; \text{ Thus } R_{eq} = 20K \parallel 20K = 10K \text{ and}$$

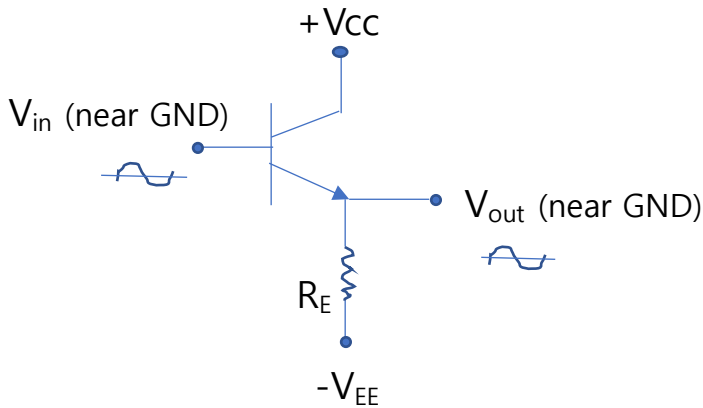
$$\omega_{1_{3dB}} = \omega_{3dB} / 2 = 314(\text{rad/s}) = 1 / R_{eq} C_1, \text{ and thus } C_1 \approx 0.33\mu\text{F}$$

HW8) Design a AC coupled common emitter follower

$$V_{CC} = 24V, f_{3dB} = 100\text{Hz}, \text{ Gain} = -100 \text{ for ac, } I_{quiescence} = 0.5\text{mA.}$$

(Hint: Use an alternative method for cascaded DC blocking capacitors)

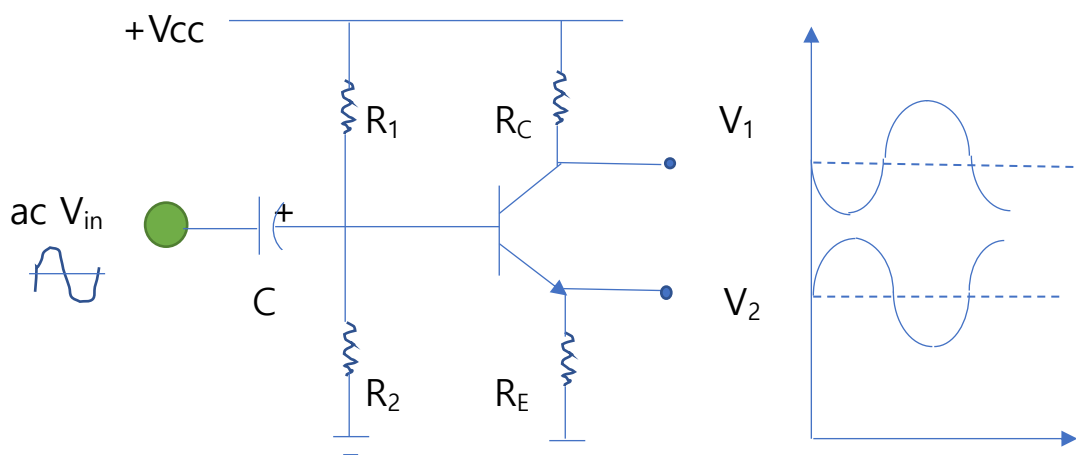
7. Emitter Follower with split supply, or "DC Coupled Emitter Follower" with split supply



This TR circuit can accept the negative swing of the  $V_{in}$ , thus can be used for current amplification with voltage replica

8. Unity-Gain Phase Splitter

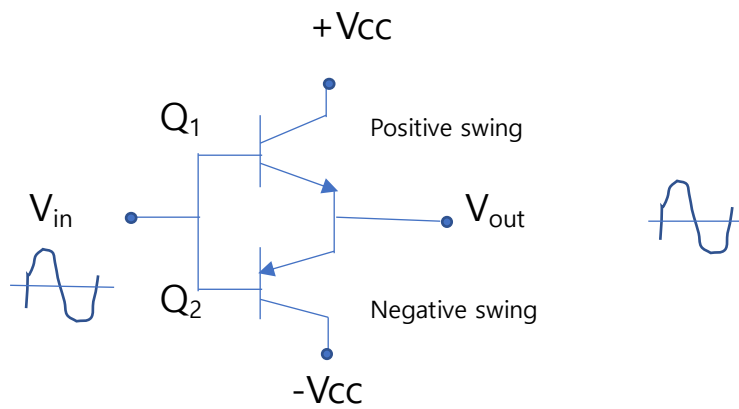
: For given input signal,  $V_{in}$  ; two output signals,  $V_1$ ,  $V_2$  of  $180^\circ$  phase difference



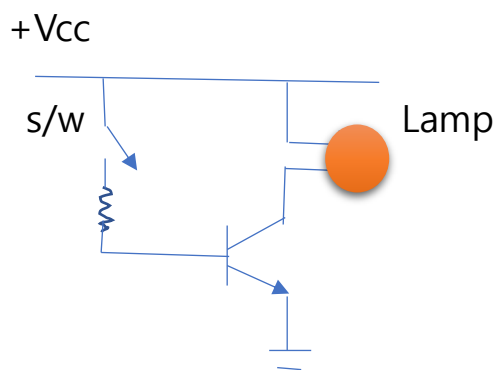
Ex) Design a unity-gain phase splitter such as;

$V_{cc}=20V$ , and  $I_{quiescence}=1mA$ ,  $V_1=15V$ ,  $V_2=5V$

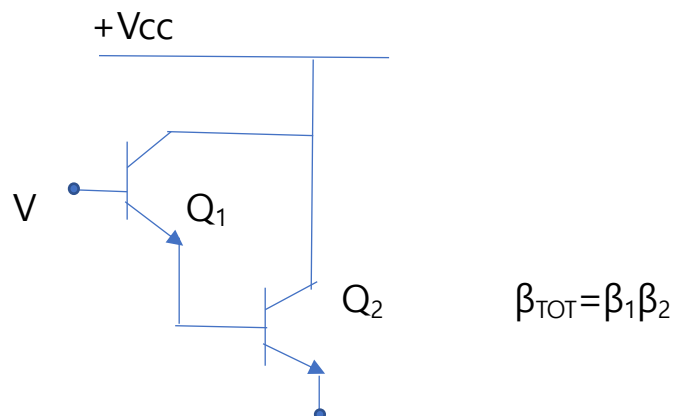
## 9. Push-Pull Amplifier



## 10. Transistor Switch



## 11. Darlington Connection



$\therefore$  Very High Gain of current amplification