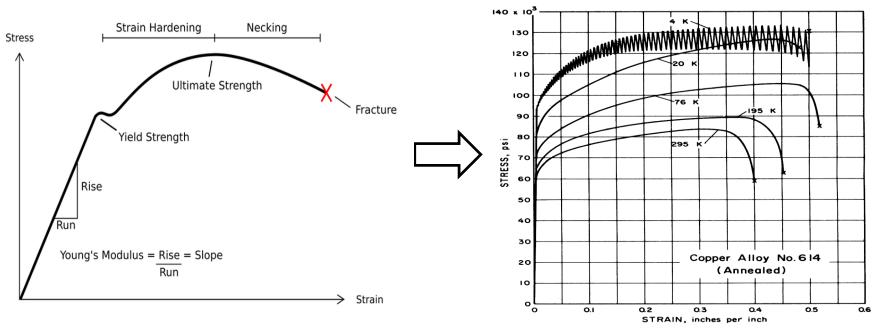
# **Cryogenic Engineering**

# Chapter 2 LOW TEMPERATURE PROPERTIES OF ENGINEEING MATERIALS

KIM, Min Soo



## 2.1 Introduction



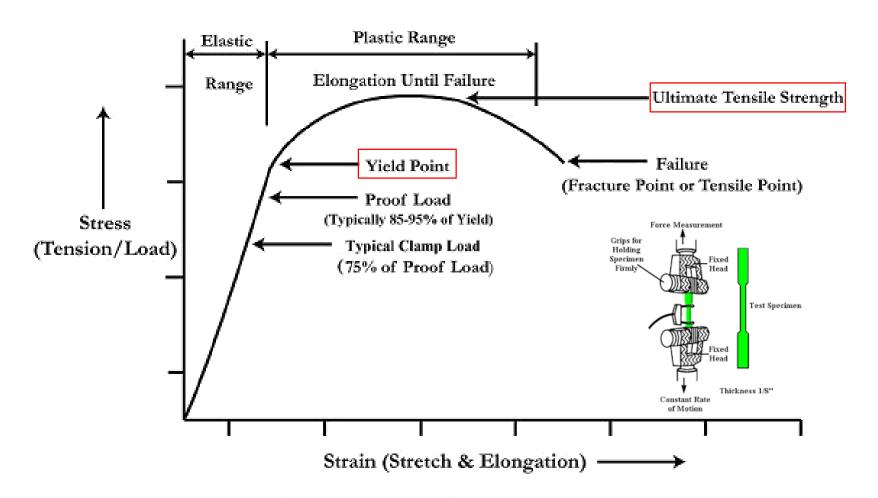
Stress-strain curve at room temperature

Stress-strain curve for cooper alloy at low temperature

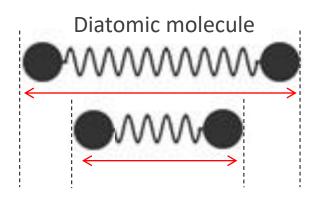
Extrapolation for material properties at very low temperature is not exact !!

- Vanishing of specific heat
- Superconductivity phenomenon
- Ductile-brittle transition in carbon steel

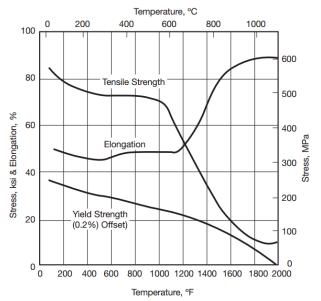
# 2.2 Ultimate and Yield Strength



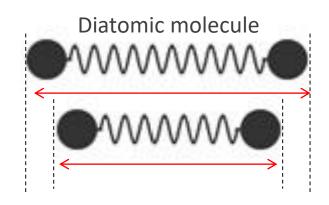
# 2.2 Ultimate and Yield Strength



Vigorous vibration at room temperature



Nickel-Iron-Chromium Alloy



Torpid vibration at low temperature

As temperature is lowered, atoms of the material vibrate less rigorously, a larger applied stress is required to tear dislocations from their atmosphere of alloying atoms.

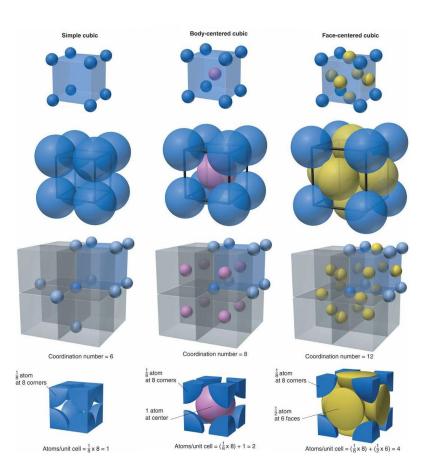
# 2.3 Impact Strength



The Charpy and the Izod impact tests

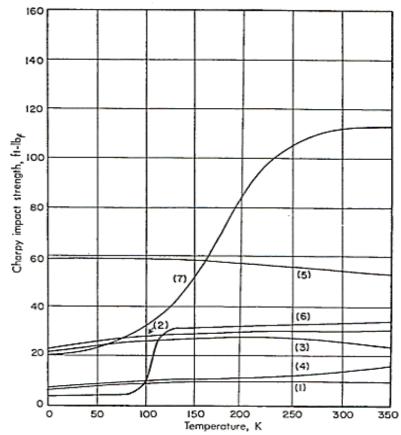
MaterialsScience2000 - Charpy Impact Test https://www.youtube.com/watch?v=tpGhqQvftAo

## 2.3.1 Lattice Structure



<Lattice structures>

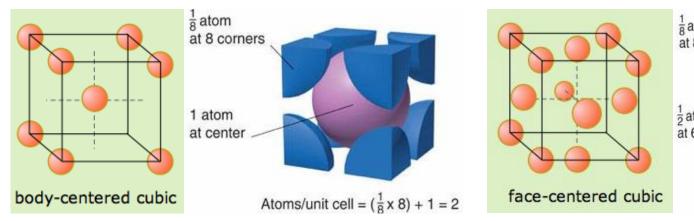
- (1) 2024-T4 aluminum; (2) beryllium copper; (3) K Monel; (4) titanium;
- (5) 304 stainless steel; (6) C1020 carbon steel; (7) 9 percent Ni steel (Durham et al. 1962)

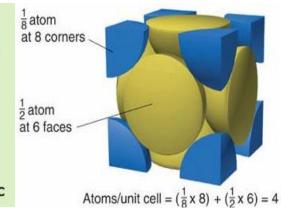


<Charpy impact strength at low temperature>
 \*Ductile-brittle transition

## 2.3.1 Lattice Structure

#### BCC (Body-Centered Cubic) vs FCC (Face-Centered Cubic)



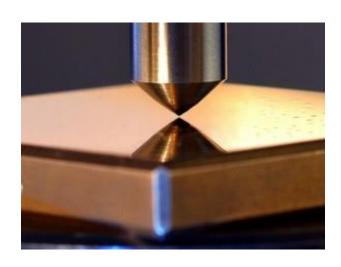


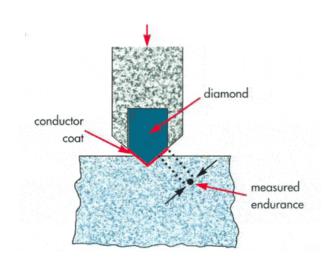
Copper-Nickel alloy
Aluminum alloy
Stainless steel
Zirconium
Titanium

Iron
Carbon alloy
Molybdenum
Zinc
Most plastics
Brittle

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**Hardness** is a measure of how resistant solid matter is to various kinds of permanent shape change when a compressive force is applied. Some materials, such as metal, are harder than others. Macroscopic hardness is generally characterized by strong intermolecular bonds, but the behavior of solid materials under force is complex; therefore, there are different measurements of hardness: **scratch hardness, indentation hardness, and rebound hardness.** 



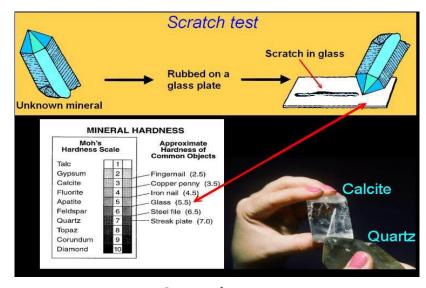


#### Scratch hardness

Scratch hardness tests are used to determine the hardness of a material to scratches and abrasion.



Pencil scratch hardness tester



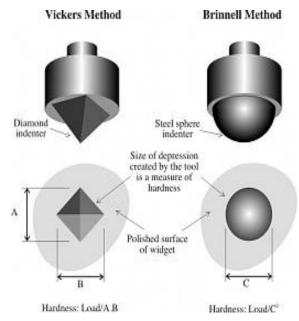
Scratch test

#### Indentation hardness

**Indentation hardness** tests are used in mechanical engineering to determine the hardness of a material to deformation.



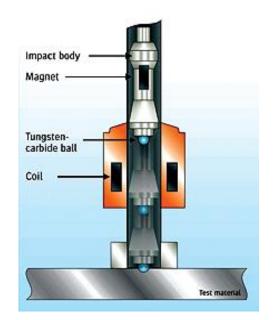
Indentation hardness tester



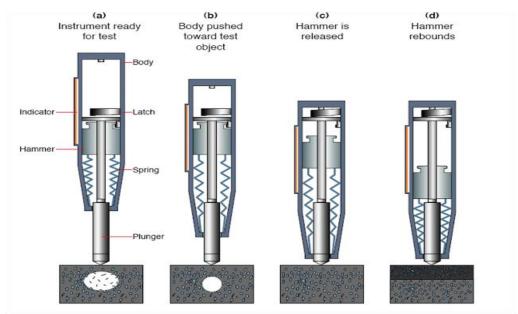
Two types of indentation

#### Rebound hardness

The **Leeb rebound hardness** test is one of the four most used methods for testing metal hardness.



Portable rebound hardness testing machine.



Procedure of rebound hardness test

In materials science, **ductility** is a solid material's ability to deform under tensile stress; this is often characterized by the material's ability to be stretched into a wire. **Malleability**, a similar property, is a material's ability to deform under compressive stress; this is often characterized by the material's ability to form a thin sheet by hammering or rolling.



Ductility test and measurement



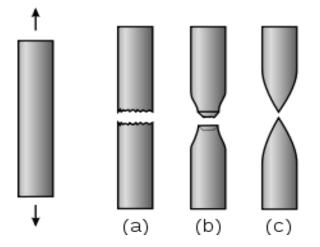
Tensile test of an AlMgSi alloy. The local necking and the cup and cone fracture surfaces are typical for ductile metals.



This tensile test of a nodular cast iron demonstrates low ductility.



Gold leaf can be produced owing to gold's malleability.

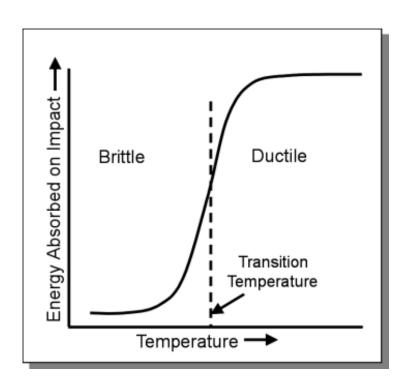


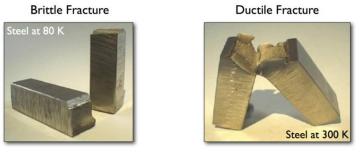
Schematic appearance of round metal bars after tensile testing.

- (a) Brittle fracture
- (b) Ductile fracture
- (c) Completely ductile fracture

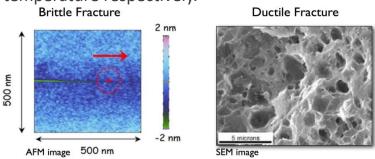
#### Ductile—brittle transition temperature

At low temperatures some metals that would be ductile at room temperature become brittle. This is known as a ductile to brittle transition.



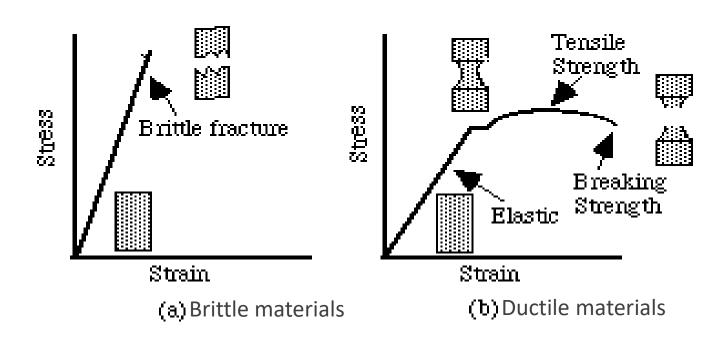


Brittle and ductile failure of steel, at low and high temperature respectively.



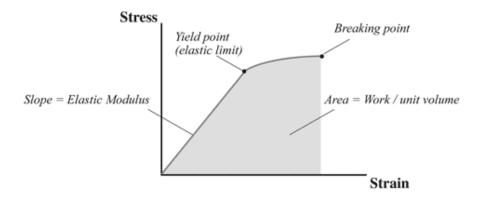
Brittle and ductile failure mechanisms, for silica and aluminium respectively. Image credits

Stress-strain diagrams for typical brittle and ductile materials



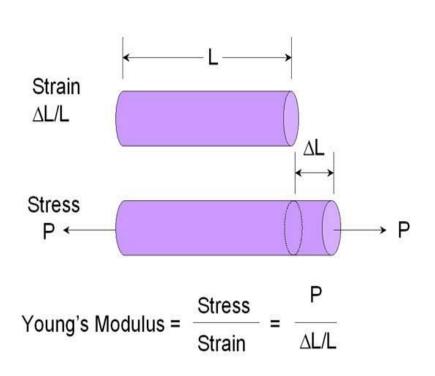
"Young's modulus" or modulus of elasticity, is a number that measures an object or substance's resistance to being deformed elastically (i.e., non-permanently) when a force is applied to it.

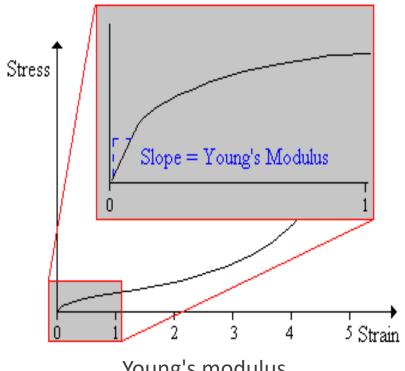
elastic modulus = 
$$\frac{\text{stress}}{\text{strain}}$$



Curve of Stress vs. Strain which describes the mechanical deformation of a solid body.

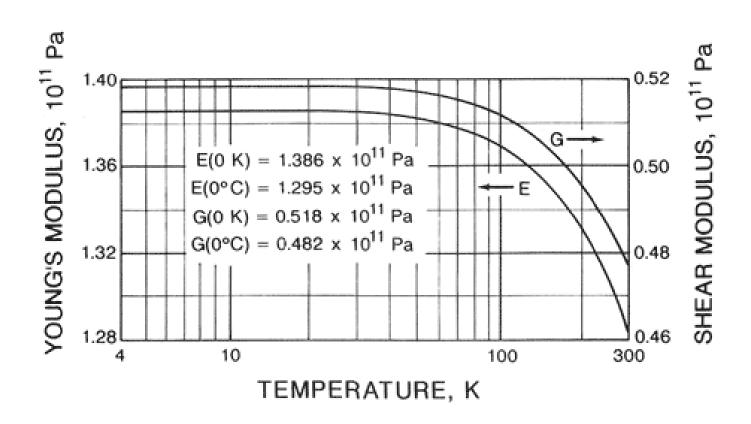
#### Young's modulus, E



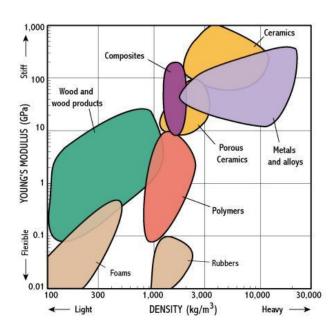


Young's modulus (slope of a stress-strain curve)

#### Young's modulus, E



#### Young's modulus, E



Young's Modulus - Density Materials Selection Chart, showing the classes of materials

Material	Youngs Modulus /GPa
Mild Steel	210
Copper	120
Bone	18
Plastic	2
Rubber	0.02

#### Shear modulus, G

In materials science, shear modulus or modulus of rigidity, denoted by G, or sometimes S or  $\mu$ , is defined as the ratio of shear stress to the shear strain.

$$G \stackrel{\text{def}}{=} \frac{\tau_{xy}}{\gamma_{xy}} = \frac{F/A}{\Delta x/l} = \frac{Fl}{A\Delta x}$$

where

$$au_{xy} = F/A$$
 = shear stress;

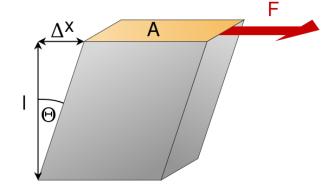
 $oldsymbol{F}$  is the force which acts

A is the area on which the force acts

in engineering,  $\gamma_{xy}=\Delta x/l= an heta$  = shear strain. Elsewhere,  $\gamma_{xy}= heta$ 

 $\Delta x$  is the transverse displacement

 $\emph{l}$  is the initial length



## ■ Shear modulus, G



Shear frame for evaluation of the in-plane shear modulus and strength of FRP

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#### ■ Bulk modulus, B

The bulk modulus (K or B) of a substance measures the substance's resistance to uniform compression. It is defined as the ratio of the infinitesimal pressure increase to the resulting relative decrease of the volume.

The bulk modulus K>0 can be formally defined by the equation

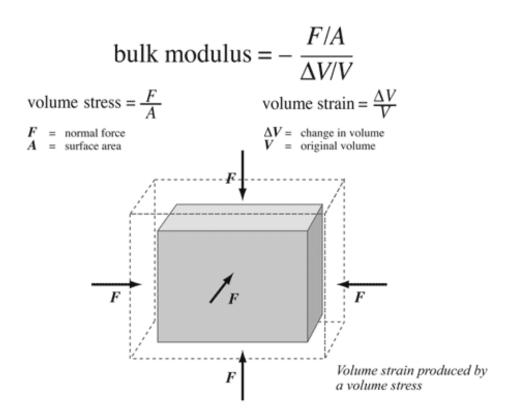
$$K = -V \frac{\mathrm{d}P}{\mathrm{d}V}$$

where P is pressure, V is volume, and dP/dV denotes the derivative of pressure with respect to volume. Equivalently

$$K = \rho \frac{\mathrm{d}P}{\mathrm{d}\rho}$$

where  $\rho$  is density and dP/d $\rho$  denotes the derivative of pressure with respect to density. The inverse of the bulk modulus gives a substance's compressibility.

#### ■ Bulk modulus, B

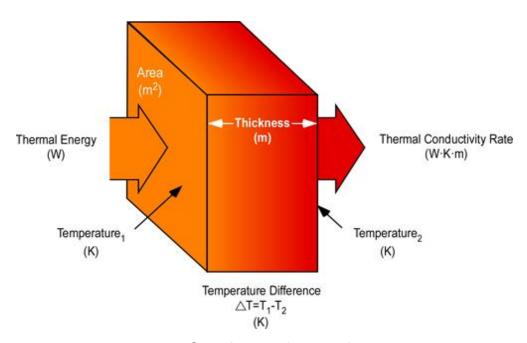


#### Relations between elastic modulus

For homogeneous isotropic materials simple relations exist between elastic constants (Young's modulus E, shear modulus G, bulk modulus K, and Poisson's ratio v) that allow calculating them all as long as two are known

$$E = 2G(1 + v) = 3K(1 - 2v)$$

 $\mathbf{k}_t$ : Heat-transfer rate per unit area divided by the temperature gradient



<Heat transfer through conduction>

$$q = -k_t A \frac{dT}{dx}$$
Fourier's law>

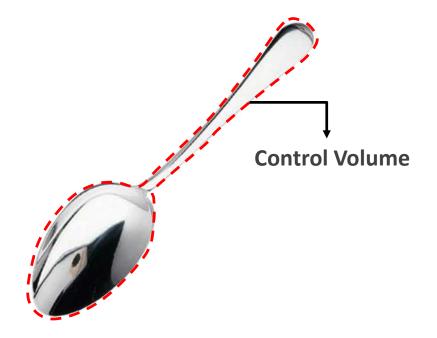
$$k_t = \left[\frac{W}{m \cdot K}\right]$$



<A stainless spoon in hot water>

$$\delta Q = du + \delta W$$

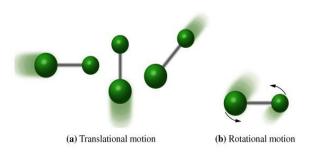
<1st law of thermodynamics>

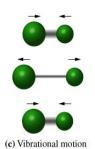


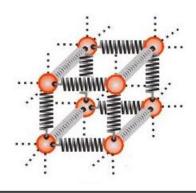
#### ■ Internal energy ( *u* )

$$\delta Q = du + \delta W$$

: 1<sup>st</sup> law of thermodynamics





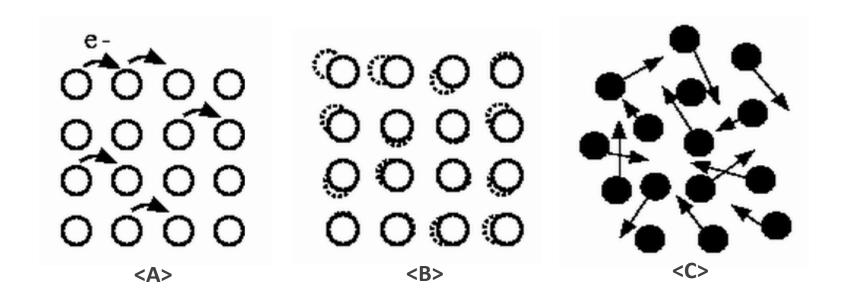


Translational energy 
$$\frac{1}{2}m(v_x^2 + v_y^2 + v_z^2)$$
 Rotational energy 
$$\frac{1}{2}I(w_x^2 + w_y^2 + w_z^2)$$
 Vibrational energy 
$$\frac{1}{2}(m\dot{x}^2 + kx^2)$$

<Internal energy for dielectric molecule>

$$\frac{1}{2}(m(\dot{x}^2+\dot{y}^2+\dot{z}^2)+k(x^2+y^2+z^2))$$
 < Internal energy for solid>

■ Three different mechanisms for conduction in materials

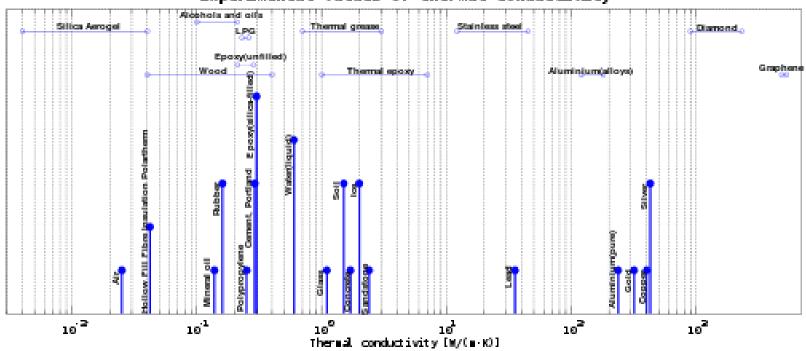


<A> : Electron motion (metallic conductor)

<B> : Lattice vibration-energy transport (phonon motion; only have energy)

<C>: Molecular motion (gases)

#### Experimental values of thermal conductivity



Experimental values of thermal conductivity

#### Gases thermal conductivity

$$k_t = \frac{1}{8}(9\gamma - 5)\rho c_v \overline{v} \lambda \text{ (Eucken, 1913)}$$

*γ*: specific heat ratio

 $\rho$ : density of material

 $c_v$ : specific heat at constant volume

 $\bar{v}$ : average particle velocity

 $\lambda$ : mean free path of particles

#### Gases thermal conductivity

$$\overline{v} = \left(\frac{8g_cRT}{\pi}\right)^2 \text{ (Present, 1958)}$$

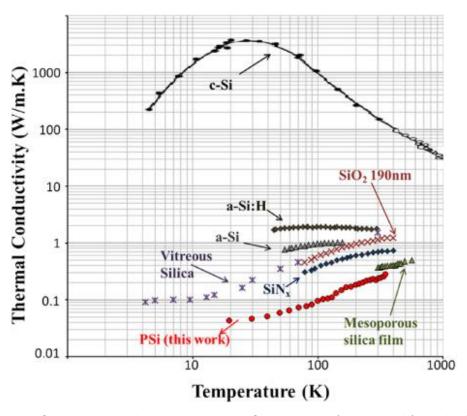
 $g_c$ : 1 kg·m/N·s<sup>2</sup>

R:  $R_u/M$ ,  $R_u = 8.31434 \frac{J}{mol} \cdot K$ 

M: molecular weight of the gas

T: absolute temperature of the gas

#### Gases thermal conductivity



Comparison of the thermal conductivity of porous Si (this work) with that of bulk crystalline silicon (Glassbrenner and Slack 1964), a-Si (Lee et al 1991), a-Si: H (Cahill et al 1989) and different other C-MOS compatible films (mesoporous silica (Shin et al 2008), vitreous silica (Smith et al 1978) and silicon nitride (Lee and Cahill 1997)).

### Solids thermal conductivity

$$k_t = \frac{1}{3}\rho c_v \overline{v}\lambda$$

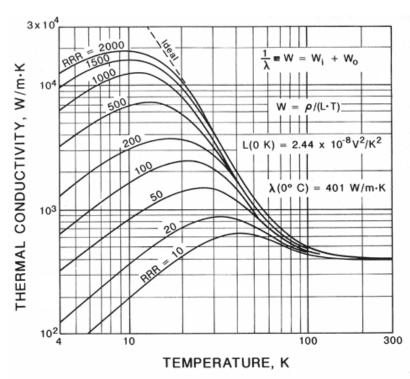
ρ: density of material

c<sub>v</sub>: specific heat at constant volume

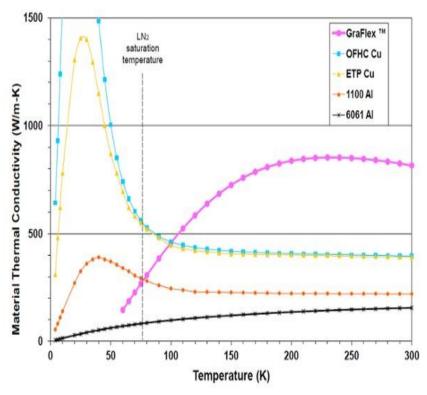
 $\overline{v}$ : average particle velocity

 $\lambda$ : mean free path of particles

#### Solids thermal conductivity



Thermal conductivity of copper alloys

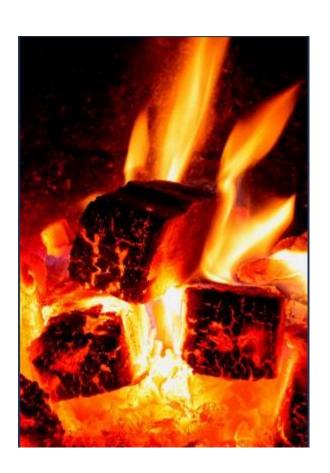


Graphite Thermal Conductivity vs Al and Cu Straps

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# 2.7 Specific Heats of Solids

#### Specific heat



The energy required to change the temperature of the substance by one degree!

- $C_p$  When constant pressure
- C<sub>n</sub> When constant volume

#### **Debye Specific Heat Function**

#### Debye model

For solids, "Debye model" represents how the specific heats change under the temperature variation

$$C_{v} = \frac{9RT^{3}}{\theta_{D}^{3}} \int_{0}^{\theta_{D}/T} \frac{x^{4}e^{x}dx}{(e^{x} - 1)^{2}} = 3R\left(\frac{T}{\theta_{D}}\right)^{3} D(\frac{T}{\theta_{D}})$$

 $\theta_D$  : Debye Characteristic temperature

 $D(T/\theta_D)$ : Debye function

where, 
$$\theta_D = \frac{hv_a}{k} \left(\frac{3N}{4\pi V}\right)^{1/3}$$

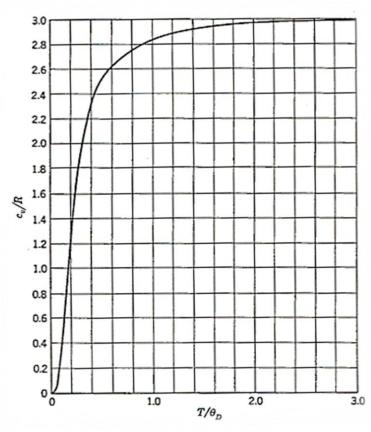
h: Planck's constant

v<sub>a</sub>: Speed of sound in the solid

k: Boltzmann's constant

N/V: Number of atoms per unit volume for the solid

#### **Debye Specific Heat Function**



• 
$$\frac{\mathrm{T}}{\mathrm{\theta_D}} > 3$$
 ,  $\frac{C_v}{R} \approx 3$  (Dulong-Petit value)

• 
$$\frac{T}{\theta_{\rm D}} < \frac{1}{12}$$
 ,  $\frac{C_v}{R} \propto T^3$ 

#### **Specific Heat Affected by Electrons**

#### According to quantum theory,

$$C_{v,e} = \frac{4\pi^4 a m_e M R^2 T}{h^2 N_0 (3\pi^2 N/V)^{2/3}} = \gamma_e T$$

a = Number of free electrons per atom

 $m_e = Electron\ effective\ mass$ 

M = atomic weight of material

R = Specific gas constant for material

T = Absolute temperature

h = Planck's constant

 $N_0 = Avogadro's number$ 

 $N/V = Number\ of\ free\ electrons\ per\ unit\ volume$ 

 $\gamma_e = Electronic \ specific - heat \ coefficient$ 

#### **Specific Heat Affected by Electrons**

Table. Electronic specific heat coefficients

	Ϋ́e		
Material	mJ/kg-K²	Btu/lb <sub>m</sub> -°R <sup>2</sup>	
Aluminum	50.4	$6.69 \times 10^{-6}$	
Beryllium	24.6	$3.27 \times 10^{-6}$	
Chromium	29.8	$3.95 \times 10^{-6}$	
Copper	11.0	$1.46 \times 10^{-6}$	
Gold	3.55	$0.471 \times 10^{-6}$	
Iron	89.9	$11.9 \times 10^{-6}$	
Nickel	124.0	$16.5 \times 10^{-6}$	
Niobium	94.9	$12.6 \times 10^{-6}$	
Platinum	34.0	$4.51 \times 10^{-6}$	
Silver	5.65	$0.749 \times 10^{-6}$	
Tantalum	32.3	$4.29 \times 10^{-6}$	
Titanium	74.1	$9.83 \times 10^{-6}$	
Zirconium	33.2	$4.41 \times 10^{-6}$	

By permission from Gopal (1966).

Ordinary temperature  $\rightarrow \gamma_e$  is small (ignorable)

Low Temperature  $\rightarrow \gamma_e$  becomes important!

# 2.8 Specific Heat of Liquids and Gases

Specific heat of a material (equipartition theorem)

$$C_{v} = \frac{1}{2}Rf$$

(*f* : number of degrees of freedom)

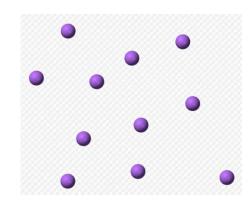
- Monatomic gas
- Degree of freedom

- Translational motion:

- Rotational motion:

$$\therefore C_{v} = \frac{3}{2}R$$

- Vibrational motion:



#### 2.8 Specific Heat of Liquids and Gases

#### ② Diatomic gas

• Degree of freedom

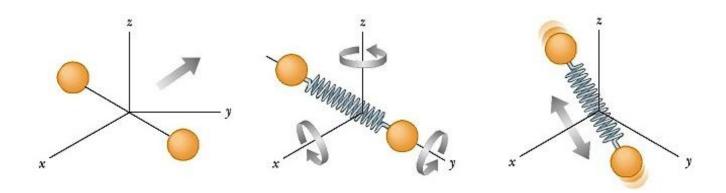
- Translational motion: 3

- Rotational motion : 2

- Vibrational motion : 2

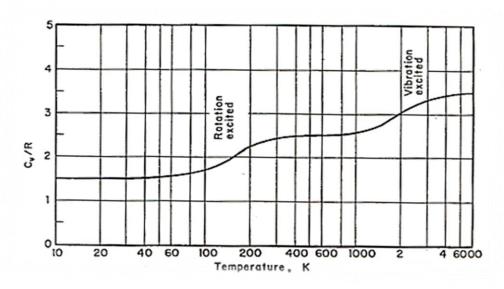
$$\therefore C_{\rm v} = \frac{7}{2} R$$

(according to the classical theory)



### 2.8 Specific Heat of Liquids and Gases

#### In the actual case, rotational, vibrational modes are quantized!



<Variation of the specific heat  $C_v$  for hydrogen gas>

0~10K Translational motion only  $(\frac{C_v}{R} = \frac{3}{2})$ 

10~1000K Translational+Rotational motion  $(\frac{C_v}{R} = \frac{5}{2})$ 

Translational+Rotational+Vibrational motion  $(\frac{C_v}{R} = \frac{7}{2})$ 

1000K~

#### Coefficient of thermal expansion

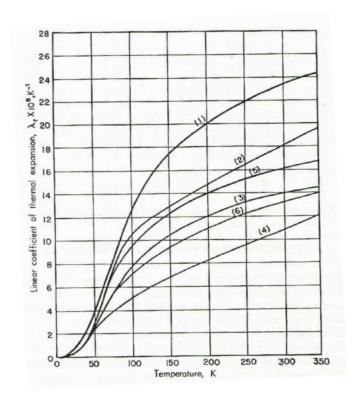
- For isotropic materials

$$\beta = 3\lambda_{t}$$

$$\beta = \frac{1}{v} \left( \frac{\partial v}{\partial T} \right)_{p}$$
 (in the vicinity of the critical point)

 $\beta$  is fractional change in volume per unit change in temperature is the linear coefficient of thermal expansion

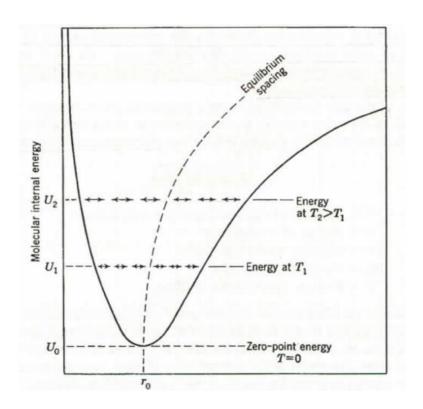
■ The temperature variation of the linear coefficient for thermal expansion for several materials



Linear coefficient of thermal expansion for several materials at low temperature:

- (1) 2024-T4 aluminum (2) beryllium copper (3) K Monel
- (2) (4) titanium (5) 304 stainless steel (6) C1020 carbon steel

■ The intermolecular potential-energy curve



Variation of the intermolecular potential energy for a pair of molecules

#### The intermolecular forces

- The intermolecular potential-energy curve is not symmetrical. Therefore, as the molecule acquires more energy, its mean position relative to its neighbors becomes larger, that is, the material expands.
- The coefficient of thermal expansion increases as temperature is increased.

#### Coefficient of thermal expansion

- For crystalline solids, the Gruneisen relation

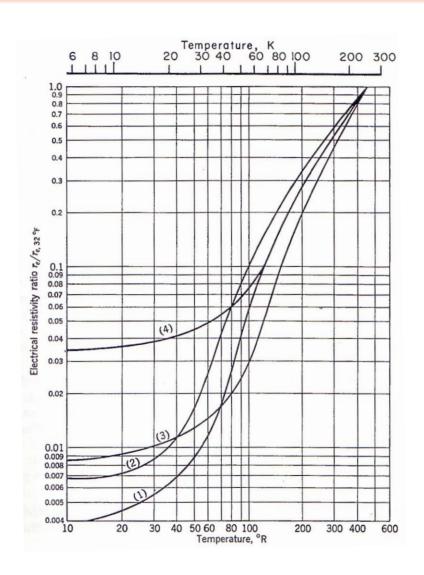
$$\beta = \frac{\gamma_G c_v \rho}{B}$$

 $\rho$  is the density of the material B is the bulk modulus  $\gamma_G$  is the Gruneisen constant

Material	Υg
Aluminum	2.17
Copper	1.96
Gold	2.40
Iron	1.60
Lead	2.73
Nickel	1.88
Platinum	2.54
Silver	2.40
Tantalum	1.75
Tungsten	1.62

Values of the Gruneisen constant for selected solids

#### 2.10 Electrical Conductivity



$$k_{e} = \frac{I/Area}{dV/dx} = \frac{I/A}{V/I} = \frac{L}{RA}$$

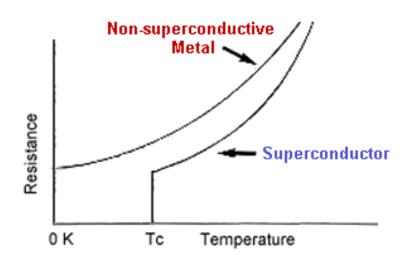
Electrical resistivity,  $\rho=\frac{1}{k_e}$ 

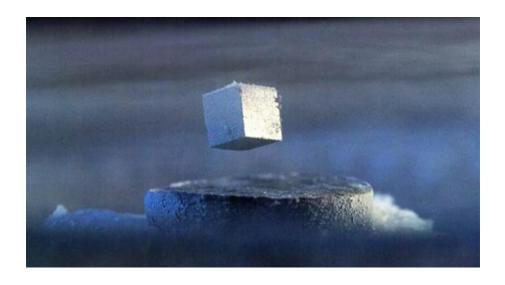
As T  $\downarrow$ , Vibrational E  $\downarrow$ 

$$q = kA \frac{dT}{dx} \qquad I = k_e A \frac{dV}{dx}$$

#### 2.11 Superconductivity

- Only at very low T
- Disappearance of all electric resistance
- Appearance of perfect diamagnetism





Paramagnetism ~ magnet diamagnetism ~ repel ferromagnetism ~ stick

#### 2.11 Superconductivity

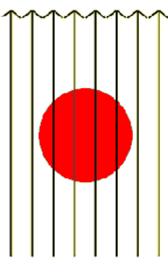
 $T:T < T_o$ 

 $\mathcal{H}: \mathcal{H}_{o}(Critical field)$ 

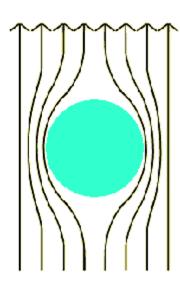
L magnetic field strength required to destroy superconductivity

I : I<sub>c</sub>(Critical current)

Lupper limit to the electric current without destroying superconductivity







Superconducting

# 2.11 Superconductivity

#### Applications



MRI (Magnetic Resonance Imaging)
High magnetic field stability

#### $LN_2(liquid N_2)$

- → Clear, Colorless
- → N.B.P. (Normal Boiling Point) : 77K
- → Produced by the distiliation of air
- → Small heat of vaporization



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Usage of LN<sub>2</sub>(liquid N<sub>2</sub>)

Quick freezing of food, Drying etc.



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#### $LO_2(liquid O_2)$

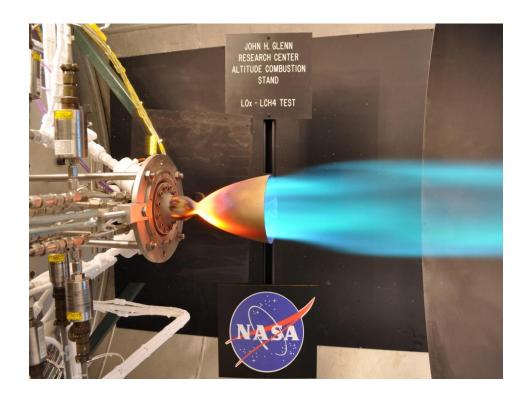
- → Slightly magnetic (paramagnetic)
- $\rightarrow$  N.B.P. (Normal Boiling Point) : 90K
- → Produced by the distillation of air
- → Slightly magnetic (paramagnetic)



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Usage of  $LO_2(liquid O_2)$ 

Fuel of rocket, welding etc.



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N.B.P. = 20.3K

Types of hydrogen atom

$$H - H$$
  $H - D$   
 $D - D$   $T - T$ 

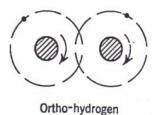
	H hydrogen	D deuterium	T tritium
proton	1	1	1
neutron	0	1	2
electron	1	1	1

N.B.P. = 20.3K

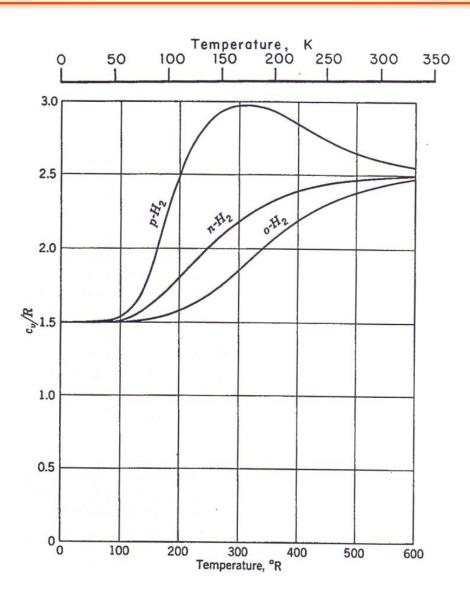
#### Types of hydrogen molecules

 $ortho-H_2$ 

 $para - H_2$ (Spins aligned, high energy) (Opposite spins, low energy)

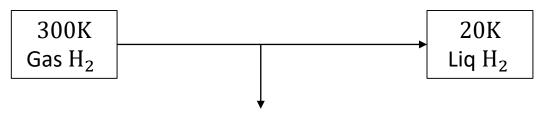




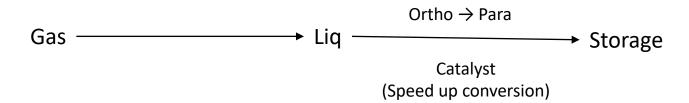


ortho — 
$$H_2 \rightarrow$$
 para —  $H_2 + \Delta\alpha$  (heat of conversion)  
70.3kJ/kg  
Latent heat 44.3kJ/kg

At high temperature is a mixture of 75%  $ortho-H_2$  and 25%  $para-H_2$  As temperature is cooled to the normal boiling point of hydrogen, the  $ortho-H_2$  concentration decreases from 75 to~0.2%

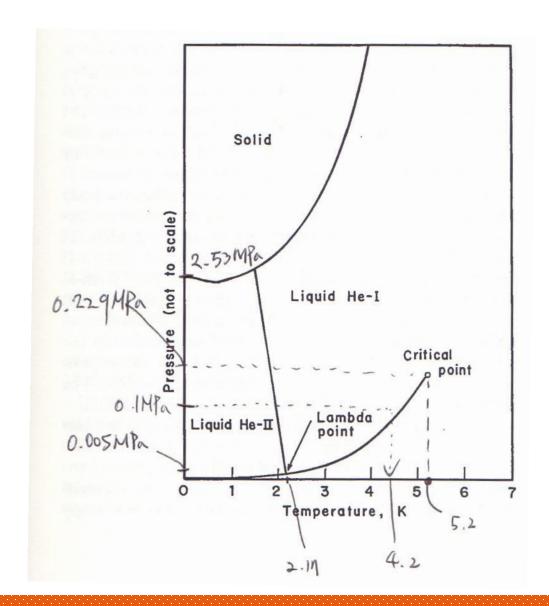


Sensible latent + Heat of conversion



#### 2.13 He<sup>4</sup>

- Difficult to liquefy
- N.B.P. = 4.2K
- No triple point



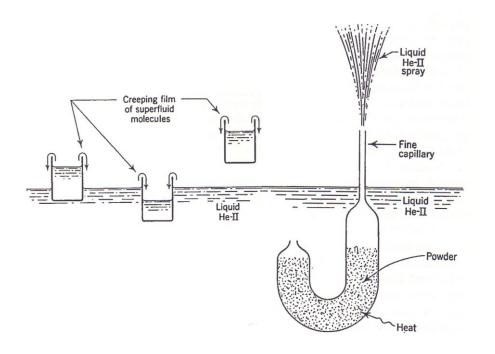
#### 2.13 He<sup>4</sup>

He - I : Normal fluid

He - II : Super fluid

Lact as if it has zero viscosity

(viscosity, 
$$\tau = \mu \frac{dV}{dr}$$
)



Behavior of superfluid

### 2.13 He<sup>4</sup>

#### ■ Video: Superfluid helium



#### 2.14 He<sup>3</sup>

- N.B.P. = 3.19K
- Super fluid transition = 3.5mK

