Radiation Source Technology

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Charged particle properties

Particle	Charge (coulomb)	Mass (kg)	Rest Energy (MeV)	A	Z	Z*
Electron $(\beta \text{ particle})$	-1.60×10^{-19}	9.11×10^{-31}	0.511			
Proton	$+1.60 \times 10^{-19}$	1.67×10^{-27}	938	1	1	1
Deuteron	$+1.60 \times 10^{-19}$	3.34×10^{-27}	1875	2	1	1
Triton	$+1.60 \times 10^{-19}$	5.00×10^{-27}	2809	3	1	1
He ⁺	$+1.60 \times 10^{-19}$	$6.64 imes 10^{-27}$	3728	4	2	1
He ⁺⁺ (α particle)	$+3.20 \times 10^{-19}$	6.64×10^{-27}	3728	4	2	2
C *	$+1.6 \times 10^{-19}$	$1.99 imes 10^{-26}$	$1.12 imes 10^4$	12	6	1
\mathbf{U}^+	$+1.6 \times 10^{-19}$	3.95×10^{-25}	2.22×10^5	238	92	1

1 eV = 1.6x10⁻¹⁹ J = 1,240 nm = 241.8 THz



Particle momentum and energy

• The special theory of relativity states that the inertia of a particle observed in a frame of reference depends on the magnitude of its speed in that frame.

$$\gamma = \frac{1}{\sqrt{1 - (\nu/c)^2}} = \frac{1}{\sqrt{1 - \beta^2}}$$

Lorentz factor

- The inertia of a particle is proportional to γ . The apparent mass is $m = \gamma m_0$.
- The particle momentum, a vector quantity, equals $\boldsymbol{p} = \gamma m_0 \boldsymbol{v}$.
- The equation of motion:

$$\frac{d\boldsymbol{p}}{dt} = \frac{d(\gamma m_0 \boldsymbol{v})}{dt} = \boldsymbol{F}$$

• The kinetic energy equals the total energy minus the rest energy:

$$E = \gamma m_0 c^2 \qquad \qquad T = (\gamma - 1) m_0 c^2$$

• Newtonian dynamics describes the motion of low-energy particles when $T \ll m_0 c^2$. $T = \frac{1}{2}m_0 v^2$ $(1+x)^{-1/2} \approx 1 - \frac{1}{2}x + \cdots$



β for particles as a function of kinetic energy

 $\beta = \frac{v}{c}$





Maxwell's equations

$$\nabla \cdot E = \rho / \epsilon_0$$
$$\nabla \cdot B = 0$$
$$\nabla \times E = -\frac{\partial B}{\partial t}$$
$$\nabla \times B = \mu_0 \epsilon_0 \frac{\partial E}{\partial t} + \mu_0 J$$

- Gauss's law
- Gauss's law for magnetism
- Faraday's law of induction
- Ampere's law with Maxwell's addition

$$\rho = e(Zn_i - n_e)$$
$$\boldsymbol{J} = e(Zn_i\boldsymbol{u}_i - n_e\boldsymbol{u}_e)$$

$$\frac{\partial \rho}{\partial t} + \boldsymbol{\nabla} \cdot \boldsymbol{J} = 0$$

• Charge continuity equation





Motions in uniform electric field

• Equation of motion of a charged particle in fields

$$m\frac{d\boldsymbol{v}}{dt} = q[\boldsymbol{E}(\boldsymbol{r},t) + \boldsymbol{v} \times \boldsymbol{B}(\boldsymbol{r},t)],$$

- Motion in constant electric field
 - ✓ For a constant electric field $E = E_0$ with B = 0,

$$\boldsymbol{r}(t) = \boldsymbol{r_0} + \boldsymbol{v_0}t + \frac{q\boldsymbol{E_0}}{2m}t^2$$

$$\frac{d\boldsymbol{r}}{dt} = \boldsymbol{v}(t)$$



- ✓ Electrons are easily accelerated by electric field due to their smaller mass than ions.
- ✓ Electrons (lons) move against (along) the electric field direction.
- ✓ The charged particles get kinetic energies.



Motions in uniform magnetic field

• Motion in constant magnetic field

$$m\frac{d\boldsymbol{v}}{dt} = q\boldsymbol{v} \times \boldsymbol{B}$$

• For a constant magnetic field $\boldsymbol{B} = B_0 \boldsymbol{z}$ with $\boldsymbol{E} = 0$,

$$m\frac{dv_x}{dt} = qB_0v_y$$
$$m\frac{dv_y}{dt} = -qB_0v_x$$
$$m\frac{dv_z}{dt} = 0$$



• Cyclotron (gyration) frequency

$$\frac{d^2 v_x}{dt^2} = -\omega_c^2 v_x \qquad \qquad \omega_c = \frac{|q|B_0}{m}$$

В



В

Motions in uniform magnetic field

• Particle velocity

$$v_x = v_{\perp} \cos(\omega_c t + \phi_0)$$

$$v_y = -v_{\perp} \sin(\omega_c t + \phi_0)$$

$$v_z = v_{z0}$$

• Particle position

$$x = r_c \sin(\omega_c t + \phi_0) + (x_0 - r_c \sin \phi_0)$$

$$y = r_c \cos(\omega_c t + \phi_0) + (y_0 - r_c \cos \phi_0)$$

$$z = z_0 + v_{z0}t$$

• Guiding center

 $(x_0, y_0, z_0 + v_{z0}t)$

• Larmor (gyration) radius

$$r_c = \frac{v_\perp}{\omega_c} = \frac{mv_\perp}{|q|B_0}$$





Gyro-frequency and radius

- The direction of gyration is always such that the magnetic field generated by the charged particle is opposite to the externally imposed field. → diamagnetic
- For electrons

$$f_{ce} = 2.80 \times 10^6 B_0 [\text{Hz}] (B_0 \text{ in gauss})$$

$$r_{ce} = \frac{3.37\sqrt{E}}{B_0}$$
 [cm] (*E* in volts)

• For singly charged ions

$$f_{ci} = 1.52 \times 10^3 B_0 / M_A [\text{Hz}] (B_0 \text{ in gauss})$$

$$r_{ci} = \frac{144\sqrt{EM_A}}{B_0}$$
 [cm] (*E* in volts, M_A in amu)

• Energy gain?



🛞 B

ION



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Electron beam sources

• Typical schematic diagram of electron beam sources



- Electron emission from solid
 - Thermionic emission
 - Field emission
 - Photoelectric emission
 - Secondary electron emission by ion or electron impact
 - Auger electron emission



Thermionic emission

- Thermionic emission (hot emission) is the heat-induced flow of charge carriers from a surface or over a potential-energy barrier.
- This occurs because the thermal energy given to the carrier overcomes the binding potential, also known as work function of the metal.
- Richardson-Dushman law (1901)

 $J = AT^2 \exp\left(-\frac{W}{kT}\right)$

- Schottky effect: field-enhanced thermionic emission
- Work function: the minimum energy (usually measured in electron volts) needed to remove an electron from a solid to a point immediately outside the solid surface (or energy needed to move an electron from the Fermi level into vacuum)





Electron flow



 $W/ThO_2 \sim 2.5$



Field emission

- Field emission (cold emission) involves the extraction of electrons from a solid by tunneling through the surface potential barrier. The emitted current depends directly on the local electric field at the emitting surface, *E*, and on its work function, *W*.
- Fowler-Nordheim model

 $J = C \frac{E^2}{W} \exp\left(-D \frac{W^{3/2}}{E}\right)$

- A small variation of the shape or surrounding of the emitter (geometric field enhancement) and/or the chemical state of the surface has a strong impact on the emitted current.
- It is most commonly an undesirable primary source of vacuum breakdown and electrical discharge phenomena.





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Photoelectric emission

- In the photoelectric effect, electrons are emitted from matter as a consequence of their absorption of energy from electromagnetic radiation of very short wavelength, such as visible or ultraviolet light.
- First observed by Heinrich Hertz in 1887
- Einstein's explanation (1905)







Secondary electron emission by ion impact

- The field of ion approaching a surface to within a distance of atomic dimensions transforms a potential well on the surface into a potential barrier. The barrier is low and narrow because the field is tremendously strong. An electron from the metal immediately tunnels into the ion and neutralizes it.
- If the energy released is greater than *W*, it may be spent on ejecting another electron.
- SEE coefficient by ion impact

 $\gamma_i = \frac{No.\,of\,\,emitted\,\,electrons}{No.\,of\,\,incident\,\,ions}$

- γ_i depends greatly on the kinetic energy of ions impinging on the solid surface.
- This process plays an important role in breakdown process for DC discharge.





Secondary electron emission by electron impact

The electron emission from a solid surface induced by electron impact.

Photon

SEE coefficient by electron impact

 $\gamma_e = \frac{No.\,of\ emitted\ electrons}{No.\,of\ incident\ electrons}$

- Photomultiplier tube (PMT)
- This process plays an important role in vacuum breakdown by high frequency fields: the oscillating electron strikes the gap walls alternatingly, on after the other.







Auger electron emission

- The Auger effect is a physical phenomenon in which the transition of an electron in an atom filling in an inner-shell vacancy causes the emission of another electron.
- When a core electron is removed, leaving a vacancy, an electron from a higher energy level may fall into the vacancy, resulting in a release of energy. This energy can be transferred to another electron, which is ejected from the atom.







Ion beam sources

Most ion sources consist of a plasma source and an extractor





Various ion sources

• DC sources (glow or arc)



• DC sources (glow or arc) with magnetic field







Various ion sources

• RF sources (13.56 MHz is widely used)



External antenna

Internal antenna



Various ion sources

• MW sources (2.45 GHz is widely used)





Example of ion sources

• LHC (Large Hadron Collider): Duoplasmatron





Example of ion sources

- KOMAC (Korea Multipurpose Accelerator Complex): MW ion source
 - > Hydrogen discharge using 2.45 GHz magnetron
 - > Pulsed proton beam extraction: 50 keV, 20 mA, 2 ms pulse beam





Example of ion sources

• Highly charged ion sources: Superconducting ECR, EBIS





Cockcroft-Walton's voltage multiplier

• The first nuclear disintegration by nuclear projectiles artificially produced in a man-made accelerator (1932).



Cockcroft and Walton, Proc. Roy. Soc. A136, 619 (1932) Cockcroft and Walton, Proc. Roy. Soc. A137, 229 (1932)



Analysis of Cockcroft-Walton's voltage multiplier circuit

• The voltage multiplier circuit is a combination of a clamping circuit and a peak detector circuit (rectifier circuit).





Van de Graaff accelerator

- A Van de Graaff [R. J. Van de Graaff, Phys. Rev. 38, 1919 (1931)] accelerator is a low-current electrostatic MeV-range high-voltage generator using corona discharge from an array of needles in gas.
- The electrons drift toward the positive electrode and are deposited on a moving belt. The belt composed of an insulating material with high dielectric strength, is immersed in insulating gas at high pressure. The attached charge is carried mechanically against the potential gradient into a high-voltage metal terminal.
- The terminal acts as a Faraday cage; there is no electric field inside the terminal other than that from the charge on the belt. The charge flows off the belt when it comes in contact with a metal brush and is deposited on the terminal.



LANL 7 MeV VDG, as injector for 24.5 MeV tandem VDG



1.5 MeV SNU Van de Graaff accelerator





Tandem Van de Graaff accelerator

- The output beam energy of a Van de Graaff accelerator can be extended a factor of 2 through the tandem configuration.
- Negative ions produced by a source at ground potential are accelerated to a
 positive high-voltage terminal and pass through a stripping cell. Collisions in the
 cell remove electrons, and some of the initial negative ions are converted to
 positive ions. They are further accelerated traveling from the high-voltage
 terminal back to ground.





Linear RF (radio-frequency) accelerator

• The particles travelling from the source are subjected to an accelerating electric field when travelling between one cavity and the next, and the electric field is reversed by the time the particles reach the following gap.





KOMAC (proton accelerator)

Features of KOMAC 100MeV linac

- 50-keV Injector (Ion source + LEBT)
- 3-MeV RFQ (4-vane type)
- 20 & 100-MeV DTL
- RF Frequency : 350 MHz
- Beam Extractions at 20 or 100 MeV
- 5 Beamlines for 20 MeV & 100 MeV

Output Energy (MeV)	20	100	
Max. Peak Beam Current (mA)	1 ~ 20	1 ~ 20	
Max. Beam Duty (%)	24	8	
Avg. Beam Current (mA)	0.1 ~ 4.8	0.1 ~ 1.6	
Pulse Length (ms)	0.1 ~ 2	0.1 ~ 1.33	
Max. Repetition Rate (Hz)	120	60	
Max. Avg. Beam Power (kW)	96	160	





Betatron: circular induction accelerator

 The betatron [D. W. Kerst, Phys. Rev. 58, 841 (1940)] is a circular induction accelerator used for electron acceleration.

$$\nabla \times E = -\frac{\partial B}{\partial t} \quad \Rightarrow \quad \oint E \cdot dl = -\frac{\partial}{\partial t} \oint B \cdot da$$

• The vertical field at R, i.e. $B_z(R)$ is related with R by

$$R = \frac{\gamma m_e v_\theta}{e B_z(R)} = \frac{p_\theta}{e B_z(R)}$$



 Particle motion on the main orbit is described by the Faraday induction law:

$$\frac{dp_{\theta}}{dt} = eE_0 = \frac{e}{2\pi R} \frac{d\Phi}{dt}$$
$$\implies p_{\theta} = \frac{e[\Phi(t) - \Phi(0)]}{2\pi R} = \frac{e}{2\pi R} \Delta \Phi$$

• Betatron condition:

$$B_z(R) = \frac{\Delta \Phi}{2\pi R^2} \approx \frac{B_0 \cdot \pi R^2}{2\pi R^2} = \frac{B_0}{2}$$





Cyclotron: circular RF accelerator with constant ω_{RF} and B

The operation of the uniform-field cyclotron [E. O. Lawrence, Science 72, 376 (1930)] is based on the fact that the gyro-frequency for non-relativistic ions is independent of kinetic energy. Resonance between the orbital motion and an accelerating electric field can be achieved for ion kinetic energy that is small compared to the rest energy.





Synchrotron

• Synchrotrons are resonant circular particle accelerators in which both the magnitude of the bending magnetic field and the rf frequency are cycled. An additional feature of most modern synchrotrons is that focusing forces are adjustable independent of the bending field.



Pohang Light Source

constant



 Sealed-tube neutron generators: Some accelerator-based neutron generators induce fusion between beams of deuterium and/or tritium ions and metal hydride targets which also contain these isotopes.



Introduction to Nuclear Engineering, Fall 2019

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• Plasma focus and plasma pinch devices: The dense plasma focus neutron source produces controlled nuclear fusion by creating a dense plasma within which heats ionized D and/or T gas to temperatures sufficient for creating fusion.





• Inertial electrostatic confinement (IEC): Inertial electrostatic confinement devices such as the Farnsworth-Hirsch fusor use an electric field to heat a plasma to fusion conditions and produce neutrons. The ions are believed to be confined in the electrostatic potential well.





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• Light ion accelerators: Traditional particle accelerators with hydrogen (H), deuterium (D), or tritium (T) ion sources may be used to produce neutrons using targets of deuterium, tritium, lithium, beryllium, and other low-Z materials.





• Nuclear fission reactors: Fission reactor sources rely on a neutron-propagated chain reaction in the fuel (usually ²³⁵U). Power reactors are optimized for heat extraction and efficient use of fuel, so they have quite a different design from research reactors that are optimized for high (external) thermal neutron flux.

 $^{235}{\rm U} + n \to {\rm X} + {\rm Y} + 2.5\,n\,,$

 $(\sim 200 \text{ MeV total energy release}, \sim 2 \text{ MeV per neutron})$

 In a typical research reactor design, one of the neutrons produced per fission is needed to sustain the chain reaction, ~0.5 is lost, and one is available for external use (i.e., ~200 MeV of heat is produced for each available neutron).

Table 2.1 Existing medium- and high-flux reactor sources and their respective parameters										
	United	United								
Country	States	States	Canada	France	France	Germany	Germany	Australia	Korea	Japan
Neutron source	HFIR	NBSR	NRU	HFR	ORPHEE	BENSC	FRM-II	OPAL	HANARO	JRR-3 M
Organization	Oak Ridge National Laboratory	National Institute of Standards and Technology	Atomic Energy of Canada Limited	Institut Laue- Langevin	Laboratoire Léon Brillouin	Helmholtz- Zentrum Berlin	Technische Universitat Munchen	Australian Nuclear Science and Technology Organization	Korea Atomic Energy Research Institute	Japan Atomic Energy Agency
Power (MW)	85	20	120	58	14	10	20	20	24 (present) 30 (designed)	20
$\begin{array}{c} Flux \ (n \cdot cm^{-2} \\ \cdot s^{-1}) \end{array}$	1.5×10 ¹⁵	3×10^{14}	3×10 ¹⁴	1.5×10^{15}	3×10 ¹⁴	2×10 ¹⁴	8×10^{14}	3×10 ¹⁴	2×10 ¹⁴	3×10^{14}
Number of cold/hot sources	1/0	1/0	0/0	2/1	1/1	1/0	1/1	1/0	1(planned)/0	1/0
Number of instruments	9(present) + 6 (planned by 2012)	24	5	26	22	22	20 (present) + 10 (under construction)	6	6	24
Existing neutron imaging instrument		BT-2 [14]			[15]	CONRAD [16]	ANTARES [17]		NR-port [18]	TNRF [19] And TNRF-2 [20]
Facility operating since	1967	1970	1957	1972 (refurbished 1993)	1980	1973	2004	2006	1997	1990

HFIR: High-Flux Isotope Reactor [21]; NBSR: National Bureau of Standards Reactor [22]; NRU: National Research Universal Reactor, Chalk River, Canada [23]; HFR: High-Flux Reactor at ILL [1, 2]; ORPHEE: reactor at LLB [24]; BENSC: Berlin Neutron Scattering Centre [25]; FRM-II: Forschungsneutronenquelle Heinz Maier-Leibniz [5]; OPAL: Open Pool Australian Light-water Reactor [6]; HANARO: High-flux Advanced Application Reactor [4]; JRR-3 M: Japan Research Reactor No. 3 Modified [3]. Consult the websites for these facilities to obtain additional information and current details. A number of smaller reactors, primarily at universities, are not listed here.



• Thermonuclear fusion reactors: A number of experiments around the world have verified the principles of d + t fusion; however, it still has to be demonstrated that a gain in energy can be achieved.

 $d + t \rightarrow \alpha (3.5 \text{ MeV}) + n (14 \text{ MeV}).$

 In hybrid reactors, high-energy neutrons generated by fusion reactions drive fission in the surrounding blanket of fissile material, burning up long-lived radioactive by-products produced by the fission process.



D-T fusion reactor

Fusion-fission hybrid reactor







- Electron beam neutron sources: Energetic electrons striking high-mass targets slow down to emit bremsstrahlung (e,γ) photons. Photons proceed to interact with target nuclei to produce (γ,n) photoneutrons.
- Early work at accelerator-driven sources was based on cyclotrons and pulsed electron-linacdriven bremsstrahlung photoneutron sources.
- The e-linac-driven sources soon reached a power limit of about 50 kW, imposed by heat transfer engineering constraints on target design which is subjected to about 2000-MeV heating per neutron production.







- Spallation neutron sources: Spallation is a violent reaction in which a target is bombarded by very high-energy particles. The incident particle, such as a proton, disintegrates the nucleus through inelastic nuclear reactions. The result is the emission of protons, neutrons, α-particles, and other particles.
- Threshold energy of spallation reaction by protons in heavy nuclei is ~100 MeV.
- It shows excellent neutron production efficiency compared with other techniques. For example, a 1-GeV proton on tungsten (A = 184) produces 18 neutrons and deposits ~30 MeV of heat per neutron.

Japan JSNS Japan
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r Atomic Energy on Agency
3000/333
1 MW
25
Mercury
L-H ₂
23 (beam ports)
2005) 2008

IPNS: Intense Pulsed Neutron Source [32]; LANSCE: Los Alamos Neutron Science Center [33]; SNS: Spallation Neutron Source [8, 9]; ISIS: [34, 35]; SINQ: Swiss Spallation Neutron Source [36, 37]; CSNS: Chinese Spallation Neutron Source [10, 11]; ESS: European Spallation Source [38, 39]; KENS: Koh-Energy-ken Neutron Source [40, 41]; JSNS: Japanese Spallation Neutron Source [8, 9]. Consult the websites for these facilities to obtain additional information and current details.

Table 2.2 Past, existing, and future spallation source and their respective parameters



History of flagship neutron facilities



