**2017 Fall** 

## "Phase Equilibria in Materials"

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1

**Contents for previous class** 

## **Review of Invariant Binary Reactions**

Positive  $\Delta H_m$ 



### **Barrier of Heterogeneous Nucleation**



#### How about the nucleation at the crevice or at the edge?

### How do we treat the non-spherical shape?



$$\Delta \boldsymbol{G}_{sub}^{*} = \Delta \boldsymbol{G}_{homo}^{*} \left( \frac{\boldsymbol{V}_{A}}{\boldsymbol{V}_{A} + \boldsymbol{V}_{B}} \right)$$

#### Effect of good and bad wetting on substrate

**Contents for today's class** 

### Chapter 6 Binary Phase Diagrams: Reactions in the Solid State

- \* Eutectoid reaction:  $\alpha \leftrightarrow \beta + \gamma$
- \* Monotectoid reaction:  $\alpha_1 \leftrightarrow \beta + \alpha_2$
- \* Peritectoid reaction:  $\alpha + \beta \leftrightarrow \gamma$

### Chapter 7 Binary Phase Diagram: Allotropy of the Components

- \* SYSTEMS IN WHICH ONE PHASE IS IN EQUILIBRIUM WITH THE LIQUID PHASE
- \* SYSTEMS IN WHICH TWO PHASES ARE IN EQUILIBRIUM WITH THE LIQUID PHASE
  - \* Metatectic reaction:  $\beta \leftrightarrow L + \alpha$  Ex. Co-Os, Co-Re and Co-Ru

### Chapter 6 Binary Phase Diagrams: Reactions in the Solid State



Disordered atomic arrangement at <u>grain boundaries</u> will reduce the strain energy factor and the interfacial energy needed to nucleate a new phase.

The finer the grain size, and hence the larger the grain boundary area, the more readily will the transformation proceed. "allotropic transformation"

# **Iron-Carbon System**



Source: Reed-Hill, Abbaschian, Physical Metallurgy Principles, 3rd Edition, PWS Publishing Company, 1994.

## **Iron Carbon Phase Diagram**



# **Cementite – What is it?**

Iron Carbide – Ceramic Compound

Purple: Carbon atoms Orange: Iron atoms



- Cementite has an orthorhombic lattice with approximate parameters 0.45165, 0.50837 and 0.67297 nm.
- There are twelve iron atoms and four carbon atoms per unit cell, corresponding to the formula Fe<sub>3</sub>C.

Source: http://www.msm.cam.ac.uk/phase-trans/2003/Lattices/cementite.html H. K. D. H. Bhadeshia

# Pearlite: What is it?



• The eutectoid transformation:

 $\gamma (0.77\% \text{ C}) \rightarrow \alpha (0.02\% \text{ C}) + \text{Fe}_3 \text{C} (6.67\% \text{ C})$ 

- Alternate lamellae of ferrite and cementite as the continuous phase
- <u>Diffusional Transformation</u>
- "Pearlite" name is related to the regular array of the lamellae in colonies. Etching attacks the ferrite phase more than the cementite. The raised and regularly spaced cementite lamellae act as diffraction gratings and a <u>pearl-like luster</u> is produced by the diffraction of light of various wavelengths from different colonies

# Pearlite



**Fig. 18.6** Pearlite consists of plates of Fe<sub>3</sub>C in a matrix of ferrite. (Vilella, J. R., *Metallographic Technique for Steel*, ASM Cleveland, 1938.) 2500X.

Reed-Hill, Abbaschian, 1994, [5]

• Two phases appear in definite ratio by the lever rule:

$$\alpha = \frac{6.67 - 0.77}{6.67} \approx 88\%$$
cementite =  $\frac{0.77 - 0}{6.67} \approx 12\%$ 

- Since the densities are same (7.86 and 7.4) lamellae widths are 7:1
- Heterogeneous nucleation and growth of pearlite colonies – but typically grows into only 1 grain

# Lamellae Nucleation



Fig. 18.7 The two primary methods of nucleating pearlite. (A) Nucleation of pearlite at an austenite grain boundary (Pitsch-Petch relation). (B) Nucleation of pearlite at a grainboundary layer of cementite (Baryatski relation).

Reed-Hill, Abbaschian, 1994

# **Lamellae Nucleation**



Fig. Growing cementite and ferrite lamellae may nucleate each other.

Reed-Hill, Abbaschian, 1994

### **Eutectic Solidification (Kinetics)**

If  $\alpha$  is nucleated from liquid and starts to grow, what would be the composition at the <u>interface</u> of  $\alpha/L$  determined?

→ rough interface (diffusion interface) & local equilibrium

How about at  $\beta/L$ ? Nature's choice? Lamellar structure





What would be a role of the <u>curvature</u> at the tip?

→ Gibbs-Thomson Effect

# **Interlamellar Spacing**

- Interlamellar spacing  $\lambda$  is almost constant in pearlite formed from  $\gamma$  at a fixed T.
- Temperature has a strong effect on spacing lower T (large  $\Delta T$ ) promotes smaller  $\lambda$ .
  - Pearlite formed at 700°C has  $\lambda \sim 1 \text{ mm}$  and Rockwell C 15.
  - Pearlite formed at 600°C has  $\lambda \sim 0.1$  mm and Rockwell C 40.
- Zener and Hillert Eq. for spacing (eq. 4.39):

$$\lambda = \frac{4\sigma_{\alpha/Fe_{3}C}T_{E}}{\Delta H_{V}\Delta T}$$

IH5: derive  $\lambda$  with maximum growth rate at a fixed  $\Delta T$  (eutectic case)

- $\sigma_{a/Fe_3C}$  = Interfacial energy per unit area of a/Fe<sub>3</sub>C boundary
- $T_E$  = The equilibrium temperature (Ae<sub>1</sub>)
- $\Delta H_V$  = The change in enthalpy per unit volume
- $\Delta T$  = The undercooling below Ae<sub>1</sub>

# Effect of Undercooling on $\lambda$



steels as indicated. (Ref 2.1)

Krauss, <u>Steels</u>, 1995

# **Effect of Interlamellar Spacing**



FIG. 16-Yield strength and hardness versus pearlite interlamellar spacing [49].

Stone et al, 1975

# Iron-Carbon (Fe-C) Phase Diagram



# **Hypoeutectoid Steel**



19

## Proeuctectoid Ferrite – Pearlite



0.38 wt% C: Plain Carbon – Medium Carbon Steel



Ta

Fig. 93. The monotectoid reaction in the Ta-Zr system (schematic).

 $\beta Zr \leftrightarrow \alpha + \beta Ta$ 

Both  $\beta Zr$  and  $\beta Ta$  have the same crystal structure (b.c.c.) but different lattice spacing.

Monotectic Monotectic  $\alpha \rightarrow \beta + \alpha 2$   $|_1 \neq \alpha + |_2 \qquad \alpha \rightarrow \frac{1}{2}$ 



Fig. 94. The monotectoid reaction in the Al-Zn system (schematic). (a) Previously accepted phase diagram; (b) recently proposed modification.

# Both $\alpha$ and $\alpha'$ are face-centered cubic phases, differing only in lattice spacing.

**Peritectoid reaction:**  $\alpha + \beta \leftrightarrow \gamma$ 





Cu-Al phase diagram

**Revision of Cu-Al phase diagram** 

Peritectic

 $| + \beta \overrightarrow{a} \alpha$ 









Fig. 97. (a) A part of the Cu-Sn phase diagram (after G. V. RAYNOR; courtesy Institute of Metals); (b) equilibrium relationships if the data in (a) are considered limiting cases of the peritectoid and sutectoid reactions.

#### **CHAPTER 7**

**Ex. Iron**- three allotropes  $\alpha$ ,  $\gamma$ ,  $\delta$ 

### **Binary Phase Diagrams. Allotropy of the Components**

Several commercially important metals exist in more than one crystalline form.

Titanium – two allotropes close-packed hexagonal α Ti stable at low temp. and bodycentered cubic β Ti stable at high temp.

Plutonium – six allotropes \_ the highest number of modifications



a. SYSTEMS IN WHICH ONE PHASE IS IN EQUILIBRIUM WITH THE LIQUID PHASE Such systems can be further divided according to whether the <u>high</u> <u>temperature allotrope forms a continuous series of solid solutions with the</u> <u>other component or not.</u>

7.1.1. The high temperature phase forms a series of solid solutions with the other component



7.1.1. The high temperature phase forms a series of solid solutions with the other component

Types of phase diagrams formed when the high temperature allotrope forms a continuous series of solid solutions with the second component.

(a) single component have two allotropic modifications.







7.1.1. The high temperature phase forms a series of solid solutions with the other component (a) single component have two allotropic modifications.

Fig. 99. Cooling of alloys through the  $\beta$  loop.

7.1.1. The high temperature phase forms a series of solid solutions with the other component(b) Both components have two allotropic modifications.

в

Δ в (d) **Complete series of solid solutions** 

are formed between each of the allotropes

Eutectoidal decomposition of high temperature allotrope β into α and γ, the low temperature allotropes of components A and B respectively.

.(c)

Α

7.1.1. The high temperature phase forms a series of solid solutions with the other component

(b) Both components have two allotropic modifications.



Fig. 100. The Ti-Zr phase diagram (schematic).

Complete series of solid solutions are formed between each of the allotropes in the system Ti-Zr.

#### a. SYSTEMS IN WHICH ONE PHASE IS IN EQUILIBRIUM WITH THE LIQUID PHASE

7.1.2. Both phases form limited solid solutions with the other component



High-temperature  $\beta$  phase, as well as the low-temperature  $\alpha$  phase form <u>limited solid solutions with component B</u>.

# **Polymorphism:** the ability of a solid material to exist in more than one form or crystal structure (Both $\alpha$ and $\beta$ are allotropes of A)

**Eutectoid reaction:**  $\alpha \leftrightarrow \beta + \gamma$ 

**Peritectoid reaction:**  $\alpha + \beta \leftrightarrow \gamma$ 



Simple eutectic system with solid-soild phase transitions

**b. SYSTEMS IN WHICH TWO PHASES ARE IN EQUILIBRIUM WITH THE LIQUID PHASE** 

 $L + \alpha \& L + \beta \text{ or } L + \beta \& L + \gamma \text{ or } L + \gamma \& L + \delta$ 



Fig. 102. Examples of phase diagrams in which both allotropes are in equilibrium with the melt.

**Metatectic reaction:**  $\beta \leftrightarrow L + \alpha$  Ex. Co-Os, Co-Re and Co-R<sup>36</sup>

#### **Metatectic reaction:** $\beta \leftrightarrow L + \alpha$ Ex. Co-Os, Co-Re and Co-Ru

(Both  $\alpha$  and  $\beta$  are allotropes of A)



Fig. 103. The metatectic reaction.

**Metatectic reaction:**  $\beta \leftrightarrow L + \alpha$  Ex. Co-Os, Co-Re and Co-Ru



Fig. 104. Derivation of the metatectic phase diagram (Fig. 103) from the free energy curves for the liquid,  $\frac{8}{\alpha}$  and  $\beta$  phases.

b. SYSTEMS IN WHICH TWO PHASES ARE IN EQUILIBRIUM WITH THE LIQUID PHASE L+  $\alpha \& L + \beta \text{ or } L + \beta \& L + \gamma \text{ or } L + \gamma \& L + \delta$ 



39

### b. SYSTEMS IN WHICH TWO PHASES ARE IN EQUILIBRIUM WITH THE LIQUID PHASE L+ $\alpha$ & L + $\beta$ or L + $\beta$ & L + $\gamma$



## **Review of Invariant Binary Reactions**



On cooling one phase going to two phases Metatectic reaction:  $\beta \leftrightarrow L + \alpha$  Ex. Co-Os, Co-Re, Co- $\overset{41}{Ru}$ 

## **Review of Invariant Binary Reactions**

Peritectic Type



On cooling two phases going to one phase

### MIDTERM: ?

## Scopes: Text ~ page 117/ Teaching note ~10 QUIZs and Homeworks

## **Eutectic Solidification (Kinetics)**

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→ rough interface (diffusion interface) & local equilibrium

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### **Eutectic Solidification**



α

$$\lambda^{*} = + \frac{2T_{\varepsilon}\gamma V_{m}}{\Delta H \Delta T_{0}} \rightarrow identical \ to \ critical \ radius$$
  
in pure metal

Gibbs-Thomson effect  

$$cf) r^* = \frac{2\gamma_{SL}}{\Delta G_V} = \left(\frac{2\gamma_{SL}T_m}{L_V}\right) \frac{1}{\Delta T}$$

 $L_v$ : latent heat per unit volume  $L = \Delta H = H^L - H^S$ 

#### \* Growth Mechanism: Gibbs-Thomson effect in a $\Delta$ G-composition diagram?



The cause of G increase is the curvature of the  $\alpha/L$  and  $\beta/L$  interfaces arising from the need to balance the interfacial tensions at the  $\alpha/\beta/L$  triple point, therefore the increase will be different for the two phases, but for simple cases it can be shown to be  $\frac{2\gamma_{\alpha\beta}V_m}{\lambda}$  for both.

**1)** If  $\lambda = \lambda^*$ , growth rate will be <u>infinitely</u> <u>slow</u> because the liquid in contact with both phases has the same composition,  $X_E$  in Figure 4.32.



 $(\Delta X)$ . (b) Model used to calculate the growth rate.

