



Link Layer

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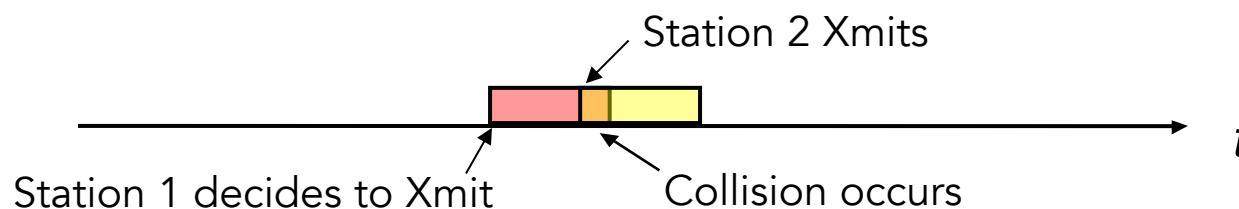
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Collision

- **Collision:** Two or more users' transmissions overlap (in time) resulting in packet loss



- **Recognition:** Some way of recognizing that a collision has occurred and signaling users involved
 - (a) Use a central controller to recognize collisions (signal distortions) and then signal users ← original Aloha
 - (b) Use a positive ACK with timeout
 - (c) Stations listen and detect their own collisions ← bus architectures
- **Retransmission:** After a collision, attempt again after some random time has elapsed (back-off)
 - The amount of time is specified by a collision resolution protocol.

Throughput Analysis of Pure Aloha

□ N stations

- Each station transmits λ (new) packets/sec
- Arrival of (new) packets from each station is Poisson
- Fixed Packet lengths with transmission time = m

$$\begin{aligned} \text{Normalized throughput (S)} &= \frac{\text{Rate of transmitting new packets}}{\text{Max. channel transmission rate}} \\ &= \frac{N\lambda \text{ packets/sec}}{\frac{1}{m} \text{ packets/sec}} \end{aligned}$$

$$\Rightarrow S = N\lambda m$$

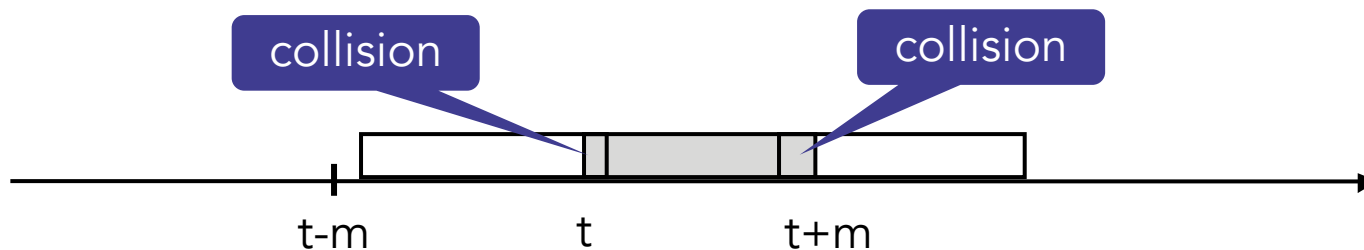
□ Additional assumption: retransmitted packets are also Poisson distributed

- Not true: Since retransmissions depend on collision instance
- Okay if random retransmission delay is long



Throughput Analysis of Pure Aloha

- Let λ' be total rate of packets attempting transmission, then $\lambda' \geq \lambda$
- Let G be actual traffic intensity or utilization, then $G = N\lambda'm$
- Consider a typical packet transmitted at time t
 - Any transmissions by any station between times $t - m$ and $t + m$ will cause a collision.



Throughput Analysis of Pure Aloha

$$\square \Pr\{\text{Successful transmission}\}$$

$$= \Pr\{\text{No arrivals in } [t - m, t + m] \mid \text{An arrival occurs at } t\}$$

$$= \Pr\{\text{No arrivals in } [t - m, t + m]\}$$

$$= \Pr\{\text{No arrivals in time interval of } 2m\}$$

$$= e^{-N\lambda'(2m)}$$

$$\square \text{ From } G = N\lambda'm,$$

$$P_s = \Pr\{\text{Successful transmission}\} = e^{-2G}$$

Recall that Poisson process gives

$$\longleftarrow P\{N(t) = n\} = \frac{(\lambda t)^n}{n!} e^{-\lambda t}$$

$$\square \text{ Also, } P_s = \frac{\# \text{ of successfully transmitted packets}}{\# \text{ of totally transmitted packets}}$$

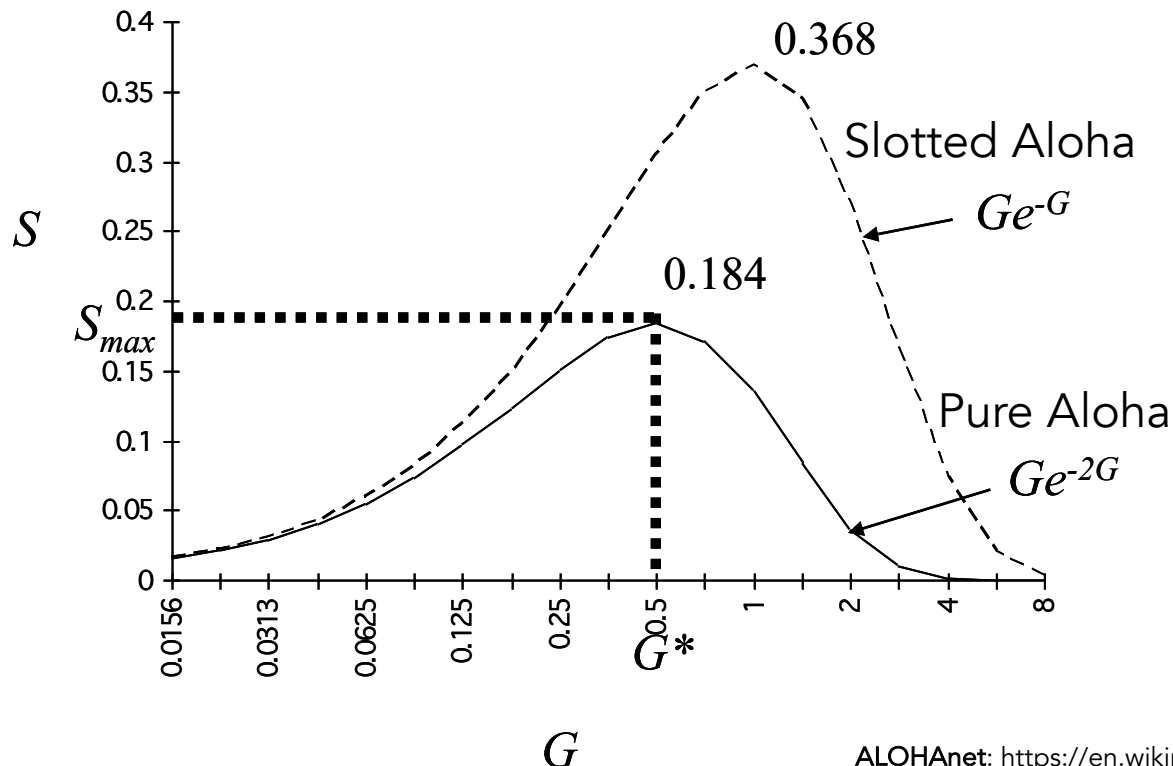
$$= \frac{(\text{throughput with new packets})}{(\text{throughput with all packets})} \begin{matrix} \longrightarrow S \\ \longrightarrow G \end{matrix}$$

$$\square \text{ Hence, } P_s = \frac{S}{G}$$



Throughput Analysis of Pure Aloha

- Pure Aloha throughput: $S = Ge^{-2G}$
 - S has the peak value $S_{max} = \frac{1}{2e}$, when $G = G^* = \frac{1}{2}$



For Aloha, the max throughput is 18% of channel capacity.

Thus it is suitable for either low traffic rate, or for highly bursty traffic

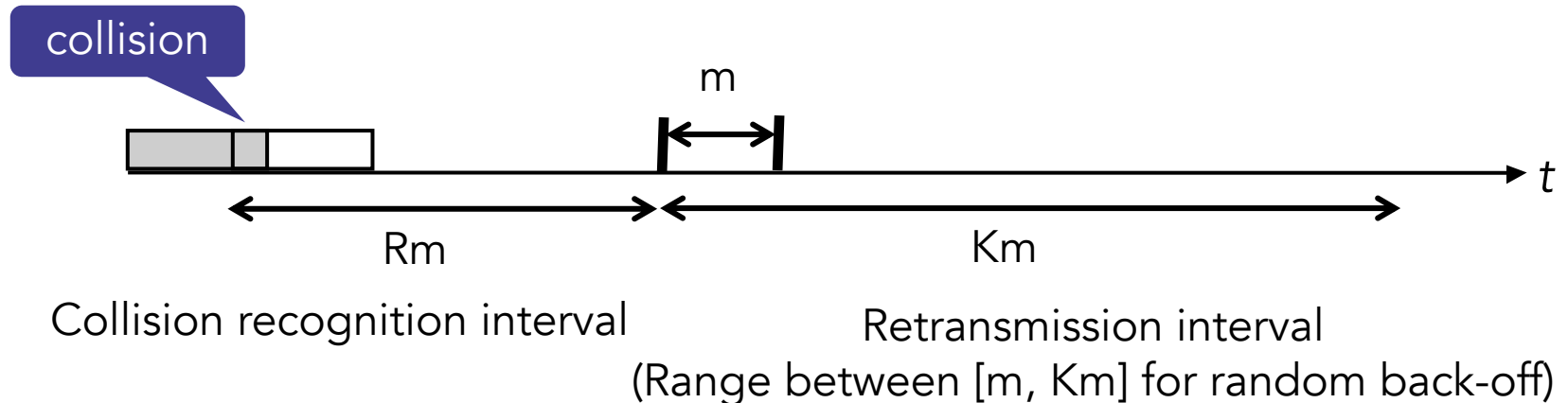
ALOHAnet: https://en.wikipedia.org/wiki/ALOHAnet#ALOHA_protocol

Time Delay Analysis of Pure Aloha

- Our simple throughput analysis of Pure Aloha is “independent” of the retransmission policy
 - However, for time delay analysis, we need to specify the **retransmission policy**
- Retransmission Policy:
 - Suppose that each message lengths is of m seconds
 - If a collision occurs, we choose an arbitrary time interval, whose length is equivalent to K -message unit times ($K \cdot m$)
 - Retransmission randomly occurs in the interval, i.e., following the uniform distribution



Time Delay Analysis of Pure Aloha



□ Collision cognition interval:

- Retransmission will take place, only after the sender noticed that a collision has occurred
- Let the round-trip delay plus processing time required to obtain the collision information be R intervals (times m)

Time Delay Analysis of Pure Aloha

- Let D be average time for a successful transmission

$$D = m + Rm + E \left(Rm + \frac{K+1}{2}m \right)$$

Average delay of random back-off
($\in [m, Km]$)

where m is message transmission time
 Rm is recognition time
 E is expected number of retransmissions

- Note that

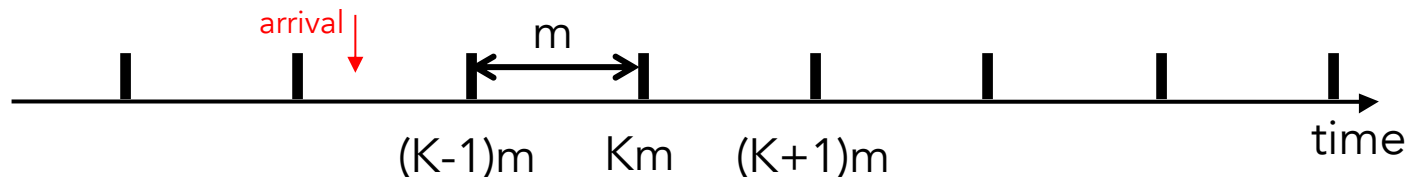
$$1 + E = \frac{\text{avg. \# of attempted transmissions}}{\text{avg. \# of successful transmissions}} = \frac{G}{S} \quad \leftarrow S = Ge^{-2G}$$

- Hence,

$$D = m + Rm + (e^{2G} - 1) \cdot \left(Rm + \frac{K+1}{2}m \right)$$

Slotted Aloha

- Time is slotted into units of message transmission times
 - Messages can only be transmitted at beginning of time slot
 - Collision occurs if another message is transmitted at the same time slot (This message arrives during $((K-1)m, Km)$)

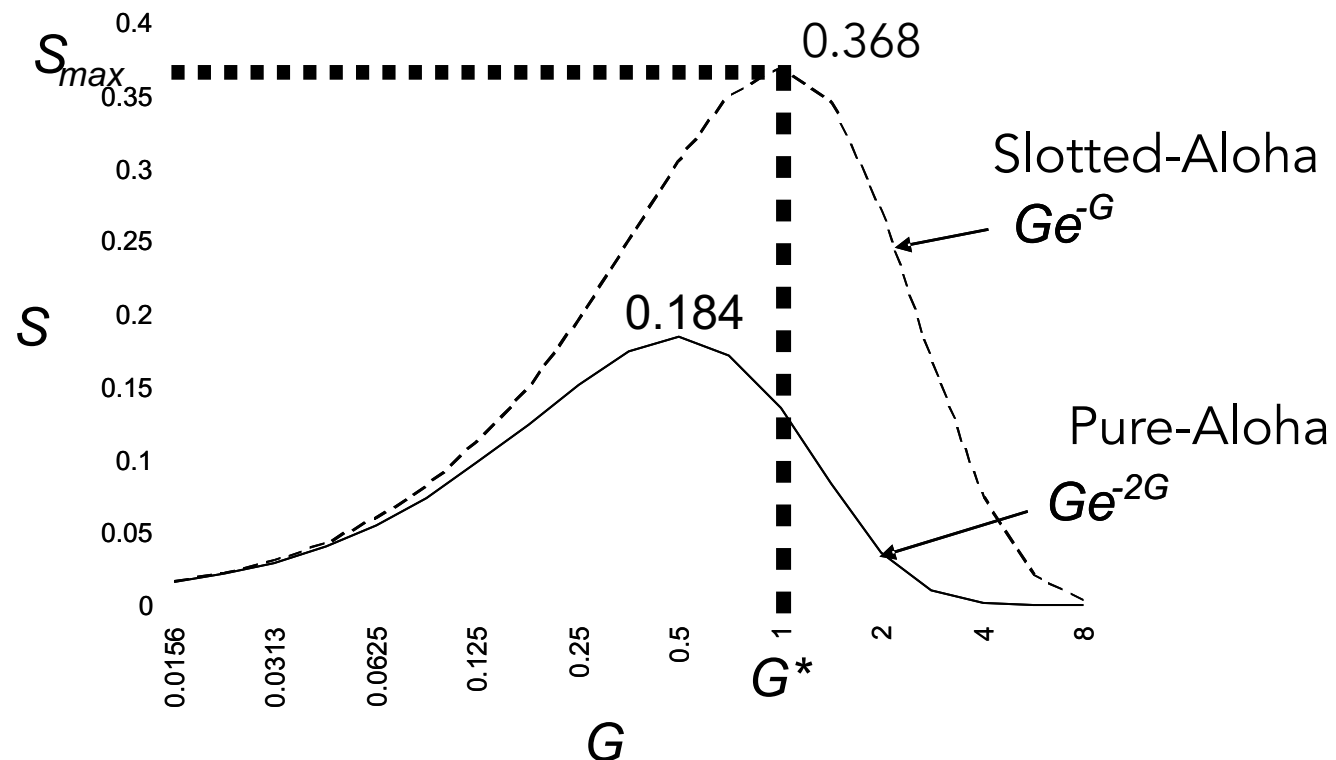


- Following the same line of analysis as Pure Aloha,

$$\left. \begin{aligned} \Pr\{\text{Success}\} &= e^{-G}, \quad S = Ge^{-G} \\ D &= 1.5m + Rm + (e^G - 1) \cdot \left(Rm + 0.5m + \frac{K+1}{2}m \right) \end{aligned} \right\} \text{Try to get this result by yourself}$$

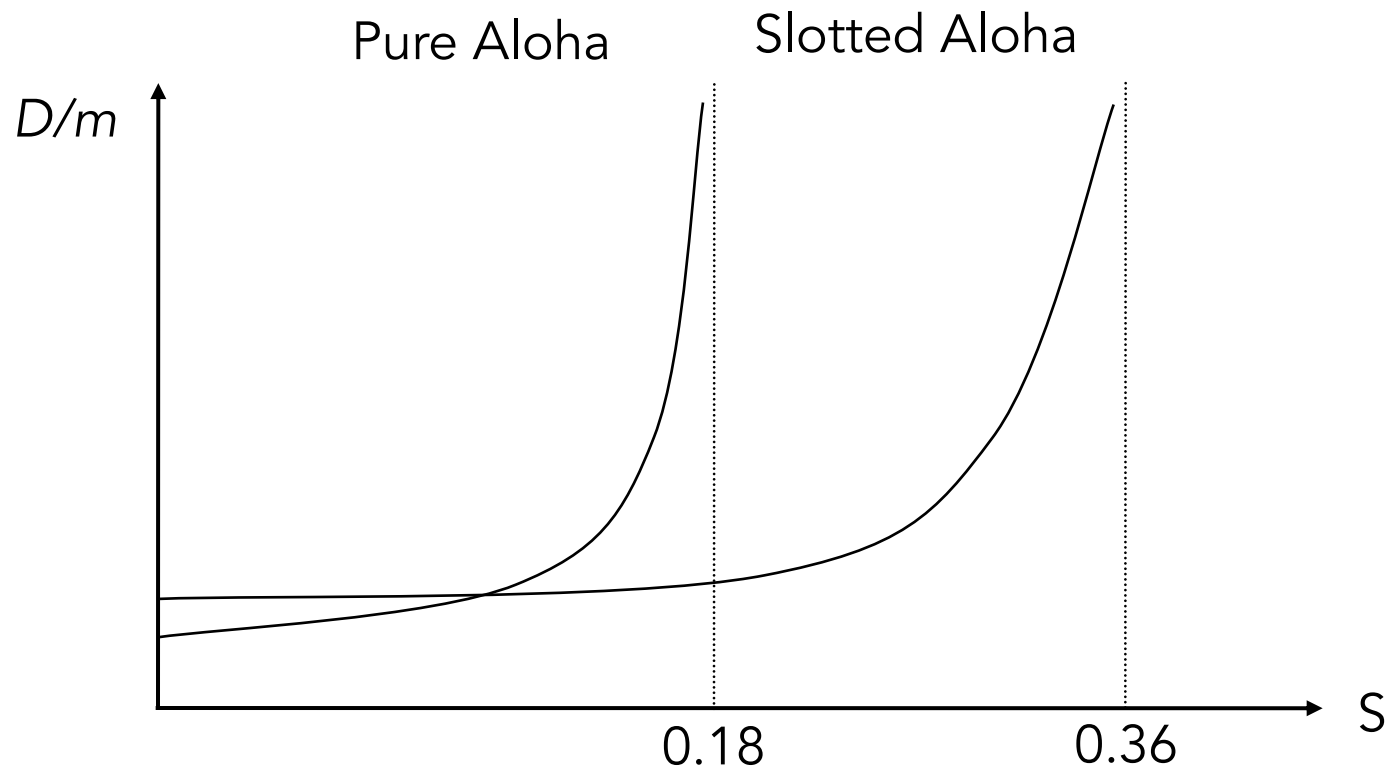
Throughput Analysis of Slotted Aloha

- Slotted Aloha throughput: $S = Ge^{-G}$
 - S has the peak value $S_{max} = \frac{1}{e}$, when $G = G^* = 1$



Performance Comparison

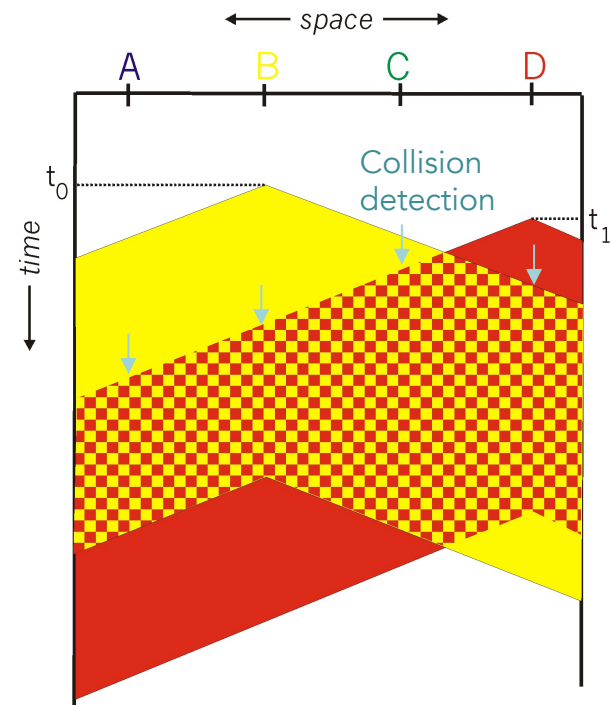
- Throughput-delay curve



CSMA/CD

□ Carrier Sense Multiple Access with Collision Detection

- All stations listen for transmissions on the line (carrier sense)
- A station can transmit only if it detects an idle channel
 - Listen-before-talk
- Two or more stations sensing an idle channel at same time may cause collisions
- Stations detecting a collision abort their transmission immediately.



http://www2.ic.uff.br/~michael/kr1999/5-datalink/5_03-LAN.htm



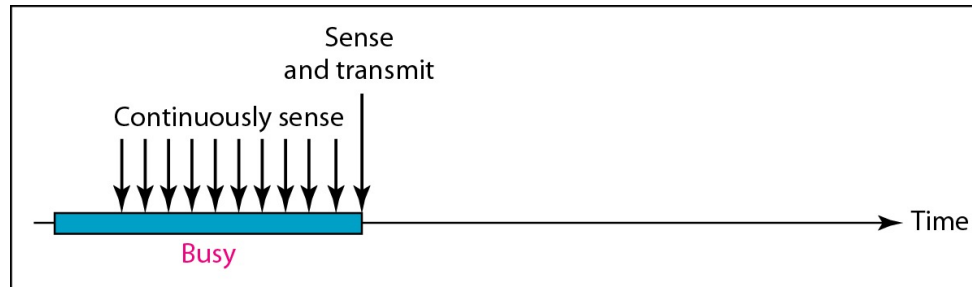
CSMA/CD

- In case that the channel is busy
 - There are variants based on what to do when the channel is sensed busy
 - **1-persistent:** Attempt transmission as soon as channel is sensed idle (Ethernet)
 - **p-persistent:** Attempt transmission with probability p once channel goes idle. With probability $(1-p)$, wait for a propagation delay interval τ and try again!
 - **Non-persistent:** Reschedule after a random waiting time, sense channel and if idle, transmit, if busy, repeat.



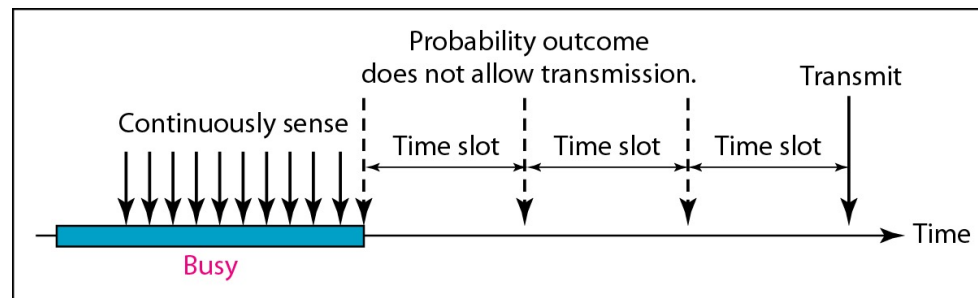
CSMA/CD

1-persistent



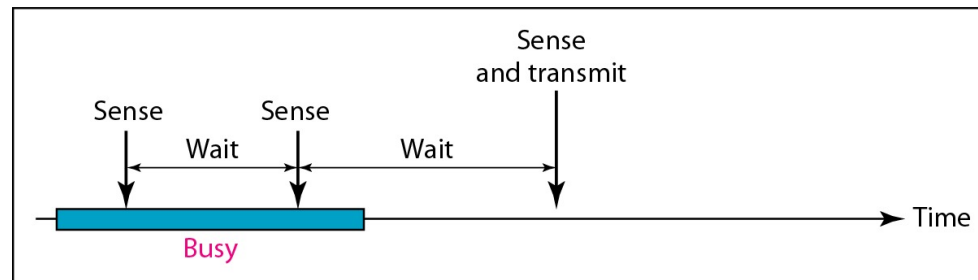
a. 1-persistent

p-persistent



c. p-persistent

non-persistent



b. Nonpersistent

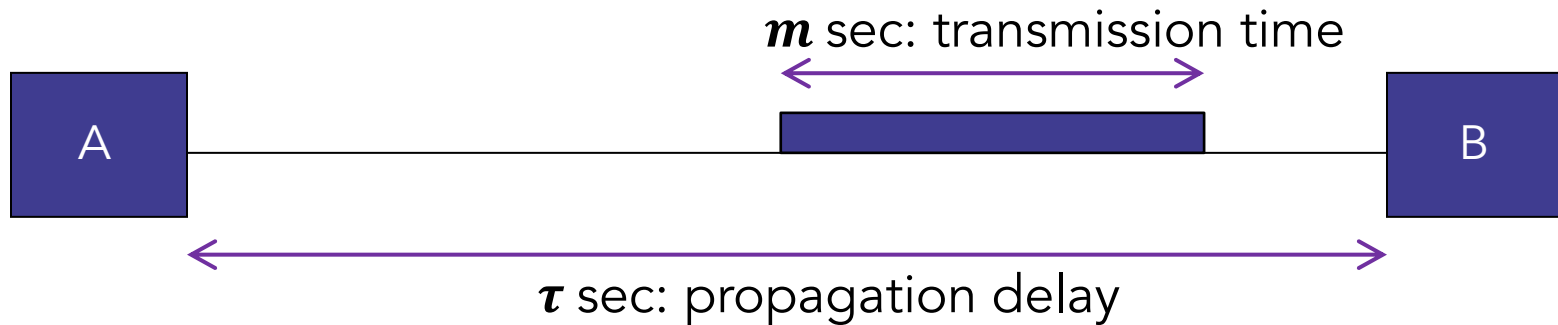
CSMA/CD

- After a collision is detected
 - Current packet transmission is aborted
 - A retransmission attempt is made at a random time, uniformly chosen within a given time interval (similar to Aloha)
 - Each time a collision occurs (for the same packet), this time interval is “doubled” (up to a maximum value) thereby reducing chance of collisions
 - Known as **binary exponential backoff**.



CSMA/CD

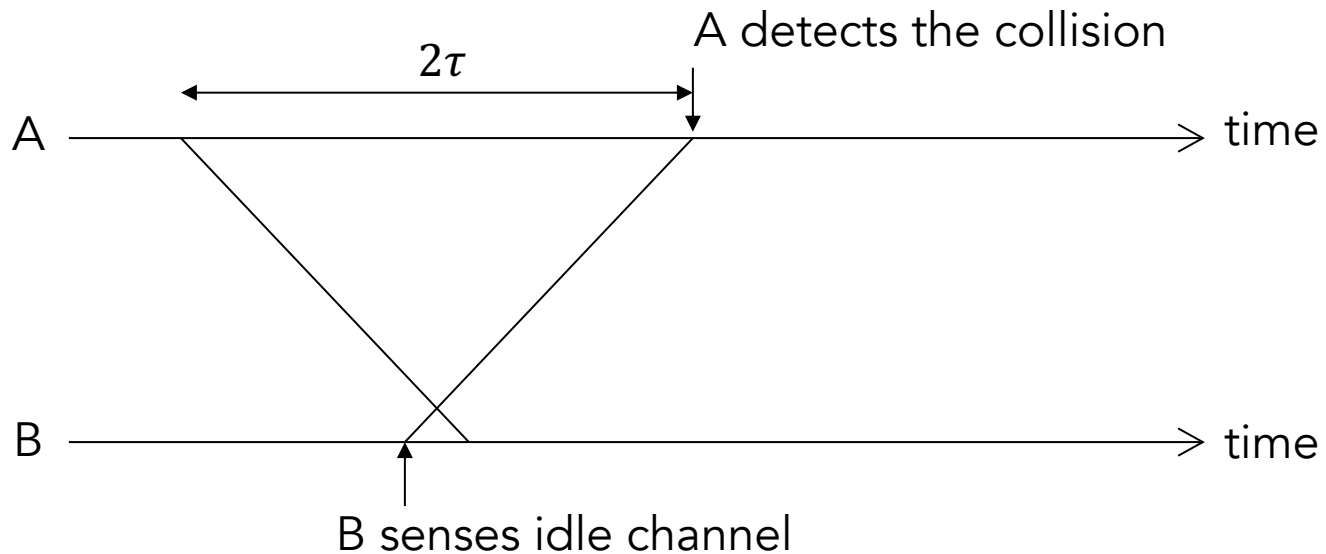
- All carrier sense protocols rely on stations being able to
 - Sense that a transmission has ended, soon after its completion
 - Sense that a transmission has started, soon after it begins
 - Need $a = \tau/m \ll 1$ for high throughput
- Suitable for
 - Local Area Network (small τ)
 - Large Networks that are low speed (large m)



Maximum Throughput of CSMA/CD

□ Collision

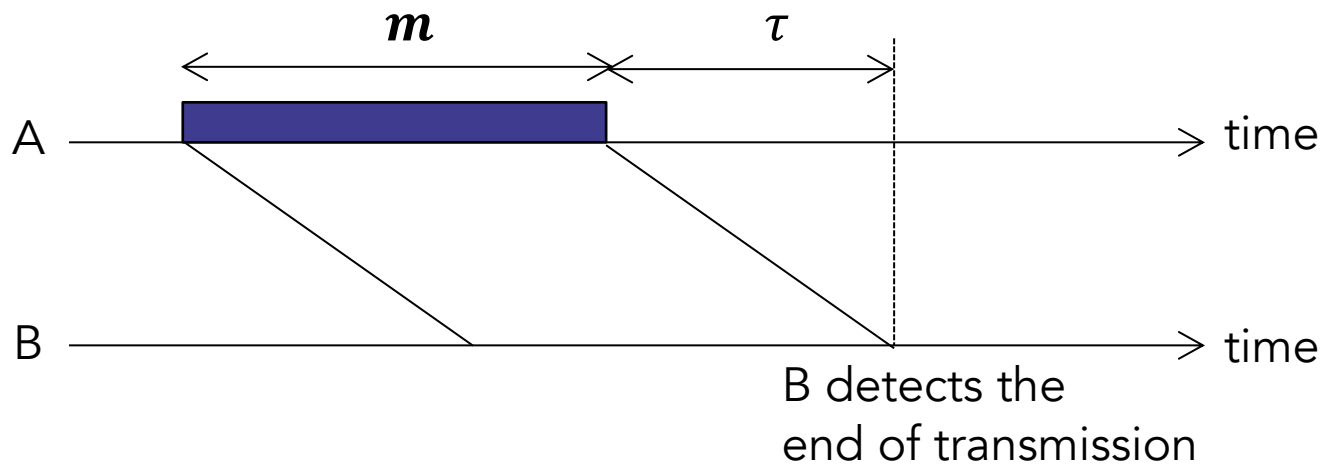
- Suppose that a collision takes place between A's & B's transmission
- In the worst case, it takes 2τ sec for A & B to detect the collision and turn off their transmissions



Maximum Throughput of CSMA/CD

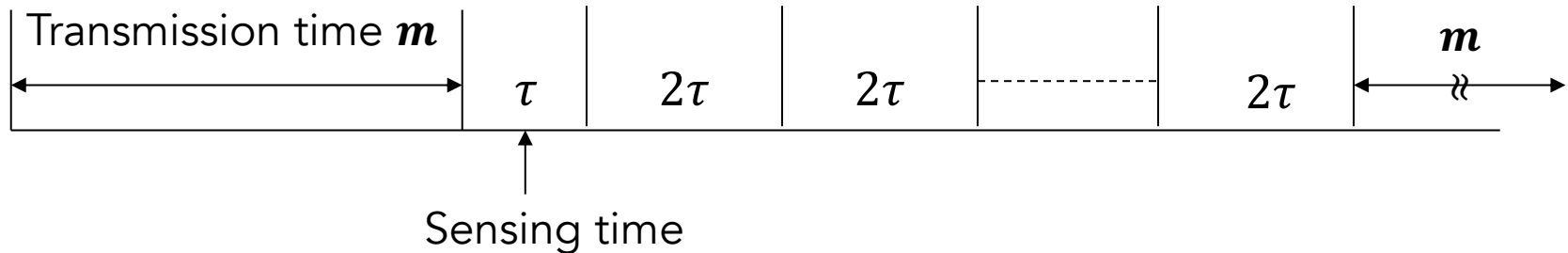
□ Sensing

- After A finishes transmission, it takes τ seconds for B to determine that A has finished transmission (idle channel)



Maximum Throughput of CSMA/CD

- Considering intervals for both collision and sensing, we consider τ and 2τ intervals after transmission as follows:



- Let J denote the expected number of 2τ intervals before a successful transmission taking place
 - J depends on the retransmission policy, e.g., binary exponential back-off etc.

Maximum Throughput of CSMA/CD

- Worst-case calculation of transmission time t_v
 - t_v is the time interval between two successful transmissions
 - Given J collisions, it takes $2\tau J$ units of time to resolve it

$$t_v = m + \tau + 2\tau J = m(1 + a(1 + 2J)), \text{ where } a = \tau/m$$

- Use a simple model of retransmissions backed by simulation
 - Assume length of collision interval is geometrically distributed in units of 2τ , with parameter $v = \Pr\{\text{no collision happens}\}$
 - Then $\Pr\{\text{collision interval} = n \cdot 2\tau\} = v(1 - v)^{n-1}$

$$J = \sum_{k=1}^{\infty} kv(1 - v)^{k-1} = \frac{1}{v}$$

- So we focus on finding v .



Maximum Throughput of CSMA/CD

□ Assume n stations are involved

- Each station attempts to transmit in a 2τ interval with probability p , independent of others

- $p = \Pr\{\text{A station wants to transmits in a } 2\tau \text{ interval}\}$

$$v = \Pr\{\text{no collisions happening}\}$$

$$= \Pr\{\text{exactly one station transmits}\}$$

$$= np(1 - p)^{n-1}$$

- $p = \frac{1}{n}$ will maximize v and provides the greatest chances of success

➔ maximized v ➔ smallest J

➔ max (worst-case) throughput.



Maximum Throughput of CSMA/CD

- Now, by setting $p = \frac{1}{n}$, we obtain that

$$v_{\max} = \left(1 - \frac{1}{n}\right)^{n-1} \rightarrow e^{-1}, \text{ as } n \rightarrow \infty$$

$$t_v = m(1 + a(1 + 2J)) = m(1 + a(1 + 2e))$$

$$\text{max throughput } \lambda_{\max} = \frac{1}{t_v} = \frac{1}{m(1 + a(1 + 2e))}$$

- Let $\rho = m\lambda_{\max}$
- Recall $a = \tau/m$: transmission time (m) must be much larger than the propagation delay (τ) for system to work well
 - If $a = 0.1$, $\rho < 0.6$
 - If $a = 0.01$, $\rho < 0.94$.

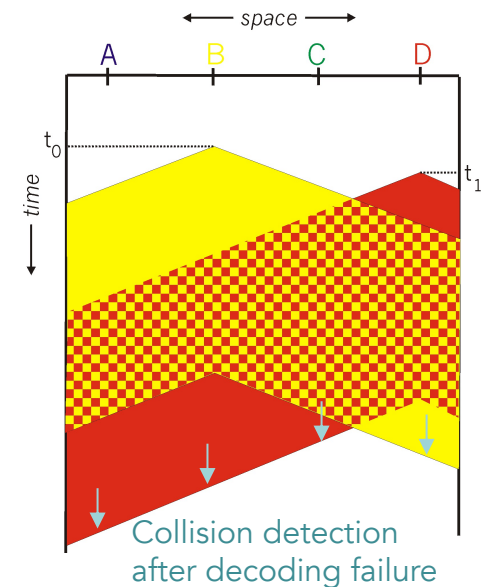


CSMA/CA

- Carrier Sense Multiple Access with **Collision Avoidance**
 - Wireless MAC protocols (like Wi-Fi) often use Collision Avoidance with carrier-sense mechanism
 - **Carrier Sense:** When a node wishes to transmit a packet, it first waits until the channel is idle
 - **Collision avoidance:** Use of a random backoff number within the maximum congestion window size

- Why not CSMA/CD?

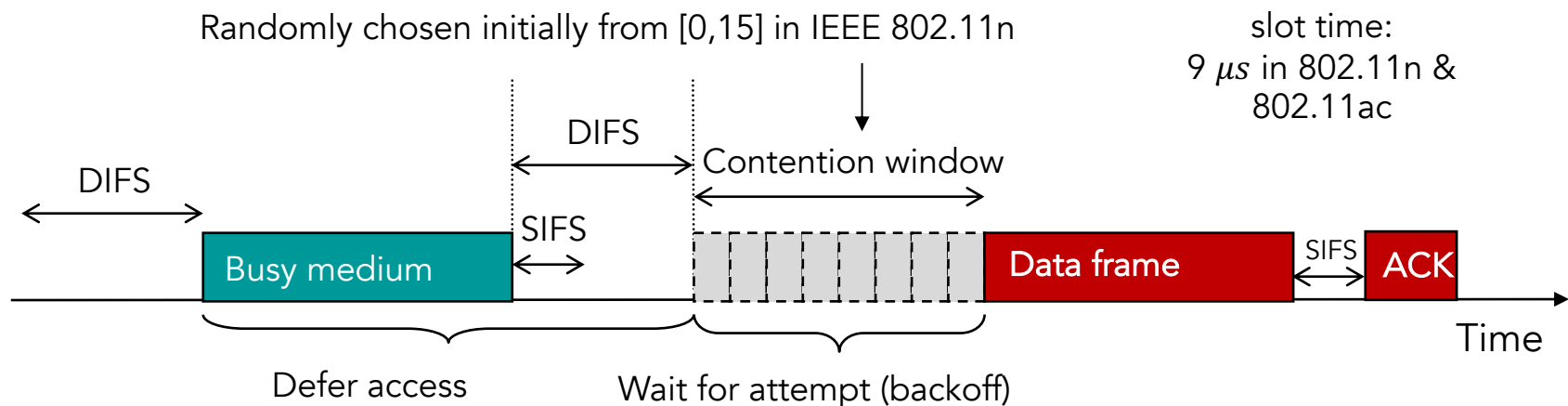
- A wireless station may NOT send data and receive collision signals at the same time
- Collision may NOT be detected in wireless networks
 - Signal fading often prevents a station of one end from hearing a collision at the other end.



CSMA/CA (802.11 DCF (distributed coordinate function))

□ Interframe spacing (of Wi-Fi; IEEE 802.11)

- Short IFS (SIFS): Typically to complete exchange in progress (i.e., between data frame and ACK), SIFS is less than DIFS
- DCF IFS (DIFS): Time to detect idle medium
- **Backoff time is (contention window) x (slot time)**
 - Contention window (cw_i) at time slot i is chosen randomly from $[0, CW[i]-1]$.
 - $CW[i]$ starts from CW_{\min} (e.g., 16) and is doubled when collision happens until it grows to Cw_{\max} (e.g., 256, 512, 1024)
 - $CW[i]$ resets to CW_{\min} when a packet transmission is successful



Example of CSMA/CA Backoff

