Step 1

Step 1: dimensional data, reflectances of the room surfaces

STEP 1. Establish dimensional data for the room. Room length, width, and height are determined by the architectural design process. In offices, schools, and many other occupancies, the work plane is typically 30 in. (760 mm) above the finished floor (AFF). In shops, 42 to 48 in. (1066 to 1220 mm); in a carpet store at floor level. The location of the working plane and placement of the lighting fixtures relative to the ceiling plane will determine the three *h* terms, representing the heights of the zonal cavities. Estimate the initial reflectances of major room surfaces (selecting reflectances that conform to those suggested by the values in Table 16.5 is fine for preliminary design). Fill in the information in a sketch, as in Fig. 16.13.

Medium-Value Colors	Reflectance (%				
White	80-85				
Light gray	45-70				
Dark gray	20-25				
Ivory white	70-80				
lvory	60-70				
Pearl gray	70-75				
Buff	40-70				
Tan	30-50				
Brown	20-40				
Green	25-50				
Olive	20-30				
Azure blue	50-60				
Sky blue	35-40				
Pink	50-70				
Cardinal red	20-25				
Red	20-40				

TABLE 15.2 Approximate Reflectance Values for Paints

From MEEB 12th Ed.

Step 2: Find CR, RCR, CCR

STEP 2. See again Fig. 16.13. Determine the three cavity ratios of the room by calculation. The basic expression for a cavity ratio (CR) is:

$$CR = 2.5 \times \frac{\text{area of cavity wall}}{\text{area of work plane}}$$
 (16.11)

In a rectangular space, the area of a given cavity wall is $h \times (2l + 2w)$ or 2h(l + w); therefore,

$$CR = \frac{2.5 \times 2h(l+w)}{\text{area of work plane}}$$
(16.12)

or

$$CR = 5h \times \frac{l+w}{l \times w}$$
(16.13)

For other than rectangular rooms, the area can be calculated as required by geometry. For instance, in a circular room, the cavity wall area = $h \times 2\pi r$ and the work plane area is πr^2 . Thus,

$$CR = \frac{2.5 \times h \times 2\pi r}{\pi r^2} = \frac{5h}{r}$$
 (16.14)

For each of the cavities in a rectangular room the cavity ratio is calculated as:

Room cavity ratio

$$RCR = 5h_{RC}\frac{l+w}{l\times w}$$
(16.15)

Ceiling cavity ratio

$$CCR = 5h_{CC}\frac{l+w}{l\times w}$$
(16.16)

Floor cavity ratio

$$FCR = 5h_{FC}\frac{l+w}{l\times w}$$
(16.17)

GENERAL INFORMATION

(Give	name of area and/or building and room number)	
2. Average maintained illumination for design:	Lux [footcandies]	
Luminaire data:	Lamp data:	
3. Manufacturer:	5. Type and color:	
4. Catalog number:	6. Number per luminaire:	
	7. Total lumens per luminaire:	

SELECTION OF COEFFICIENT OF UTILIZATION

	ρ=_% ρ=_%	hcc = ↓ I =
8. Step 1: Fill in sketch at right.	← p = _ %	h _{RC} = ↓ w=
9. Step 2: Determine Cavity Ratios by formulas.	~_ρ=_% γ ^ρ =_%	h _{FC} =
9a. Room cavity ratio, RCR =		
9c. Floor cavity ratio, FCR =		
10. Step 3: Obtain effective ceiling cavity reflectance (Pcc) from Table 16.2.	ρ _{cc} =

11. Step 4: Obtain effective floor cavity reflectance (ρ_{FC}) from Table 16.2.	ρ _{FC} =	
12. Step 5: Obtain coefficient of utilization (CU) from manufacturer's data.	CU =	

SELECTION OF LIGHT LOSS FACTORS

Unrecoverable	Recoverable
13. Luminaire ambient temperature	17. Room surface dirt depreciation
14. Voltage to luminaire	18. Lamp lumen depreciation
15. Luminaire surface depreciation	19. Lamp burnouts factor
16. Other factors (components)	20. Luminaire dirt depreciation LDD

21. Total light loss factor, LLF (product of individual factors above): _____

CALCULATIONS

(Average maintained illumination level)

	Number of luminaires -	(Illuminance) × (Area)
Number of luminaires =		(Lumens per luminaire) × (CU) × (LLF)
22.	=	
	1	(number of luminaires) \times (lumens per luminaire) \times (CU) \times (LLF)
Lux [tootcandles] =	(area)	
23.	=	=
24. Ca	Iculated by:	Date:

Fig. 16.13 Zonal cavity method calculation form. (Courtesy of IESNA.)

- Steps 3, 4: find $\rho_{\rm CC}$, $\rho_{\rm FC}$
 - Use $\rho_{\rm w}$ from Step 1
 - CCR = 0 for surface mounted or recessed fixtures
 - FCR = 0 for carpet stores (if the floor is the working plane)
- Step 5:select CU
 - From the manufacturers' data or Table 16.1 (MEEB 12th Ed.)
 - Interpolation may be necessary
 - For ρ_{Fc} other than 20%, refer to Table 16.6
- Step 6: calculate the illuminance and the number of fixtures



Fig. 16.12 Zonal cavity method flow chart.

For estimation of $\rho_{\rm CC} \rightarrow$ use $\rho_{\rm C}$, $\rho_{\rm w}$, and CCR For estimation of $\rho_{\rm FC} \rightarrow$ use $\rho_{\rm Fr}$, $\rho_{\rm w}$, and FCR

TABLE 16.5 Percent Effective Ceiling or Floor Cavity Reflectance (ρ_{CC} , ρ_{FC}) for Various Reflectance Combinations

Percent Ceilin or Floor Reflectance	ig ρC ρ _F :		9	0			8	0			70			50			3	0			10	
Percent Wa Reflectance	all Pw:	90	70	50	30	80	70	50	30	70	50	30	70	50	30	65	50	30	10	50	30	10
Ceiling or	0	90	90	90	90	80	80	80	80	70	70	70	50	50	50	30	30	30	30	10	10	10
Floor Cavity	0.2	89	88	86	85	79	78	77	76	68	67	66	49	48	47	30	29	29	28	10	10	9
Ratios—CCR	0.4	88	86	83	81	78	76	74	72	67	65	63	48	46	45	30	29	27	26	11	10	9
OFFCK	0.6	88	84	80	76	77	75	71	68	65	62	59	47	45	43	29	28	26	25	11	10	9
	0.8	87	82	77	73	75	73	69	65	64	60	56	47	43	41	29	27	25	23	11	10	8
	1.0	86	80	74	69	74	71	66	61	63	58	53	46	42	39	29	27	24	22	11	9	8
	1.2	86	78	72	65	73	70	64	58	61	56	50	45	41	37	29	26	23	20	12	9	7
	1.4	85	77	69	62	72	68	62	55	60	54	48	45	40	35	28	26	22	19	12	9	7
	1.6	85	75	66	59	71	67	60	53	59	52	45	44	39	33	28	25	21	18	12	9	7
	1.8	84	73	64	56	70	65	58	50	57	50	43	43	37	32	28	25	21	17	12	9	6
	2.0	83	72	62	53	69	64	56	48	56	48	41	43	37	30	28	24	20	16	12	9	6
	2.2	83	70	60	51	68	63	54	45	55	46	39	42	36	29	28	24	19	15	13	9	6
	2.4	82	68	58	48	67	61	52	43	54	45	37	42	35	27	28	24	19	14	13	9	6
	2.6	82	67	56	46	66	60	50	41	53	43	35	41	34	26	27	23	18	13	13	9	5
	2.8	81	66	54	44	66	59	48	39	52	42	33	41	33	25	27	23	18	13	13	9	5
	3.0	81	64	52	42	65	58	47	38	51	40	32	40	32	24	27	22	17	12	13	8	5
	3.5	79	61	48	37	63	55	43	33	48	38	29	39	30	22	26	22	16	11	13	8	5
	4.0	78	58	44	33	61	52	40	30	46	35	26	38	29	20	26	21	15	9	13	8	4
	4.5	77	55	41	30	59	50	37	27	45	33	24	37	27	19	25	20	14	8	14	8	4
	5.0	76	53	38	27	57	48	35	25	43	32	22	36	26	17	25	19	13	7	14	8	4



610 mm (2 ft) wide

TABLE 16.1 Coefficients of Utilization for Typical Luminaires with Suggested Maximum Spacing Ratios (Continued)

50

10

.62

.64

.42

.29

.25

.18

.39

.26

19

36

28

.17

.23 .20

50 30

.83 .83 .83

.75 .73 .72

.68 .65

.62 ,58

.56 .51 .47

.50 .45 .41

.45 .40 .36

.41 .36 .32

.37 .31 .28

.33 .28 .24

.72 .72 .72

.65 ,64 .62

.59

.54 .50 .48

.49

.44 .40 .37

40 .36 .33

.36 .32

.33

.29 ,25 .22

.50

.44 .42 .41

.38 .36 .34

.34 .31 .28

.30 ,27 .24

.26 .23 .20

.24

.21 .18 .15

.19 .16 .13

.17

.72 .72 .72

.64 .62 .60

.57 .54 .51

.51 .48 .45

.46 .42

.41 .37 .34

.38 .33 .30

.34

30 .26 -22

.27 .23

.56 .56 .56

.50 .49 .48

.45 .43 .41

.41

.37 .34 .32

.34 .30

.31 27 25

.28 .25 .22

.25 22 .20

.23

.70 .70 .70

F3. 82 .60

.57 .54 .52

52 .48 45

.47 .43 .40

.42

.38 .34 .30

.34 .30 .27

.31 .26

.20

.24

0

.23 .20 .28 .57 .54

.45

.28

.50 .50

,20

.14 .12

.29

38

.20

.38 .34

.23

0

0

66

.59

.52

A6

.41

.36

.31

.27

.24

20

.56

50

.45

40

36

.31

.28

.25

21

.19

12

10

.00

.07

.06

.05

.05

.04

03

.03

59

.50

.44

.38

34

.29

26

.23

19

17

.50

44

39

34

.30

.26

23

.21

18

16

:63

,55

49

.43

37

.33

29

25

22

19

TABLE 16.6 CU Adjustment Factors for Effective Floor Cavity Reflectances Other Than 20% (Any Wall Reflectance)^a

For 30% effective floor cavity reflectance, *multiply* the CU value for 20% floor cavity reflectance by the appropriate factor from the following table.

For 10% effective floor cavity reflectance, *divide* the CU value for 20% floor cavity reflectance by the appropriate factor from the following table.

	Percent Effective Ceiling Cavity Reflectance, ρ _{cc}								
Room Cavity Ratio	80	70	50	10					
1	1.08	1.06	1.04	1.01					
2	1.06	1.05	1.03	1.01					
3	1.04	1.04	1.03	1.01					
4	1.03	1.03	1.02	1.01					
5	1.03	1.02	1.02	1.01					
6	1.02	1.02	1.02	1.01					
7	1.02	1.02	1.01	1.01					
8	1.02	1.02	1.01	1.01					
9	1.01	1.01	1.01	1.01					
10	1.01	1.01	1.01	1.01					

Source: Extracted from the IESNA Lighting Handbook (1993); reprinted with permission.

^aFor more precise data that address varying p_W values, see the current *IESNA Lighting Handbook*.

Example in 12th Ed.

Fluorescent lamp used

Example 16.1 (12th Ed.)

EXAMPLE 16.1 It is suggested that the reader photocopy Fig. 16.35 and fill it in as the solution to this example is developed.

Given. Assume a classroom with dimensions of $(W \times L \times H)$: 6 m \times 8 m \times 3.7 m (19.7 \times 26.3 \times 12.1 ft), at an elementary school. Initial reflectances are: ceiling 80%, entire wall 50%, floor 20%. (Note that the sketch in Fig. 16.35 can accommodate different reflectances for the upper, center, and lower

wall sections.) The goal is to provide adequate illuminance using fluorescent fixtures. Assume yearly maintenance, lamp replacement at burnout, proper voltage and ballasts, and a medium clean atmosphere.

- (a) illuminance target
 - IESNA handbook: 500 Lux
 - Lines 1, 2, and 8 of Fig 16.13

(b) Luminaire selection

- for a classroom situation
 - Low direct glare (high VCP): a large proportion of their time in a heads-up position
 - Low veiling reflections because of the seeing task
 - High efficiency and low energy use to meet ANSI/ASHRAE/IESNA Standard 90.1 and most governmental requirements
 - Minimum maintenance: poor cleaning and maintenance situation in many schools
- indirect lighting is not chosen (although the ceiling height is sufficient)
 - Indirect lighting depends on a highly reflective ceiling, requiring yearly cleaning and repainting at intervals not exceeding 5 years. This is not generally the case in public schools.
- Luminaire No. 44 from Table 16.1 (12th Ed.) chosen
 - Two lamp fluorescent unit with louvers that exhibit 45° cutoff and crosswise batwing distribution

TABLE 16.1 Coefficients of Utilization for Typical Luminaires with Suggested Maximum Spacing Ratios (Continued)

	Typical Distribution		4	80		-	70			50	_	0
	Lumens	pw2 -	> 50	30	10	50	30	10	50	30	10	0
Typical Luminaire	Mainténance Maximum Calegory S/MH	RCR	(Coefficients of Utilization for 20% Effective File (pts = 20)						floor Ca	ectance	
44	IV N.A.	0	.71	.71	.71	70	.70	.70	.66	.66	.66	,60
	C	t	.65	.63	.61	.63	.62	.60	.51	.59	.58	.54
12	061	2	.59	.55	.53	.58	.55	.52	.55	.53	.51	.48
		3	.53	-49	.46	52	.48	.45	50	.47	.45	.42
	111	4	.47	.43	.40	.47	.43	.40	.45	.42	.39	,37
	00 ·	5	.42	,38	.34	.42	.37	.34	.41	.37	.34	.32
A-4	45).	6	.38	.33	.30	38	.33	.30	.37	.33	30	.28
		7	.34	.29	.26	.33	.29	.28	.33	.28	25	,24
Radial batwing distribution-		8	.30	.25	.22	30	.25	.22	.29	.25	22	.20
louvered fluorescent unit		9	27	.22	18	26	22	18	26	.21	18	.17
			-						-			

(c) Steps

- For easy maintenance, the mounting height is 1.95m (MH=h_{RC}=1.95m=2.7m-0.75m)
- The recommended maximum S/MH: 1.5-2.0

STEP 1. The required data that should appear in the sketch in Fig. 16.35 are

$h_{\rm RC} = 1.95 {\rm m}$
/= 8 m
$p_w = 50\%$
w = 6 m

STEP 2. From Equations 16.8, 16.9, and 16.10

$$\frac{l+w}{l\times w} = 0.29$$

RCR = $5h_{RC}\frac{l+w}{l\times w}$
RCR = $5(1.95)(0.29) = 2.84$
CCR = $5(1)(0.29) = 1.46$
FCR = $5(0.75)(0.29) = 1.09$

STEP 3. From Table 16.2 obtain effective reflectances: For ρ_{CC} use $\rho_{C} = 0.8$, $\rho_{W} = 0.5$, and CCR = 1.46. Therefore,

$$p_{CC} = 0.61$$

STEP 4. For ρ_{FC} use $\rho_F = 0.2$, $\rho_W = 0.5$, and FCR = 1.09. Therefore,

 $\rho_{FC} = \frac{0.18}{0.19}$ by interpolation

(c) steps

STEP 5. Interpolation between RCR of 2.8 and 3.0 is necessary. The CU for the selected luminaire-No. 44 of Table 16.1-can now be obtained by double interpolation.

ρ W = 0.50		CU	
pCC →	0.70	0.61	0.50
RCR			
2.0	0.58		0.55
2.84		?	
3.0	0.52		0.50

Design CU = 0.52. No correction from Table 16.3 is required, as ρ_{FC} is close to 20%. At this stage, lines 9 through 12 of Fig. 16.35 can be filled in.

STEP 6. The LLF (see Section 16.20) results from establishing items 13 to 20 of Fig. 16.35. These are:

Items 13–16	0.88	
Item 17	0.92 ((direct lighting)
Item 18	0.85	(Fluorescent, replacement on burnout)
Item 19	0.95	(individual replacement on burnout)
Item 20	0.80	(Category IV \leftarrow Table 16.1)
Item 21: LLF = (0.88)	0.92 (0.85	5)(0.95)(0.80) = 0.54

$$N = \frac{(500 \text{ lux})(6 \times 8 \text{ m})}{2(3200 \text{ lm})(0.52)(0.54)} = 13.35$$



Luminaire layout

- the room be treated as a single (student area & teacher area)
- Two lengthwise rows for VCP
- The window wall row has a separate switch and is farther from the wall than the inside row due to the daylight.
- To prevent reflected glare, the sixth fixture in the outside row is off the line.
- For chalkboard lighting, two single lamp installed
- The number of fixtures: 11 + 0.5 + 0.5 = 12
 - The number of required fixtures: 13.35
 - Actual minimum maintained lighting level: 12/13.35 * 500 = 450 Lux
 - The designer must decide if this is OK.



Fig. 16.36 Layout of pendant parabolic aluminum reflector luminaires in a typical classroom. The units have a modified batwing distribution in the crosswise direction, which mandates their being hung with their long axis parallel to the line of sight, as shown. Furthermore, the fixtures have lower brightness in that direction, that is, VCP for students in the head-up position is excellent. Note that the distance between the outside fixture row and the window wall is more than one-half of the side-to-side spacing because of daylight contribution during school hours, whereas the inside fixture row to inside wall spacing is less than one-half of the side-to-side spacing in order to maintain sufficient illuminance near that wall. The single fixture to the right of the teacher's desk (to the teacher's left) was so placed to avoid the veiling reflections that would result from a fixture directly above the desk and to take advantage of the fixture's transverse batwing distribution characteristic.

Example 16.2

EXAMPLE 16.2 Assume a large modern business office, with dimensions of ($L \times W \times$ hung ceiling H) 60 ft \times 100 ft \times 8 ft (18 \times 30 \times 2.4 m). Initial reflectances are 0.80, 0.50, and 0.30. Provide general lighting using fluorescent lamps with high-efficiency ballasts in recessed troffer luminaires. The space is fully air-conditioned. Lamps are replaced on a burnout basis, and the fixture is then cleaned.

- Illuminance: 500 Lux
- Luminaires with parabolic diffusers, reflectors, and/ or baffles, which exhibit very low high-angle luminance.

- Office workstation: halfheight partitions, varying viewing directions → Luminaire's directionality is negative.
- A specular parabolic baffled 2ft square unit selected: two 32W, T8, with 2,800 initial lumens (Fig. 16.37, CDC, CU)
- Category I

REK D/RIK-D 2/31-U

Stieling angle : Farl. 50 - Norm. 50

Recessed moustan luminaire with parabolic mirrored louver (without mirrored reflector)





1		CO	EFF	IC	IE	EN	TS	C	F	U	TI	LI	ZA	T.	10	N		_	
				L	IMI	NAT	AE	EFF	101	IEN	CY :							0.	61
TACT.	CETLING PCC		60		2	70		1	50	-1	- 30			10			a		
	WAL	LS	ρ_{W}	50	30	10	50	30	10	10	30	10	50	39	10	50	30	10	g
뒲	FL.	NOFI	$\rho_{\rm FC}$	20	21	20	20	20	20	20	20	20	20	29	20	20	20	50	20
	1	1		54	61	59	62	60	58	EO	58	55	57	\$55	54	55	54	53	52
AT10 - ROR	2		37	54	51	35	53	50	24	51	43	52	50	48	50	48	47	45	
	3		53	49	4B	53	49	46	51	48	45	49	47	44	48	45	44	42	
	4		49	45	42	49	45	41	17	44	41	16	43	40	45	12	40	39	
	5		45	41	38	45	41	37	14	40	37	42	39	37	-41	39	38	33	
1	5		42	37	34	41	37	34	40	35	33	39	35	33	38	拓	33	32	
11	7		38	34	30	38	33	30	37	33	30	36	33	30	35	32	30	20	
2	8		35	31	26	35	31	26	24	30	27	33	30	27	33	30	27	26	
ĝ.	9		11	30	26	33	28	26	12	28	5	31	28	25	31	28	25	24	
-	11	10		30	26	23	30	26	27	30	25	24	20	26	23	29	35	21	72
-	1	CON	AL S	UMN	AR	Y				T	1	VG		1	cd/	m²	1		
ZONE LONENS				T	LAM	P	1	FIX	1	0	G.	N	NRO	1	4	5'	1	AR	
- 0	0 - 30 1455			25	41.0		5 3		5091		5041		4295		5				
0 - 10 2420		-	41.	41.7		68.2		50		3	3092		3009		2624		1		
0 - 50 4312		-	57.1		92.3		30		-	00		/35		665		-			
0 - 70 1550		-	61.4		00.9		15		-	75		1 1		1 15					
0 - 90 3640		-	51	2		100	0	70			35		15		34		7		
90	- 180		0		E.1	0		0.	1	1.1	75		28		14			21	
0 - 140 3550			61.1	2		100.	0	19-13	BO .		31		1	21 3		31			

Fig. 16.37 Complete photometric data on a 2-ft (610-mm) square fixture with a 36-cell mirrored parabolic louver. The unit uses two T8 U-shaped 32-W fluorescent lamps. Note that the transverse distribution characteristic has a modified batwing shape typical of this type of louver. The louver's specular finish yields very low brightness at high angles, as can be seen from both the distribution curve and the luminance (cd/m²) data. (Courtesy of Zumtobel-STAFF.)

Calculations. The reader should fill in a copy of Fig. 16.35 as we proceed. The working plane is taken as the desktop height (i.e., 30 in. or 2.5 ft).

STEP 1. $h_{CC} = 0$; $h_{RC} = 5.5$; $h_{FC} = 2.5$.

STEP 2. CCR = 0; RCR = 0.73; FCR = 0.33.

STEP 3. $\rho_W = 50\%$; $\rho_{CC} = 80\%$ (for a recessed fixture we use the ceiling reflectance).

STEP 4. From Table 16.2, $p_{FC} = 29\%$.

STEP 5. We find CU for $\rho_{FC} = 20\%$ by extrapolation:

RCR	CU	
0.73	?	
1.0	0.64	CU = 0.66
2.0	0.57	

STEP 6. From Table 16.3, the multiplier for $\rho_{FC} = 30\%$ (close to 29%) is 1.085.

STEP 7. Final CU = 1.085 (0.66) = 0.72.

STEP 8. LLF per Fig. 16.35:



Zonal Cavity calculation by approximation

- reasonable approximation of Zonal Cavity Calculation (B.F. Jones, 1983)
- Assumptions
 - all rooms are square
 - RCR, ρ_{CC}, ρ_{FC}, LLF (refer to Fig.16.38)



Fig. 16.38 Sheet for illuminance calculation using an approximate zonal cavity method (based on a method developed by B. F. Jones).

EXAMPLE 16.3 Classroom as in Example 16.1 by approximation.

1. "Square" the room.

$$w_{\rm SQ} = 6 + \frac{8 - 6}{3} = 6\frac{2}{3}$$

2. Assume

$$\rho_{CC} = 70; \ \rho_{W} = 50; \ \rho_{FC} = 20$$

3. Calculate RCR

$$RCR = \frac{10 \times 1.95}{6\frac{2}{3}} = \frac{19.5}{6.66} = 2.93$$

 Obtain CU from Table 16.1, fixture No. 44. CU = 0.52 by visual inspection.

5. Calculate fixtures

$$N = \frac{500(6 \times 8 \text{ m})}{2(3200)(0.52)(0.55)}$$

= 13.11 fixtures

Thus, the result is substantially the same as the accurate calculation. Let us also check Example 16.2. ■

EXAMPLE 16.4 Office as in Example 16.2 by approximation.

1.
$$w_{SQ} = 60 + \frac{100 - 60}{3} = 73 \text{ ft}$$

2. $\rho_{CC} = 80; \rho_w = 50; \rho_{FC} = 20$
3. $RCR = \frac{10 \times 5.5}{73} = \frac{55}{73} = 0.75$
4. $CU = 0.66$ by inspection (mental interpolation)
5. $LLF = 0.55$
6. $area / luminaire = \frac{2 \times 2800 \times 0.66 \times 0.55}{50 \text{ fc}}$

 $= 40.6 \, \text{sq ft} \, (3.8 \, \text{m}^2)$

This result is within 5.5% of the more precise calculation. Thus, we see that these simple approximations give answers sufficiently accurate for most uses and are therefore recommended.

Conclusions

- For preliminary calculations of rectangular rooms: use the simple method (Fig. 16.38)
- For rooms where a high degree of accuracy is desired and actual reflectances are known, use the long method
- For rooms of unusual shape or rooms with special conditions (coffered ceilings, mixed-material walls, partial height partitions): use lighting simulation
- For spaces in which a number of different solutions are to be tried, use lighting simulation

Example in 13th Ed.

LED used

Example 16.1 (p.783)

EXAMPLE 16.1 Fig. 16.13 is a compact and useful worksheet for zonal cavity calculations—using this worksheet to track these examples is recommended. To simplify this example, it is worked using only SI units; the exact same process would apply with I-P units.

Given. Assume a classroom with dimensions of (W \times L \times H): 6 m \times 8 m \times 3.7 m, in an elementary school. Initial surface reflectances are: ceiling 80%, entire wall 50%, floor 20%. (Note that the Fig.16.13 worksheet can accommodate different reflectances for the upper, center, and lower wall sections.) The basic lighting objective is to provide adequate illuminance using LED fixtures. Assume a yearly maintenance cycle, lamp replacement at burnout, proper voltage and ballasts, and a medium-clean dirt condition. Considering the above, select luminaire *type a* from Table 16.4 as an initial informed trial fixture. This selection would meet requirements 1 through 4.

Although its distribution curve (see Table 16.4) shows no upward component, some fixtures of this basic design have slots in the top of the reflector to provide a 5% to 10% uplight component. In practice, such a unit would avoid an excessively dark ceiling and high luminance ratios between fixture and background. The mounting height is assumed as 2.7 m to permit an uplight component. The recommended maximum SC would be between 1.5 and 2.0. The work plane height is 750 mm.

Example 16.1 (p.783)

STEP 1. The information that should appear in the sketch in Fig. 16.13 is:

$$\begin{array}{ll} h_{\rm FC} = 1.0 \, {\rm m} & h_{\rm RC} = 1.95 \, {\rm m} \\ h_{\rm FC} = 0.75 \, {\rm m} & l = 8 \, {\rm m} \\ \rho_{\rm C} = 80\% & w = 6 \, {\rm m} \\ \rho_{\rm F} = 20\% & \rho_{\rm W} = 50\% \end{array}$$

STEP 2. Determine the three cavity ratios as follows:

$$\frac{l+w}{l\times w} = 0.29$$
$$RCR = 5h_{RC}\frac{l+w}{l\times w}$$

STEP 3. Obtain effective reflectances from Table 16.5. For ρ_{CC} use $\rho_{C} = 0.8$, $\rho_{W} = 0.5$, and CCR = 1.46. Thus,

$$p_{\rm CC} = 0.61$$

STEP 4. To determine ρ_{FC} use $\rho_F = 0.2$, $\rho_W = 0.5$, and FCR = 1.09. Thus,

 $\rho_{FC} = \frac{0.18}{0.19}$ (by interpolation)

$$RCR = 5(1.95)(0.29) = 2.84$$

 $CCR = 5(1)(0.29) = 1.46$

FCR = 5(0.75)(0.29) = 1.09

STEP 5. With a room cavity ratio of 2.84, the CU for the selected luminaire—*type a* (direct distribution)—can be extracted from Table 16.4 by interpolation.

$ \rho_{w} = 0.50 $	CU						
$\rho_{CC} \rightarrow$	0.70	0.61	0.50				
RCR	APPEND		(Version)				
2.0	0.94	-2	0.91				
2.84		?					
3.0	0.85		0.82				

The CU = 0.85. No correction from Table 16.6 is required, as ρ_{FC} is close to 20%. At this point, lines 9 through 12 of Fig. 16.13 can be filled in.

STEP 6. The LLF (see *light loss factor* subsection) is established by estimating items 13 to 20 in Fig. 16.13. These are assumed as:

Items 13–16 (collectively)	0.88
Item 17	0.92 (direct lighting)
Item 18	0.87 (LED, replacement on burnout)
Item 19	0.95 (individual replacement on burnout)
Item 20	0.80 (Category IV)
Item 21: $LLF = (0.88)((0.92)(0.88))$	(0.95)(0.80) = 0.535

Significant improvement in CU compared to FL !!

STEP 7. Complete the illuminance calculation. A typical classroom normally consists of a student seating area and a teacher's area. The illuminance requirement is approximately the same for both, so the room can be treated as a single entity for visual task purposes. Assuming 7900 lumens (at 4000K and 80 CRI) per luminaire, the number *N* of luminaires required to provide design illuminance is:

$N = (500 \text{ lx})(6 \times 8 \text{ m}) / (7900 \text{ /m})(0.85)(0.54)$ = 6.6

The use of 6.6 fixtures is not possible, so the designer would need to decide whether 6 fixtures would be adequate (this would provide a maintained illuminance of 455 lux—substantially below the design target) or whether 7 or 8 fixtures should be used. Eight fixtures would simplify luminaire layout in the ceiling plane but result in substantially more illuminance than required; an eight-fixture layout might also better conform to the recommended SC limits for the luminaire. Perhaps a similar fixture with somewhat lower lumen output could be used. Lighting design does not stop with the fixture count.

The remaining lines of Fig. 16.13 can now be completed.

.uminaire Type	Photometric Distribution	RCC→ RW→ RFC→	80 80 80 50 30 10 20 20 20	70 70 70 50 30 10 20 20 20	50 50 50 50 30 10 20 20 20	30 30 30 50 30 10 20 20 20	10 10 10 50 30 10 20 20 20	MDDCL
a. direct		RCR1 0 1 2 3 4 5 6 7 8 9 10	119 119 119 107 103 100 96 90 85 86 79 74 77 70 64 69 61 55 63 55 49 57 49 43 51 43 37 46 38 32 42 34 29	116 116 116 105 101 99 94 89 84 85 78 73 76 69 64 68 61 55 62 54 49 56 48 43 50 43 37 45 38 32 41 34 29	111 111 111 101 98 96 91 86 82 82 76 72 74 68 63 66 60 55 60 53 48 54 47 42 49 42 37 44 37 32 40 33 28	106 106 106 97 95 93 87 84 81 79 75 71 72 66 62 64 59 54 59 52 48 53 47 42 48 41 37 43 37 32 39 33 28	102 102 102 93 91 90 84 82 79 77 73 69 70 65 61 63 58 54 57 52 46 47 41 37 42 36 32 38 32 28	0.301 0.288 0.270 0.255 0.242 0.227 0.214 0.204 0.194 0.184
a. direct-indirect		0 1 2 3 4 5 6 7 8 9 10	105 105 105 93 89 86 82 76 71 72 65 60 64 57 51 57 49 44 51 43 38 46 38 32 41 33 28 37 29 24 33 26 21	96 96 96 85 82 79 75 70 66 66 61 56 59 53 48 53 46 41 47 40 35 42 35 30 38 31 26 34 27 23 31 24 20	79 79 79 70 68 66 62 59 56 55 51 48 50 45 41 44 39 35 40 34 30 36 30 26 32 27 23 29 23 20 26 21 17	64 64 64 57 55 54 51 48 46 45 42 40 41 37 34 36 33 30 33 29 26 29 25 22 26 22 19 24 20 17 21 17 15	49 49 49 44 43 43 40 38 37 36 34 32 32 30 28 29 26 24 26 23 21 23 21 18 21 18 16 19 16 14 17 14 12	0.138 0.130 0.121 0.114 0.108 0.101 0.095 0.090 0.086 0.081
		0 1 2 3 4 5 6 7 8 9 10	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	89 89 89 78 76 73 69 65 61 61 56 51 55 49 44 49 42 38 44 37 33 39 33 29 36 29 25 32 26 22 29 23 19	68 68 68 60 58 57 53 50 48 48 44 41 43 38 35 38 34 30 34 30 26 31 26 23 28 23 20 25 21 18 23 19 16	48 48 48 43 42 41 39 37 35 35 33 31 31 29 27 28 25 23 25 23 20 23 20 18 21 18 16 19 16 14 17 14 12	31 31 31 28 27 27 25 24 24 23 22 21 21 19 18 19 17 16 17 16 14 16 14 13 14 12 11 13 11 10 12 10 9	0.058 0.057 0.054 0.051 0.049 0.046 0.044 0.044 0.042 0.041 0.039

ABLE 16.4 Coefficients of Utilization for Three Typical LED Luminaires

bbreviations: RCC = effective reflectance of ceiling cavity; RW = average reflectance of wall surfaces; RFC = effective reflectance of floor cavity; RCR = room cavity ratio; WDRC = wall direct radiation vefficient

nese values and images were extracted by the authors from data generously provided by TRILUX gmbH & Co. for the following luminaires: type a-direct: ArimoS Sky; type b-direct-indirect: LuceoS H1-L; nd type c-indirect: Parelia H-L.

WDRC

WDRC: The ratio of the wall illuminance caused by that component of light from luminaires in a room cavity that arrives without being reflected by room surfaces to the quotient of the total lamp flux divided by the floor area.

Example 16.2 (p.784)

EXAMPLE 16.2 Assume a large business office, with dimensions of ($L \times W \times$ hung ceiling H) 60 ft \times 100 ft \times 8 ft. Initial reflectances (ceiling, wall, floor) are 0.80, 0.50, and 0.30. Provide uniform illuminance using LED fixtures. Lamps are replaced on a burnout basis, and the fixture is then cleaned.

SOLUTION

Because of the low ceiling height specified, a direct luminaire (such as *type a* in Table 16.4) will be required; this luminaire will be installed in the ceiling plane and will have only a direct distribution component. A section through such a fixture, and its characteristic lumen distribution curve, are shown in Table 16.4.

Calculations. This example is developed using only I-P units; the procedure would be the same using SI units. The working plane is taken as the desktop height (i.e., 30 in. or 2.5 ft).

STEP 1. $h_{CC} = 0$; $h_{RC} = 5.5$; $h_{FC} = 2.5$.

STEP 2. CCR = 0; RCR = 0.73; FCR = 0.33.

STEP 3. $\rho_W = 50\%$; $\rho_{CC} = 80\%$ (for a recessed or surface mounted fixture there is no ceiling cavity and the ceiling reflectance is ρ_{CC}).

STEP 4. From Table 16.5, $\rho_{FC} = 29\%$.

STEP 5. For a RCR of 0.73 and a ρ_{FC} of 20%, the CU can be found by extrapolation:

RCR	CU
0	119
0.73	?
1.0	107

For a RCR of 0.73, CU is interpolated from Table 16.4 as 110. Even though this value is mathematically correct, it is physically impossible. A luminaire cannot deliver more light than it produces. The problem in this case is that the CU tables for LED fixtures give quirky results at low RCR values due to the procedures used to develop the tables. As a workaround, it is suggested that a CU value of 95 (0.95) be used in this case—as a compromise between the data and reality. **STEP 6.** From Table 16.6, the multiplier for $\rho_{FC} = 30\%$ (close enough to 29% to avoid interpolation) is 1.085.

110 119

STEP 7. Final CU = $1.085 \frac{(0.95)}{(0.95)} = \frac{1.0}{1.0}$ (rounded down to not mess with the laws of physics).

STEP 8. LLF following the steps in Fig. 16.13:

1.0	0.92 (direct lighting)
1.0	0.87 (LED, replacement on burnout)
0.9	0.95 (individual replacement on burnout)
0.92	0.80 (Category IV)

LLF = 0.503

STEP 9. Using the area per luminaire approach for this large space:

area/luminaire = (7900 lm) (1.0 CU) (0.54 LLF) /

50 fc design target

area/luminaire = 85 ft^2 79.4 ft²

An area of 85 ft² per fixture feels excessive and might lead to non-uniformity of illuminance. As in Example 16.1 (the school classroom), finding an LED luminaire with lower lumen output would increase the required number of fixtures and decrease the area served per fixture.

Zonal Cavity calculation by approximation

EXAMPLE 16.3 Consider the classroom as in Example 16.1, but by approximation.

1. "Square" the room.

$$W_{\rm SQ} = 6 + \frac{8-6}{3} = 6^2/_3$$

2. Assume:

$$\rho_{CC} = 70; \, \rho_{W} = 50; \, \rho_{FC} = 20$$

3. Calculate RCR.

$$\text{RCR} = \frac{10 \times 1.95}{6^2/_3} = \frac{19.5}{6.66} = 2.93$$

- Obtain CU from Table 16.4, fixture type a. CU = 0.85 by visual inspection.
- 5. Calculate required number of fixtures (N).

$$N = (500)(6 \times 8m) / (7900)(0.85)(0.55) = 6.5$$

Thus, the approximate result (6.5) is substantially the same as from the more detailed calculations (6.6). Next, consider the analysis in Example 16.2 by approximation. **EXAMPLE 16.4** Consider the office as in Example 16.2, but by approximation.

1.
$$W_{SQ} = 60 + \frac{100 - 60}{3} = 73 \, \text{ft}$$

2.
$$\rho_{CC} = 80; \rho w = 50; \rho_{FC} = 20$$

3. RCR =
$$\frac{10 \times 5.5}{73} = \frac{55}{73} = 0.75$$

- 4. CU = 1.0 by inspection (eyeball interpolation); reduced to 0.95 as discussed in Example 16.2
- 5. LLF = 0.55
- 6. area/luminaire = (7900)(0.95)(0.55)/50 fc

$= 82.6 \, \text{ft}^2$

This approximate result (82.6) is within 5% of the more precise calculation result (85). Thus, these simple approximations give answers sufficiently accurate for most uses.

Step 1:

Jones).

GENERAL INFORMATION

 (a) Project identification:
 (Give name of area and lor building and room number)

 (b) Average maintained illumination for design:
 lux [footcandles]

 Luminaire data:
 Lamp data:

 (c) Manufacturer:
 (e) Type and color:

 (d) Catalog number:
 (g) Total lumens per luminaire:

SELECTION OF COEFFICIENT OF UTILIZATION



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Effect of cavity reflectances on illuminance (1)

- N = X / CU
 - No. of luminaires = E * Area / (lamps per fixture * initial lumens per lamp * CU * LLF)
- The impact of the reflectances of the various room cavities on CU
 - Fig. 16.15: semi-indirect
 - Fig. 16.16: direct-indirect
 - Fig. 16.17: direct (spread)
- For indirect lighting: ceiling cavity reflectance
- For direct lighting: floor reflectance



Fig. 16.15 Effect of surface reflectances on the CU of a luminaire with semi-indirect distribution. As expected, because the ceiling becomes the secondary light source, its reflectance has the most pronounced effect. With this particular fixture having a 25% downward component, the floor finish also has an appreciable effect, increasing the CU by an average of 10% for a 30% reflectance floor. The effect of wall reflectance increases as rooms become smaller and the proportion of wall surface becomes larger. The change in CU between a 30% and a 50% reflectance wall varies from 15% for a 400-ft² (37-m²) room to 5% for a 4000-ft² (372-m²) room. (Redrawn with SI units by Lisa Leal.)

- For indirect and semi-indirect: the ceiling reflectance has the most pronounced effect.
- The floor finish also has an appreciable effect: increasing CU by 10% for a 30% reflectance floor.
- The effect of wall reflectance naturally increases as rooms become smaller.
- The change in CU between a 30% and a 50% wall reflectance varies from 15% for a 400ft² (37m²) room to 5% for a 4,000 ft² (372m²) room.





- Fig. 16.16 (direct—indirect)
 - The effects of the ceiling and floor are most pronounced. (Fig.16.16(a) & Fig.16.16(b))
 - The wall reflectance effect is appreciable in small rooms. (Fig.16.16(c))



Fig. 16.16 Effect of surface reflectances (a: floor, b: ceiling, c: wall) on the CU of a luminaire with direct–indirect distribution. With such distribution, the effects of the ceiling and floor are most pronounced, with an appreciable wall effect only in small rooms. (Redrawn with SI units by Lisa Leal.)

- Fig. 16.17 (direct spread)
 - Floor finish is most important
 - Wall reflectance is important only in small rooms.
 - As these fixtures have no upward component, all ceiling illumination is derived from reflection. Thus, in a room with floor reflectance of less than 20%, ceiling finish has no effect on room illumination.



Fig. 16.17 Effect of surface reflectances on the CU of a luminaire with direct (spread) distribution. Floor finish is most important, with wall reflectance important only in small rooms. As these fixtures have no upward component, all ceiling illumination is derived from reflection. Thus, in a room with floor reflectance of less than 20%, ceiling finish has no effect on room illumination.

Effect of cavity reflectance on illuminance (2)

- Lighting costs amount to 3-5% of the total construction cost, such as offices.
- A 20% differential in lighting fixtures can amount to as much as 1% of the total construction cost.
 - N =X/CU (\rightarrow CU increased by 25%, N decreased by 20%)
- Reduced number of lighting fixtures
 - Reduced construction cost, reduced electricity use, reduced maintenance cost (relamping), reduced internal heat generation, HVAC system downsizing, reduced fan energy, reduced cooling energy
- Performance assessment in stakeholder dialogues
 - Stakeholders: lighting designer, HVAC designer, architect, construction manager, owner, occupant, etc.
 - Blind belief should be avoided. → uncertainty analysis & sensitivity analysis

Calculating illuminance at a point

- The IESNA lumen method: uniform illuminance assumed.
- The lumen method is inapplicable to the following:
 - Nonuniform lighting layout
 - Other than horizontal (e.g., wall-washers)
 - Architectural lighting elements (e.g. coves, valances, etc.)
 - Nonstandard light sources (CU data are not available).
- Three methods
 - Design aids: isolux charts, illuminance "cone" charts, illuminance tables and charts.
 - Longhand calculation: Fig.16.22
 - Lighting simulation tools

Architectural lighting

Refer to Ch.17: residential lighting





Examples of cove lighting

Design aids

- Curves, charts, plots and tables prepared by the luminaire manufacturer, designer
- Types
 - Isolux charts (Fig.16.19)
 - Illuminance "cone" charts (Fig. 16.20)
 - Illuminance tables and charts (Fig. 16.21)

Isolux charts

- Called isofootcandle charts
- Use of an isolux diagram for a single luminaire (Fig 16.19 either calculated or measured)
- A sum of the illuminance contribution of every other luminaire



Fig. 16.19 The ellipses represent isolux lines for a single luminaire at a given height above the work plane. They are centered on the point (the work area of a desk) for which the illuminance must be determined. The total illuminance at that point is the sum of the individual luminaire contributions. The center of the luminaire is the point of reference. Therefore, when two or more isolux lines pass through a fixture, its contribution is determined by the interpolated isolux line passing through its center. Note the symmetry around the vertical axis, necessitating a plot of only half of the ellipses. Note that the chart could be plotted with isofootcandle lines.

Illuminance "cone" charts

- Max. E at center, 0.5E at the circumference
- Only two values (E, 0.5E) are given in contrast to the isolux diagram (Fig. 16.19)



Fig. 16.20 For downlights with symmetrical circular distribution, a "cone of light," as shown, can be drawn. The illuminance at varying distances on the beam centerline directly below the luminaire is given in the center column. A circle with a circumference at which the illuminance is half of this maximum is drawn at each distance from the downlight (2 ft, 4 ft, etc.). The numbers in the left column show the diameter of this (beam) circle. Similar diagrams are available in SI units. (Courtesy of Zumtobel-STAFF.)

Illuminance tables and charts

- The illuminance pattern on a wall is shown in Fig.16.21
- Similar charts are available for other luminaire spacings.



Fig. 16.21 Addition of an interior reflector to the downlight of Fig. 16.44 converts it to a dual-purpose downlight and wallwash unit. In this I-P unit example, the wall illuminances (in fc) produced by multiple units spaced 3 ft apart and ceiling-mounted 3 ft from the wall are given in the chart. Similar charts are available for other luminaire spacings (and in SI units). (Courtesy of Zumtobel-STAFF.)

Calculating illuminance from a point source

The basis of point source calculations is the inverse square law:

$$fc = \frac{cp}{D^2}$$

where *fc*, *cp*, and *D* are footcandle illuminance, candlepower intensity, and distance, respectively. Refer to Fig. 16.22. The horizontal illuminance at a point *P* as shown in Fig. 16.22 is:

horizontal
$$E = \frac{cp}{D^2} \cos \theta$$

and the vertical illuminance at that same point is

vertical
$$E = \frac{cp}{D^2} \sin \theta$$



Fig. 16.22 Relationship between intensity in candlepower (cp) and illuminance when the source can be considered a point source—that is, when the inverse square law applies. The source's major dimension must not exceed 0.2D to be considered a point source. Using feet yields fc; using meters yields lux. (Redrawn by Martin Lee.)

Example 16.5

EXAMPLE 16.5 Referring to Fig. 16.22 and the candlepower distribution curve of Fig. 16.23, find the horizontal and vertical illuminance at point *P*, which is 10 ft below and 12 ft horizontally distant from the source. The same analysis process would apply if using SI dimensions.

SOLUTION

$$H = 10 \text{ ft } R = 12 \text{ ft}$$

$$\theta = \tan^{-1} \frac{12}{10} = 50^{\circ}$$

$$\sin \theta = 0.766 \quad \cos \theta = 0.643$$

$$cp \text{ at } 50^{\circ} = 6600 \text{ (from Fig. 16.23)}$$

Horizontal illuminance: $\frac{6600}{10^2} \times (0.643)^3 = 17.5 \text{ fc}$
Vertical illuminance: $\frac{6600}{12^2} \times (0.766)^3 = 20.8 \text{ fc}$



Fig. 16.23 Typical candlepower distribution plot.

Calculating illuminance from linear and area sources

from a point source to a point



from a point source to a receiving area

 $\Phi = \int \frac{I(\theta, \psi) \cos \xi}{D^2} dA \qquad \Phi: \text{ flux transferred from a point source to a differential area}$ $\Phi = \sum_{i=1}^{n} I(\theta_i, \psi_i) \cos \xi_i \frac{a_i}{D_i^2}$ $\overline{E} = \frac{\Phi}{A} \qquad E: \text{ Average illuminance}$

Calculating illuminance from linear and area sources

- from a diffuse area source to a point
- from a diffuse area source to a receiving area
- from a non-diffuse area source to a point

Integration over the surface of the luminaire gives

$$E = \frac{1}{A} \int \frac{I(\theta, \psi) \cos \xi}{D^2} dA \qquad E = \frac{1}{A} \sum_i I(\theta_i, \psi_i) \cos \xi_i \frac{a_i}{D_i^2}$$

where the summation is over all the discrete pieces of the luminaire, and

- $I(\theta_i, \psi_i)$ = intensity of the *i*th piece of the luminaire surface to point *P*,
- ξ_i = incident angle for flux from the *i*th piece of the luminaire surface,
- a_i = area of the *i*th piece of the luminaire surface,
- D_i = distance between the *i*th piece of the luminaire surface and point *P*,
- A = area of the luminaire surface.

from a non-diffuse area source to a receiving area

Calculating illuminance from linear and area sources

- These manual methods are laborious and frequently less than reliable.
- Lighting simulation is strongly recommended for point-by-point illuminance calculation.

Simulation-based lighting design

- The calculations are performed accurately and rapidly.
- The designer can change design parameters with less effort than hand calculations.
- List of lighting simulation tools: <u>https://www.buildingenergysoftwaretools.com/</u> → lighting simulation

Evaluating glare potential

- Direct Glare
 - Control of direct glare is addressed (see Ch.6)
- In Ch.16, reflected glare is a focus.

Control of reflected glare

- No perfect solution to the reflected glare so far.
- Several techniques to minimize
 - (a) Physical arrangement of sources, task, and observer
 - (b) Adjusting brightness (eye adaptation level)
 - (c) Design of the light source so that it causes minimal reflected glare.
 - (d) Changing the task quality