

Last lecture

Diffusers  
Nozzle  
Flowmeters } Ch. 6

Energy seminar

Final Exam 11-13:30 Thurs Dec 9      Location: 301-204  
↳ everything except seminar

Ch. 1 → Definitions fluid, properties, etc.  $r, \theta$   
Lagrangian vs. Eulerian  
Material } derivative  $\frac{DQ}{Dt} = \frac{\partial Q}{\partial t} + \mathbf{V} \cdot \nabla Q$   
Total }  
Substantial }

Reynolds #  
Flow lines  
Types of flow

Ch. 2 → Pressure in a stationary (static) fluid (liquid) → hydrostatics  
rotating  
constant linear  $\vec{a}$

$F, X_{cp}, Y_{cp}$  → on surfaces

Pascal's Principle

Buoyancy, stability

**Ch. 3.**

MOST IMPORTANT

(Analytical)  
algebraic  
equations

Control volume analysis (Eulerian)  
→ Reynolds Transport Theorem → Eulerian (control volume)  
Lagrangian (particle) }  
mass } conservation  
momentum }  
energy }

Control volume moving at constant velocity  
Bernoulli Equation.

Ch. 4.  
(analytical)  
differential  
equations

Differential control volume  
differential equations for  
mass conservation  $\rightarrow$  continuity eqn.  
momentum conservati:  $\rightarrow$  Navier-Stokes eqn.

Solutions for special cases

$\Psi, \phi$

vorticity  $\nabla \times \vec{V}$  & angular velocity

(numerical section  $\rightarrow$  not covered)

Ch. 5  
(experimental)

Dimensional analysis, dimensions vs. units  
Principle of dimensional homogeneity  
Buckingham  $\pi$  Theorem  $\rightarrow$   $\pi$ 's  
Similarity between model & prototype  
Difficulties in achieving similarity  
Nondimensionalization of equations

Ch. 6.  
application  
to internal  
flows

Internal flow

$$Re_d = \frac{\rho V d}{\mu}$$

Laminar vs. turbulent flow.

$h_f$

$f(Re_d)$  for laminar & turbulent flows

Moody Chart

Hagen-Poiseuille flow, etc.

Structure of laminar boundary layer vs. turbulent boundary layer

boundary layer

hydraulic diameter for non-circular ducts

Minor losses  $\rightarrow$  bends, valves, etc.

diffusers/nozzles

Flowmeters.

inner overlap  
outer

diffusers/wings  
flowmeters.

Ch. 7  
application to  
external flows.

external flows  $\rightarrow$  boundary layers  
streamlined (slender) vs. bluff bodies  
attached vs. separated flows  
laminar vs. turbulent flat plate flows

integral analysis of  $\left[ \begin{array}{l} \text{laminar} \\ \text{turbulent} \end{array} \right]$  flat plate attached boundary layers

$$D \propto \theta \quad \& \quad \tau_w \propto \frac{d\theta}{dx}$$

$$\frac{\delta}{x}, \frac{\delta^*}{x}, \frac{\theta}{x}, \tau_w, D = \int_A \tau_w dA$$

$$C_f \equiv \frac{\tau_w}{\left(\frac{\rho u_0^2}{2}\right)}$$

$$C_D \equiv \frac{D}{\left(\frac{\rho u_0^2}{2}\right) A}$$

$H \equiv \delta^*/\theta \rightarrow$  condition of boundary layer