2021 Fall

"Phase Transformation in Materials"

11.17.2021

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Contents in Phase Transformation

Background to understand phase transformation

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(Ch1) Thermodynamics and Phase Diagrams
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(Ch2) Diffusion: Kinetics

(Ch3) Crystal Interface and Microstructure

Representative Phase transformation

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(Ch4) Solidification: Liquid → Solid
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(Ch5) Diffusional Transformations in Solid: Solid → Solid

(Ch6) Diffusionless Transformations: Solid → Solid

Contents for today's class

< Phase Transformation in Solids >

- 1) Diffusional Transformation: Thermally-activated process= rate∞ exp(-∆G*/kT)
- 2) Non-diffusional Transformation: Athermal Transformation

- Precipitate nucleation in solid (homogeneous/ heterogeneous)
- Precipitate growth
 - 1) Growth behind Planar Incoherent Interfaces
 - 2) Diffusion Controlled lengthening of Plates or Needles
 - 3) Thickening of Plate-like Precipitates by Ledge Mechanism

Q1: What kind of representative diffusion transformations in solid exist?

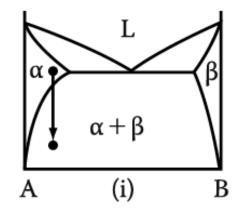
5. Diffusion Transformations in solid

: diffusional nucleation & growth

(a) Precipitation

$$\alpha' \rightarrow \alpha + \beta$$

Metastable supersaturated solid solution



Homogeneous Nucleation

$$\Delta G = -V\Delta G_{V} + A\gamma + V\Delta G_{S}$$

Heterogeneous Nucleation

$$\Delta G = -V\Delta G_V + A\gamma + V\Delta G_S \qquad \Delta G_{het} = -V(\Delta G_V - \Delta G_S) + A\gamma - \Delta G_d$$

$$N_{\text{hom}} = \omega C_0 \exp\left(-\frac{\Delta G_m}{kT}\right) \exp\left(-\frac{\Delta G^*}{kT}\right)$$

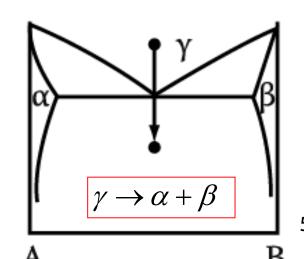
suitable nucleation sites ~ nonequilibrium defects (creation of nucleus~destruction of a defect(- ΔG_d))

(b) Eutectoid Transformation

Composition of product phases differs from that of a parent phase.

→ long-range diffusion

Which transformation proceeds by short-range diffusion?

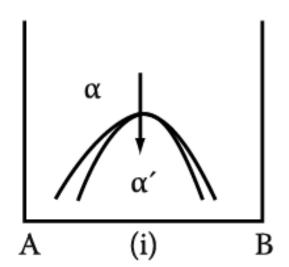


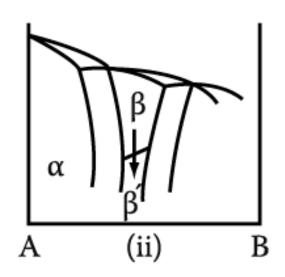
5. Diffusion Transformations in solid

(c) Order-Disorder Transformation

$$\alpha \rightarrow \alpha'$$

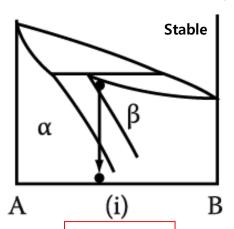
Disorder Order (high temp.) (low temp.)

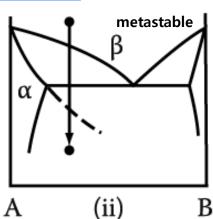




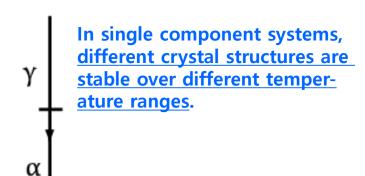
(d) Massive Transformation

: The original phase decomposes into one or more new phases which have the <u>same composition</u> as the parent phase, but <u>different crystal structures</u>.





(e) Polymorphic Transformation



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Q2: Homogeneous nucleation in solid?

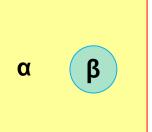
Free Energy Change Associated with the Nucleation

Negative and Positive Contributions to ΔG ?

1) Volume Free Energy : $-V\Delta G_V$

2) Interface Energy : A_{γ}

3) Misfit Strain Energy : $V\Delta G_{\rm S}$



$$\Delta G = -V\Delta G_{V} + A\gamma + V\Delta G_{S}$$

for spherical nucleation

$$\Delta G = -\frac{4}{3}\pi r^3 (\Delta G_V - \Delta G_S) + 4\pi r^2 \gamma$$

Plot of
$$\Delta G$$
 vs r?

$$r^* = ?$$

$$\Lambda G^* = ?$$

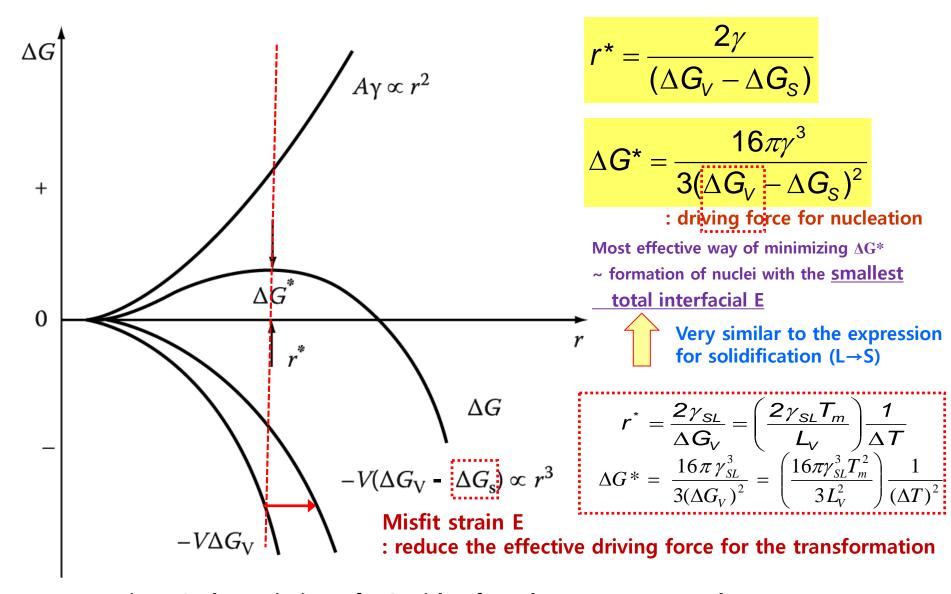


Fig. 5.2 The variation of ΔG with r for a homogeneous nucleus. There is a activation energy barrier ΔG^* .

Concentration of Critical Size Nuclei per unit volume

$$C^* = C_0 \exp(-\Delta G^* / kT)$$

 C_0 : number of atoms per unit volume in the parent phase

Homogeneous Nucleation Rate

If each nucleus can be made supercritical at a rate of f per second,

$$N_{\text{hom}} = f C^*$$

$$f = \omega \exp(-\Delta G_m/kT)$$

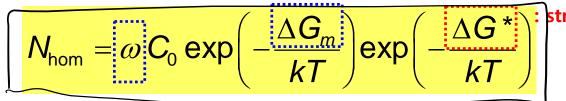
: f depends on how frequently a critical nucleus can receive an atom from the α matrix.

 $\omega \propto vibration frequency, area of critical nucleus$ ΔG_m : activation energy for atomic migration

$$N_{\text{hom}} = \omega C_0 \exp\left(-\frac{\Delta G_m}{kT}\right) \exp\left(-\frac{\Delta G^*}{kT}\right)$$

: This eq. is basically same with eq (4.12) except considering temp. dependence of f.

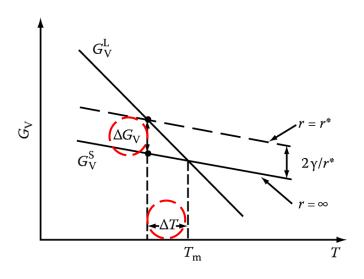
Homogeneous Nucleation rate
$$N_{\rm hom} = f_0 C_o \exp(-\frac{\Delta G_{\rm hom}^*}{kT})$$
 nuclei / m³·s



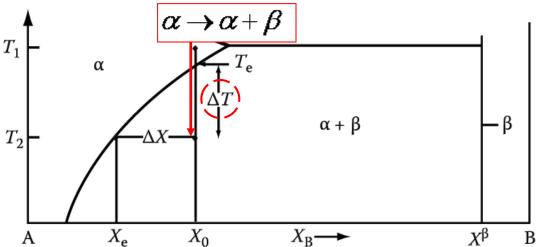
strongly temp. dependent ΔG*는 온도에 민감

$$\Delta G^* = \frac{16\pi\gamma^3}{3(\Delta G_V - \Delta G_S)^2}$$
 ΔG_V (driving force for precipitation)_main ΔG_V $\Delta G_$

 ΔG_V (driving force for precipitation)_main factor of ΔG^*







- 1) For X_0 , solution treatment at T_1
- 2) For X_0 , quenching down to T_2

$$\alpha' \rightarrow \alpha + \beta$$

: supersaturated α with B \rightarrow β precipitation in α

Total Free Energy Decrease per Mole of Nuclei ΔG_0



: overall driving force for transformation/ different with driving force for nucleation

Driving Force for Precipitate Nucleation

$$\alpha \rightarrow \alpha + \beta$$

$$\Delta \mathbf{G}_{\mathbf{V}} = \frac{\Delta \mathbf{G}_n}{V_m}$$

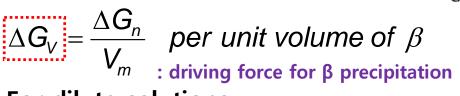
$$\Delta G_1 = \mu_A^{\alpha} X_A^{\beta} + \mu_B^{\alpha} X_B^{\beta}$$

: Decrease of total free E of system by removing a small amount of material with the nucleus composition (X_B^{β}) (P point)

$$\Delta G_2 = \mu_A^{\beta} X_A^{\beta} + \mu_B^{\beta} X_B^{\beta}$$

: Increase of total free E of system by forming β phase with composition X_Bβ (Q point)

$$\Delta G_n = \Delta G_2 - \Delta G_1$$
 (length PQ)

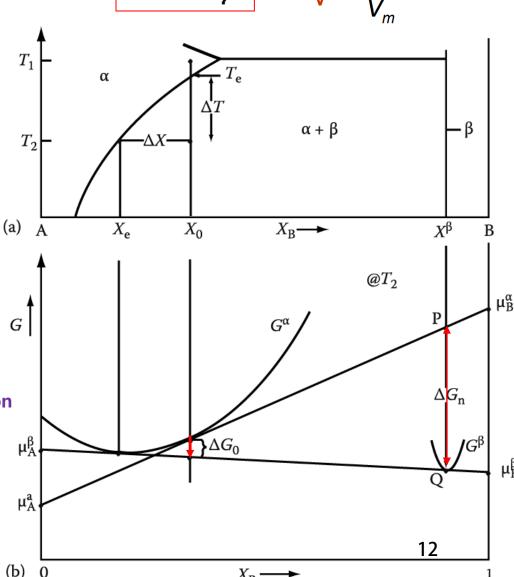


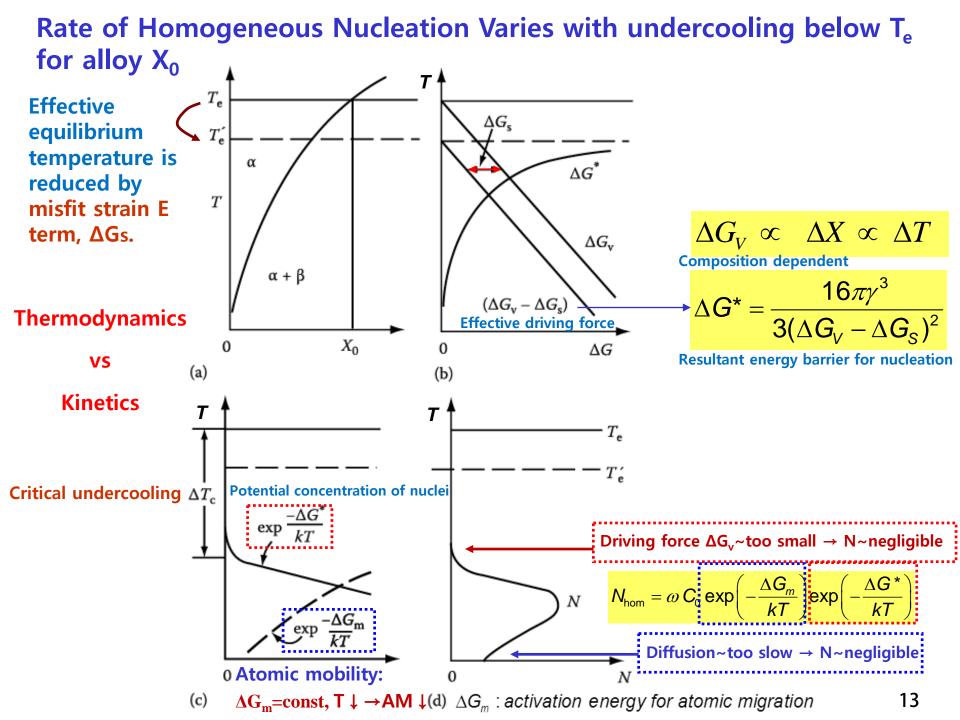
For dilute solutions,

$$\Delta G_V \propto \Delta X_{\text{Composition dependent}} \text{where } \Delta X = X_0 - X_e$$

$$\Delta G_V \propto \Delta X \propto \Delta T$$

∝ undercooling below T_e





The Effect of ΔT on ΔG^*_{het} & ΔG^*_{hom} ?_Critical undercooling, ΔT_c

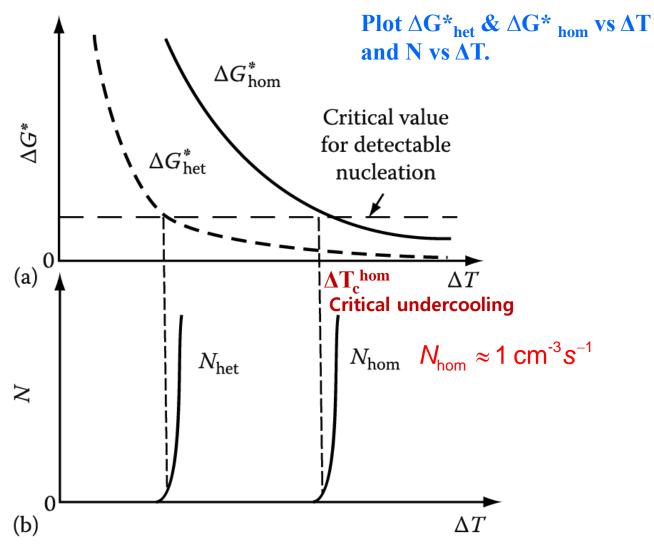


Fig. 4.9 (a) Variation of ΔG^* with undercooling (ΔT) for homogeneous and heterogeneous nucleation.

(b) The corresponding nucleation rates assuming the same critical value of ΔG^*

The Effect of Alloy Composition on the Nucleation Rate

Compare the two plots of T vs N(1) and T vs N(2).

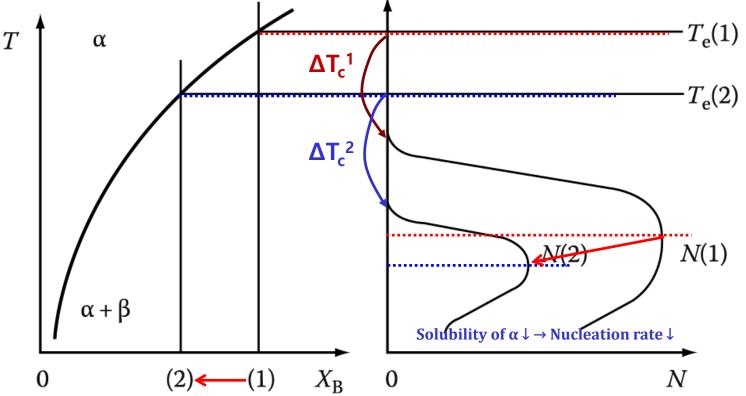


Fig. 5.5 The effect of alloy composition on the nucleation rate. The nucleation rate in alloy 2 is always less than in alloy 1.

지금까지의 논의는 생성되는 핵이 β 상과 같은 구조, 평형 조성을 갖고, 형상은 구 라고 가정 단, 실제 어떤 핵이 형성되느냐? \rightarrow 어느 경우 최소의 $\Delta G*$ 필요로 하나? \rightarrow <u>최소의 총 계면에너지를 갖는 핵 생성</u>

- (a) 핵이 모상과 방위관계를 갖고 <u>정합계면</u> 형성하면 $\to \Delta Gs$ 증가 & Te' 감소 그러나, Te' 이하에서는 정합계면 생성에 의한 <u>y 감소</u>가 ΔGs 증가 효과보다 더 커질 수 있음. $\to \Delta G*$ 크게 감소 $\to \Delta G$ 발생 가능
- (b) In most system, α, β phase~ <u>different crystal structure</u> \rightarrow <u>부정합 핵은 γ가 커서 평형</u> <u>β상의 균일 핵생성 불가능</u> \rightarrow <u>metastable phase β' 균일핵생성 (GP Zones, Section 5.5.1)</u>

Q3: Heterogeneous nucleation in solid?

most cases, heterogeneous nucleation_suitable nucleation sites ~ nonequilibrium defects (creation of nucleus~destruction of a defect($-\Delta G_d$) & reducing the activation E barrier)

$$\Delta G_{het} = -V(\Delta G_{V} - \Delta G_{S}) + A\gamma - \Delta G_{d}$$

Nucleation on Grain Boundaries

Assumption: ΔG_S (misfit strain E)= 0,

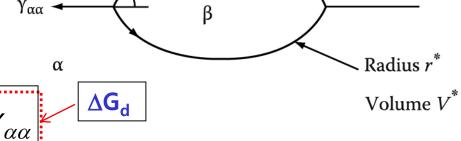
Optimum embryo shape should be that which minimizes the total interfacial free E.

$$\cos \theta = \gamma_{\alpha\alpha}/2\gamma_{\alpha\beta}$$

(by assuming $\gamma_{\alpha\beta}$ is isotropic and equal for both grains)

Critical nucleus size(V*) for grain-boundary nucleation

 $\gamma_{\alpha\beta}$



$$\Delta G = -V\Delta G_V + A_{\alpha\beta}\gamma_{\alpha\beta} - A_{\alpha\alpha}\gamma_{\alpha\alpha}$$
Volume *V*

Excess free E associated with the embryo~analogous to solidification on a substrate (Section 4.1.3) (next page)

Barrier of Heterogeneous Nucleation in S→L transformation

$$\Delta G_{het} = -V_{S} \Delta G_{V} + A_{SL} \gamma_{SL} + A_{SM} \gamma_{SM} - A_{SM} \gamma_{ML}$$

$$\Delta G^{*} = \frac{16 \pi \gamma_{SL}^{3}}{3 \Delta G_{V}^{2}} \cdot S(\theta) = \frac{16 \pi \gamma_{SL}^{3}}{3 \Delta G_{V}^{2}} \cdot \frac{(2 - 3 \cos \theta + \cos^{3} \theta)}{4}$$

$$A = \frac{16 \pi \gamma_{SL}^{3}}{3 \Delta G_{V}^{2}} \cdot S(\theta) = \frac{16 \pi \gamma_{SL}^{3}}{3 \Delta G_{V}^{2}} \cdot \frac{(2 - 3 \cos \theta + \cos^{3} \theta)}{4}$$

$$A = \frac{16 \pi \gamma_{SL}^{3}}{3 \Delta G_{V}^{2}} \cdot S(\theta) = \frac{16 \pi \gamma_{SL}^{3}}{3 \Delta G_{V}^{2}} \cdot \frac{(2 - 3 \cos \theta + \cos^{3} \theta)}{4}$$

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$$A = \frac{16 \pi \gamma_{SL}^{3}}{3 \Delta G_{V}^{2}} \cdot S(\theta) = \frac{16 \pi \gamma_{SL}^{3}}{3 \Delta G_{V}^{2}} \cdot \frac{(2 - 3 \cos \theta + \cos^{3} \theta)}{4}$$

Shape factor

$S(\theta)$ has a numerical value ≤ 1 dependent only on θ (the shape of the nucleus)

$$\Delta G_{het}^* = S(\theta) \Delta G_{hom}^*$$

$$\Rightarrow r^* = \frac{2 \gamma_{SL}}{\Delta G_V} \quad and \quad \Delta G^* = \frac{16 \pi \gamma_{SL}^3}{3 \Delta G_V^2} \cdot S(\theta)$$

$$\Delta G_{het}^* = \Delta G_{homo}^* \left(\frac{2 - 3 \cos \theta + \cos^3 \theta}{4} \right)$$

$$\frac{V_{A}}{V_{A} + V_{B}} = \frac{2 - 3\cos\theta + \cos^{3}\theta}{4} = S(\theta)$$

most cases, heterogeneous nucleation_suitable nucleation sites ~ nonequilibrium defects (creation of nucleus~destruction of a defect($-\Delta G_d$) & reducing the activation E barrier)

$$\Delta G_{het} = -V(\Delta G_{V} - \Delta G_{S}) + A\gamma - \Delta G_{d}$$

Nucleation on Grain Boundaries

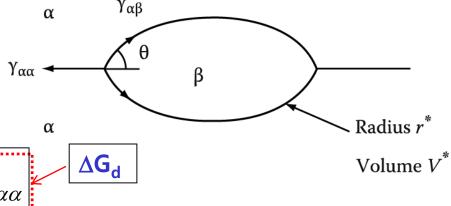
Assumption: ΔG_S (misfit strain E)= 0,

Optimum embryo shape should be that which minimizes the total interfacial free E.

$$\cos \theta = \gamma_{\alpha\alpha}/2\gamma_{\alpha\beta}$$

(by assuming $\gamma_{\alpha\beta}$ is isotropic and equal for both grains)

Critical nucleus size(V*) for grain-boundary nucleation



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 $\Delta G = -V \Delta G_{V} + A_{\alpha\beta} \gamma_{\alpha\beta} - A_{\alpha\alpha} \gamma_{\alpha\alpha}$

Excess free E associated with the embryo~analogous to solidification on a substrate (Section 4.1.3)

Critical radius of the spherical caps

$$r^* = 2\gamma_{\alpha\beta} / \Delta G_V$$

r* is not related to $\gamma_{\alpha\alpha}$

Activation E barrier for heterogeneous nucleation

$$\frac{\Delta G^*_{het}}{\Delta G^*_{hom}} = \frac{V^*_{het}}{V^*_{hom}} = S(\theta)$$

$$S(\theta) = \frac{1}{2}(2 + \cos\theta)(1 - \cos\theta)^2$$

$$\Delta G_{het}^* \sim \cos\theta \sim \gamma_{\alpha\alpha}/2\gamma_{\alpha\beta}$$
 $\Rightarrow \begin{array}{c} \gamma_{\alpha\alpha} : \gamma_{\alpha\beta} \geq 2 \rightarrow \mathbf{0} = 0 \\ \text{No energy barrier for nucleation} \end{array}$

Reduction by boundary effect

$$\gamma_{\alpha\alpha}:\gamma_{\alpha\beta} \geq 2 \rightarrow \mathbf{0} = 0$$

$$\Delta G_{het}^* = \Delta G_{homo}^* \left(\frac{2 - 3\cos\theta + \cos^3\theta}{4} \right)$$

How can V* and ΔG^* be reduced even further?

→ By nucleation on a grain edge or a grain corner.

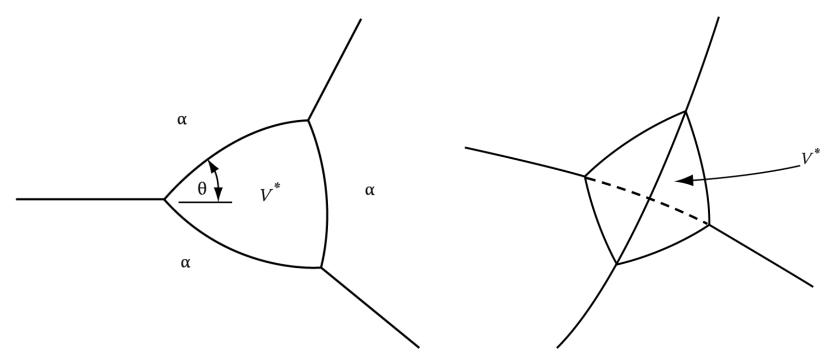


Fig. 5.7 Critical nucleus shape for nucleation on a grain edge. Fig. 5.8 Critical nucleus shape for nucleation on a grain corner.

Compare the plots of $\Delta G_{het}^* / \Delta G_{hom}^* vs \cos \theta$ for grain boundaries, edges and corners

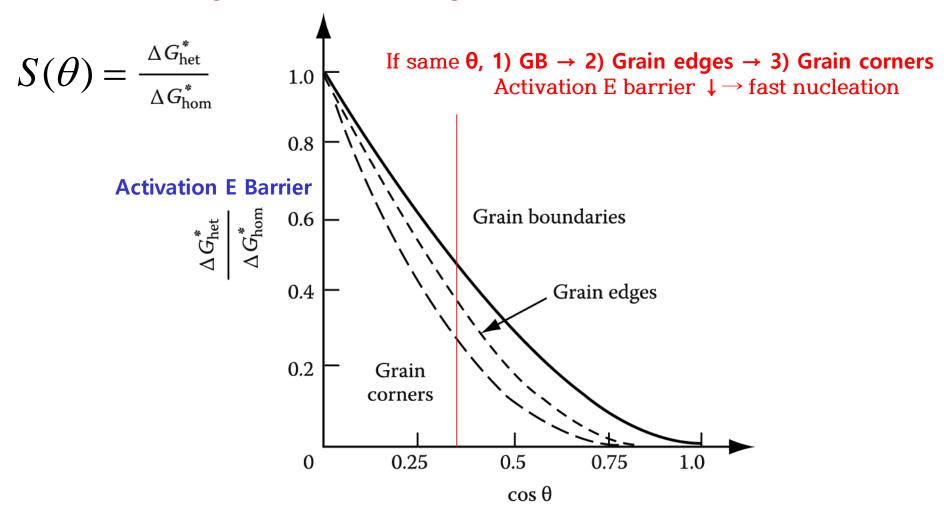


Fig. 5.9 The effect of θ on the activation energy for grain boundary nucleation relative to homogeneous nucleation.

High-angle grain boundaries (high interfacial E) are particularly effective nucleation sites for incoherent precipitates with high $\gamma_{\alpha\beta}$.

If the matrix and precipitate make a <u>coherent interface</u>, V^* and ΔG^* can be <u>further reduced</u> as shown in Fig. 5.10. The nuclei will then have an orientation relationship with one of the grains.

< Nucleus with Coherent Interface >

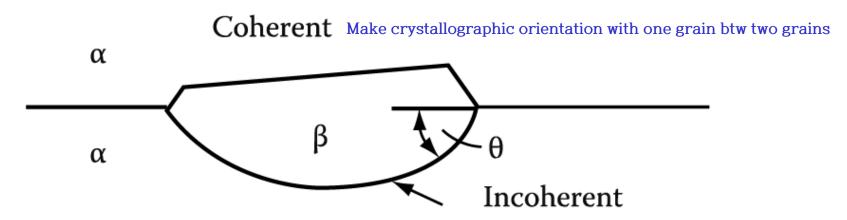


Fig. 5. 10 The critical nucleus size can be reduced even further by forming a low-energy coherent interface with one grain.

* Other planar defects, such as inclusion/matrix interfaces, stacking faults (relatively low E), and free surfaces, dislocations and excess vacancies (?) can behave in a similar way to grain boundaries in reducing ΔG^* .

Rate of Heterogeneous Nucleation

Decreasing order of ΔG^* , i.e., increasing ΔG_d

(Activation Energy Barrier for nucleation)

- 1) homogeneous sites
- 2) Vacancies 단독으로 또는 작은 군집체 상태로 핵생성에 영향/확산속도 증가 & 불일치 변형에너지 감소
- 3) dislocations 전위주위의 격자비틀림→ 핵생성시 전체변형에너지 감소 / 용질원소 편석 / 손쉬운 확산경로
- 4) stacking faults 매우 낮은 에너지/총계면에너지 ↓ 효과적이지 못함 → 강력한 불균일 핵생성처는 아님
- 5) grain boundaries and interphase boundaries
- 6) free surfaces

: Nucleation should always occur most rapidly on sites near the bottom of the list.

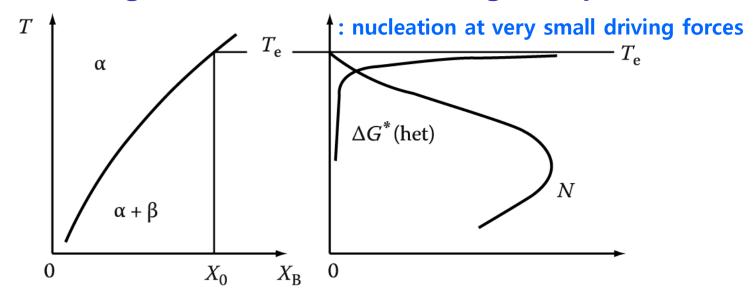
However, the relative importance of these sites depends on the relative concentrations of the sites, C1.

$$N_{het} = \omega \overline{C_1} \exp \left(-\frac{\Delta G_m}{kT}\right) \exp \left(-\frac{\Delta G^*}{kT}\right) \quad nuclei \ m^{-3} s^{-1}$$

C₁: concentration of heterogeneous nucleation sites per unit volume

$$N_{\text{hom}} = \omega \overline{C_0} \exp\left(-\frac{\Delta G_m}{kT}\right) \exp\left(-\frac{\Delta G^*}{kT}\right)$$
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The Rate of Heterogeneous Nucleation during Precipitation



* Relative magnitudes of the heterogeneous and homogeneous volume nucleation rates

$$\frac{N_{het}}{N_{hom}} = \frac{C_1}{C_0} exp \left(\frac{\Delta G^*_{hom} - \Delta G^*_{het}}{kT} \right)$$

Ignore ω and ΔG_m due to small deviation

∆G* ~ always smallest for heterogeneous nucleation

Exponential factor : very large quantity $\frac{N_{het}}{N} > 1$ High heterogeneous nucleation rate

$$\rightarrow \frac{N_f}{N}$$

 $\frac{N_{het}}{N_{hom}} = \frac{C_1}{C_0} exp\left(\frac{\Delta G^*_{hom} - \Delta G^*_{het}}{kT}\right)$

For D = 50 μ m, δ = 0.5 nm

 $\frac{C_1}{C} = \frac{\delta}{D} \approx 10^{-5}$

C_1/C_0 for GB nucleation?

$$\frac{C_1}{C_0} = \frac{\delta(GB \text{ thickness})}{D(grain \text{ size})}$$

: the number of atoms on heterogeneous sites relative to the number within the matrix

$$\frac{C_1}{C_2} = \left(\frac{\delta}{D}\right)^2 \rightarrow \text{for nucleation on grain edge}$$

$$\frac{C_1}{C_2} = \left(\frac{\delta}{D}\right)^3 \rightarrow \text{for nucleation on grain corner}$$

V*

C₁/C₀ for Various Heterogeneous Nucleation Sites

Grain boundary	$\frac{\text{Grain edge}}{D = 50 \mu\text{m}}$	$\frac{\text{Grain corner}}{D = 50 \mu\text{m}}$	Dislocations		Excess vacancies
$D = 50 \mu\text{m}$			10^5 mm^{-2}	10^8 mm^{-2}	$X_{\rm v} = 10^{-6}$
10^{-5}	10^{-10}	10^{-15}	10^{-8}	10 ⁻⁵	10^{-6}

$$\frac{N_{het}}{N_{hom}} = \frac{C_1}{C_0} exp\left(\frac{\Delta G_{hom}^* - \Delta G_{het}^*}{kT}\right)$$

C₁/C₀ for Various Heterogeneous Nucleation Sites

각각의 핵생성처에서 경쟁적으로 핵생성 발생: 구동력 조건에 따라 전체 핵생성 속도에 dominant하게 영향을 미치는 site 변화

$\frac{\text{Grain boundary}}{D = 50 \mu\text{m}}$	$\frac{\text{Grain edge}}{D = 50 \mu\text{m}}$	$\frac{\text{Grain corner}}{D = 50 \mu\text{m}}$	Dislocations		Excess vacancies
			10^5 mm^{-2}	10^8 mm^{-2}	$X_{\rm v} = 10^{-6}$
10^{-5}	10^{-10}	10^{-15}	10^{-8}	10^{-5}	10^{-6}

In order to make nucleation occur exclusively on the grain corner, how should the alloy be cooled?

- 1) At very small driving forces (△G_v), when activation energy barriers for nucleation are high, the highest nucleation rates will be produced by grain-corner nucleation.
- **ΔG**_v

 ↓
 increase
- 2) dominant nucleation sites: grain edges → grain boundaries
- 3) At very high driving forces it may be possible for the (C_1/C_0) term to dominate and then homogeneous nucleation provides the highest nucleation rates.

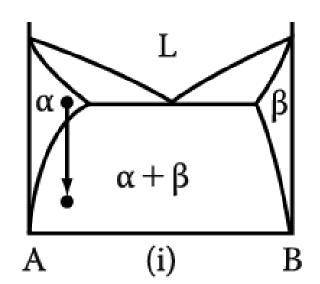
^{*} The above comments concerned nucleation <u>during isothermal transformations</u> 26 (driving force for nucleation: [isothermal] constant ↔ [continuous cooling] increase with time)

Contents for today's class

< Phase Transformation in Solids >

Diffusional Transformation

(a) Precipitation



Homogeneous Nucleation

Effect of misfit strain energy

$$\Delta G = -V\Delta G_{V} + A\gamma + V\Delta G_{S}$$

$$\Delta G = -V\Delta G_{V} + A\gamma + V\Delta G_{S}$$

$$r^* = \frac{2\gamma}{(\Delta G_V - \Delta G_S)} \Delta G^* = \frac{16\pi\gamma^3}{3(\Delta G_V - \Delta G_S)^2}$$

$$N_{\text{hom}} = \omega C_0 \exp\left(-\frac{\Delta G_m}{kT}\right) \exp\left(-\frac{\Delta G^*}{kT}\right) \qquad \frac{N_{\text{het}}}{N_{\text{hom}}} = \frac{C_1}{C_0} \exp\left(\frac{\Delta G^*_{\text{hom}} - \Delta G^*_{\text{het}}}{kT}\right)$$

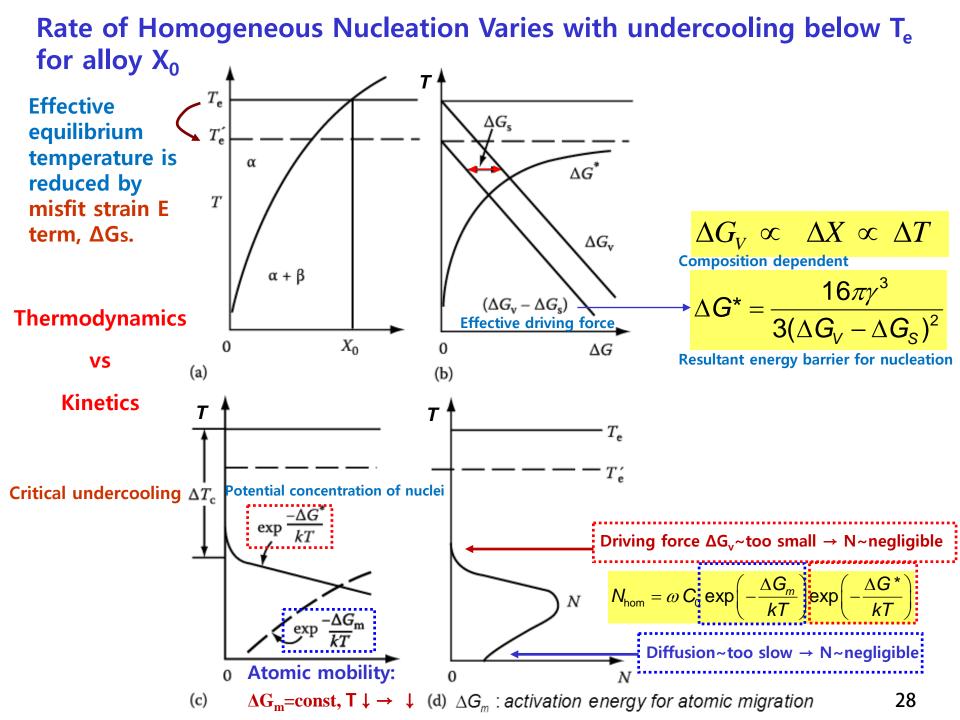
Heterogeneous Nucleation

suitable nucleation sites ~ nonequilibrium defects (creation of nucleus~destruction of a defect($-\Delta G_d$))

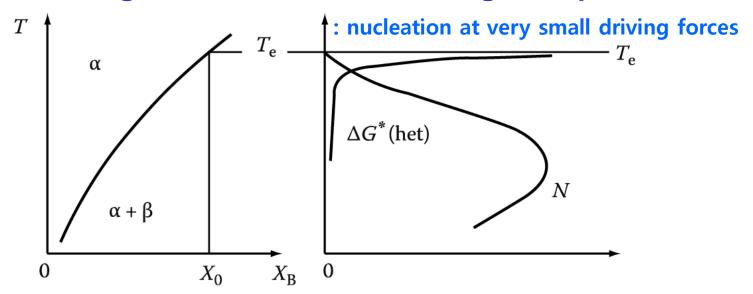
$$\Delta G_{het} = -V(\Delta G_{V} - \Delta G_{S}) + A\gamma - \Delta G_{d}$$

$$\frac{\Delta G^*_{het}}{\Delta G^*_{hom}} = \frac{V^*_{het}}{V^*_{hom}} = S(\theta)$$

$$\frac{N_{het}}{N_{hom}} = \frac{C_1}{C_0} \exp\left(\frac{\Delta G^*_{hom} - \Delta G^*_{het}}{kT}\right)$$



The Rate of Heterogeneous Nucleation during Precipitation



* Relative magnitudes of the heterogeneous and homogeneous volume nucleation rates

$$\frac{N_{het}}{N_{hom}} = \frac{C_1}{C_0} exp \left(\frac{\Delta G^*_{hom} - \Delta G^*_{het}}{kT} \right)$$

 ω 와 ΔG_m 의 차이는 미비하여 무시

 $\Delta G^* \sim \text{always smallest}$ for heterogeneous nucleation : very large quantity $\frac{N_{het}}{N} > 1$ High heterogeneous nucleation rate

$$\Rightarrow \frac{r}{\Lambda}$$

$$\frac{N_{het}}{N_{hom}} = \frac{C_1}{C_0} exp\left(\frac{\Delta G^*_{hom} - \Delta G^*_{het}}{kT}\right)$$

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C₁/C₀ for Various Heterogeneous Nucleation Sites

각각의 핵생성처에서 경쟁적으로 핵생성 발생: 구동력 조건에 따라 전체 핵생성 속도에 dominant하게 영향을 미치는 site 변화

$\frac{\text{Grain boundary}}{D = 50 \mu\text{m}}$	$\frac{\text{Grain edge}}{D = 50 \mu\text{m}}$	$\frac{\text{Grain corner}}{D = 50 \mu\text{m}}$	Dislocations		Excess vacancies
			10^5 mm^{-2}	10^8 mm^{-2}	$X_{\rm v} = 10^{-6}$
10^{-5}	10^{-10}	10^{-15}	10^{-8}	10^{-5}	10^{-6}

In order to make nucleation occur exclusively on the grain corner, how should the alloy be cooled?

1) At very small driving forces (ΔG_v), when activation energy barriers for nucleation are high, the highest nucleation rates will be produced by grain-corner nucleation.



- 2) dominant nucleation sites: grain edges → grain boundaries
- 3) At very high driving forces it may be possible for the (C_1/C_0) term to dominate and then homogeneous nucleation provides the highest nucleation rates.

^{*} The above comments concerned nucleation during isothermal transformations (driving force for nucleation: [isothermal] constant ↔ [continuous cooling] increase with time)

2021 Fall

"Phase Transformation in Materials"

11.22.2021

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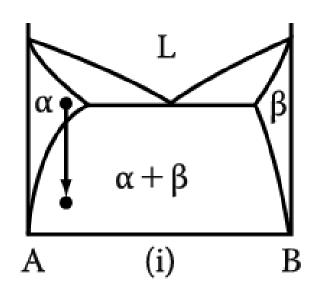
Office hours: by an appointment

Contents for previous class

< Phase Transformation in Solids >

Diffusional Transformation

(a) Precipitation



Homogeneous Nucleation

Effect of misfit strain energy

$\Delta G = -V\Delta G_{V} + A\gamma + V\Delta G_{S}$

$$r^* = \frac{2\gamma}{(\Delta G_{\text{V}} - \Delta G_{\text{S}})} \Delta G^* = \frac{16\pi\gamma^3}{3(\Delta G_{\text{V}} - \Delta G_{\text{S}})^2}$$

$$N_{\text{hom}} = \omega C_0 \exp\left(-\frac{\Delta G_m}{kT}\right) \exp\left(-\frac{\Delta G^*}{kT}\right) \qquad \frac{N_{\text{het}}}{N_{\text{hom}}} = \frac{C_1}{C_0} \exp\left(\frac{\Delta G^*_{\text{hom}} - \Delta G^*_{\text{het}}}{kT}\right)$$

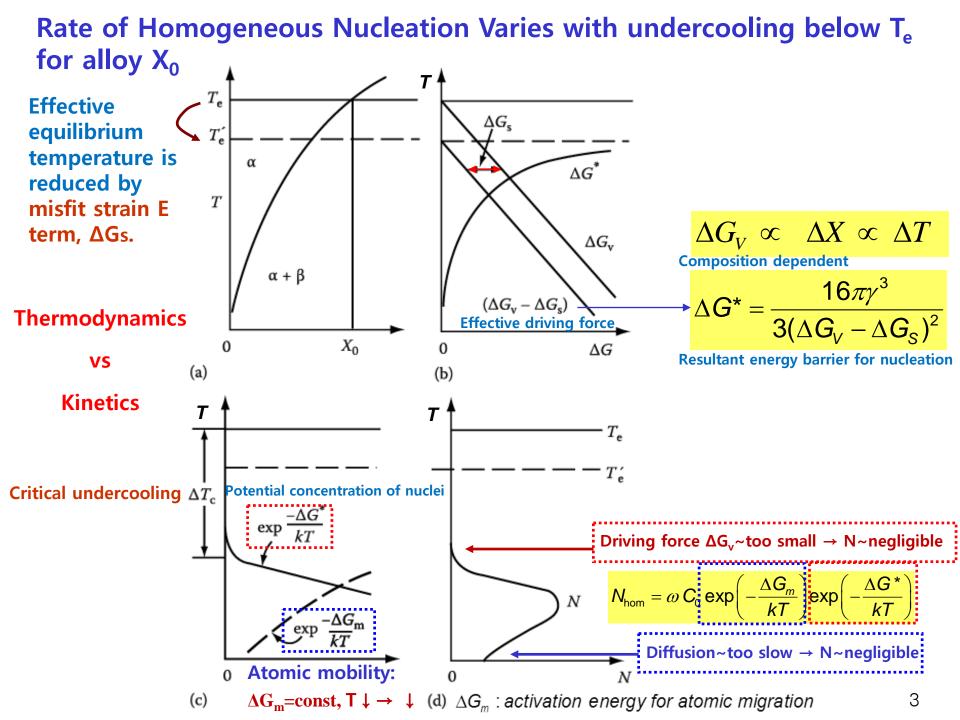
Heterogeneous Nucleation

suitable nucleation sites ~ nonequilibrium defects (creation of nucleus~destruction of a defect($-\Delta G_d$))

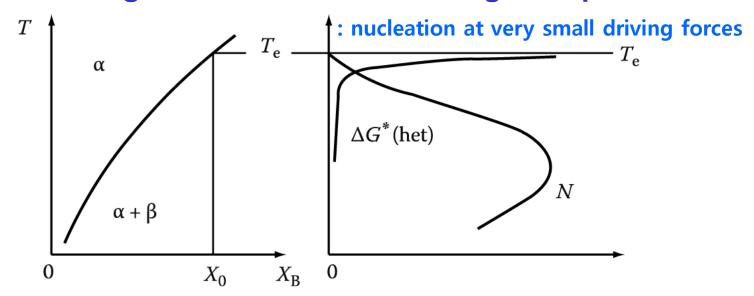
$$\Delta G_{het} = -V(\Delta G_{V} - \Delta G_{S}) + A\gamma - \Delta G_{d}$$

$$\frac{\Delta G^*_{het}}{\Delta G^*_{hom}} = \frac{V^*_{het}}{V^*_{hom}} = S(\theta)$$

$$\frac{N_{het}}{N_{hom}} = \frac{C_1}{C_0} \exp\left(\frac{\Delta G_{hom}^* - \Delta G_{het}^*}{kT}\right)$$



The Rate of Heterogeneous Nucleation during Precipitation



* Relative magnitudes of the heterogeneous and homogeneous volume nucleation rates

$$\frac{N_{het}}{N_{hom}} = \frac{C_1}{C_0} exp\left(\frac{\Delta G^*_{hom} - \Delta G^*_{het}}{kT}\right)$$

ω 와 ΔG_m 의 차이는 미비하여 무시

∆G* ~ always smallest for heterogeneous nucleation

$$\Rightarrow \frac{N_{het}}{N} > 1$$

Exponential factor : very large quantity $\Rightarrow \frac{N_{het}}{N} > 1$ High heterogeneous nucleation rate

$$\frac{N_{het}}{N_{hom}} = \frac{C_1}{C_0} exp\left(\frac{\Delta G^*_{hom} - \Delta G^*_{het}}{kT}\right)$$

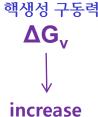
C₁/C₀ for Various Heterogeneous Nucleation Sites

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Q4: Precipitate growth:

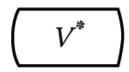
- 1) Growth behind Planar Incoherent Interfaces
- 2) Diffusion Controlled lengthening of Plates or Needles
- 3) Thickening of Plate-like Precipitates by Ledge Mechanism

5.3 Precipitate Growth

Initial precipitate shape
~minimizes the total interfacial free E

Coherent or semicoherent facets

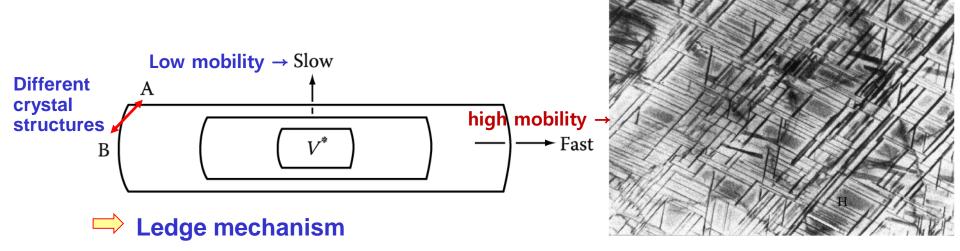
Precipitate growth → interface migration : shape~determined by the relative migration rates



Smoothly curved incoherent interfaces

If the nucleus consists of semi-coherent and incoherent interfaces,

what would be the growth shape?



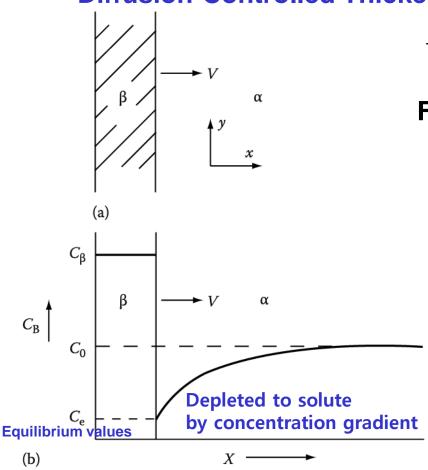
Thin disk or plate

→ Origin of the Widmanstätten morphology

Incoherent interface → similar to rough interface

 \rightarrow local equilibrium \rightarrow diffusion-controlled

Diffusion-Controlled Thickening: precipitate growth rate



$$\rightarrow v = f(\Delta T \text{ or } \Delta X, t)$$

From mass conservation,

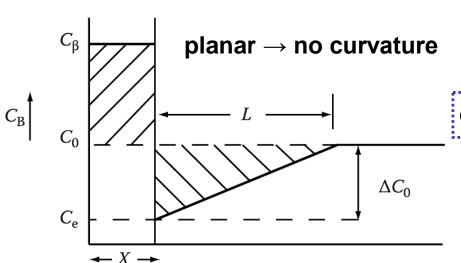
$$(C_{\beta} - C_{e})dx$$
 mole of B
= $J_{B} = D(dC/dx)dt$

D: interdiffusion coefficient or interstitial diffusion coeff.

$$v = \frac{dx}{dt} = \frac{D}{C_{\beta} - C_{e}} \cdot \frac{dC}{dx}$$

Depends on the concentration gradient at the interface dC/dx 8

Simplification of concentration profile (Zener)



$$v = \frac{dx}{dt} = \frac{D}{C_{\beta} - C_{e}} \cdot \frac{dC}{dx}$$

$$dC/dx = \Delta C_0/L \leftarrow L = 2(C_\beta - C_0)x/\Delta C_0$$

$$:: (C_{\beta} - C_0)x = L\Delta C_0/2$$

$$V = \frac{D(\Delta C_0)^2}{2(C_{\beta} - C_e)(C_{\beta} - C_0)x}$$

Thickness of the slab

if
$$C_{\beta} - C_0 \cong C_{\beta} - C_e$$
 and $X = CV_m$, $\Delta C_0 \rightarrow \Delta X_0 = X_0 - X_e$ (simplification)

$$\Delta C_0 \to \Delta X_0 = X_0 - X_\epsilon$$

$$xdx = \frac{D(\Delta X_0)^2}{2(X_\beta - X_e)^2} dt \xrightarrow{\text{integral}} x = \frac{\Delta X_0}{X_\beta - X_e} \sqrt{(Dt)}$$
Thickness of the slape of the sla

$$X = \frac{\Delta X_0}{X_{\beta} - X_e} \sqrt{(Dt)}$$

Thickness of the slab

$$x \propto \sqrt{(Dt)}$$

Parabolic growth

$$V = \frac{\Delta X_0}{2(X_{\beta} - X_e)} \sqrt{\frac{D}{t}}$$

$$V \propto \Delta X_0$$
, $V \propto \sqrt{(D/t)}$

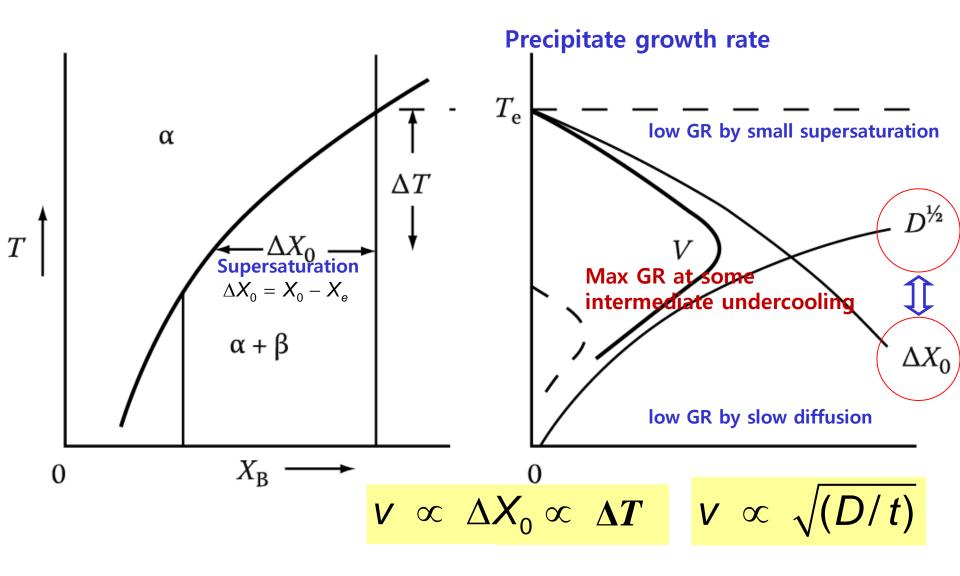


Fig. 5.16 The effect of temperature and position on growth rate, v.

Effect of "Overlap" of Separate Precipitates

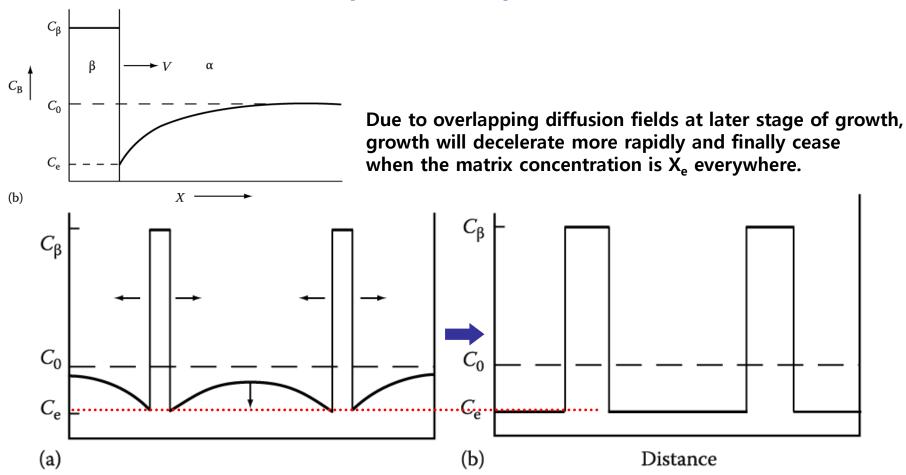
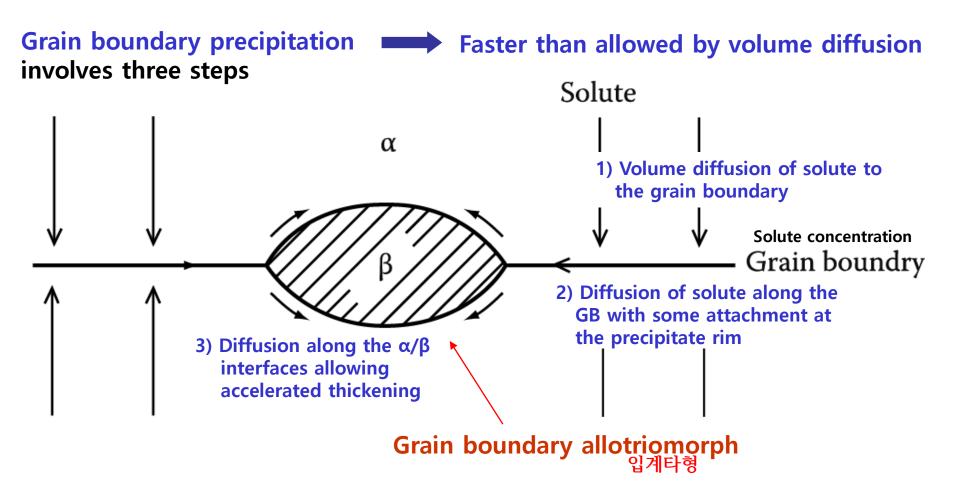


Fig. 5.17 (a) Interference of growing precipitates <u>due to overlapping</u> <u>diffusion fields</u> at later stage of growth. (b) Precipitate has stopped growing.



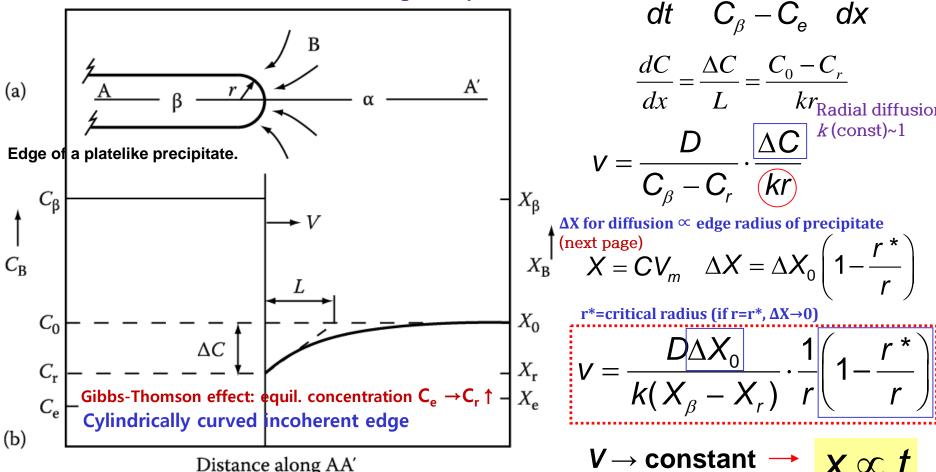
치환형 확산이 일어나는 경우 매우 중요/ 침입형 고용체에서는 체적 확산 속도가 크기 때문에 입계나 전위를 통한 단거리 확산은 상대적으로 중요하지 않음.

Fig. 5.18 Grain-boundary diffusion can lead to rapid lengthening and thickening of grain boundary precipitates, especially by substitutional diffusion.

2) Diffusion Controlled lengthening of Plates or Needles

Plate Precipitate of constant thickness

Volume diffusion-controlled continuous growth process



From mass conservation,

$$V = \frac{dx}{dt} = \frac{D}{C_{\beta} - C_{e}} \cdot \frac{dC}{dx}$$
$$\frac{dC}{dx} = \frac{\Delta C}{L} = \frac{C_{0} - C_{r}}{kr_{\text{Radial d}}}$$

$$V = \frac{D}{C_{\beta} - C_{r}} \cdot \frac{\Delta C}{kr}$$
kadial diffusion in the second s

$$X_{\rm B} \quad X = CV_{m} \quad \Delta X = \Delta X_{0} \left(1 - \frac{r}{r}\right)$$

r*=critical radius (if r=r*, $\Delta X \rightarrow 0$)

$$V = \frac{D\Delta X_0}{k(X_{\beta} - X_r)} \cdot \frac{1}{r} \left(1 - \frac{r^*}{r} \right)$$

$$V \rightarrow \text{constant} \rightarrow \chi \propto t$$
(If t=2r, v = constant) Linear growth

Concentration profile along AA' in (a).

Needle \rightarrow Gibbs-Thomson increase in G = $2\gamma V_m/r$ instead of $\gamma V_m/r$

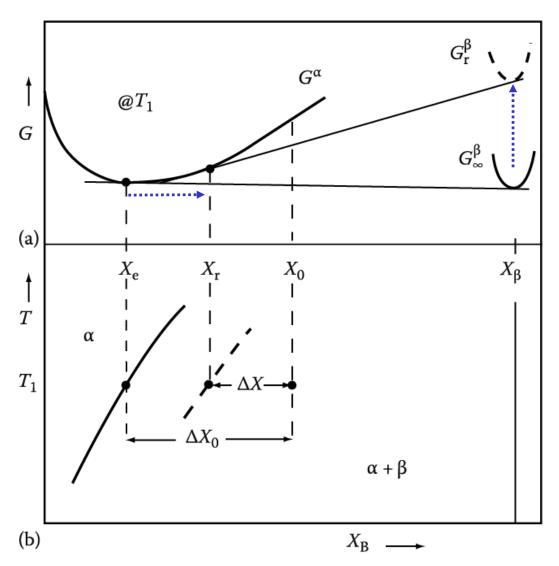
→ the same equation but the different value of r*

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2) Diffusion Controlled lengthening of Plates or Needles

Volume diffusion-controlled continuous growth process/ curved ends

The Gibbs-Thomson Effect: curvature of α/β interface~ extra pressure $\Delta P=2\gamma/r$



$$\Delta G = \Delta P \cdot V \sim 2 \gamma V_m / r$$

Interfacial E → total free E↑

$$\Delta X = \Delta X_0 \left(1 - \frac{r^*}{r} \right)$$

f *: critical nucleus, radius

$$\Delta X = X_0 - X_r$$

$$\Delta X_0 = X_0 - X_e$$

$$r \uparrow \longrightarrow \Delta X \uparrow$$

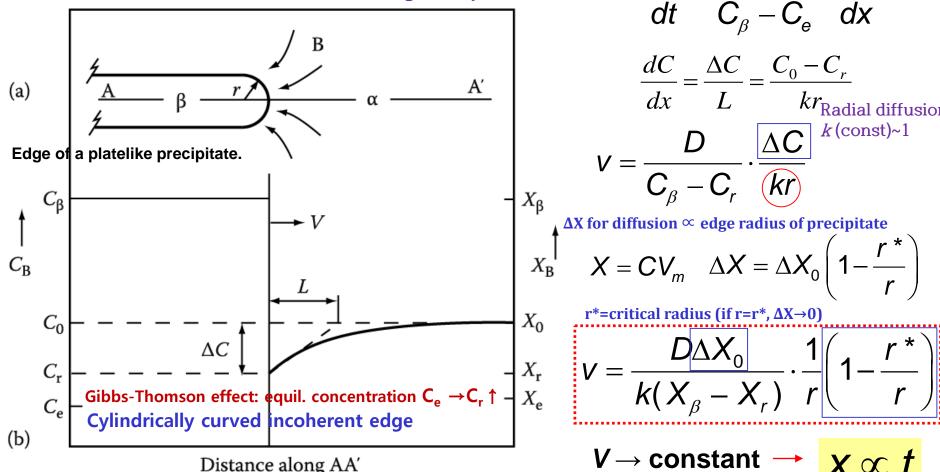
Fig. 5.20 Gibbs-Thomson effect.(a) Free E curves at T1. (b) corresponding phase diagram.

^{* &}lt;u>In platelike precipitates</u>, the edges are often <u>faceted</u> and observed to migrate by a <u>ledge mechanism</u>.

2) Diffusion Controlled lengthening of Plates or Needles

Plate Precipitate of constant thickness

Volume diffusion-controlled continuous growth process



From mass conservation,

$$v = \frac{dx}{dt} = \frac{D}{C_{\beta} - C_{e}} \cdot \frac{dC}{dx}$$
$$\frac{dC}{dx} = \frac{\Delta C}{L} = \frac{C_{0} - C_{r}}{kr_{\text{Radial del}}}$$

$$V = \frac{D}{C_{\beta} - C_{r}} \cdot \frac{\Delta C}{kr}$$

$$k \text{(const)} \sim 1$$

$$X_{\rm B}$$
 $X = CV_{m}$ $\Delta X = \Delta X_{0} \left(1 - \frac{r}{r}\right)$

r*=critical radius (if r=r*, $\Delta X \rightarrow 0$)

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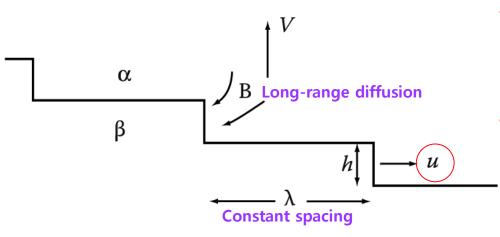
→ the same equation but the different value of r*

15

3) Thickening of Plate-like Precipitates

Thickening of Plate-like Precipitates by Ledge Mechanism

→ planar incoherent interface with high accommodation factors



- For the diffusion-controlled growth, a monoatomic-height ledge should be supplied constantly.
- sources of monatomic-height ledge

 → spiral growth, 2-D nucleation,
 nucleation at the precipitate edges,
 or from intersections with other
 precipitates (heterogeneous 2-D)

Half Thickness Increase

If the edges of the ledges are incoherent,

Assuming the diffusion-controlled growth,

$$u = \frac{D\Delta X_0}{k(X_{\beta} - X_e)h}$$

$$v = \frac{uh}{\lambda}$$

$$V = \frac{D}{C_{\beta} - C_{r}} \cdot \frac{\Delta C}{kr}$$

very similar to that of plate lengthening

$$V = \frac{D\Delta X_0}{k(X_{\beta} - X_e)\lambda}$$

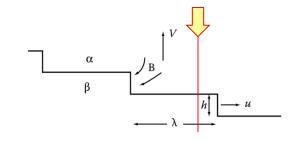
(Here, h = r and $X_r = X_e$, no Gibbs-Thomson effect)

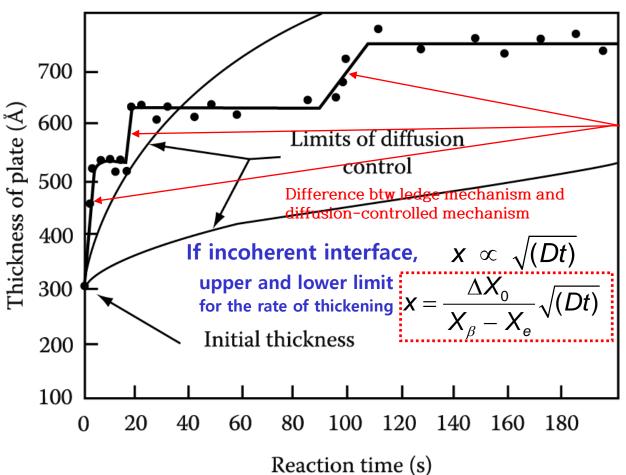
Distance btw ledges

3) Thickening of Plate-like Precipitates

Except spiral growth, supplement of ledge with constant λ is difficult.

Thickening of γ Plate in the Al-Ag system





What does this data mean?

<u>appreciable intervals of time</u> (no perceptible increase in plate thickness)

& thickness increases rapidly as an interfacial ledge passes.



Evidence for the low mobility of semi-coherent interfaces



Thickening rate is not constant

"Ledge nucleation" is rate controlling.

Fig. 5. 22 The thickening of a γ plate in an Al-15 wt% Ag alloy at 400 °C measure the thickening rates of individual precipitate plates by using hot-stage TEM.

Precipitate growth

1) Growth behind Planar Incoherent Interfaces

Diffusion-Controlled Thickening: $\chi \propto \sqrt{(Dt)}$ Parabolic growth

$$V = \frac{D(\Delta C_0)^2}{2(C_\beta - C_e)(C_\beta - C_0)x}$$

$$V \propto \Delta X_0 \propto \sqrt{(D/t)}$$
Supersaturation

$$V \propto \Delta X_0 \propto \sqrt{(D/t)}$$
Supersaturation

2) Diffusion Controlled lengthening of Plates or Needles

Diffusion Controlled lengthening:

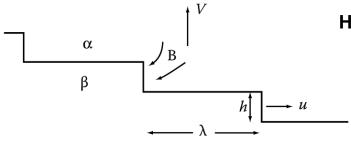
$$V = \frac{D\Delta X_0}{k(X_\beta - X_r)} \cdot \frac{1}{r} \left(1 - \frac{r^*}{r} \right)$$

$$V \to \text{constant} \to \chi \propto t$$
Linear growt

$$V \rightarrow \text{constant} \rightarrow \chi \propto t$$
Linear growth

3) Thickening of Plate-like Precipitates

Thickening of Plate-like Precipitates by Ledge Mechanism



Half Thickness Increase

$$v = \frac{uh}{\lambda} \longrightarrow v = \frac{D\Delta X_0}{k(X_{\beta} - X_e)\lambda}$$

u) rate of lateral migration

Contents for today's class

< Phase Transformation in Solids >

1) Diffusional Transformation (a) Precipitation

Q1: Overall Transformation Kinetics-TTT diagram "Johnson-Mehl-Avrami Equation"

Q2: Precipitation in Age-Hardening Alloys

Q3: Age Hardening

Q4: How can you design an alloy with high strength at high T?

Q5: Quenched-in vacancies vs Precipitate-free zone

Q1: Overall Transformation Kinetics-TTT diagram

"Johnson-Mehl-Avrami Equation"

5.4 Overall Transformation Kinetics – TTT Diagram

If isothermal transformation,

The fraction of Transformation as a function of Time and Temperature

$$\rightarrow f(t,T)$$

Plot f vs log t.

- isothermal transformation
- $f \sim \text{volume fraction of } \beta \text{ at any time; } 0 \sim 1$

Plot the fraction of transformation (1%, 99%) in T-log t coordinate.

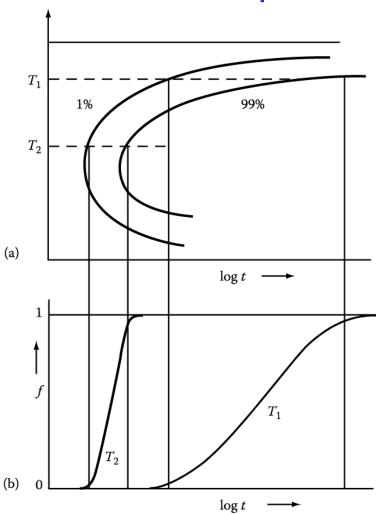


Fig. 5.23 The percentage transformation versus time for different transformation temperatures.

Time-Temperature-Transformation Curves (TTT)

 How much time does it take at any one temperature for a given fraction of the liquid to transform (nucleate and grow) into a crystal?

• $f(t,T) \sim \pi I(T) \mu(T)^3 t^4/3$

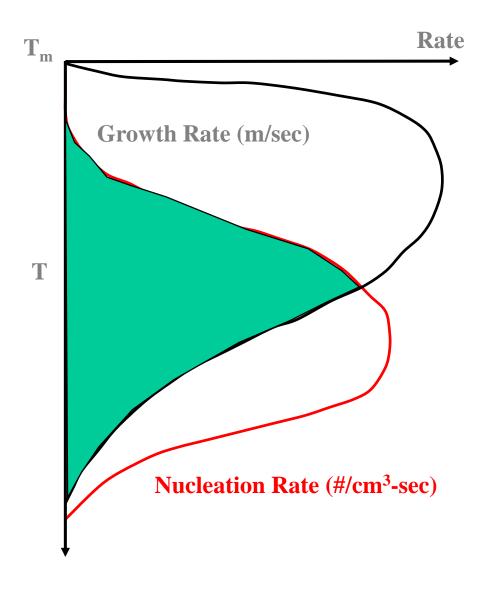
where *f* is the fractional volume of crystals formed, typically taken to be 10⁻⁶, a barely observable crystal volume.

Nucleation rates

Growth rates

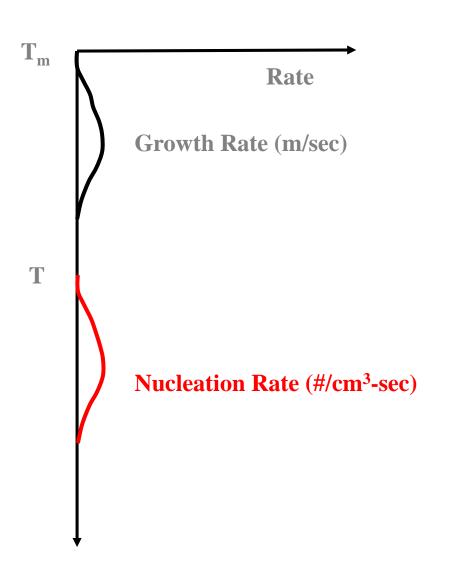
$$I = n v \exp \left\{ \left(\frac{16\pi \Delta H_{cryst}}{81RT} \right) \left(\frac{T_m}{\Delta T} \right)^2 \right\} \exp \left\{ \frac{-\Delta E_D}{RT} \right\} \quad \mu(T) = \left(\frac{fRT}{3N\pi a^2 \eta(T)} \right) \left(1 - \exp \left[\left(\frac{\Delta H_m}{RT} \right) \left(\frac{\Delta T}{T_m} \right) \right] \right)$$

Nucleation and Growth Rates – Poor Glass Formers



- Strong overlap of growth and nucleation rates
- Nucleation rate is high
- Growth rate is high
- Both are high at the same temperature

Nucleation and Growth Rates – Good Glass Formers



- No overlap of growth and nucleation rates
- Nucleation rate is small
- Growth rate is small
- At any one temperature one of the two is zero

* Time-Temperature-Transformation diagrams

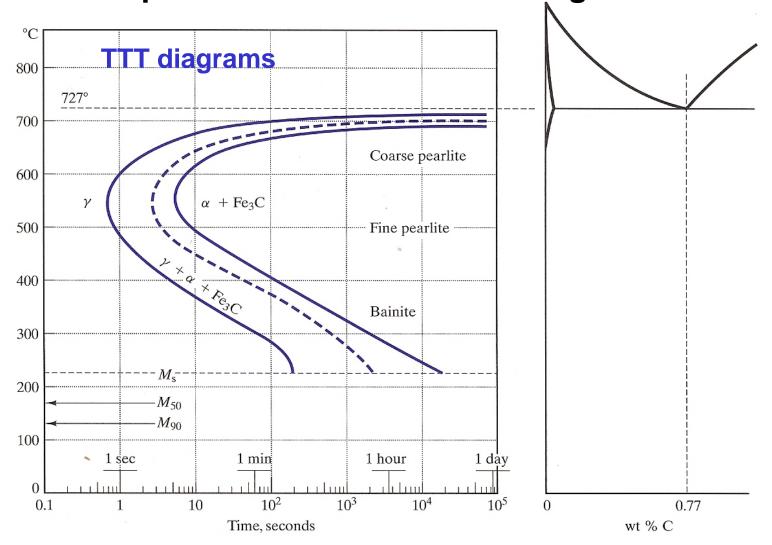


FIGURE 10.11 A more complete TTT diagram for eutectoid steel than was given in Figure 10.7. The various stages of the time-independent (or diffusionless) martensitic transformation are shown as horizontal lines. M_s represents the start, M_{50} represents 50% transformation, and M_{90} represents 90% transformation. One hundred percent transformation to martensite is not complete until a final temperature (M_f) of -46° C.

* Continuous Cooling Transformation diagrams

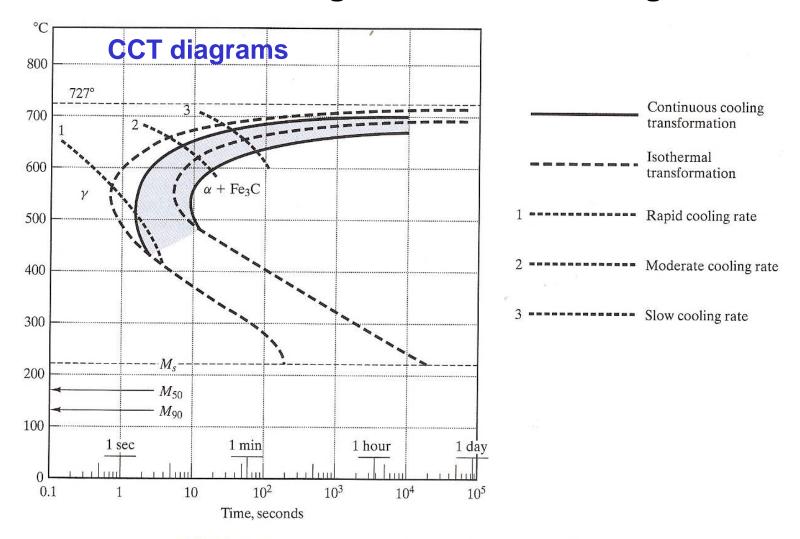


FIGURE 10.14 A continuous cooling transformation (CCT) diagram is shown superimposed on the isothermal transformation diagram of Figure 10.11. The general effect of continuous cooling is to shift the transformation curves downward and toward the right. (After Atlas of Isothermal Transformation and Cooling Transformation Diagrams, American Society for Metals, Metals Park, OH, 1977.)

Influence factors for f(t,T): nucleation rate, growth rate, density and distribution of nucleation sites, impingement of adjacent cells

Three Transformation Types

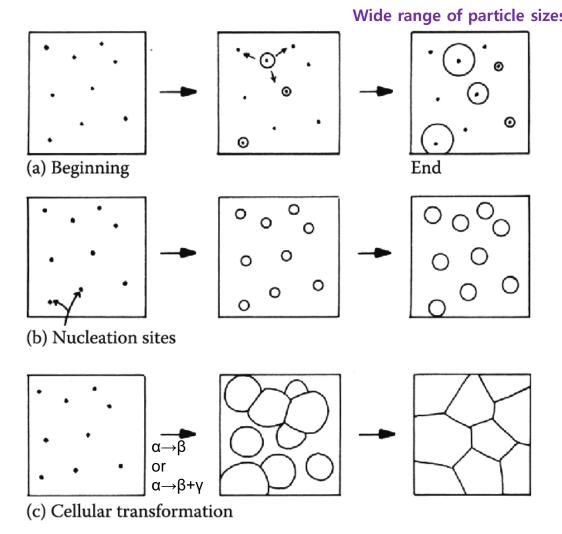


Fig. 5.24 (a) Nucleation at a constant rate during the whole transformation. (b) Site saturation – all nucleation occurs at the beginning of transformation. (c) A cellular transformation.

Wide range of particle sizes (a) continuous nucleation

Metastable α phase with many nucleation sites by quenching to T_t

 \rightarrow f depends on the nucleation rate and the growth rate.

(b) all nuclei present at t = 0

 \rightarrow f depends on the *number* of nucleation sites and the growth rate.

(c) All of the parent phase is consumed by the transformation product.

Transformation terminate by the impingement of adjacent cells growing with a constant velocity.

→ pearlite, cellular ppt, massive transformation, recrystallization

$$\alpha \rightarrow \beta$$

Transformation Kinetics

Avrami proposed that for a three-dimensional nucleation and growth process kinetic law

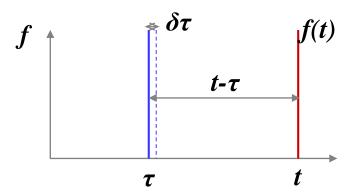
$$f = 1 - \exp(-kt^n)$$
 Johnson-Mehl-Avrami equation

$$f$$
: volume fraction transformed = $\frac{\text{Volume of new phase}}{\text{Volume of specimen}}$

- > Assumption:
 - √ reaction produces by nucleation and growth
 - √ nucleation occurs randomly throughout specimen
 - √ reaction product grows rapidly until impingement

Constant Nucleation Rate Conditions

- Nucleation rate (/) is constant.
- Growth rate (v) is constant.
- No compositional change



$$df_e = \frac{\begin{pmatrix} \text{Vol. of one particle nucleated} \\ \text{during } d\tau \text{ measured at time t} \end{pmatrix} \times \begin{pmatrix} \text{number of nuclei} \\ \text{formed during } d\tau \end{pmatrix}}{\text{Volume of specimen}}$$

$$df_{e} = \frac{\frac{4}{3}\pi [v(t-\tau)]^{3} \times (IV_{0}d\tau)}{V_{0}}$$

$$V = \frac{4}{3}\pi r^{3} = \frac{4}{3}\pi (vt)^{3}$$

$$V' = \frac{4}{3}\pi v^{3} (t-\tau)^{3}$$

$$V = \frac{4}{3}\pi r^{3} = \frac{4}{3}\pi (vt)^{3}$$
$$V' = \frac{4}{3}\pi v^{3} (t - \tau)^{3}$$

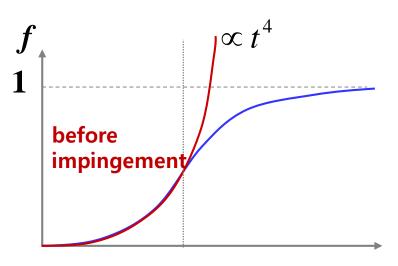
Constant Nucleation Rate Conditions

consider impingement + repeated nucleation effects

$$df = (1 - f)df_e \qquad df_e = \frac{df}{1 - f}$$

$$f_e = -\ln(1 - f)$$

$$f(t) = 1 - \exp(-f_e(t)) = 1 - \exp(-\frac{\pi}{3}Iv^3t^4)$$
* Short time:
1-exp(z)~Z (z «1)
* Long time:
t→∞, f→1



Johnson-Mehl-Avrami Equation

$$f = 1 - \exp(-kt^n)$$

k: Tsensitive f(I, v) $-\frac{\pi}{3}Iv^3$

 $n: 1 \sim 4$ (depend on nucleation mechanism)

Growth controlled.

Nucleation-controlled.

If no change of nucleation mechanism during phase transformation, n is not related to T.

i.e.
$$50\%$$
 transform $Exp(-0.7) = 0.5$

$$kt_{0.5}^n = 0.7$$
 $t_{0.5} = \frac{0.7}{k^{1/n}}$ $\frac{\pi}{3}Iv^3$ $t_{0.5} = \frac{0.9}{I^{1/4}v^{3/4}}$

Rapid transformations are associated with (large values of k), or (rapid nucleation, / and growth rates, ν) \rightarrow C curve

5.4 Overall Transformation Kinetics

If isothermal transformation,

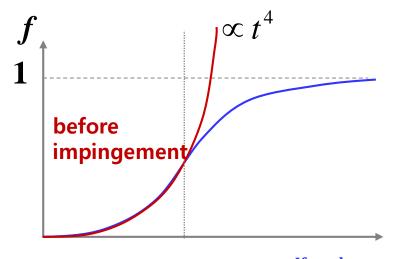
The fraction of Transformation as a function of Time and Temp. $\rightarrow f(t,T)$



TTT Diagram CCT Diagram

* Constant Nucleation Rate Conditions

$$f(t) = 1 - \exp(-f_e(t)) = 1 - \exp\left(-\frac{\pi}{3}Iv^3t^4\right) + \frac{1 - \exp(z) \sim Z \ (z \ll 1)}{t \to \infty, f \to 1}$$
* Long time:
$$t \to \infty, f \to 1$$



Johnson-Mehl-Avrami Equation

$$f = 1 - \exp(-kt^n)$$

 $f = 1 - \exp(-kt^{n})$ $k: T \text{ sensitive } f(I, v) \qquad -\frac{\pi}{3}Iv^{3}$

 $n: 1 \sim 4$ (depend on nucleation mechanism)

Growth controlled.

Nucleation-controlled.

* Short time:

If no change of nucleation mechanism during phase transformation, n is not related to T.

i.e.
$$50\%$$
 transform $Exp(-0.7) = 0.5$

$$kt_{0.5}^n = 0.7$$
 $t_{0.5} = \frac{0.7}{k^{1/n}}$ $\frac{\pi}{3}Iv^3$ $t_{0.5} = \frac{0.9}{I^{1/4}v^{3/4}}$

Rapid transformations are associated with (large values of k), or (rapid nucleation, / and growth rates, ν) \rightarrow C curve

Q2: Precipitation in Age-Hardening Alloys

The theory of nucleation and growth can provide general guidelines for understanding civilian transformation.

5.5 Precipitation in Age-Hardening Alloys

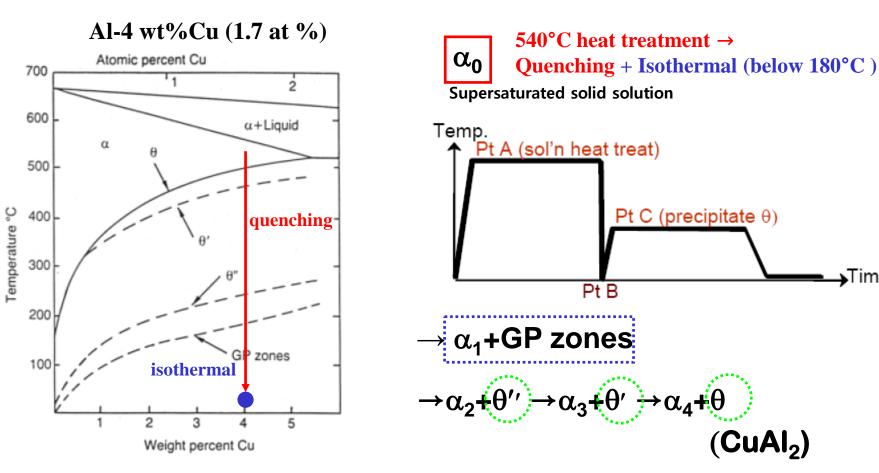
Table 5.2 Some precipitation-Hardening Sequences

Base Metal	Alloy	Precipitation Sequence
Aluminum	Al-Ag	GPZ (spheres) $\rightarrow \gamma'$ (plates) $\rightarrow \gamma$ (Ag ₂ Al)
	Al–Cu	GPZ (disks) $\rightarrow \theta''$ (disks) $\rightarrow \theta'$ (plates) $\rightarrow \theta$ (CuAl ₂)
	Al-Cu-Mg	$GPZ (rods) \rightarrow S' (laths) \rightarrow S (CuMgAl_2) (laths)$
	Al-Zn-Mg	GPZ (spheres) $\rightarrow \eta'$ (plates) $\rightarrow \eta$ (MgZn ₂) (plates or rods)
	Al-Mg-Si	$GPZ \; (rods) \mathop{\rightarrow} \beta' \; (rods) \mathop{\rightarrow} \beta \; (Mg_2Si) \; (plates)$
Copper	Cu–Be	GPZ (disks) $\rightarrow \gamma' \rightarrow \gamma$ (CuBe)
	Cu-Co	GPZ (spheres) $\rightarrow \beta$ (Co) (plates)
Iron	Fe-C	ϵ -carbide (disks) \rightarrow Fe ₃ C (plates)
	Fe-N	α'' (disks) \rightarrow Fe ₄ N
Nickel	Ni-Cr-Ti-Al	γ' (cubes or spheres)

Source: Mainly from Martin, J.W., in Precipitation Hardening, Pergamon Press, Oxford, 1968.

5.5 Precipitation in Age-Hardening Alloys

Precipitation in Aluminum-Copper Alloys



O'solvuses. (Reproduced from G. Lorimer, Precipitation Processes in Solids, K.C. Russell and H.I. Aaronson (Eds.), The Metallurgical Society of AMIE, 1978, p. 87.)

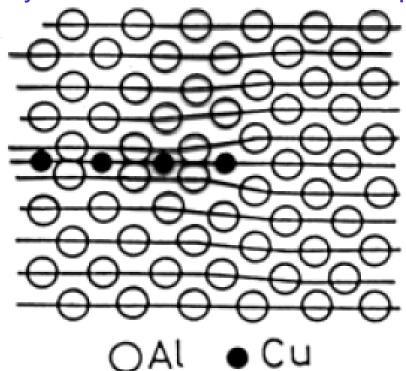
Fig. 5.25 Al-Cu phase diagram showing the metastable GP zone, Θ'' and In most system, α , β phase \sim different crystal structure \rightarrow incoherent nuclei with large $\gamma \sim$ impossible to homogeneous nucleation of $\beta \rightarrow$ Homogeneous nucleation of metastable phase β' (GP Zones, Section 5.5.1)

5.5.1 GP Zones

$$\Delta G_{\theta}^* > \underline{(\Delta G_V - \Delta G_s)} >> \Delta G_{zone}^*$$

The zones minimize their strain energy by choosing a discshape perpendicular to the elastically soft <100> directions in the fcc matrix (as shown in Fig. 5.26).

2 atomic layers thick and 10 nm in diameter with a spacing of ~10 nm



Fully coherent Cu-rich area with very low interfacial E

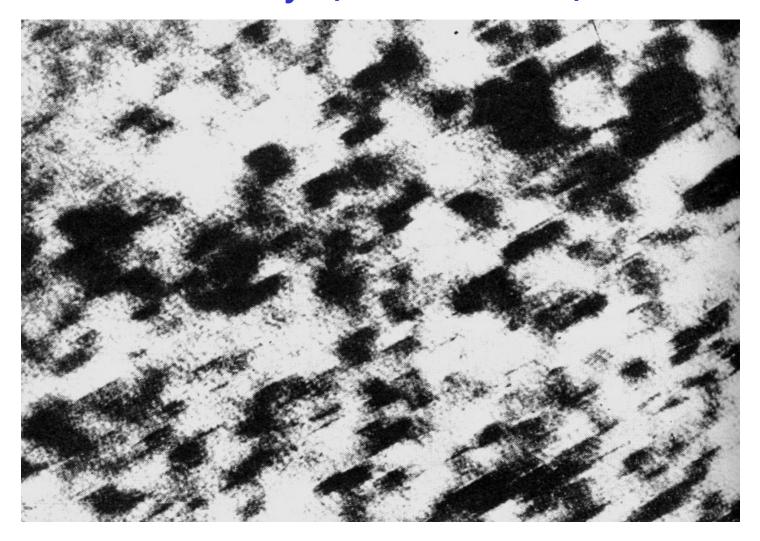
Fig. 5.26 Section through a GP zone parallel to the (200) plane. (Based on the work of V. Gerold: Zeitschrift für Metallkunde 45 (1954) 599.)

: 이러한 응집체는 완전한 석출 입자로 볼 수 없으며, 때때로 석출대 (zone)로 명명함.

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The zone appear to be homogeneously nucleated, however, excess vacancies are thought to play an important role in their formation (be returned to later)

GP zones of Al-Cu alloys (x 720,000, TEM)



Fully coherent, about 2 atomic layers thick and 10 nm in diameter with a spacing of ~ 10 nm

Transition phases

$$\alpha_0 \rightarrow \alpha_1 + \text{GP zone} \rightarrow \alpha_2 + \theta'' \rightarrow \alpha_3 + \theta' \rightarrow \alpha_4 + \theta \text{ (CuAl}_2\text{)}$$

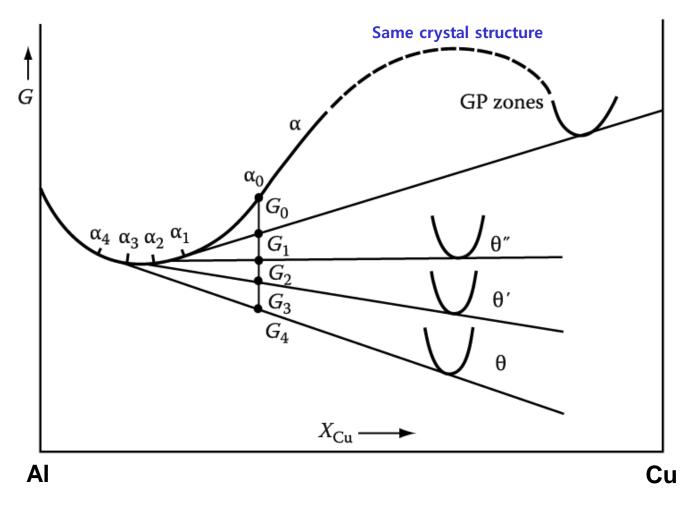
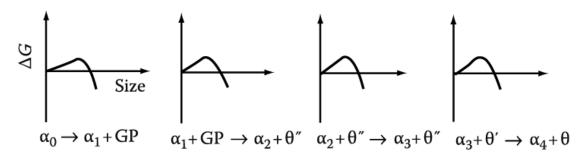


Fig. 5.27 A schematic molar free energy diagram for the Al-Cu system.

$\alpha_0 \rightarrow \alpha_1 + GP zone \rightarrow \alpha_2 + \theta'' \rightarrow \alpha_3 + \theta' \rightarrow \alpha_4 + \theta (CuAl_2)$

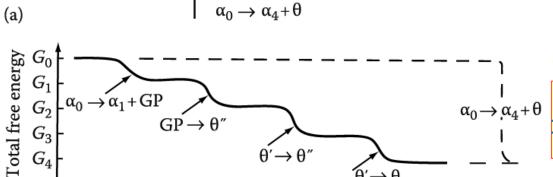
Low Activation Energy of Transition Phases



∵ the crystal structures of the transition phases are intermediate between those of the matrix and the equilibrium phase.

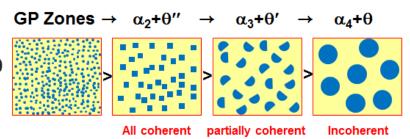
Transition phases (중간상, $\theta'' \otimes \theta'$): a high degree of coherence, low interfacial E contribution to min ΔG*.

Equilibrium phase (평형상, θ): complex crystal structure that is incompatible with the matrix → high E interfaces and high ΔG^* .



Time

(b)



G of the alloy decreases more rapidly via the transition phases than by direct transformation to the equilibrium phase.

(a) The activation E barrier to the formation of each transition phase is very small in comparison to the barrier against the direct precipitation of the equilibrium phase. (b) Schematic diagram showing the total free E of the alloy versus time.

 $\theta' \rightarrow \theta$

The Crystal Structures of θ'' , θ' and θ

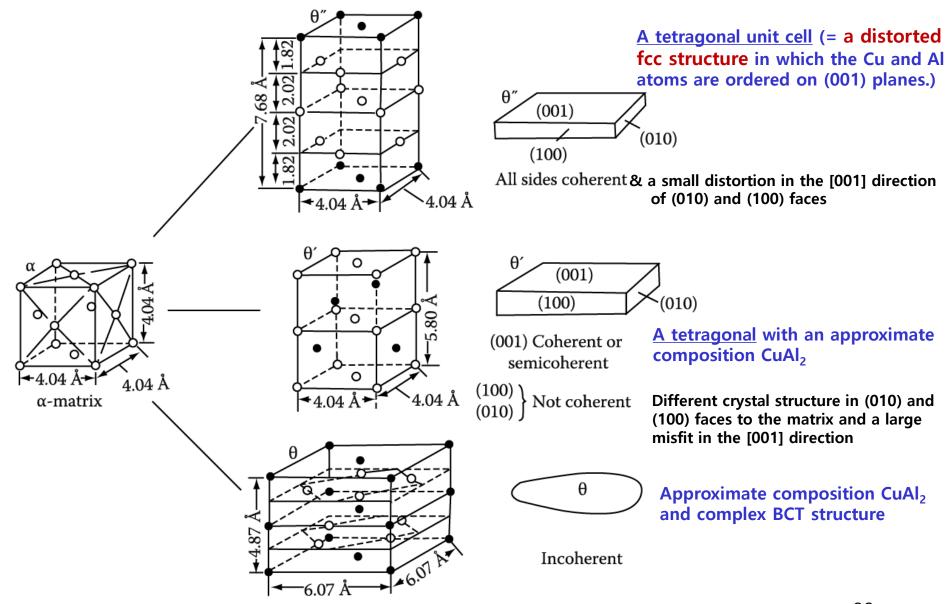
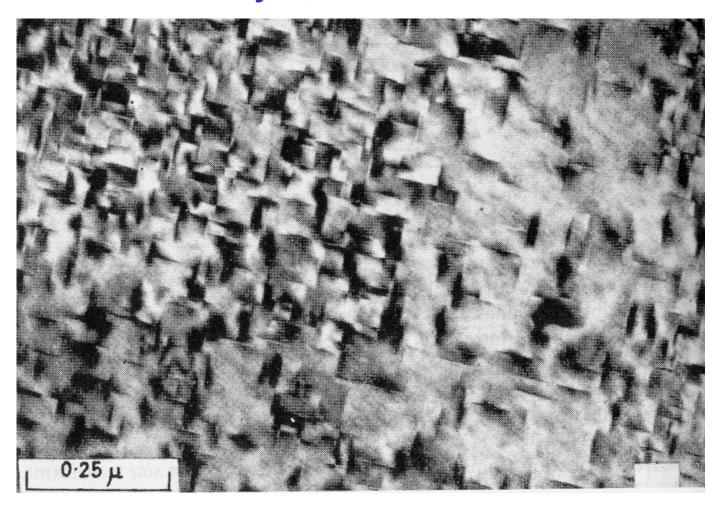


Fig. 5.29 Structure and morphology of θ ", θ ' and θ in Al-Cu (\bigcirc Al. \blacksquare Cu).

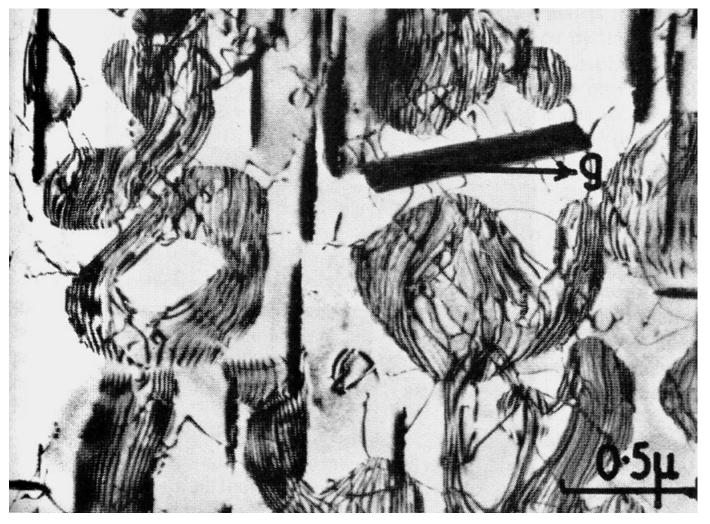
θ'' of Al-Cu alloys (x 63,000, TEM)



Tetragonal unit cell, essentially a distorted fcc in which Cu and Al atoms are ordered on (001) planes, fully-coherent plate-like ppt with $\{001\}_{\alpha}$ habit plane. ~ 10 nm thick and 100 nm in diameter (larger than GP zones).

: Like the GP zones, the θ'' precipitates are visible by virtue of the coherency-strain fields caused by the misfit perpendicular to the plates.

θ' of Al-Cu alloys (x 18,000, TEM)



 θ' has (001) planes that are identical with $\{001\}_{\alpha}$ and forms as plates on $\{001\}_{\alpha}$ with the same orientation relationship as θ'' . But, (100), (010) planes \rightarrow incoherent, \sim 1 μ m in diameter.

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θ of Al-Cu alloys x 8,000



CuAl₂: complex body centered tetragonal, incoherent or complex semicoherent

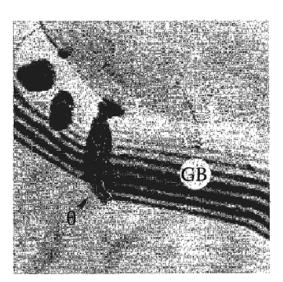
: large size and coarse distribution of the precipitates

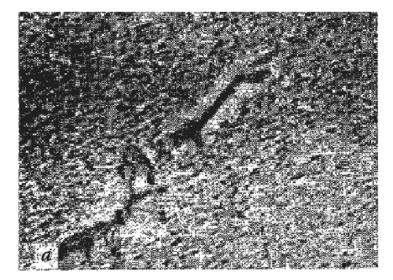
Nucleation sites in Al-Cu alloys

(0) GP zones $\rightarrow \theta$ ":

GP zones

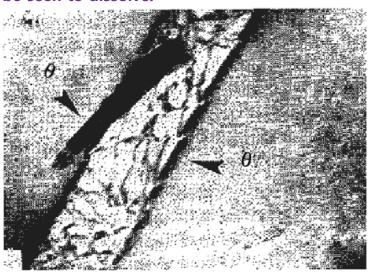
~ very potent nucleation sites for θ "





(a) θ " $\rightarrow \theta$ '. θ ' nucleates at dislocation (x 70,000). : Dislocation can reduce the misfit in two <100> matrix directions.

As the θ' grows the surrounding, less-stable θ'' phase can be seen to dissolve.



(b) θ nucleation on grain boundary (GB)(x 56,000) (c) $\theta' \to \theta$. θ nucleates at θ' /matrix interface (x 70,000). : governed by the need to reduce the large interfacial energy contribution to ΔG^* for this phase

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* Effect of Aging Temperature on the Sequence of Precipitates

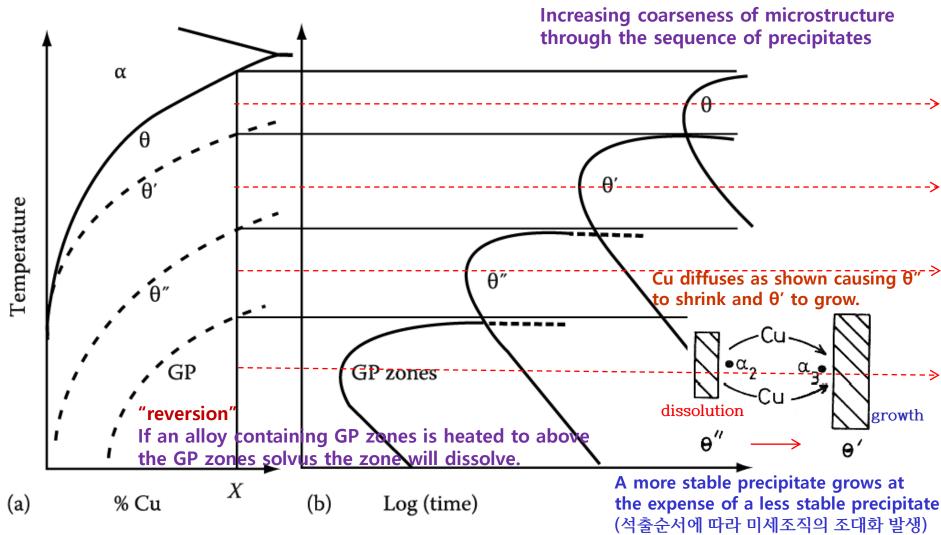


Fig. 5.32 (a) Metastable solvus lines in Al-Cu (schematic).

(b) Time for start of precipitation at different temperatures for alloy X in (a).

Q3: Age Hardening

5.5.4. Age Hardening

Transition phase precipitation → great improvement in the mechanical properties

Coherent precipitates→highly strained matrix→the main resistance to the ® movement: solid solution hardening

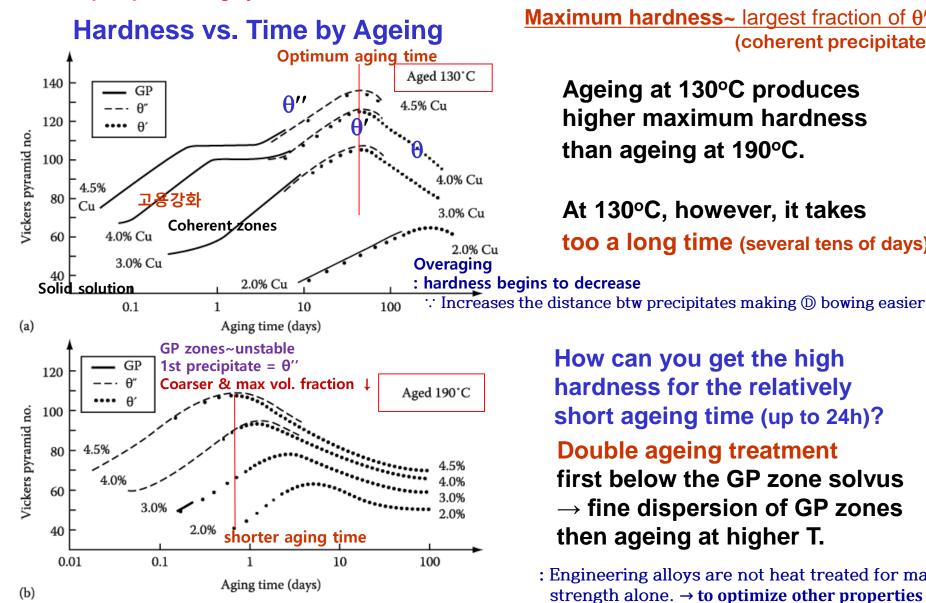


Fig. 5. 37 Hardness vs. time for various Al-Cu alloys at (a) 130 $^{\circ}$ C (b) 190 $^{\circ}$ C

Maximum hardness~ largest fraction of θ'' (coherent precipitates)

Ageing at 130°C produces higher maximum hardness than ageing at 190°C.

At 130°C, however, it takes too a long time (several tens of days).

How can you get the high hardness for the relatively short ageing time (up to 24h)?

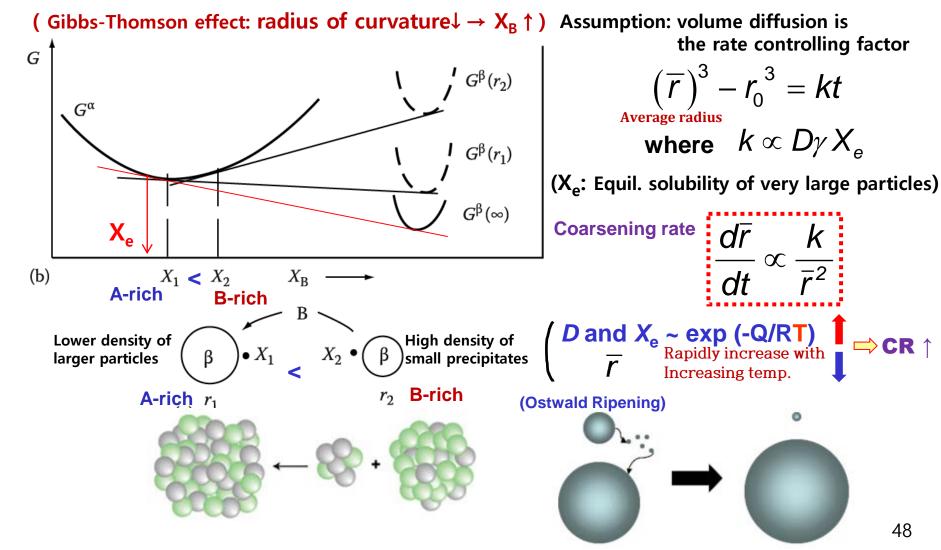
Double ageing treatment first below the GP zone solvus → fine dispersion of GP zones then ageing at higher T.

: Engineering alloys are not heat treated for max. strength alone. → to optimize other properties best heat treatment in practice

Q4: How can you design an alloy with high strength at high T?

5.5.6. Particle Coarsening (smaller total interfacial area→loss of strength or disappearance of GB pining effect→ particular concern in the design of materials for high temp. applications)

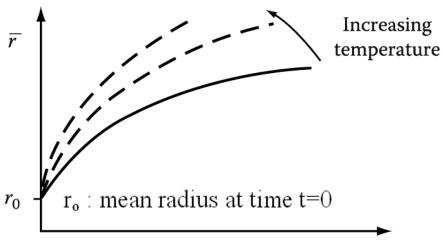
Two Adjacent Spherical Precipitates with Different Diameters



: Concentration gradient in matrix→diffusion→small particle_shrink/ large particle_grow

5.5.6. Particle Coarsening

The Rate of Coarsening with Increasing Time and Temp.



Time

~ Particular concern in the design of materials for high temperature applications

Undesirable degradation of properties: less strength/ disappearance of GB pinning effects

How can you design an alloy with high strength at high T?

→ fine precipitate dispersion

hint)
$$\frac{d\overline{r}}{dt} \propto \frac{k}{\overline{r}^2}$$
 $k \propto D\gamma X_e$

1) low γ

heat-resistant Nimonic alloys
based on Ni-rich Ni-Cr → ordered fcc
Ni₃(Ti,Al) in Ni-rich matrix → high strength
Ni/γ' interface~ "fully coherent" (10 ~ 30 mJ m⁻²)

Maintain a fine structure at high temperature

→ improve creep-rupture life

2) low X_e (Oxide~ very insoluble in metals): fine oxide dispersion in a metal matrix Ex) dispersed fine ThO₂ (thoria) in W and Ni

→ strengthened for high temperature

3) low *D*

Cementite dispersions in tempered steel

- \rightarrow high **D** of carbon \rightarrow very quickly coarsening
- a. substitutional alloying element
- → segregates to carbide → slow coarsening
- **b.** strong carbide-forming elements
- \rightarrow more stable carbides \rightarrow lower X_e

Q5: Quenched-in vacancies vs Precipitate-free zone

5.5.3. Quenched-in Vacancies

If $X_v < X_v^c$ critical vacancy supersaturation, Precipitate nucleation $X \rightarrow$ formation of PFZ

In the vicinity of grain boundaries on subsequent aging,

- a) Excess ♥→ ® nucleation and moving ↑: Heterogeneous nucleation sites ↑
- **b)** Excess $\textcircled{v} \rightarrow$ atomic mobility \uparrow at ageing temp: speeds up the process of nucleation and growth
- ex) rapid formation of GP zones at the relatively low aging temperature. (possible to RT aging in Al-Cu alloy)

a) Precipitate-Free Zone(PFZ) due to Vacancy Diffusion during quenching

Solute concentration within the zone ~ largely unchanged, but no precipitate at GB ∴ a critical vacancy supersaturation must be exceeded for nucleation to occur.

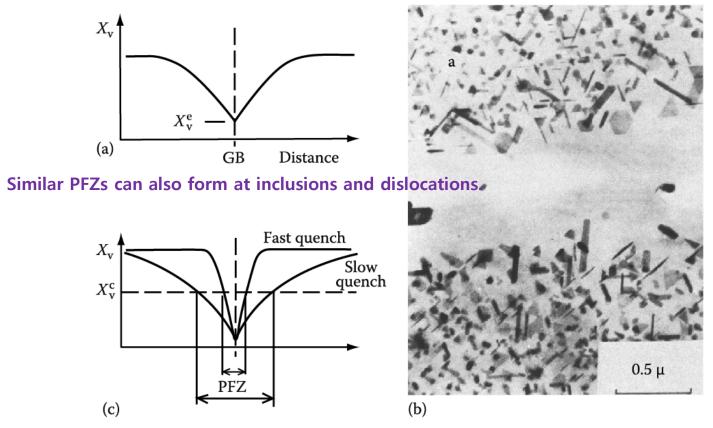


Fig. 5.35 A PFZ due to vacancy diffusion to a grain boundary during quenching.

- (a) Vacancy concentration profile. (b) A PFZ in an Al-Ge alloy (x 20,000)
- (c) Dependence of PFZ width on critical vacancy concentration X_{ν}^{c} and rate of quenching.

* Equilibrium Vacancy Concentration

at equilibrium
$$\left(\frac{dG}{dX_V} \right)_{X_V = X_V^e} = 0$$

$$\Delta H_V - T\Delta S_V + RT \ln X_V^e = 0$$

A constant ~3, independent of T Rapidly income
$$X_{V}^{e} = exp \frac{\Delta S_{V}}{R} exp \frac{-\Delta H_{V}}{RT}$$

putting $\Delta G_V = \Delta H_V - T\Delta S_V$

$$X_{V}^{e} = exp \frac{-\Delta G_{V}}{RT}$$

increases exponentially with increasing T

In practice, ∆H_V is of the order of 1 eV per atom and X_V^e reaches a value of about 10⁻⁴~10⁻³ at the melting point of the solid

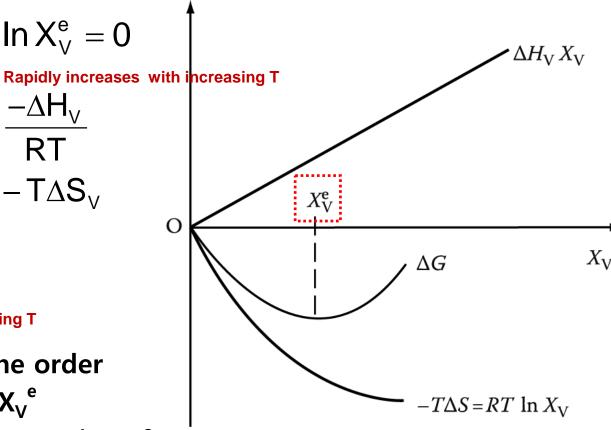


Fig. 1.37 Equilibrium vacancy concentration.

: adjust so as to reduce G to a minimum

b) Another cause of PFZs can be the nucleation and growth of GB precipitates during cooling from the solution treatment temperature.

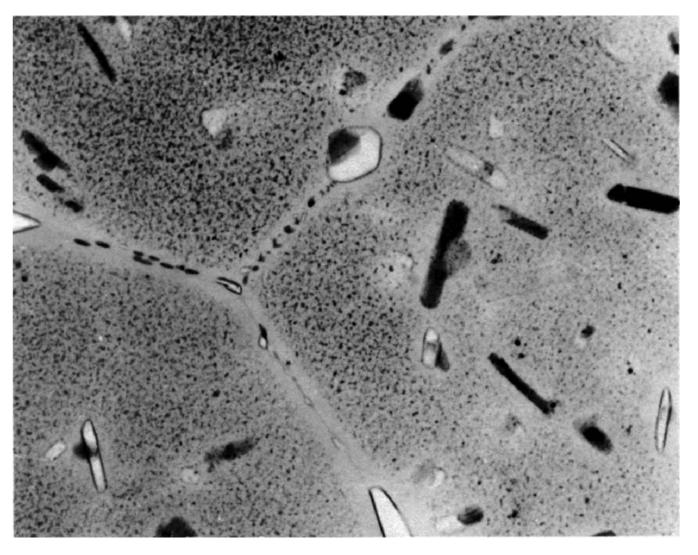


Fig. 5.36 PFZs around grain boundaries in a high-strength commercial Al-Zn-Mg-Cu alloy. 53 Precipitates on grain boundaries have extracted solute from surrounding matrix. (x 59,200)